

# Tutorial - 1

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Q.1)

→ space complexity of Binary search algorithm:

① Iterative -  $O(1)$

② Recursive -  $O(\log n)$  due to recursive call stack is used.

Q.2)

→ space complexity for Bubble sort:

① Space complexity is  $O(n)$  if array not sorted.

② Space complexity is  $O(n)$  if array is already sorted.

Q.3)

1)

frequency count

1) for ( $i = 1$  to  $n$ ) do  $\rightarrow n$

2) for ( $j = 1$  to  $i$ ) do  $\rightarrow n(n+1)/2$

3) for ( $k = 1$  to  $j$ ) do  $\rightarrow n(n+1)(n+2)/6$   
 $x = x + 1$

$$f(n) = n + \frac{n(n+1)}{2} + \frac{n(n+1)(n+2)}{6}$$

2)

$i = 1$

$f(n)$

while ( $i \leq n$ ) do  $\rightarrow n$

{

$x = x + 1;$

$\rightarrow n$

$i = i + 1;$

$\rightarrow n$

$$\underline{f(n) = 3n + 1}$$

$$f(n) = 3n + 1$$

Q. Q) calculate Time and space complexity :-

A] Algo Transpose ( $a_{1,n}$ )

{

for  $i=1$  to  $n-1$  do  $\rightarrow n-1$

for  $j=i+1$  to  $n$  do  $\rightarrow n-1 \times (n-1)$

{

$t = a[i, j]$ ;  $a[i, j] = a[j, i]$ ;  $a[j, i] = t$ ;

}

}

.

Time complexity =  $O(n^2)$

Space complexity =

additional space is  $O(1)$ ,

Auxiliary space used  $O(n^2)$  i.e. for  
space used for matrix.

B] Algo Mult ( $a_{1,b}, b_{1,n}$ )

{

for  $i=1$  to  $n$  do

$\rightarrow n$

for  $j=1$  to  $n$  do

$\rightarrow n \times n$

{

$c[i, j] = 0$ ;

for  $k=1$  to  $n$  do

$\rightarrow n \times n \times n$

$c[i, j] = c[i, j] + a[i, k] * b[k, j];$

}

}

.

$f(n) = n^3 + n^2 + n$

Time complexity =  $O(n^3)$

Space complexity =  $O(1)$  [additional]

=  $O(n^2)$  [Auxillary space]