

Maths 30/3, 2015

DHRUV PARASHAR

1 SECTION A

- 1.1. In Figure 1.1, a tower AB is 20 m high and BC, its shadow on the ground, is $20\sqrt{3}$ m long. Find the Sun's altitude.

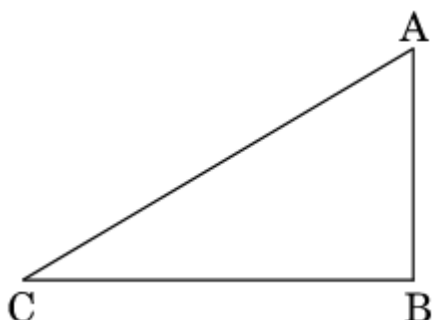


Fig. 1.1.

- 1.2. Two different dice are tossed together. Find the probability that the product of the two numbers on the top of the dice is 6.
- 1.3. If the quadratic equation

$$px^2 - 2\sqrt{5}px + 15 = 0$$

has two equal roots, then find the value of p .

- 1.4. In 1.4, PQ is a chord of a circle with centre O and PT is a tangent. If $\angle QPT = 60^\circ$, Find $\angle PRQ$.

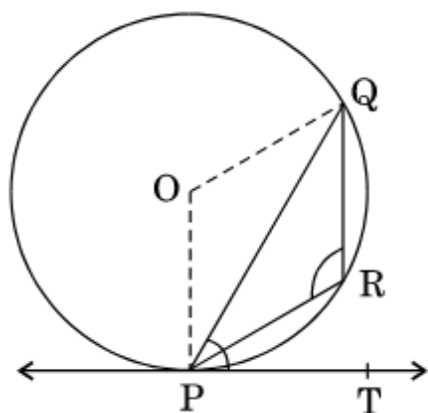


Fig. 1.4.

2 SECTION B

- 2.1. In an AP, if

$$S_5 + S_7 = 167$$

$$S_{10} = 235$$

then find the AP, where S_n denotes the sum of its first n terms.

- 2.2. The points

$$A = \begin{pmatrix} 4 \\ 7 \end{pmatrix}$$

$$B = \begin{pmatrix} p \\ 3 \end{pmatrix}$$

$$C = \begin{pmatrix} 7 \\ 3 \end{pmatrix}$$

are the vertices of a right triangle, right-angled at B. Find the value of p .

- 2.3. In Figure 2.3, two tangents RQ and RP are drawn from an external point R to the circle with centre O. If $\angle PRQ = 120^\circ$, then prove that $OR = PR + RQ$.

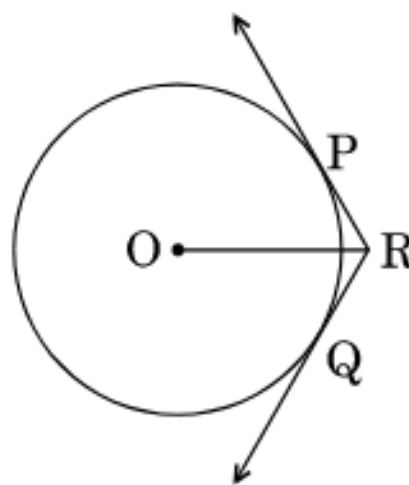


Fig. 2.3.

- 2.4. In Figure 2.4, a triangle ABC is drawn to circumscribe a circle of radius 3 cm, such that the segments BD and DC are respectively

of lengths 6 cm and 9 cm. If the area of $\triangle ABC$ is 54cm^2 , then find the lengths of sides AB and AC.

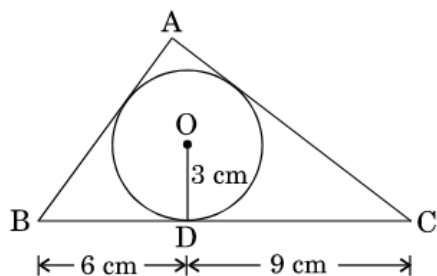


Fig. 2.4.

2.5. Find the relation between x and y if the points

$$\begin{aligned} A &= \begin{pmatrix} x \\ y \end{pmatrix} \\ B &= \begin{pmatrix} -5 \\ 7 \end{pmatrix} \\ C &= \begin{pmatrix} -4 \\ 5 \end{pmatrix} \end{aligned}$$

are collinear.

2.6. Solve the following quadratic equation for x:

$$4x^2 + 4bx - (a^2 - b^2) = 0$$

3 SECTION C

3.1. Due to sudden floods, some welfare associations jointly requested the government to get 100 tents fixed immediately and offered to contribute 50% of the cost. If the lower part of each tent is of the form of a cylinder of diameter 4.2 m and height 4 m with the conical upper part of same diameter but of height 2.8 m, and the canvas to be used costs Rs. 100 per sq. m, find the amount, the associations will have to pay. What values are shown by these associations? [Use $\pi = \frac{22}{7}$]

3.2. A hemispherical bowl of internal diameter 36 cm contains liquid. This liquid is filled into 72 cylindrical bottles of diameter 6 cm. Find the height of the each bottle, if 10% liquid is wasted in this transfer.

3.3. A cubical block of side 10 cm is surmounted by a hemisphere. What is the largest diameter that the hemisphere can have? Find the cost of painting the total surface area of the solid

so formed, at the rate of Rs. 5 per 100 sq. cm. [Use $\pi = 3.14$]

3.4. 504 cones, each of diameter 3.5 cm and height 3 cm, are melted and recast into a metallic sphere. Find the diameter of the sphere and hence find its surface area. [Use $\pi = \frac{22}{7}$]

3.5. Solve for x :

$$\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$$

3.6. The angle of elevation of an aeroplane from a point A on the ground is 60° . After a flight of 15 seconds, the angle of elevation changes to 30° . If the aeroplane is flying at a constant height of $1500\sqrt{3}$ m, find the speed of the plane in km/hr.

3.7. Find the area of the minor segment of a circle of radius 14 cm, when its central angle is 60° . Also find the area of the corresponding major segment. [Use $\pi = \frac{22}{7}$]

3.8. The 13^{th} term of an AP is four times its 3^{rd} term. If its fifth term is 16, then find the sum of its first ten terms.

3.9. Find the coordinates of a point P on the line segment joining

$$A = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$B = \begin{pmatrix} 6 \\ 7 \end{pmatrix}$$

such that $AP = \frac{2}{5}AB$.

3.10. A bag contains, white, black and red balls only. A ball is drawn at random from the bag. If the probability of getting a white balls is $\frac{3}{10}$ and that of black ball is $\frac{2}{5}$, then find the probability of getting a red ball. If the bag contains 20 black balls, then find the total number of balls in the bag.

4 SECTION D

4.1. At a point A, 20 metres above the level of water in a lake, the angle of elevation of a cloud is 30° . The angle of depression of the reflection of the cloud in the lake, at A is 60° . Find the distance of the cloud from A.

4.2. A card is drawn at random from a well-shuffled deck of playing cards. Find the probability that the card drawn is

- a) a card of spade or an ace.
- b) a black king.
- c) neither a jack nor a king.
- d) either a king or a queen

4.3. In 4.3, PQRS is a square lawn with side PQ = 42 metres. Two circular flower beds are there on the sides PS and QR with centre at O, the intersection of its diagonals. Find the total area of the two flower beds (shaded parts).

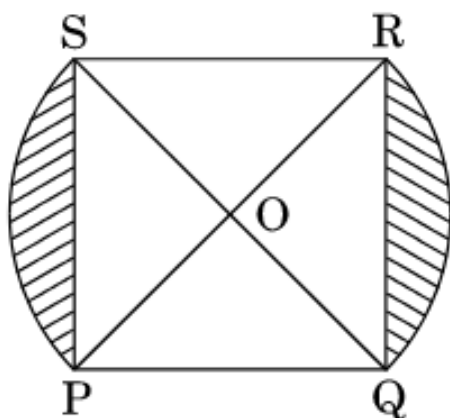


Fig. 4.3.

- 4.4. From each end of a solid metal cylinder, metal was scooped out in hemispherical form of same diameter. The height of the cylinder is 10 cm and its base is of radius 4.2 cm. The rest of the cylinder is melted and converted into a cylindrical wire of 1.4 cm thickness. Find the length of the wire. [Use $\pi = \frac{22}{7}$]
- 4.5. The diagonal of a rectangular field is 16 metres more than the shorter side. If the longer side is 14 metres more than the shorter side, then find the lengths of the sides of the field.
- 4.6. Prove that the lengths of the tangents drawn from an external point to a circle are equal.
- 4.7. Prove that the tangent drawn at the mid-point of an arc of a circle is parallel to the chord joining the end points of the arc.
- 4.8. A truck covers a distance of 150 km at a certain average speed and then covers another 200 km at an average speed which is 20 km per hour more than the first speed. If the truck covers the total distance in 5 hours, find the first speed of the truck.
- 4.9. An arithmetic progression 5, 12, 19, ... has 50 terms. Find its last term. Hence find the sum of its last 15 terms.

4.10. Construct a triangle ABC in which AB = 5 cm, BC = 6 cm and $\angle ABC = 60^\circ$. Now construct another triangle whose sides are $\frac{5}{7}$ times the corresponding sides of $\triangle ABC$.

4.11. Find the values of k for which the points

$$A = \begin{pmatrix} k+1 \\ 2k \end{pmatrix}$$

$$B = \begin{pmatrix} 3k \\ 2k+3 \end{pmatrix}$$

$$C = \begin{pmatrix} 5k-1 \\ 5k \end{pmatrix}$$

are collinear.