

We say that  $B=\{\vec{u},\vec{v}\}$  is an orthogonal basis if the vectors that form it are perpendicular. In other words,  $\vec{u}$  and  $\vec{v}$  form an angle of  $90^\circ$ .

$\vec{u} = (3, 0), \vec{v} = (0, -2)$  form an orthogonal basis since the scalar product between them is zero and this a sufficient condition to be perpendicular:

$$\vec{u} \cdot \vec{v} = 3 \cdot 0 + 0 \cdot (-2) = 0$$

We say that  $B=\{\vec{u},\vec{v}\}$  is an orthonormal basis if the vectors that form it are perpendicular and they have length 1. Namely,  $\vec{u}$  and  $\vec{v}$  form an angle of  $90^\circ$  and  $|\vec{u}|=1, |\vec{v}|=1$ .

$\vec{u} = (1, 0), \vec{v} = (0, -1)$  form an orthonormal basis since the vectors are perpendicular (its scalar product is zero) and both vectors have length 1.

Perpendicular:  $\vec{u} \cdot \vec{v} = 1 \cdot 0 + 0 \cdot (-1) = 0$ .

Unitary vectors (length 1):  $|\vec{u}| = \sqrt{1^2 + 0^2} = \sqrt{1} = 1, |\vec{v}| = \sqrt{0^2 + (-1)^2} = \sqrt{1} = 1$ .