$QV = \mu V \Rightarrow V^T QV = V^T \mu V = \mu(V^T V)$
Again, VTQV 70 (11), and VTV 70, so μ 70.
Thus, the eigenvalues of P and Q are non-negative.
(b) $Pu = \lambda u \implies A^{T}Au = \lambda u$
\Rightarrow AATAU = AAU = A(AU)
Thus, Q(Au) = 1 (Au), so Au is an eigenvector of P with eigenvalue 1, if u is an eigenvector of P with eigenvalue 1.
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Similarly, let v be an eigenvector of Q with eigenvalue μ , ΔD $QV = \mu V \Rightarrow AA^TV = \mu V$ $AA^TV = \mu V$ AA

(c) Suppose V; is an eigenvector of Q with eigenvalue A;

Thus, $QV_i = \lambda_i V_i \implies AA^TV_i = A_i V_i$ $U_i = A^TV_i$, so $AU_i = A(A^TV_i) = AA^TV_i$ $U_i = A^TV_i$, so $AU_i = A(A^TV_i) = AA^TV_i$ $U_i = A^TV_i$, $U_i = A^TV_i$ $U_i = A^TV_i$

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Case I: m > n

UV^{T} = \begin{bmatrix} v_{1} \mid v_{2} \mid \dots \mid v_{m} \end{bmatrix} \begin{bmatrix} v_{1} \mid v_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} u_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid v_{2} \mid \dots \mid v_{m} \end{bmatrix} \begin{bmatrix} u_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid v_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} u_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid u_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{1} \mid u_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{1} \mid u_{1} \mid u_{1} \mid u_{1} \mid u_{2} \mid \dots \mid v_{n} \end{bmatrix} \begin{bmatrix} v_{1} \mid u_{1} \mid v_{1} \mid u_{1} \mid v_{1} \mid u_{1} \mid u_{1} \mid u_{1} \mid v_{1} \mid
```

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Case II: m < n

UTV^{T} = [v_{1}|v_{2}|...|v_{m}][r_{1}, r_{2}][u_{1}|u_{2}|...|u_{n}]^{T}

= [v_{1}|v_{2}|...|v_{m}][r_{1}u_{1}|r_{2}u_{2}|...|r_{m}u_{m}]^{T}

= [r_{1}v_{1}|r_{2}v_{2}|...|r_{m}v_{m}][u_{1}|u_{2}|...|u_{m}]^{T}

= [Au_{1}|Au_{2}|...|Au_{m}][u_{1}|u_{2}|...|u_{m}]^{T}

= A[u_{1}|u_{2}|...|Au_{m}][u_{1}|u_{2}|...|u_{m}]^{T}

= A[u_{1}|u_{2}|...|u_{m}][u_{1}|u_{2}|...|u_{m}]^{T}
```