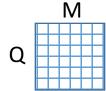
## Data from the content tagging

U: # users

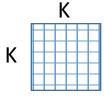
Q: # items

K: # knowledge components

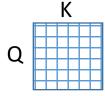
M: # adaptive modules



scope: boolean, shows items belonging to adaptive modules



 $m_w$ : numeric (0-1), shows pre-requisite relations among knowledge components



*m\_tagging*: integer (0 or 1), shows tagging of items with knowledge components



difficulty: numeric (0-1), shows tagging of items with difficulty levels

The ordering of users, items, knowledge components and adaptive modules never changes. Their indices serve as internally used IDs.

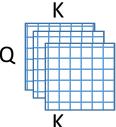
## Data initialized by us

U: # users

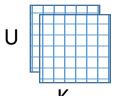
Q: # items

K: # knowledge components

M: # adaptive modules

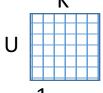


*m\_guess, m\_slip, m\_trans*: numeric (≥0), odds of guessing ,slipping, knowledge transfer



 $m_L_i$ : numeric ( $\geq 0$ ), initial odds of mastery

 $m_L$ : current odds of mastery, in the beginning of the algorithm initialized equal to  $m_L$ 



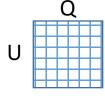
*m\_exposure*: integer, # exposures to a KC, initialized with all 0s

 $m_{confidence}$ : numeric ( $\geq 0$ ), exposure relevance to a KC, initialized with all 0s



last\_seen: integer, the ID of the item last served to a user.

Initialized with -1s (or any other value not encountered among item IDs)



m\_unseen: boolean, shows which items have been served to a user, initialized with all "True"



transactions: data-frame containing column [user, item, time, score], each row records a transaction.

Initialized with zero rows.

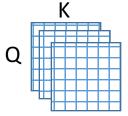
## Data derived for convenience

U: # users

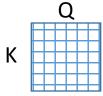
Q: # items

K: # knowledge components

M: # adaptive modules



m\_guess\_neg\_log, m\_p\_guess, m\_slip\_neg\_log, m\_p\_slip, m\_x0\_mult, m\_x1\_0\_mult, m\_k: numeric



*m\_difficulty:* numeric, derived from *difficulty* 

## **Parameters**

epsilon: numeric (e.g. 1e-10), a convenience cutoff

eta: numeric (e.g. 0.0), relevance threshold

M: numeric (e.g. 20.0), information threshold

r\_star: numeric (e.g. 0.0), forgiveness threshold

*L\_star*: numeric (e.g. 2.2), mastery certainty threshold (for logarithm of mastery odds)

W\_r, W\_c, W\_d, W\_p: numeric, importance weights of recommendation sub-strategies

stopOnMastery: boolean, a recommendation strategy parameter