

The first statistical studies were demographic so a large part of the vocabulary has been preserved.

1. Population : the group on which the statistical study will be based.
2. Individual

An experiment can be modeled with a binomial distribution whenever :

1. There are only two possible events resulting from the experiment : A, \bar{A} (success and defeat).
2. The probability of every event A, \bar{A} are the same in any happening of the experiment (p and $q = 1 - p$, respectively). Namely if a coin is flipped several times, the probability of having 'heads' does not change.
3. Any realization of the experiment is independent from the rest.

A binomial random variable will give the number of successes when having happened a certain number of experiments.

It turns out to be useful to analyze the number of times that 'heads' is obtained when flipping a coin n times.

The binomial distribution is usually represented by $B(n,p)$, with :

1. n : number of happenings of the random experiment.
2. P : probability of success in doing an experiment.

So if we want to study the binomial distribution that models 10 flips of a coin (in which the 'heads' and 'tails' are equally probable) we have :

$$B(10, \frac{1}{2})$$

The probability function of the binomial distribution is :

$$p(X = k) = \binom{n}{k} p^k \cdot q^{n-k}$$

1. n : number of experiments
2. k : number of success
3. p : success probability
4. q : defeat probability

The combinatorial number is defined :

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

Calculate the probability of obtaining 8 'heads' when flipping a coin ten times.

Distribution $B(10, \frac{1}{2})$

Number of experiments : $n = 10$

Number of successful result: $k = 8$

Probability of each success and each defeat : $p = q = \frac{1}{2}$

$$p(X = 8) = \binom{10}{8} \left(\frac{1}{2}\right)^8 \left(\frac{1}{2}\right)^2 = 0.044$$

The average of a binomial distribution is :

$$\mu = n \cdot p$$

The variance is :

$$\sigma^2 = n \cdot p \cdot q = n \cdot p (1 - p)$$

The standard deviation is :

$$\sigma = \sqrt{n \cdot p \cdot q}$$