

Known some trigonometric ratio of one angle, we can easily calculate the rest through the following relationships:

1. $\sin^2 \alpha + \cos^2 \alpha = 1$
2. $1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha} = \sec^2 \alpha$

So, if we want to know the trigonometric ratios of one angle α , we only need to know one of them and the quadrant where the angle is.

Let's suppose we have an angle α and we know that $\sin \alpha = \frac{1}{2}$ and that it belongs to the first quadrant, then it's quite easy to calculate its tangent and its cosine.

We only need to do the following:

$$\sin^2 \alpha + \cos^2 \alpha = 1 \Rightarrow \frac{1}{4} + \cos^2 \alpha = 1 \Rightarrow \cos^2 \alpha = \frac{3}{4} \Rightarrow$$

$$\Rightarrow \cos \alpha = \sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2}$$

$$1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha} \Rightarrow \tan^2 \alpha = \frac{1}{\frac{3}{4}} - 1 = \frac{4}{3} - 1 = \frac{1}{3} \Rightarrow$$

$$\Rightarrow \tan \alpha = \sqrt{\frac{1}{3}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$$