

Tutorial No-5

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Q. 1) Suppose you have 6 containers whose weight are 30, 10, 80, 20, 60, 5 & ship whose capacity is 100. Find an optimal solution to this instance of container loading problem.

→ In container loading problem, all containers are of same size with constraint $\sum_{i=1}^n w_i x_i \leq C$

where $x_i = 0$ or 1 (0 if not included, 1 if included)

w_i = weight of container
 C = capacity

- To obtain optimal solution, we sort the given weight in increasing order.

weights = { 5, 10, 20, 30, 50, 60 }
 ↑ ↑ ↑ ↑ ↑ ↑
 w_6 w_2 w_4 w_3 w_1 w_5

stage 1 :- we include container 6
 $5 \times 1 \leq 100$

solution set = { 0, 0, 0, 0, 0, 1 }

stage 2 :- we include container 2
 $5 + (10 \times 1) \leq 100$

solution set = { 0, 1, 0, 0, 0, 1 }

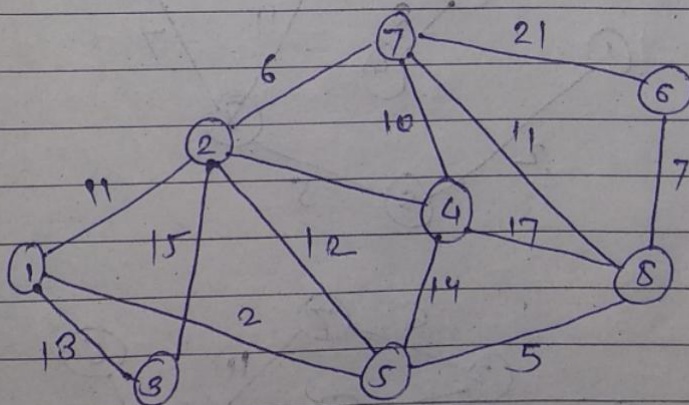
Stage 3:- we include container 4,
 $15 + (20 \times 1) \leq 100$
 solution set = $\{0, 1, 0, 1, 0, 1\}$

Stage 4:- we include container 3
 $35 + (30 \times 1) \leq 100$
 solution set = $\{0, 1, 1, 1, 0, 1\}$

Stage 5:- as weight of next container that we can include is 50. since $65 + 50$ is not less than 100, so it ~~was~~ not get included.

So maximum no. of container that are get loaded is 4. with weight 65.
 containers $\rightarrow \{2, 3, 4, 5\}$

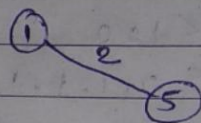
Q.2) Compute a minimum cost spanning tree for the graph using (a) prim's algorithm (b) kruskal's algorithm.



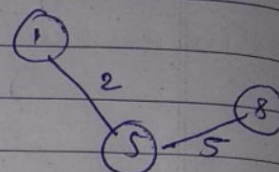
→ (a) prim's algorithm:

— select a minimum cost edge from graph
then select a minimum cost edge
from graph which is connected to
already selected vertex.

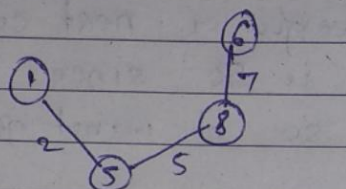
step ①



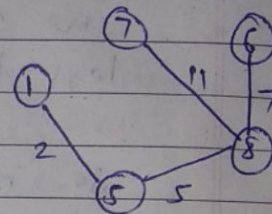
step ②



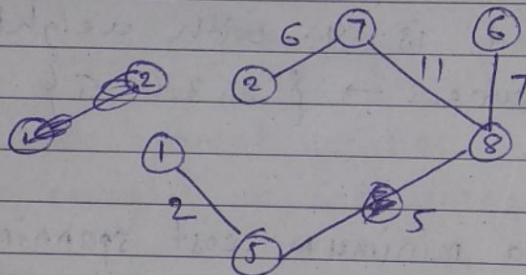
step ③



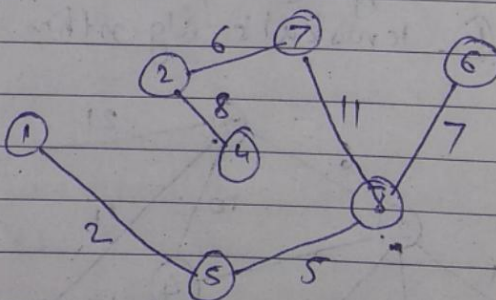
step ④



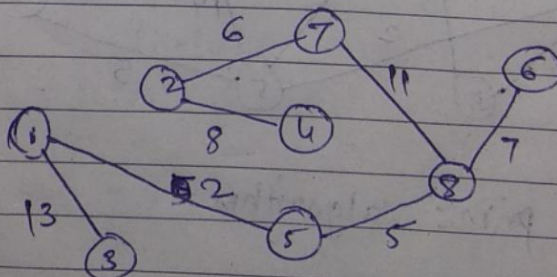
step ⑤



step ⑥



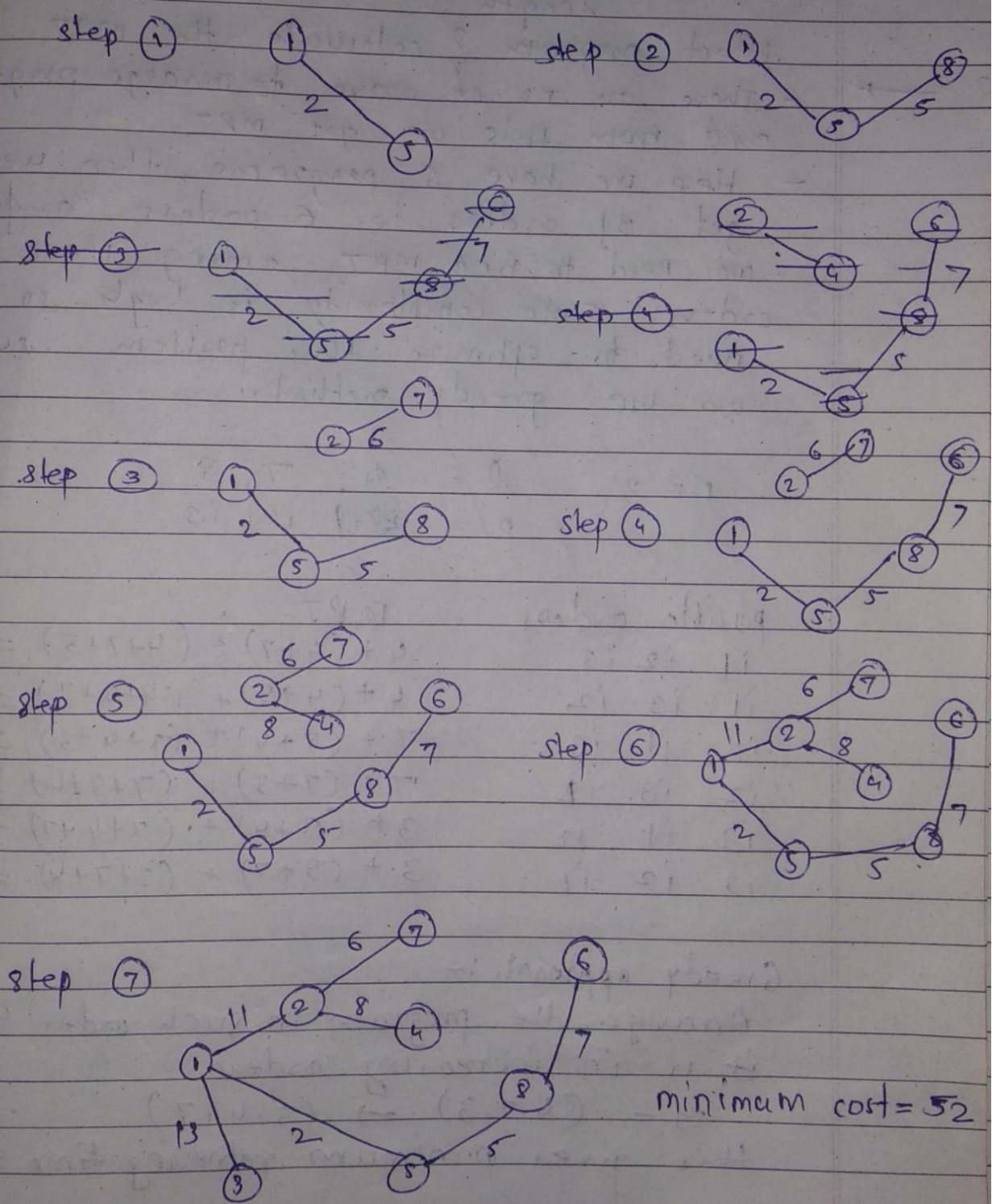
step ⑦



minimum cost = ~~52~~ 52

② Kruskal's Algorithm:-

- always select minimum cost edge, but if it form cycle don't considered it. discard it.



minimum cost = 52

Q.3) consider the following data and find a permutation data that result in optimal solution. (minimum MRT)

program	i1	i2	i3
length	4	7	3

select program & calculate the MRT.

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- There are no. of ways to arrange programs and from this we get MRT.
 - Here we have 3 programs then we get $3!$ orders i.e. 6 orders and we need to find MRT among these orders. Time complexity is high so we need to optimize this problem. so we use greedy method.

$$n = 3 \quad l = 4, 7, 3$$

$$p = i1, i2, i3$$

possible orders	MRT
i1 i2 i3	$4 + (4+7) + (4+7+3) = 29$
i1 i3 i2	$4 + (4+3) + (4+3+7) = 25$
i2 i1 i3	$7 + (7+4) + (7+4+3) = 32$
i2 i3 i1	$7 + (7+3) + (7+3+4) = 31$
i3 i1 i2	$3 + (3+4) + (3+4+7) = 24$
i3 i2 i1	$3 + (3+7) + (3+7+4) = 27$

Greedy approach :-

Arrange the program in such order that length it is in increasing order

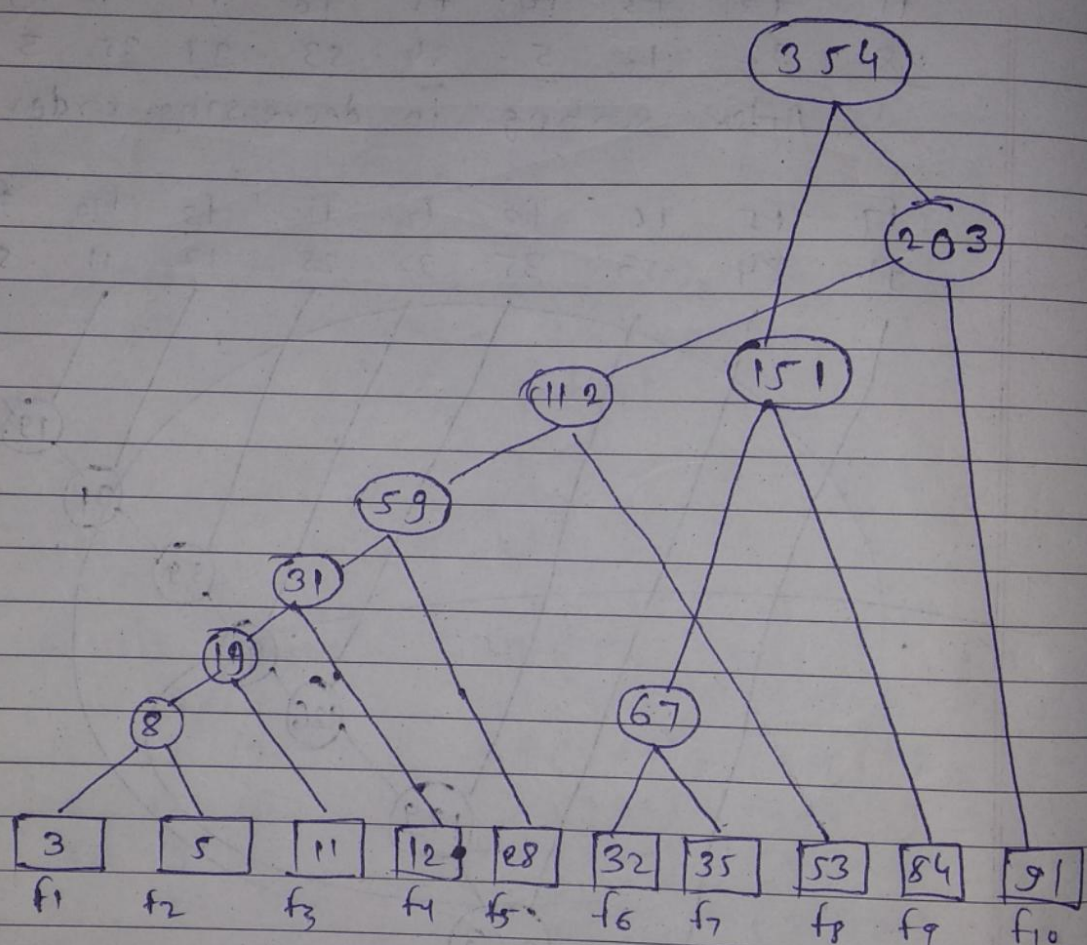
eg - $(4, 7, 3) \rightarrow (3, 4, 7)$

this gives minimum retrieving time = 24

Q.4) find an optimal binary merge pattern for ten files whose length are
28, 32, 12, 5, 84, 53, 91, 35, 3 & 11

Here we use greedy method

- Always choose 2 files with lowest/least length

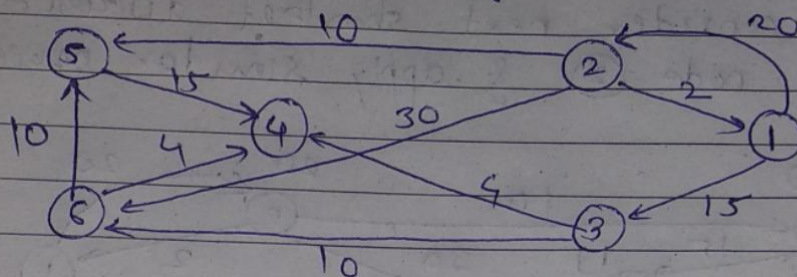


Total optimal cost

$$= 8 + 19 + 31 + 59 + 67 + 112 + 151 + 203 + 354$$

$$= \underline{\underline{1004}}$$

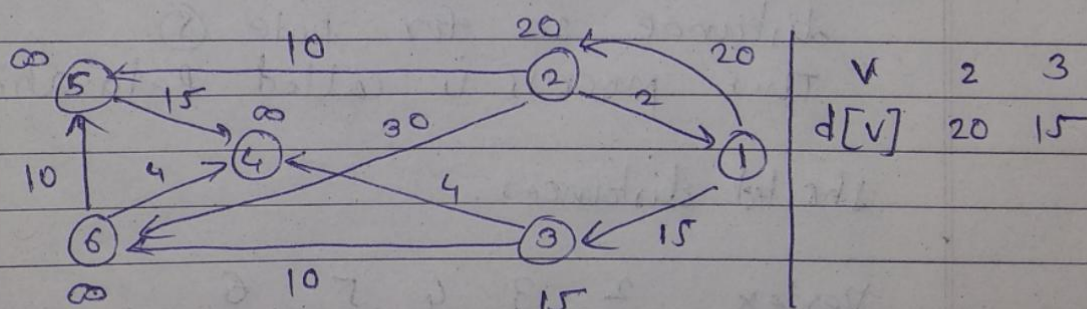
Q.5) use algo. shortest path to obtain in non decreasing order the lengths of the shortest paths from vertex 1 to all remaining vertices in the diagram.



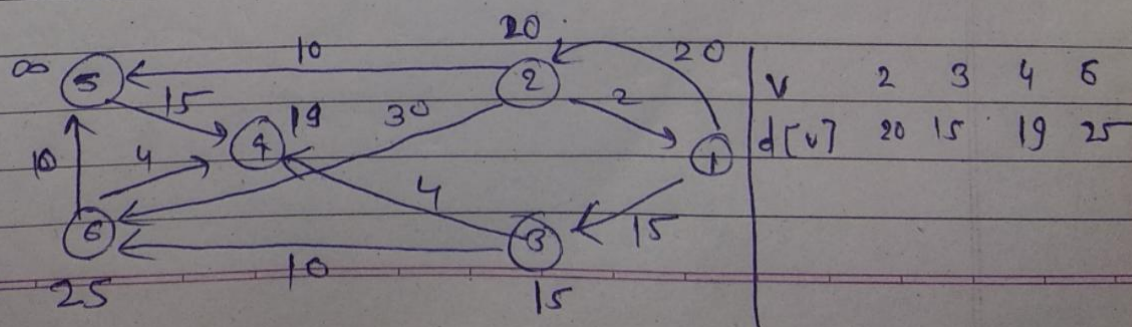
→ Here we use Dijkstra's algorithm
- Here we can apply Relaxation i.e.
if $(d[u] + c(u,v) < d[v])$
 $d[v] = d[u] + c(u,v)$

source node ①.

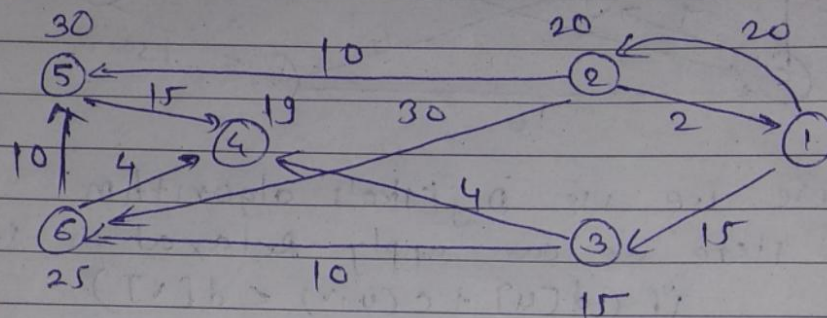
from this only node 2 & 3 is connected directly so vertices other than these are set to at ∞ distance.



now we consider node ③ among node ② & ③ as its distance is lowest & apply similar process.



now next node with lowest distance from source node ① is node ④ but from node ④ there is no any outgoing edge, so we consider next shortest distance node i.e. node ② & apply similar process.



As to reach node ⑤ we have to path one from node ③ to ⑥ and then ⑥ to ⑤ it cost 35.

whereas from node ③ to node ⑤ it cost 30. so we choose shortest path distance 30 for node ⑤.

This process is called relaxation.

shortest distances:

Vertex	2	3	4	5	6
distance	20	15	19	30	25