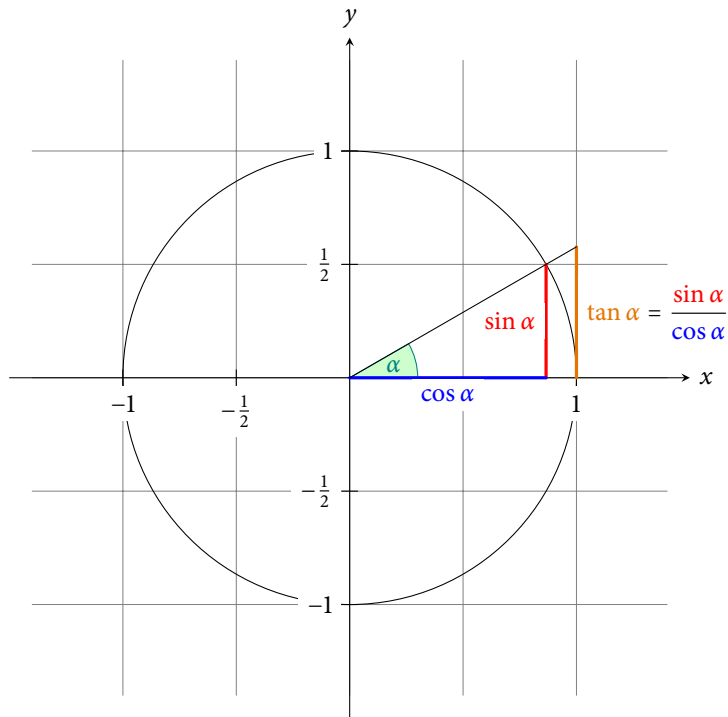


## 1 A TRIGONOMETRY EXAMPLE



The **angle**  $\alpha$  is  $30^\circ$  in the example ( $\pi/6$  in radians). The **sine of**  $\alpha$ , which is the height of the red line, is

$$\sin \alpha = \frac{1}{2}.$$

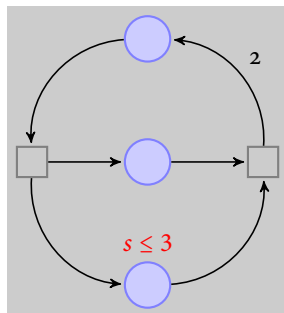
By the Theorem of Pythagoras we have  $\cos^2 \alpha + \sin^2 \alpha = 1$ . Thus the length of the blue line, which is the **cosine of**  $\alpha$ , must be

$$\cos \alpha = \sqrt{1 - \frac{1}{4}} = \frac{1}{2}\sqrt{3}.$$

This shows that **tan**  $\alpha$ , which is the height of the orange line, is

$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{1}{\sqrt{3}}.$$

## 2 PETRI-NETS



replacement  
of the **capacity**  
by **two places**  
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