## Solution of 11.16.3.14

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Question:- If the letters of the word ASSASSI-NATION are arranged at random. Find the Probability that

- (a) Four S's come consecutively in the word
- (b) Two I's and two N's come together
- (c) All A's are not coming together
- (d) No two A's are coming together

**Solution:** Number of letters in word 'ASSASSINA-TION' = 13

Letter's are 3A's, 4S's, 2I's, 2N's, 1T's and 1O's

Total ways of arranging letters =  $\frac{13!}{3!4!2!2!}$ (1)

(a) Let X be a random variable such that

$$X = \begin{cases} 1, & \text{If All } S's \text{ are together as a unit} \\ 0, & \text{otherwise} \end{cases}$$
 (2)

Then,

$$p_X(1) = \frac{\frac{10!}{3!2!2!}}{\frac{13!}{3!4!2!2!}}$$

$$= \frac{2}{143}$$
(4)

(b) Let Y be a random variable such that

$$Y = \begin{cases} 1, & 2I's \text{ and } 2N's \text{ together} \\ 0, & \text{otherwise} \end{cases}$$
 (5)

Then,

$$p_{Y}(1) = \frac{\frac{10!4!}{3!4!2!2!}}{\frac{13!}{3!4!2!2!}}$$

$$= \frac{2}{143}$$
(6)

(c) Let Z be a random variable suct that

$$Z = \begin{cases} 0, & \text{All } A's \text{ together} \\ 1, & \text{Only } 2A's \text{ together} \\ 2, & \text{No } 2A's \text{ are together} \end{cases}$$
 (8)

Then,

(d)

$$p_Z(0) = \frac{\frac{11!}{4!2!2!}}{\frac{13!}{3!4!2!2!}}$$

$$= \frac{1}{26}$$
(9)

$$=\frac{1}{26}\tag{10}$$

$$\implies p_Z^{'}(0) = 1 - \frac{1}{26}$$
 (11)

$$=\frac{25}{26}$$
 (12)

$$p_Z(2) = \frac{\frac{11!10!}{3!8!4!2!2!}}{\frac{13!}{3!4!2!2!}}$$
(13)  
=  $\frac{15}{26}$  (14)

$$=\frac{15}{26}$$
 (14)