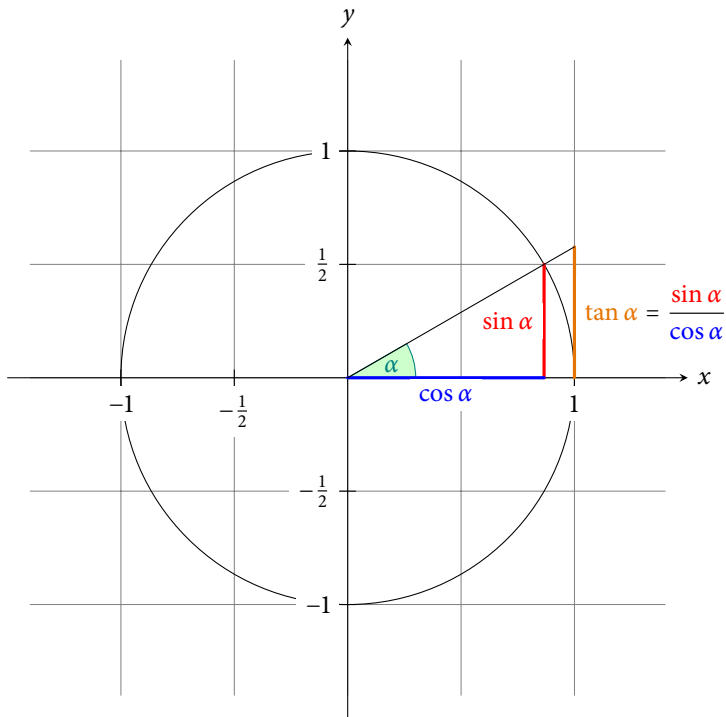


1 A TRIGONOMETRY EXAMPLE



The **angle** α is 30° in the example ($\pi/6$ in radians). The **sine of** α , which is the height of the red line, is

$$\sin \alpha = \frac{1}{2}.$$

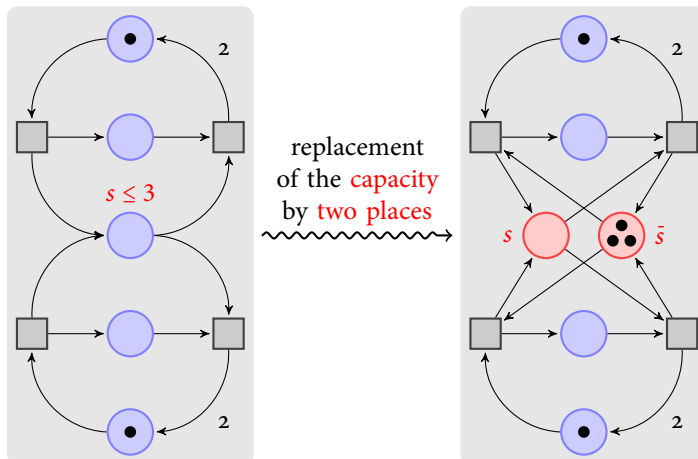
By the Theorem of Pythagoras we have $\cos^2 \alpha + \sin^2 \alpha = 1$. Thus the length of the blue line, which is the **cosine of** α , must be

$$\cos \alpha = \sqrt{1 - \frac{1}{4}} = \frac{1}{2}\sqrt{3}.$$

This shows that **tan** α , which is the height of the orange line, is

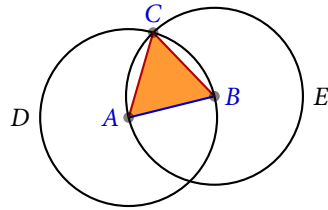
$$\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{1}{\sqrt{3}}.$$

2 PETRI-NETS



3 EUCLID'S ELEMENTS

3.1 Book I, Proposition I



Proposition I

To construct an *equilateral triangle* on a given *finite straight line*.

Let *AB* be the given *finite straight line*. It is required to construct an *equilateral triangle* on the *straight line AB*.

Describe the circle *BCD* with center *A* and radius *AB*. Again describe the circle *ACE* with center *B* and radius *BA*. Join the *straight lines CA* and *CB* from the point *C* at which the circles cut one another to the points *A* and *B*.

Now, since the point *A* is the center of the circle *CDB*, therefore *AC* equals *AB*. Again, since the point *B* is the center of the circle *CAE*, therefore *BC* equals *BA*. But *AC* was proved equal to *AB*, therefore each of the straight lines *AC* and *BC* equals *AB*. And things which equal the same thing equal one another, therefore *AC* also equals *BC*. Therefore the three straight lines *AC*, *AB*, and *BC* equal one another. Therefore the *triangle ABC* is equilateral, and it has been constructed on the given finite *straight line AB*.

3.2 Book I, Proposition II

