

what is Model ?



vehicle



kinetics >>

Fuel >>

Aerodynamics >>

? features ?

elemental description of any

system

Physical >>

Mathematical >>

A model must contain the dynamics of the system.
mathematical modelling is not unique. It depends on the perspective.

electrical,
circuit

O/P |  I/P

Mathematical modelling

A set of eqs

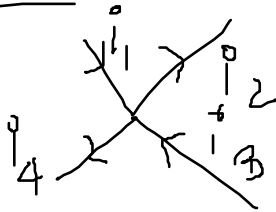
Ex:

Governing

physics

KCL

$\vec{v} \rightarrow \rightarrow \rightarrow$
Bernoulli's eqn



Types of mathematical modelling:-

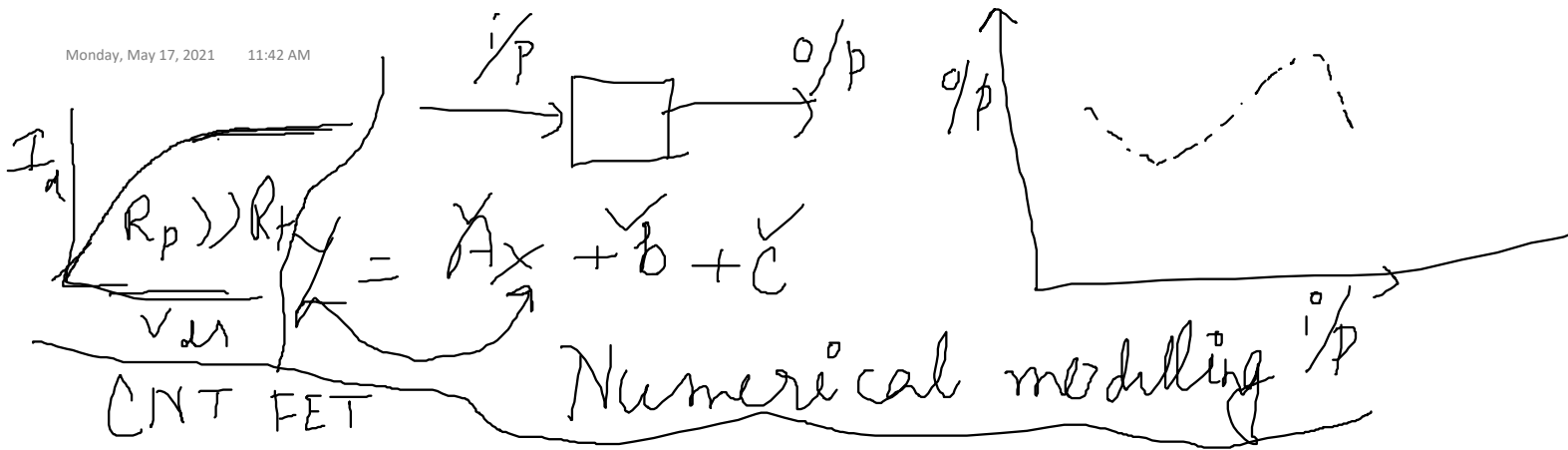
- ✓ 1) Differential equation (time domain approach) ✓
- 2) State space modelling (✓)
- ✓ 3) Transfer function (frequency domain approach) ✓

$t=0$ state variables

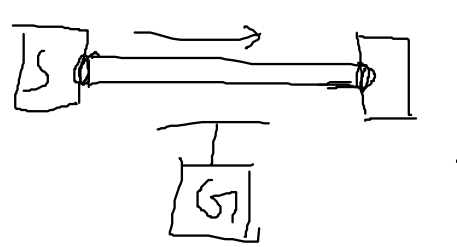
$t \geq 0$ i/p any time



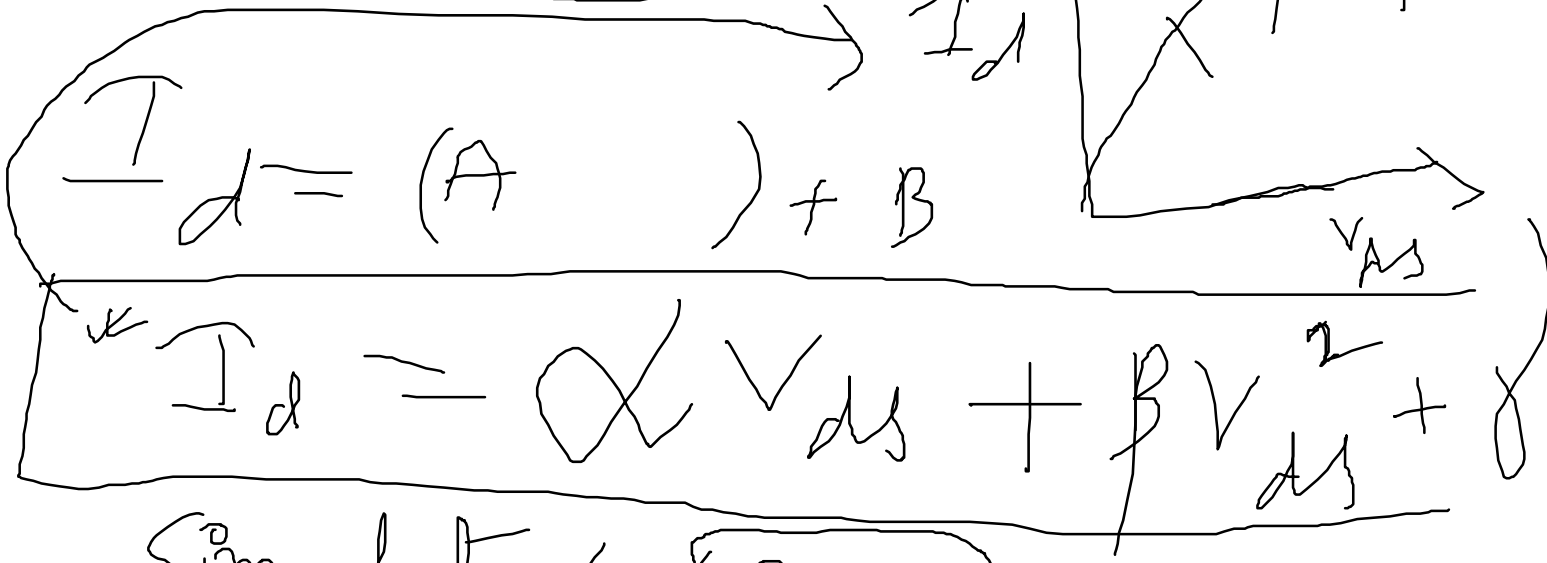
Numerical method modelling



compact model
physics based

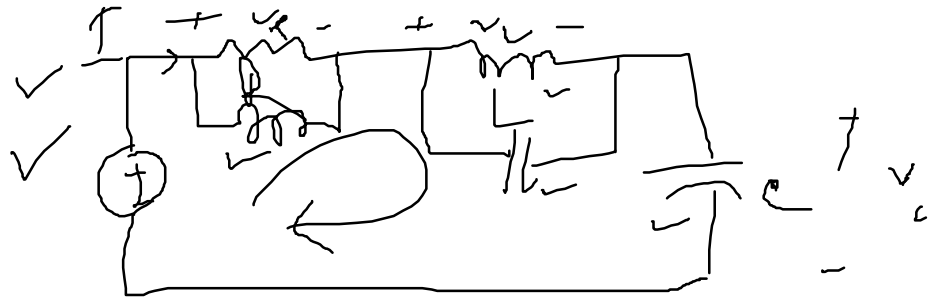


PTM



Simulator / BSIM

KVL



$$V = V_R + V_L + V_C$$

$$\frac{dv}{dt} = R \frac{dI}{dt} + L \frac{d^2 I}{dt^2} + \frac{1}{C} I$$

$$\Rightarrow \frac{d^2 I}{dt^2} + \frac{R}{L} \frac{dI}{dt} + \frac{1}{LC} I = \frac{dv}{dt}$$

4

$$\frac{I(s)}{V(s)} = \frac{1}{R + Ls + \frac{1}{Cs}}$$
$$= \frac{Cs}{1 + RCs + LCs^2}$$

$$\frac{d^2 I}{dt^2} + \frac{R}{L} \frac{dI}{dt} + \frac{1}{L} \frac{I}{C} = \frac{1}{L} \frac{dV}{dt}$$

$$t \geq 0$$

I have written a set of 2 1st order differential equation instead of the 2nd order DE.

$$\frac{dI_L}{dt} = -\frac{R}{L} I - \frac{1}{L} V_C + \frac{V}{L} \quad (1)$$

$$\frac{dV_C}{dt} = \frac{I_L}{C} \quad (2)$$

$$\begin{bmatrix} \frac{dI_L}{dt} \\ \frac{dV_C}{dt} \end{bmatrix} = \begin{bmatrix} -R/L & -1/L \\ 1/C & 0 \end{bmatrix} \begin{bmatrix} I_L \\ V_C \end{bmatrix} + \begin{bmatrix} 1/L \\ 0 \end{bmatrix} V$$