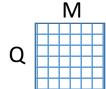
Data from the content tagging

U: # users

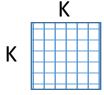
Q: # items

K: # knowledge components

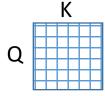
M: # adaptive modules



scope: boolean, shows items belonging to adaptive modules



 m_w : numeric (0-1), shows pre-requisite relations among knowledge components



m_tagging: integer (0 or 1), shows tagging of items with knowledge components



difficulty: numeric (0-1), shows tagging of items with difficulty levels

The ordering of users, items, knowledge components and adaptive modules never changes. Their indices serve as internally used IDs.

Data initialized by us

U: # users

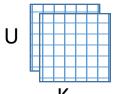
Q: # items

K: # knowledge components

M: # adaptive modules

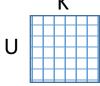
2

m_guess, m_slip, m_trans: numeric (≥0), odds of guessing ,slipping, knowledge transfer



 $m \ L \ i$: numeric (≥ 0), initial odds of mastery

 m_L : current odds of mastery, in the beginning of the algorithm initialized equal to m_L



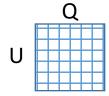
m_exposure: integer, # exposures to a KC, initialized with all 0s

 $m_{confidence}$: numeric (≥ 0), exposure relevance to a KC, initialized with all 0s



last_seen: integer, the ID of the item last served to a user.

Initialized with -1s (or any other value not encountered among item IDs)



m_unseen: boolean, shows which items have been served to a user, initialized with all "True"



transactions: data-frame containing columns [user, item, time, score], each row records a transaction.

Initialized with zero rows.

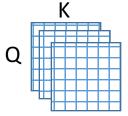
Data derived for convenience

U: # users

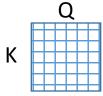
Q: # items

K: # knowledge components

M: # adaptive modules



m_guess_neg_log, m_p_guess, m_slip_neg_log, m_p_slip, m_x0_mult, m_x1_0_mult, m_k: numeric



m_difficulty: numeric, derived from *difficulty*

Parameters

epsilon: numeric (e.g. 1e-10), a convenience cutoff

eta: numeric (e.g. 0.0), relevance threshold

M: numeric (e.g. 20.0), information threshold

r_star: numeric (e.g. 0.0), forgiveness threshold

L_star: numeric (e.g. 2.2), mastery certainty threshold (for logarithm of mastery odds)

W_r, W_c, W_d, W_p: numeric, importance weights of recommendation sub-strategies

stopOnMastery: boolean, a recommendation strategy parameter