

Find Last Occurrence

Code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for (int i = 0; i < n; i++) {
        arr[i] = scn.nextInt();
    }
    int target = scn.nextInt();
    System.out.println(BSUB(arr, n, target));
}

public static int BSUB(int[] arr, int n, int target) {
    int i = 0;
    int j = n - 1;
    while ( i <= j ) {
        int mid = (i + j) / 2;
        if ( target == arr[mid] ) {
            if ( mid + 1 < n && arr[mid] == arr[mid + 1] ) {
                i = mid + 1;
            } else {
                return mid;
            }
        } else if ( target < arr[mid] ) {
            j = mid - 1;
        } else {
            i = mid + 1;
        }
    }
    return -1;
}
```

$$\underline{\underline{T.C = O(\log N)}}$$

$$\underline{\underline{S.C = O(1)}}$$

Find The Index of Rotation (distinct)

arr = [8, 9, 10, 11, 12, 1, 2, 3, 4, 5, 6, 7]

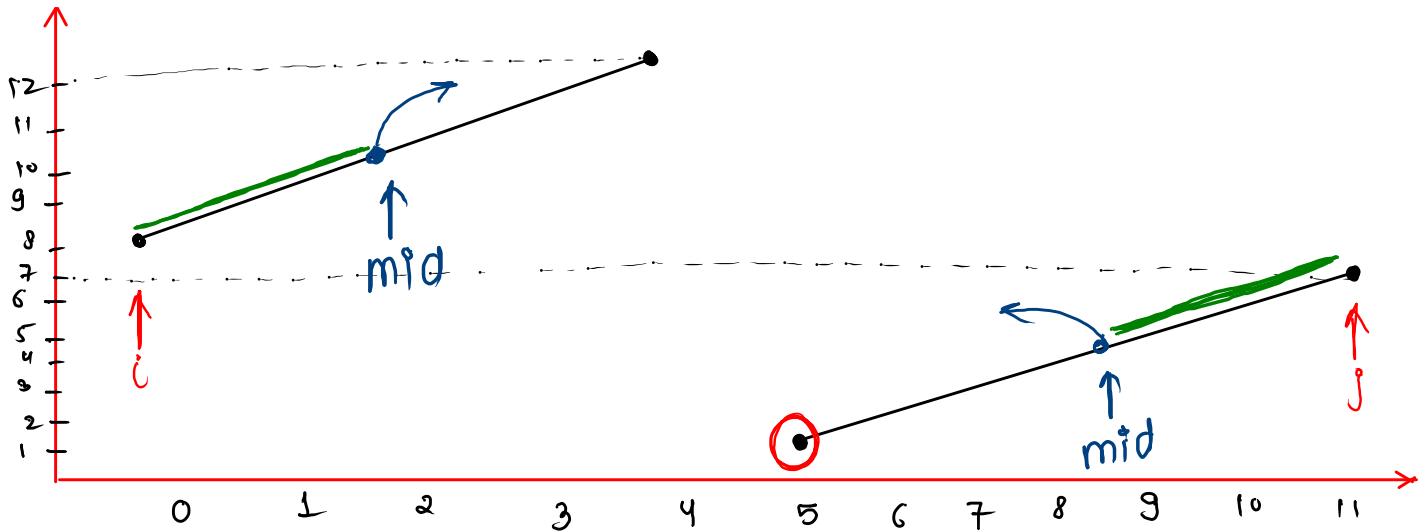
Indices: 0 1 2 3 4 5 6 7 8 9 10 11

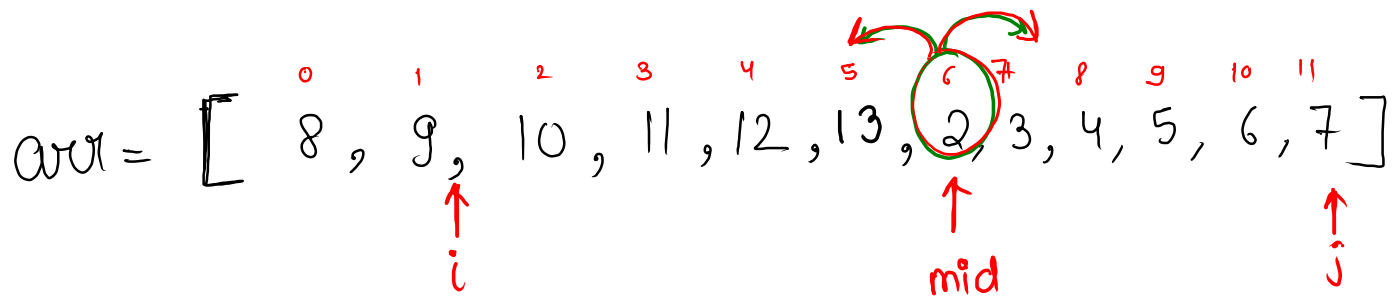
Annotations:
 - Red arrows point to index 0 (labeled 'i'), index 4 (labeled 'mid'), and index 11 (labeled 'j').
 - Blue arrows show a search path from index 5 to index 4, then to index 5, and finally to index 4.

ans = 4

target = smallest element idex

my goal





```

i = 0, j = n - 1;
while ( i <= j )
    mid = (i + j) / 2;
    next = (mid + 1) % n;
    prev = (mid - 1 + n) % n;
    if (arr[mid] <= arr[prev] && arr[mid] <= arr[next]) {
        return mid - 1;
    } else if (arr[mid] <= arr[j]) {
        j = mid - 1;
    } else if (arr[mid] >= arr[i]) {
        i = mid + 1;
    }
}

```

Note:-

$$\text{clockwise rotation} = \underline{\underline{(x \% n)}}$$

size
↙

$$\text{anti-clockwise rotation} = \underline{\underline{(x + n) \% n}}$$

code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    int[] arr = new int[n];
    for (int i = 0; i < n; i++) {
        arr[i] = scn.nextInt();
    }
    System.out.println(findIndex(arr, n));
}

public static int findIndex(int[] arr, int n) {
    int i = 0;
    int j = n - 1;
    while ( i <= j ) {
        int mid = (i + j) / 2;
        int prev = (mid - 1 + n) % n;
        int next = (mid + 1) % n;
        if ( arr[mid] <= arr[prev] && arr[mid] <= arr[next] ) {
            return mid - 1;
        } else if ( arr[mid] <= arr[j] ) {
            j = mid - 1;
        } else if ( arr[mid] >= arr[i] ) {
            i = mid + 1;
        }
    }
    return -1;
}
```

Find Square Root

$$n = 64, \quad n = 79$$

$$ans = 8$$

$$ans = 8.76 \\ = 8$$

(Note:- Binary Search can be applied on an imaginary range as well)

$$\underline{\underline{n = 30}}$$

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 30

↑
j

↑
i

↑

mid

$$i = 1$$

$$j = 30$$

$$mid = \cancel{15} \cancel{7} \cancel{3} \cancel{5} 6$$

$$\underline{\underline{ans = j}}$$

$$mid * mid == n$$

$$\underline{mid * mid < n}, \quad i = mid + 1;$$

$$\underline{mid * mid > n}, \quad j = mid - 1;$$

dry
run

$n = 48$ ↑
mid
1 6 7 8 9 11 12 23 24 48
↑ ↑
j i

$i = 1, j = n;$

while ($i \leq j$) {

 int mid = $(i + j) / 2;$

 if ($\text{mid} * \text{mid} == n$) {

 a [return mid;]

 } else if ($\text{mid} * \text{mid} < n$) {

 b [$i = \text{mid} + 1;$]

 } else if ($\text{mid} * \text{mid} > n$) {

 c [$j = \text{mid} - 1;$]

 }

}

$T.C = O(\log N)$

code

```
public static void main(String[] args) {
    Scanner scn = new Scanner(System.in);
    int n = scn.nextInt();
    System.out.println(findSqrt(n));
}

public static int findSqrt(int n) {
    int i = 1;
    int j = n;
    while ( i <= j ) {
        int mid = ( i + j ) / 2;
        if ( mid * mid == n ) {
            return mid;
        } else if ( mid * mid < n ) {
            i = mid + 1;
        } else if ( mid * mid > n ) {
            j = mid - 1;
        }
    }
    return j;
}
```

$T.C = O(\log N)$

$S.C = O(1)$

use j as an answer when looking for just smaller element.