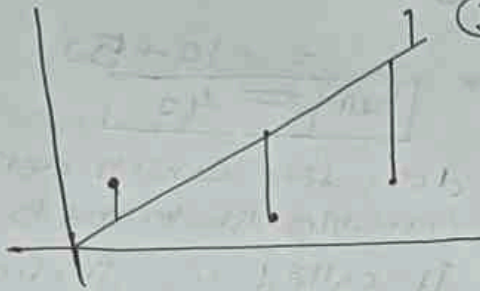


# \* Gradient descent \*

① Gradient descent is a first-order iterative optimization algorithm for finding a local minimum of a differentiable function.  
 Optimization means best performance achieved.

\* intuition: we want best fit line



\* we try to make minimum loss function

$$L = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$\hat{y}_i = mx_i + b$$

$$L = \sum_{i=1}^n (y_i - mx_i - b)^2$$

Data

cgpa	Package
-	-
-	-
-	-
-	-

This formula is depends on  $m$  &  $b$

$L(m, b)$

mean  $L$  is function depends on  $(m, b)$

Value of

② Suppose our data  $m$  value is known to us which is

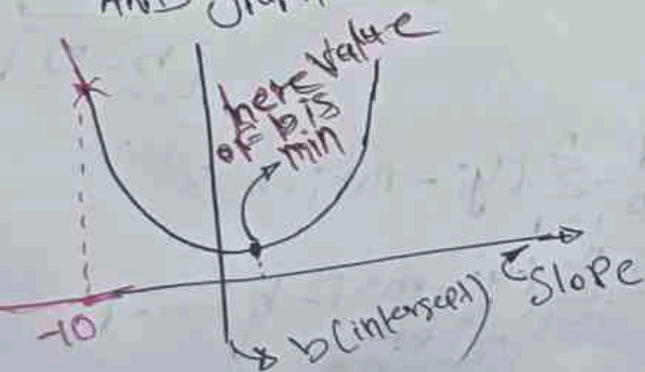
$$m = 78.35$$

$$L = \sum_{i=1}^n (y_i - 78.35x_i - b)^2$$

$L(b)$

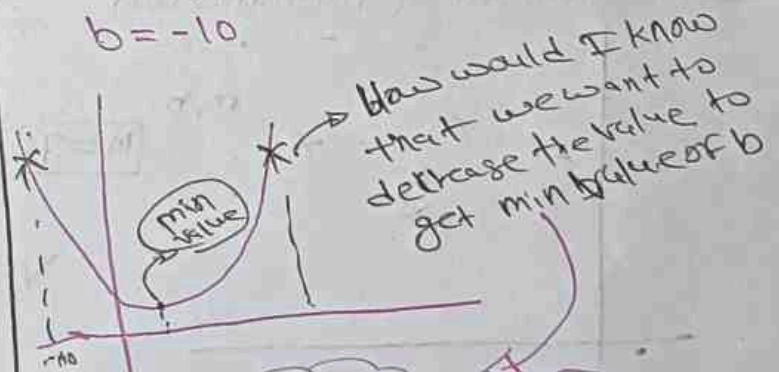
$L \rightarrow b^2$

\*  $L$  and  $b$  relationship is depends on square AND graph will be



\* Step 1: Select random value of  $b_{min}$

$$b = -10$$



Ans is Slope finding

Understanding of Slope

\* Slope: It is how line is tilted  
 Differentiation is a tool to find out Slope when graph of function is curve

Ex:  $y = x^2$



By differentiating

$$\frac{dy}{dx} = 2x$$

Slope(x) = 2x

x = 1 slope = 2

x = 2 slope = 4

x = -1 slope = -2

① Slope will tell us where is minimum value of b

\* IF slope is -ve then go forward

\* IF slope is +ve then go backward

\*\*\*

$$b_{new} = b_{old} - \text{slope}$$

b<sub>old</sub> = -10

assume slope

$$b_{new} = -10 - (-50)$$

$$= -10 + 50$$

$$b_{new} = 40$$

derivative which depends on two variables like m and b both then

it called as gradient or

Approximate gradient

② When to stop?

\*  $b_{new} - b_{old}$  is ~~very~~ becomes very small (around 0)

Then we will stop

\* Iteration 1000, 100, ...  
→ epochs

\* Mathematical Formulation



$$m = 78.35$$

\* Gradient descent

In terms of b

Step 1: Start with a random value suppose  $b = b'$

for i in epochs:

$$\eta = 0.01$$

$$b_{new} = b_{old} - \eta \times \text{slope}$$

$$b = 0$$

Here we find value of slope

$$L = \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$\frac{dL}{db} = \frac{d}{db} \left( \sum_{i=1}^n (y_i - \hat{y}_i)^2 \right)$$

$$\hat{y}_i = mx_i + b$$

$$\frac{d}{db} \sum_{i=1}^n (y_i - mx_i - b)^2$$

$$2 \sum_{i=1}^n (y_i - mx_i - b) \times -1$$

no b term it becomes 0

It means  
If we change  
b then how much  
change occurs  
in L



$$-2 \sum_{i=1}^n (y_i - mx_i - b)$$

← This is equation of slope

for  $b=0$

assume  $m = 78.35$

$$\text{Slope} = -2 \sum_{i=1}^n (y_i - 78.35 * x_i = 0)$$

Slope ( $b=0$ )

Code Time:-

from sklearn.datasets import make\_regression  
import numpy as np

← This is use to make dataset

$X, y = \text{make\_regression}(n\_samples=4, n\_features=1, n\_informative=1, n\_targets=1, noise=80, random\_state=13)$

rows

shape of x

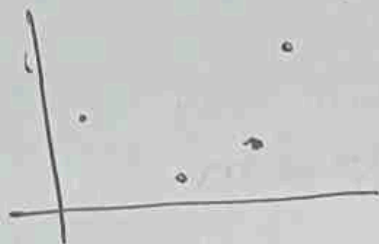
output + feature

import matplotlib.pyplot as plt

how much output

Randomly Not perfect linear data

plt.scatter(X, y)



from sklearn.linear\_model import LinearRegression

reg = LinearRegression()

reg.fit(X, y)

reg.coef\_ → min slope (m)

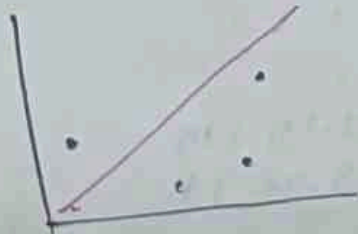
output → 78.35

reg.intercept\_

→ 26.1596 → min intercept value (b)

plt.scatter(X, y)

plt.plot(X, reg.predict(X), color='red')



# Lets apply Gradient Descent by assuming slope is constant

$$m = 78.35$$

# And let's assume the starting value of intercept  $b = 0$

$$y_{pred} = ((78.35 * x) + 0).reshape(4)$$

$$m = 78.35$$

$$b = 0$$

$$\text{loss\_slope} = -2 * \text{np.sum}(y - m * x.reshape(4) - b)$$

$$\text{loss\_slope}$$

$$\# \text{xslope} = \text{loss\_slope}$$

Now we want to do  $b_{\text{new}} = b_{\text{old}} - \eta * \text{xslope}$

$$\eta = 0.01$$

$$b = 0$$

$$\# \text{stepSize} = \eta * \text{loss\_slope}$$

$$b = b - \text{stepSize}$$

$$b$$

$$\rightarrow 20.92$$

\* Now we are making class to calculate only  $b$  for now \*

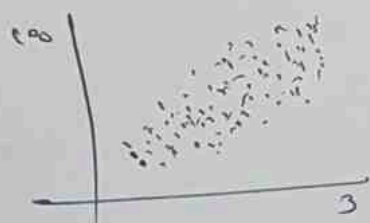
From sklearn.datasets import make\_regression

import matplotlib.pyplot as plt

import numpy as np

$X, y = \text{make\_regression}(n\_samples=100, n\_feature=1, n\_informative=1, n\_targets=1, \text{noise}=20)$

plt.scatter(X, y)



# Actual result for comparing our result after making own class to calculate  $b$ .

from sklearn.linear\_model import LinearRegression

lr = LinearRegression()

lr.fit(X, y)

print(lr.coef\_)

print(lr.intercept\_)

Output:-

$[29.19] m$

$[-3.35] b$

~~class~~  
~~n-def~~  $m = 29.19$

class GDRegressor:

def \_\_init\_\_(self, learning\_rate, epochs):

self.m = 29.19

self.b = -120

self.lr = learning\_rate

self.epochs = epochs

def fit<sup>self.sub</sup>(x, y):

# calculate the b using GD

for i in range(self.epochs):

loss\_slope = -2 \* np.sum(y - ~~self.m~~ x.ravel() - self.b)

self.b = self.b - (self.lr \* loss\_slope)

print(self.b)

gd.GDRegressor(0.01, 100)

\* Effect of learning rate \*

$\eta = 0.02$      $\eta = 0.1$      $\eta = 0.5$

if very low  
→ then very slow  
and more epochs

\* The universality of Gradient Descent

\* Now How to calculate m & b

Step 1: initiate random vals for m and b

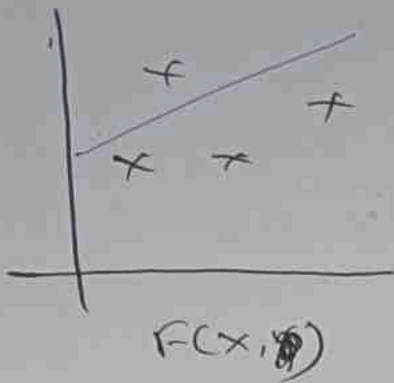
$m = 1$  and  $b = 0$

② epochs = 100    lr = 0.01

for i in epochs:

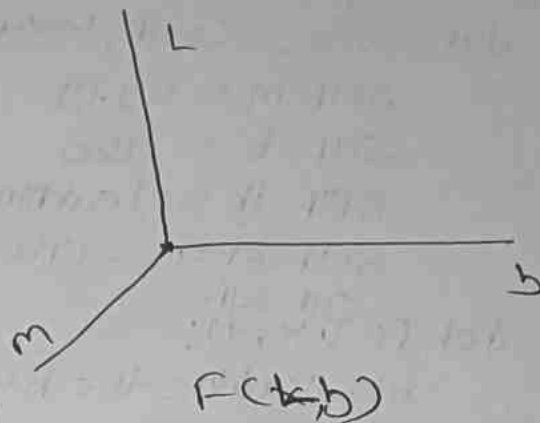
$b = b - \eta \text{slope}$   
 $m = m - \eta \text{slope}$  } both slopes are different





$$L = \sum_{i=1}^n (y_i - \hat{y}_i)^2 = \sum (y_i - mx_i - b)^2$$

$$L(m, b)$$



$$b\text{-slope} = \frac{\partial L}{\partial b}$$

$$m\text{-slope} = \frac{\partial L}{\partial m}$$

$$\sum (y_i - mx_i - b)^2$$

$$\frac{\partial L}{\partial b} = 2 \sum (y_i - mx_i - b)$$

$$\text{Slope}_b = -2 \sum (y_i - mx_i - b)$$

$$= \text{Slope}_b \text{ at } b=0$$

$$\frac{\partial L}{\partial m} = 2 \sum (y_i - mx_i - b) x_i$$

$$2 \sum (y_i - mx_i - b) x_i$$

$$\text{Slope}_m = 2 \sum_{i=1}^n (y_i - mx_i - b) x_i$$

$$\text{Slope}_m \text{ at } m=1$$

\* Improvement in code \*

Now data is little bit change

$X, y = \text{make\_regression}(n\text{-samples}=100, n\text{-features}=1,$   
 $n\text{-informative}=1, n\text{-targets}=1,$   
 $\text{noise}=20, \text{random\_state}=13)$

from sklearn.linear\_model import LinearRegression

lr = LinearRegression()

lr.fit(x, y)

Print(lr.coef\_) *#Value of m*

Print(lr.intercept\_) *#value of b*

→ [27.8280] *#m*

-2.2947 *#b*

*#This is calculating to Tally the ans with our class*

from sklearn.model\_selection import cross\_val\_score

np.mean(cross\_val\_score(lr, x, y, scoring='r2', cv=10))

Class GDRegressor:

def \_\_init\_\_(self, learning\_rate, epochs):

self.m = 100

self.b = -120

self.lr = learning\_rate

self.epochs = epochs

def fit(self, x, y):

for i in range(self.epochs):

loss\_slope\_b = -2 \* np.sum(y - self.m \* x.ravel() - self.b)

loss\_slope\_m = -2 \* np.sum((y - self.m \* x.ravel() - self.b) \* x.ravel())

self.b = self.b - (self.lr \* loss\_slope\_b)

self.m = self.m - (self.lr \* loss\_slope\_m)

Print(self.m, self.b)

gd = GDRegressor(0.001, 100)

gd.fit(x, y)

→ 27.8280, -2.254

*m*      *b*

# Also making function to Predict

```
def Predict(self, x)
```

```
    return self.m * x + self.b
```

```
from sklearn.model_selection import train_test_split
```

```
x_train, x_test, y_train, y_test = train_test_split(x, y, test-  
size=0.2, random_state=2)
```

```
y_pred = lt.Predict(x_test)
```

```
from sklearn.metrics import r2_score
```

```
r2_score(y_test, y_pred)
```

→ 0.63 → this is ~~the~~ before class

Now

```
gd.fit(x_train, y_train)
```

```
y_pred = gd.Predict(x_test)
```

```
from sklearn.metrics import r2_score
```

```
r2_score(y_test, y_pred)
```

→ 0.63 → out class result

(\*) Impact on gradient Descent of Hyperparameter, loss Function & Data.

① learning rate

② loss Function

③ Data.

① learning rate:-

① low LR: ① IF LR is 0.002

① Very small steps are getting

① more epoch value

① not much optimize



- ② Moderate LR: ① One optimize result  
 ②.2) ③ Not want more number of epochs  
 ④ Get faster result

- ③ High LR: ④ It get bigger and bigger step  
 ⑤.80 ⑤ And some-times it <sup>may</sup> not converge to minimum value of loss.

## ② Effect of loss function:

①  $L = \sum_{i=1}^n (y_i - \hat{y}_i)^2$  → This loss function is convex function

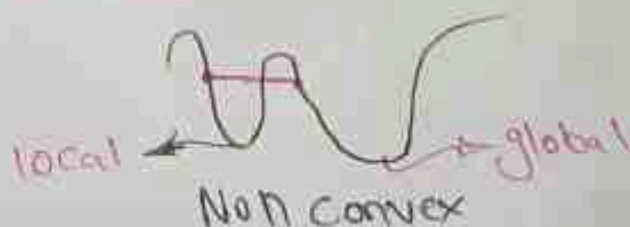
\* Now what is convex function

① IF we draw a line between two points that line never cross the function that function is called convex function.

Ex:



Non convex Ex.:



① In convex function there is only one minima and that is global minima

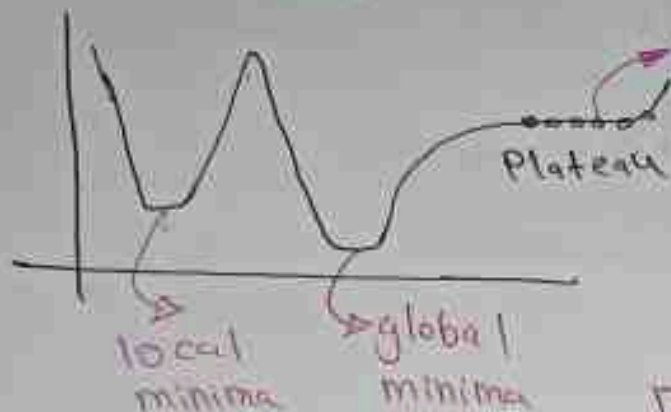
① In non convex function there is more than one minima we called them global minima and local minima

③ In Non convex function there are two problems

- ①
    - local minima is here:
    - more than 2 minima
- ↳ Solution may be converge on local minima.

our algo. converge here and we should not go anywhere.

② Plateau:-



To get out from Plateau there are we want to increase our epochs

⊛ And more time taken to train

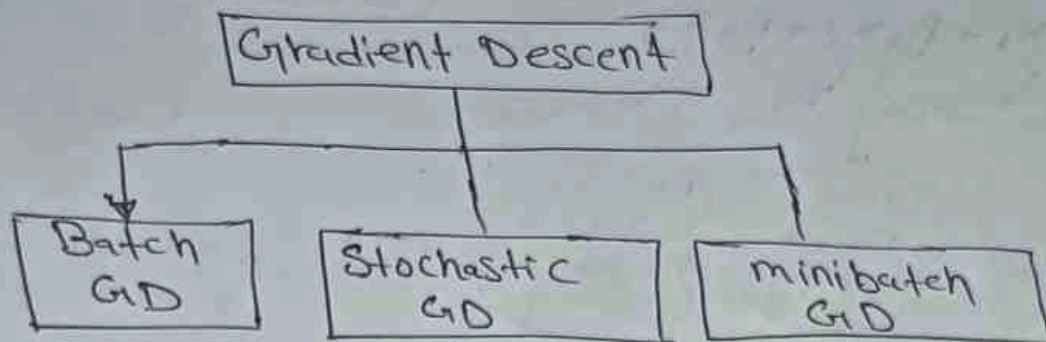
In 3D Plateau become Saddle Point

only Name change idea is same

⊛ Effect of Data:

• IF data is well scaled then our algorithm will fast converge towards the minima.

## \*Types of gradient descent\*



$$\left. \begin{aligned} m_n &= m_0 - \eta \times (\text{slope})_{m=0} \\ b_n &= b_0 - \eta \times (\text{slope})_{b=0} \end{aligned} \right\} \begin{array}{l} \text{We update the value of} \\ m \text{ \& } b \text{ by viewing all data} \\ \text{This is batch GD.} \end{array}$$

## \*Stochastic GD\*

⊙ In this we update the values of  $m$  &  $b$  by viewing single row

⊙ This is Fast

⊙ Suitable for big/large data

## \*mini batch GD\*

\*Fixed Batch size

\*If data is of 300 rows and batch size = 30  
Our values of  $m$  &  $b$  will change after 30 rows not after full data.

\*We already learn batch gradient descent to understand ~~the~~ gradient descent for two variables

we learn for: GyPa / IPa

Now we are learning Batch gradient descent for more than two variable

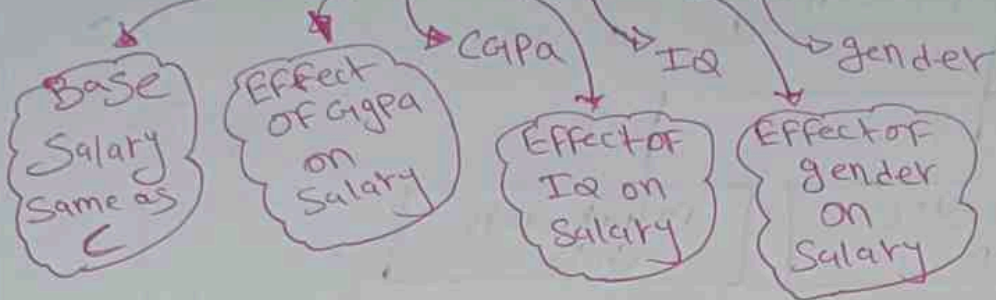
GyPa / IQ / gender / CPa

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$$



## \* Understand the equation \*

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$$



## \* N Dimensional Data \*

$$\{\beta_0, \beta_1, \beta_2, \dots, \beta_n\}$$

Values required to find the value of  $y$  Predict

## \* Mathematical Formulation \*

Gpa | IQ | IPa

$x_1$	$x_2$	$y$
8.1	93	3.2
7.5	95	3.5

$$y \text{ (IPa)} = \beta_0 + \beta_1 x_1 \text{ (Gpa)} + \beta_2 x_2 \text{ (IPa)}$$

Step 1: Start with random value

generally  $\beta_0 = 0, \beta_1, \beta_2 = 1$

Step 2: Epoch = 100, lr = 0.1

$$\beta_0 = \beta_0 - \eta \text{slope} \rightarrow \frac{\partial L}{\partial \beta_0}$$

$$\beta_1 = \beta_1 - \eta \text{slope} \rightarrow \frac{\partial L}{\partial \beta_1}$$

$$\beta_2 = \beta_2 - \eta \text{slope} \rightarrow \frac{\partial L}{\partial \beta_2}$$

Intercept

$$L(\beta_0, \beta_1, \beta_2)$$

$$L = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2 \quad \{\text{rows}=2, \text{cols}=2+\}$$

(MSE)

$$= \frac{1}{2} [(y_1 - \hat{y}_1)^2 + (y_2 - \hat{y}_2)^2]$$

$$\hat{y}_i = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2}$$

$$\hat{y}_1 = \beta_0 + \beta_1 x_{11} + \beta_2 x_{12}$$

$$\hat{y}_2 = \beta_0 + \beta_1 x_{21} + \beta_2 x_{22}$$

$x_1$	$x_2$	$y$
8.1	9.3	3.2
7.5	9.5	3.5

Annotations:  $x_{11}$  points to 8.1,  $x_{12}$  points to 9.3,  $y_1$  points to 3.2,  $y_2$  points to 3.5,  $x_{21}$  points to 7.5,  $x_{22}$  points to 9.5.

$$= \frac{1}{2} [(y_1 - (\beta_0 + \beta_1 x_{11} + \beta_2 x_{12}))^2 + (y_2 - (\beta_0 + \beta_1 x_{21} + \beta_2 x_{22}))^2]$$

$$\frac{\partial L}{\partial \beta_0} = \frac{1}{2} [2(y_1 - \hat{y}_1)(-1) + 2(y_2 - \hat{y}_2)(-1)]$$

$$\frac{\partial L}{\partial \beta_0} = -\frac{2}{2} [(y_1 - \hat{y}_1) + (y_2 - \hat{y}_2)]$$

for N rows

$$\frac{\partial L}{\partial \beta_0} = -\frac{2}{n} [(y_1 - \hat{y}_1) + (y_2 - \hat{y}_2) + (y_3 - \hat{y}_3) + \dots + (y_n - \hat{y}_n)]$$

$$\frac{\partial L}{\partial \beta_0} = -\frac{2}{n} \sum_{i=1}^n (y_i - \hat{y}_i)$$

→ This is give the value of slope

$$\beta_0 = \beta_0 - n(\text{slope})$$

This value is calculated by  $\frac{\partial L}{\partial \beta_0}$

\* Now Calculating of  $\beta_1$  slope \*

$$L = \frac{1}{2} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$L = \frac{1}{2} [(y_1 - \hat{y}_1)^2 + (y_2 - \hat{y}_2)^2]$$

$$L = \frac{1}{2} [(y_1 - \beta_0 - \beta_1 x_{11} - \beta_2 x_{21})^2 + (y_2 - \beta_0 - \beta_1 x_{21} - \beta_2 x_{22})^2]$$

$$\frac{\partial L}{\partial \beta_1} = \frac{1}{2} [2(y_1 - \hat{y}_1)(-x_{11}) + 2(y_2 - \hat{y}_2)(-x_{21})]$$

$$\boxed{\frac{\partial L}{\partial \beta_1} - \beta_1 x_{11} = -x_{11}}$$

$$\frac{\partial L}{\partial \beta_1} = \frac{-2}{n} [(y_1 - \hat{y}_1)(x_{11}) + (y_2 - \hat{y}_2)(x_{21}) + (y_3 - \hat{y}_3)(x_{31}) + \dots + (y_n - \hat{y}_n)(x_{n1})]$$

$$\boxed{\frac{\partial L}{\partial \beta_1} = \frac{-2}{n} \sum_{i=1}^n (y_i - \hat{y}_i) x_{i1}}$$

$x_{i1}$  is represent all values of Column 1

$x_1$	$x_2$	$y$
8.1	93	3.2
7.5	95	3.5

$$\boxed{\frac{\partial L}{\partial \beta_2} = \frac{-2}{n} \sum_{i=1}^n (y_i - \hat{y}_i) x_{i2}}$$

\* For m cols \*

$$\boxed{\frac{\partial L}{\partial \beta_m} = \frac{-2}{n} \sum_{i=1}^n (y_i - \hat{y}_i) x_{im}}$$



Class GDRegressor:

def \_\_init\_\_(self, learning\_rate=0.01, epochs=100):

self.coef\_ = None

self.intercept\_ = None

self.lr = learning\_rate

self.epochs = epochs

def fit(self, x\_train, y\_train):

self.intercept\_ = 0

self.coef\_ = np.ones(x\_train.shape[1])

for i in range(self.epochs):

# updating all the coef & intercept

First understand the intercept formula.

$$\frac{\partial L}{\partial \beta_0} = -\frac{2}{n} \sum_{i=1}^n (y_i - \hat{y}_i)$$

$$(y_i - \hat{y}_i) \rightarrow x$$

→ this is nothing but our y\_train

$$= -\frac{2}{n} \sum_{i=1}^n x$$

→ This is nothing but formula for calculating mean

understand calculation to finding y hat

x1	x2	x3	y
-1	-1	-1	-

→ for first row

$$\hat{y}_1 = \beta_0 + \beta_1 x_{11} + \beta_2 x_{12} + \beta_3 x_{13}$$

$$\hat{y}_2 = \beta_0 + \beta_1 x_{21} + \beta_2 x_{22} + \beta_3 x_{23}$$

$$\hat{y}_i = \beta_0 + [x_{i1} \ x_{i2} \ x_{i3}] \begin{bmatrix} \beta_1 \\ \beta_2 \\ \beta_3 \end{bmatrix}$$

$$\hat{y} = \beta_0 + \text{np.dot}(\text{coef\_}, \text{x\_train})$$

Formula becomes  $\beta_0 + \text{np.dot}(\text{x\_train}, \text{coef\_})$

(353, 10) (10, 1) \*\*\*\*  
x\_train shape coef shape (353, 1)

We can calculate for all values in x\_train by using vectorization

$$\hat{y} = \text{np.dot}(X_{\text{train}}, \text{self.coef\_}) + \text{self.intercept\_}$$

$$\text{intercept\_der} = -2 * \text{np.mean}(y_{\text{train}} - \hat{y})$$

$$\text{self.intercept\_} = \text{self.intercept\_} - (\text{self.it} * \text{intercept\_der})$$

# Now time to calculate coef-

For single:

$$\frac{\partial L}{\partial \beta_1}, \frac{\partial L}{\partial \beta_2}, \frac{\partial L}{\partial \beta_n}$$

~~Simple~~  
 (\*) How to find out this at game time?

$$\frac{\partial L}{\partial \beta_1} = -\frac{2}{n} \sum_{i=1}^n (y_i - \hat{y}_i) x_{i1}$$

$x_1$	$x_2$	$y$	$\hat{y}$
1	2	5	6
3	4	7	8

$$y = \begin{bmatrix} 5 \\ 7 \end{bmatrix} \quad \hat{y} = \begin{bmatrix} 6 \\ 8 \end{bmatrix}$$

$$y - \hat{y} = \begin{bmatrix} -1 \\ -1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} -4 + -3 \end{bmatrix}$$

$$\textcircled{-8}$$

$$\left[ \begin{bmatrix} y - \hat{y} \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \right] \times -\frac{2}{n}$$

$$\frac{\partial L}{\partial \beta_1} = \dots = \frac{\partial L}{\partial \beta_{10}}$$

$$= \left[ (y_i - \hat{y}_i) \times \text{train} \right] \times -\frac{2}{n}$$

$$\begin{matrix} \nearrow & \nwarrow \\ (353, 1)^T & (353, 10) \end{matrix}$$

$$(1, 353) \quad (353, 10)$$

$$(1, 10) \times -\frac{2}{n} = (1, 10) \rightarrow \text{coef\_der}$$

$$\text{Coef\_der} = -2 * \text{np.dot}((y\_train - y\_hat), x\_train) / x\_train.shape[0]$$

$$\text{self.coef\_} = \text{self.coef\_} - (\text{self.lr} * \text{coef\_der})$$

def predict(self, x\_test):

return np.dot(x\_test, self.coef\_) + self.intercept

gdr = GDRegressor(epochs=100, learning\_rate=0.5)

gdr.fit(x\_train, y\_train)

152.0135 [14.3891 -173.72 491.54 323.91,  
-39.32 -116.010 -194.04 103.38  
451.63 97.57]

y\_pred = gdr.predict(x\_test)

r2\_score(~~y\_test~~, y\_pred)

0.45



# \* Stochastic Gradient Descent \*

## \* Problem with Batch GD \*

$n = 1000$

$cols = 5 \rightarrow 6 \text{ Coefs}$

$Epoch = 50$

50

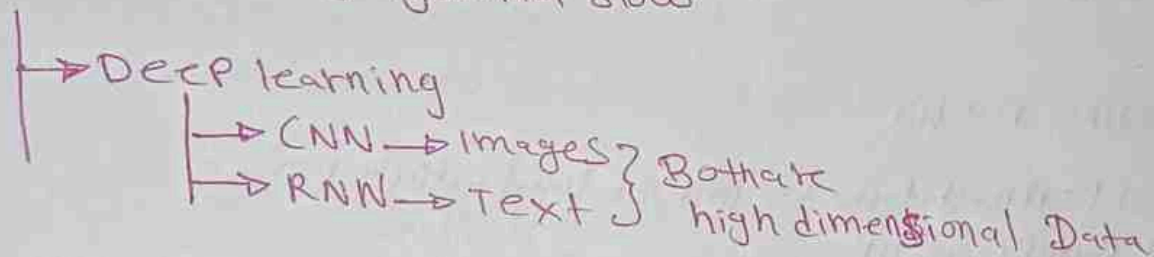
$1 \rightarrow 1000$

$6 \rightarrow 6000$

$6000 \times 50 = 300000$

derivatives  
want to calculate

① It makes algorithm slow



\* And In Deep Learning most of the time we are not use Batch GD

In coding Part we did vectorization to calculate  $\hat{y}$

$$\hat{y} = \text{np.dot}(X_{\text{train}}, \text{self.coef\_}) + \text{self.intercept\_}$$

In this we used numpy and avoid loop

\* When we are calculating  $\hat{y}$  we load full  $X_{\text{train}}$  data load on RAM.

\* And if data is very large then it could give (error) Not exactly error but system not support (Hardware Problem)

\* To resolve this all Problem we shifted toward Stochastic GD

\* In Batch gradient descent value of coef. is change after checking full data. only one time changes

\* In Stochastic we change value of coef. by seeing/checking a single row.

—————  $\rightarrow$  row update

\* In 1 single epoch n updates will do

- $\rightarrow$  faster convergence
- $\rightarrow$  row is select randomly
- $\rightarrow$  Not give steady (ans) soln

\* Now, coding Part \*

```
from sklearn.datasets import load_diabetes.  
import numpy as np
```

```
from sklearn.linear_model import LinearRegression
```

```
from sklearn.metrics import r2_score.
```

```
from sklearn.model_selection import train_test_split.
```

```
X, y = load_diabetes(return_X_y=True)
```

```
Print(X.shape)
```

```
Print(y.shape)
```

$\rightarrow (442, 10)$

$\rightarrow (442, )$

```
x(X, y = load_diabetes(return_X_y=True))
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y,  
                                                    test_size=0.2, random_state=2)
```

```
reg = LinearRegression()
```

```
reg.fit(X_train, y_train)
```

```
Print(reg.coef_) # m  $\rightarrow$   $[-3.16 \ -205.46 \ 516.68 \ 840.62 \ -835.54$ 
```

```
Print(reg.intercept_) # b  $\rightarrow 151.88$ 
```



$y\_pred = reg.predict(x\_test)$

$r2\_score(y\_test, y\_pred)$

→ 0.439988

\*Now we make our class to Predict Coefficient\*

Class SGDRegressor:

def \_\_init\_\_(self, learning\_rate=0.01, epochs=100):

self.coef\_ = None

self.intercept\_ = None

self.lr = learning\_rate

self.epochs = epochs

def fit(self, x\_train, y\_train):

self.intercept\_ = 0

self.coef\_ = np.ones(x\_train.shape[1])

for i in range(self.epochs):

for j in range(x\_train.shape[0]):

idx = np.random.randint(0, x\_train.shape[0])

y\_hat = np.dot(x\_train[idx], self.coef\_) + self.intercept\_

In BGD

$$\frac{\partial L}{\partial \beta_0} = \frac{-2}{m} \sum_{i=1}^m (y_i - \hat{y}_i)$$

1

collectively

Not required in SGD

\*for SGD\*

\*\*

$$\frac{\partial L}{\partial \beta_0} = -2 (y_i - \hat{y}_i)$$

intercept\_der = -2 \* (y\_train[idx] - y\_hat)

self.intercept\_ = self.intercept\_ - (self.lr \* intercept\_der)



Coef\_der.

$$\frac{\partial L}{\partial \beta_1} = -\frac{2}{n} \sum_{i=1}^n (y_i - \hat{y}_i) x_{i1}$$

↓  
In Batch GD

$$\frac{\partial L}{\partial \beta_1} = -2 (y_i - \hat{y}_i) x_{i1}$$

Coef\_der = -2 \* (y\_train[idx] - y\_hat), X\_train[idx]  
Self.coef\_ = Self.coef\_ - (Self.lr \* Coef\_der)

X\_train.shape

→ (353, 10)

⊛ Rule of matrix multiplication ⊛

A → (m × n) Shape

B → (n × p) Shape

C → (m × p) Shape

$$(353, 10) * (1, 1) = (10)$$

⊛ In this SGD Algorithm we converge to our minimum loss value by giving less number of epochs.

Sgd = SGDRegressor(learning\_rate=0.01, epochs=50)

Sgd.fit(X\_train, y\_train)

→ 150.8948 [54.28, -67.43 851.20 251.38 17.26  
-18.74 -165.85 123.27 314.84 123.52]

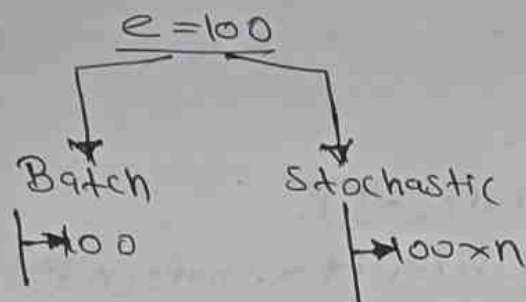
y\_pred = Sgd.predict(X\_test)

r2\_score(y\_test, y\_pred)

→ 0.4325

## \* Time comparison \*

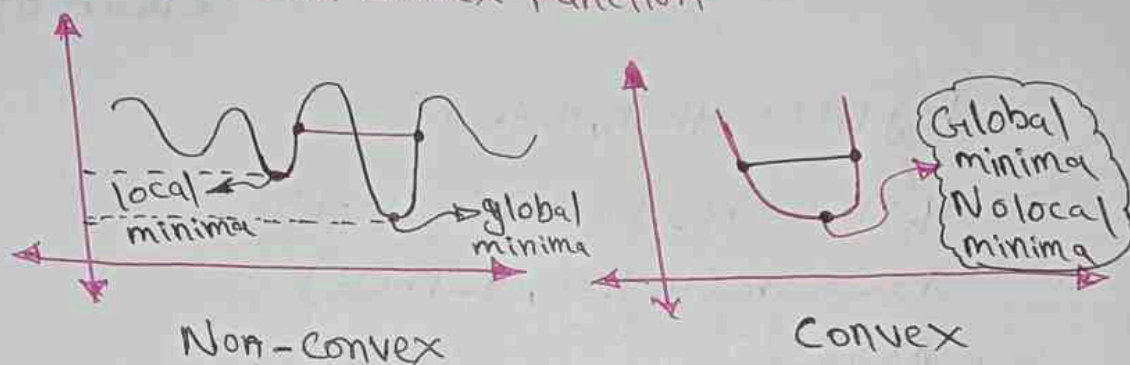
no. of epoch  $\rightarrow$  fixed



## \* When to use Stochastic GD

① Big data

② When we have non convex function



\* Because of stochastic nature of SGD it could be ~~how~~ get out from local minima (It has <sup>that</sup> velocity which is not stop it to local minima.)

## \* Problem with SGD

① In Stochastic GD, even after reaching the optimal solution, the algorithm continues to update parameters and does not stop exactly at the minimum.

\* To solve this problem we use one concept called learning schedule.

\* learning schedule: Learning rate schedule is a strategy in machine learning where the learning rate is changed (usually reduced) during training instead of keeping it constant, so that the model learn fast at the beginning and converges smoothly later.

\*Code:-

$t_0, t_1 = 5, 50$

```
def learning_rate(t):  
    return  $t_0 / (t + t_1)$ 
```

```
for i in range(epochs):
```

```
    for j in range(x.shape[0]):
```

```
        lr = learning_rate( $i * x.shape[0] + j$ )
```

\* Using Sklearn SGD Regressor \*

```
from sklearn.linear_model import SGDRegressor
```

```
reg = SGDRegressor(max_iter=100, learning_rate='constant',  
                    eta=0.01)
```

```
reg.fit(x_train, y_train)
```

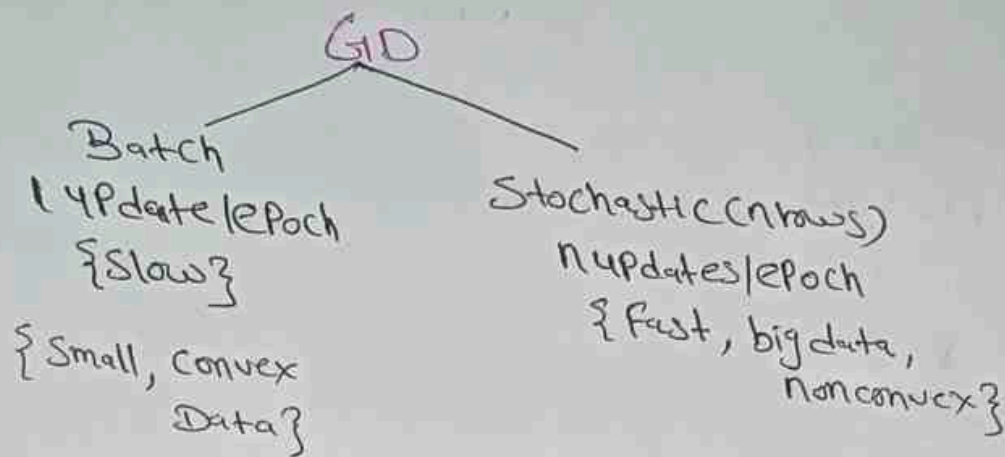
```
y_pred = reg.predict(x_test)
```

```
r2_score(y_test, y_pred)
```

→ 0.4305



## \* Mini-Batch Gradient Descent \*



Minibatch GD: Combination of Batch & Stochastic GD

Batch  $\rightarrow$  Group of rows

$n=1000$   
 $\rightarrow$  Batches  $\rightarrow$  100  $\rightarrow$  TB  $\rightarrow$  10

Batches updates/epochs

1000  $\rightarrow$  10  $\rightarrow$  Batches  $\rightarrow$  10 updates

### \* Coding Part \*

```
from sklearn.datasets import load_diabetes
```

```
import numpy as np
```

```
from sklearn.linear_model import LinearRegression
```

```
from sklearn.metrics import r2_score
```

```
from sklearn.model_selection import train_test_split  
import random
```

```
X, y = load_diabetes(return_X_y=True)
```

```
print(X.shape)
```

```
print(y.shape)
```

$\rightarrow$  442, 10  
(442,)

$X_{\text{-train}}, X_{\text{-test}}, Y_{\text{-train}}, Y_{\text{-test}} = \text{train\_test\_split}(X, Y, \text{test\_size}=0.2, \text{random\_state}=2)$

`reg = LinearRegression()`

`reg.fit(X_train, Y_train)`

`Print(reg.coef_)`

`Print(reg.intercept_)`

→  $\begin{bmatrix} -9.160 & -205.46 & 516.68 & 340.62 & -895.54 & 561.21 \\ 153.88 & 126.73 & 861.12 & 52.41 & 151.88 \end{bmatrix}$

151.88

`Y_Pred = reg.predict(X_test)`

`r2score = (Y_test, Y_Pred)`

→ 0.4399

`class MBGDRegressor:`

`def __init__(self, batch_size, learning_rate=0.01, epochs=100):`

`self.coef_ = None`

`self.intercept_ = None`

`self.lr = learning_rate`

`self.epochs = epochs`

`self.batch_size = batch_size`

`def fit(self, X_train, Y_train):`

`self.intercept_ = 0`

`self.coef_ = np.ones(X_train.shape[1])`

`for i in range(self.epochs):`

`for j in range(int(X_train.shape[0] / self.batch_size)):`

`idx = random.sample(range(X_train.shape[0]),`

$$y\_hat = np.dot(x\_train[idx], self.coef_) + self.intercept\_$$

$$intercept\_der = -2 * np.mean(y\_train[idx] - y\_hat)$$

$$coef\_der = -2 * np.dot((y\_train[idx] - y\_hat), x\_train[idx])$$

$$self.coef\_ = self.coef\_ - (self.lr * coef\_der)$$

Print(self.intercept\_, self.coef\_)

def Predict(self, x\_test)

return np.dot(x\_test, self.coef\_) + self.intercept\_

mbt = MBGDRegressor(batch\_size = int(x\_train.shape[0]/10),  
learning\_rate = 0.01,  
epochs = 100)

mbt.fit(x\_train, y\_train)

→ 154.8374 [38.40 -142.67 457.28 303.60 -17.99  
-85.81 -192.04 116.18 407.24 105.80]

y\_pred = mbt.predict(x\_test)

r2\_score(y\_test, y\_pred)

→ 0.45188

\* How to use MBGD in sklearn \*

from sklearn.linear\_model import SGDRegressor

sgd = SGDRegressor(learning\_rate='constant', eta0=0.2)

# Partial\_fit(x, y, sample\_weight=None)

↳ Using this we can pass subset of x\_train, y\_train



batch-size = 35

for i in range(100)

idx = random-sample(range(x-train.shape[0]), batch-size)

Sgd.Partial-Fit(X-train[idx], y-train[idx])

Sgd.Coeff-

•  $\rightarrow [49.19, -67.84, 338.57, 247.97, 25.30, -24.71,$   
 $-155.45, 116.19, 312.91, 133.36]$

Sgd.intercept-

$\rightarrow 148.61$

y-Pred = Sgd.Predict(X-test)

r2\_score(y-test, y-Pred)

$\rightarrow 0.4271$