

Tutorial No-5

Q.1) suppose you have 6 containers whose weight are 50, 10, 30, 20, 60, 5 & ship whose capacity is 100. Find an optimal solution to this instance of container loading problem.

→ In container loading problem, all containers one of same size with constraint $\sum_{i=1}^m w_i x_i \leq C$

where $x_i = 0$ or 1 (0 if not included
1 if included)

w_i = weight of container

C = capacity

- To obtain optimal solution, we sort the given weight in increasing order

$$\text{weights} = \{5, 10, 20, 30, 50, 60\}$$

↑ ↑ ↑ ↑ ↑ ↑
 $w_6 \quad w_2 \quad w_4 \quad w_3 \quad w_1 \quad w_5$

stage 0 :- we include container 6
 $5 \times 1 \leq 100$

$$\text{solution set} = \{0, 0, 0, 0, 0, 1\}$$

stage 1 :- we include container 2
 $5 + (10 \times 1) \leq 100$

$$\text{solution set} = \{0, 1, 0, 0, 0, 1\}$$

Stage 8:- we include container 4,

$$15 + (20 \times 1) \leq 100$$

$$\text{solution set} = \{0, 1, 0, 1, 0, 1\}$$

Stage 9:- we include container 3

$$35 + (30 \times 1) \leq 100$$

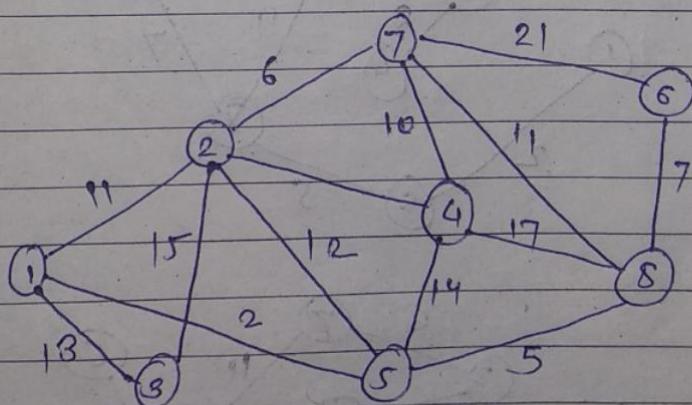
$$\text{solution set} = \{0, 1, 1, 1, 0, 1\}$$

Stage 5:- as weight of next container that we can include is 50. since $65 + 50$ is not less than 100, so it ~~is~~ not get included.

∴ maximum no. of container that are get loaded is 4. with weight 65.

$$\text{containers} \rightarrow \{2, 3, 4, 5\}$$

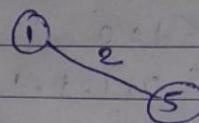
- Q.2) Compute a minimum cost spanning tree for the graph using
 (a) prim's algorithm
 (b) kruskal's algorithm.



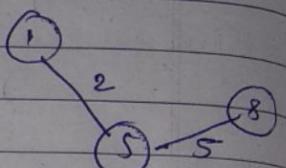
→ (a) prim's algorithm!

— select a minimum cost edge from graph
 then select a minimum cost edge
 from graph which is connected to
 already selected vertex.

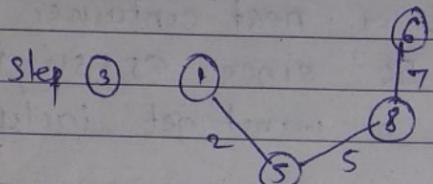
Step ①



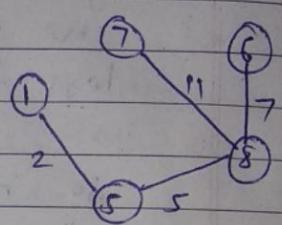
Step ②



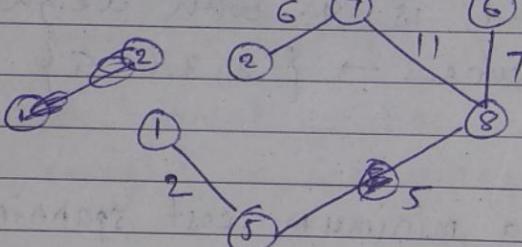
Step ③



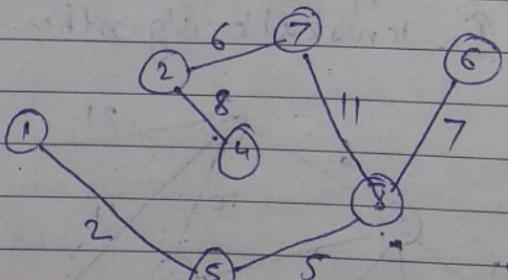
Step ④



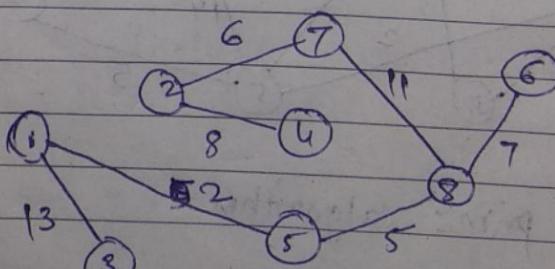
Step ⑤



Step ⑥

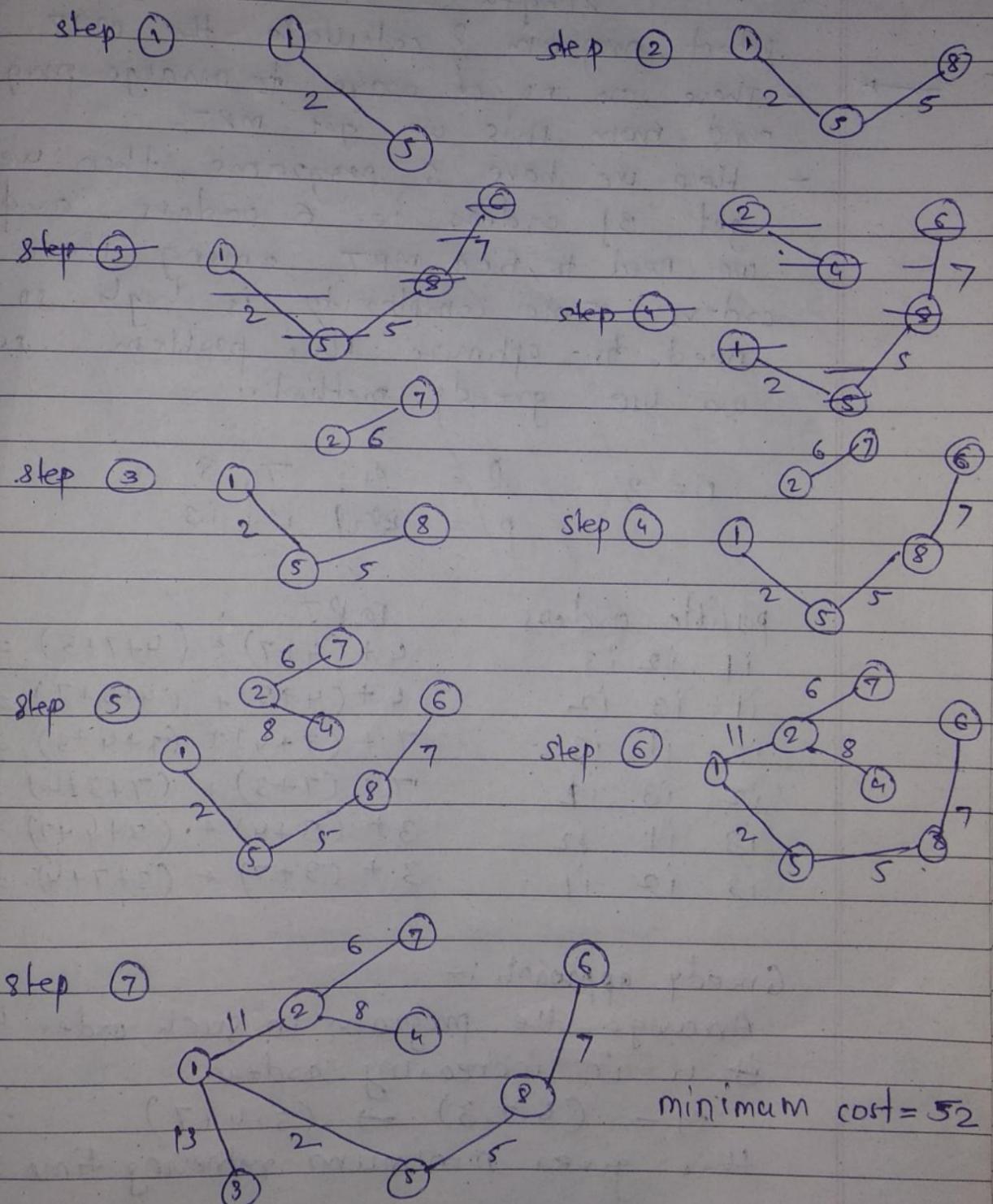


Step ⑦

minimum cost = ~~52~~ 52

② Kruskal's Algorithm:-

- always select minimum cost edge, but if it form cycle don't consider it. discard it.



Q. 3) consider the following data and find a permutation data that result in optimal solution. (minimum MRT)

program	i1	i2	i3
length	4	7	3

Select program & calculate the MRT.

- - There are no. of ways to arrange programs and from this we get MRT.
- Here we have 3 programs then we get $3!$ orders i.e. 6 orders and we need to find MRT among these orders. Time complexity is high so we need to optimize this problem. so we use greedy method.

$$n = 3 \quad l = 4, 7, 3 \\ p = i1, i2, i3$$

possible orders

i1 i2 i3

i1 i3 i2

i2 i1 i3

i2 i3 i1

i3 i1 i2

i3 i2 i1

MRT

$$4 + (4+7) + (4+7+3) = 29$$

$$4 + (4+3) + (4+3+7) = 25$$

$$7 + (7+4) + (7+4+3) = 32$$

$$7 + (7+3) + (7+3+4) = 31$$

$$3 + (3+4) + (3+4+7) = 24$$

$$3 + (3+7) + (3+7+4) = 27$$

Greedy approach :-

Arrange the program in such order that length it is in increasing order.

$$\text{eg} - (4, 7, 3) \rightarrow (3, 4, 7)$$

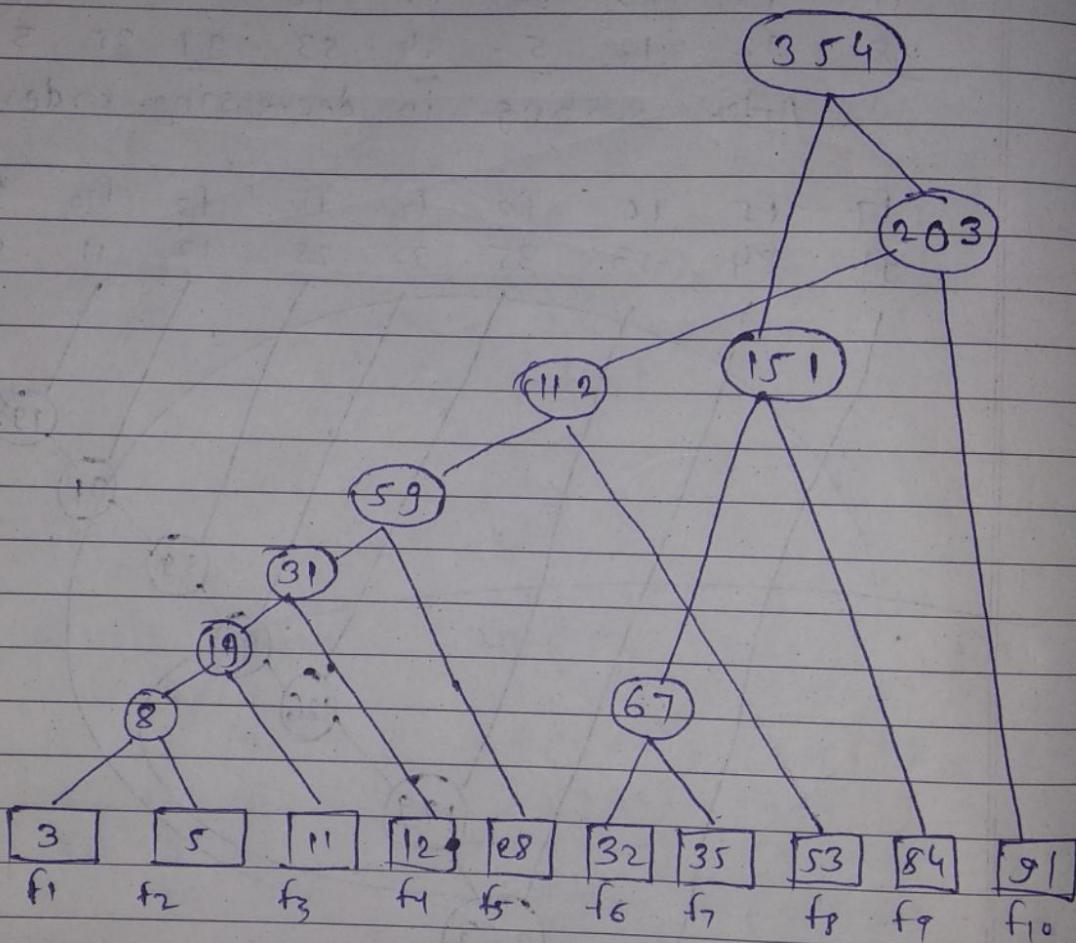
this gives minimum retrieving time = 24.

Q.4) find an optimal binary merge pattern for ten files whose length are

28, 32, 12, 5, 84, 53, 91, 35, 3 & 11

Here we use greedy method

- Always choose 2 files with lowest/least length

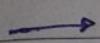
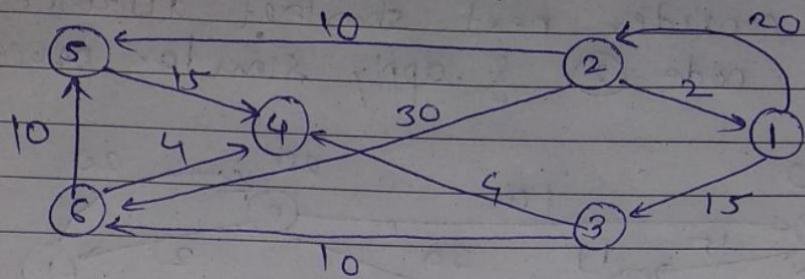


Total optimal cost

$$\begin{aligned}
 &= 8 + 19 + 31 + 59 + 67 + 112 + 151 + 203 + 354 \\
 &= \underline{\underline{1004}}
 \end{aligned}$$

Q.5)

use algo. shortest path to obtain in non decreasing order the lengths of the shortest paths from vertex 1 to all remaining vertices in the diagram.

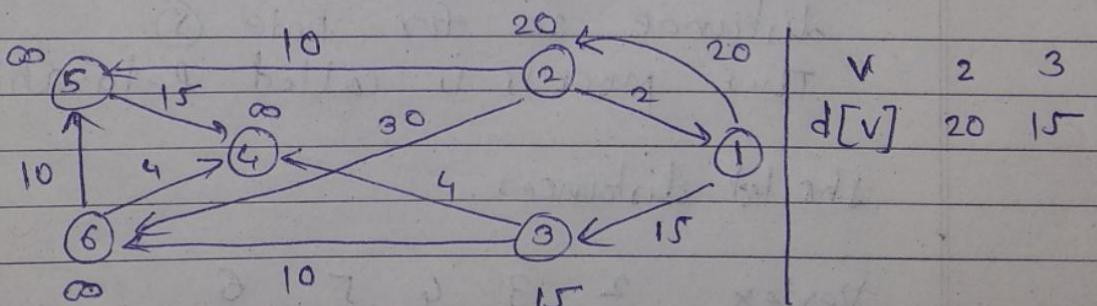


Here we use Dijkstra's algorithm

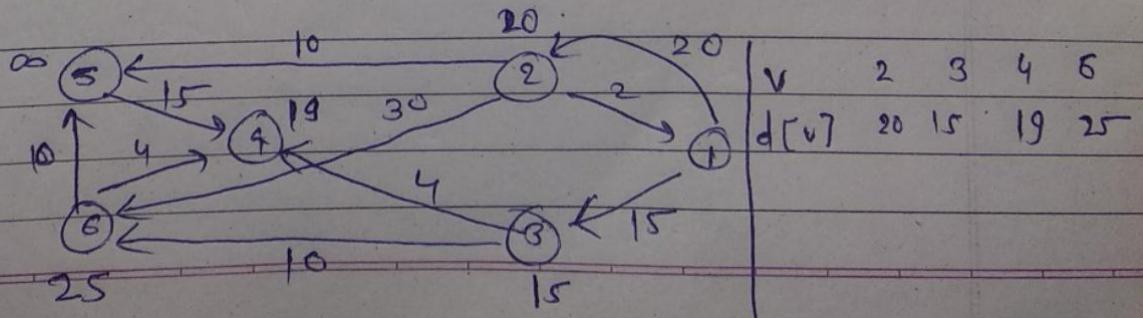
- Here we can apply Relaxation i.e.
- $$\text{if } (d[u] + c(u,v) < d[v]) \\ d[v] = d[u] + c[u,v]$$

source node 1

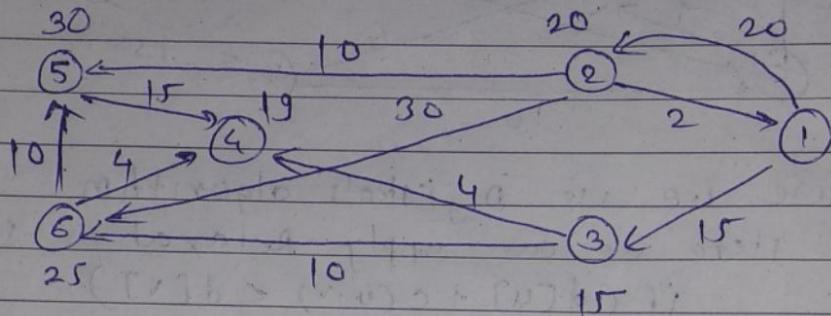
from this only node 2 & 3 is connected directly so vertices other than these are set to at ∞ distance.



now we consider node 3 among node 2 & 3 as its distance is lowest & apply similar process.



now next node with lowest distance from source node ① is node ④ but from node ④ there is no any outgoing edge so we consider next shortest distance node i.e. node ② & apply similar process.



As to reach node ⑤ we have to path one from node ③ to ⑥ and then ⑥ to ⑤ it cost 35.

Whereas from node ③ to nod ⑤ it cost 30. so we choose shortest path distance so for node ⑤.

This process is called Relaxation.

shortest distance:

Vertex	2	3	4	5	6
distance	20	15	19	30	25