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Solution of 1.3.2

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Question:- We are given the three vertices of a triangle (A, B, C) $.D_1$ is a point on line BC such that AD is perpendicular to BC. Find the equation of AD.

Solution:

$$\mathbf{A} = \begin{pmatrix} 1 \\ -1 \end{pmatrix} \tag{1}$$

$$\mathbf{B} = \begin{pmatrix} -4\\6 \end{pmatrix} \tag{2}$$

$$\mathbf{C} = \begin{pmatrix} -3\\ -5 \end{pmatrix} \tag{3}$$

From Question 1.3.1 we got normal vector of $AD(\mathbf{n})$:-

$$\mathbf{n} = \begin{pmatrix} -1\\11 \end{pmatrix} \tag{4}$$

Now, normal form of line AD is:-

$$\mathbf{n}^{\mathsf{T}}(\mathbf{x} - \mathbf{A}) = 0 \tag{5}$$

$$\mathbf{n}^{\mathsf{T}}\mathbf{x} = \mathbf{n}^{\mathsf{T}}\mathbf{A} \tag{6}$$

$$\begin{pmatrix} -1 & 11 \end{pmatrix} \mathbf{x} = \begin{pmatrix} -1 & 11 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \tag{7}$$

$$\begin{pmatrix} -1 & 11 \end{pmatrix} \mathbf{x} = -12 \tag{8}$$

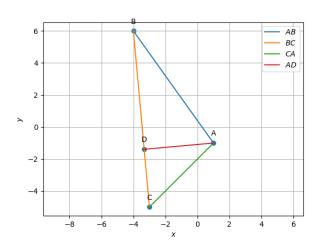


Fig. 0. Line AD