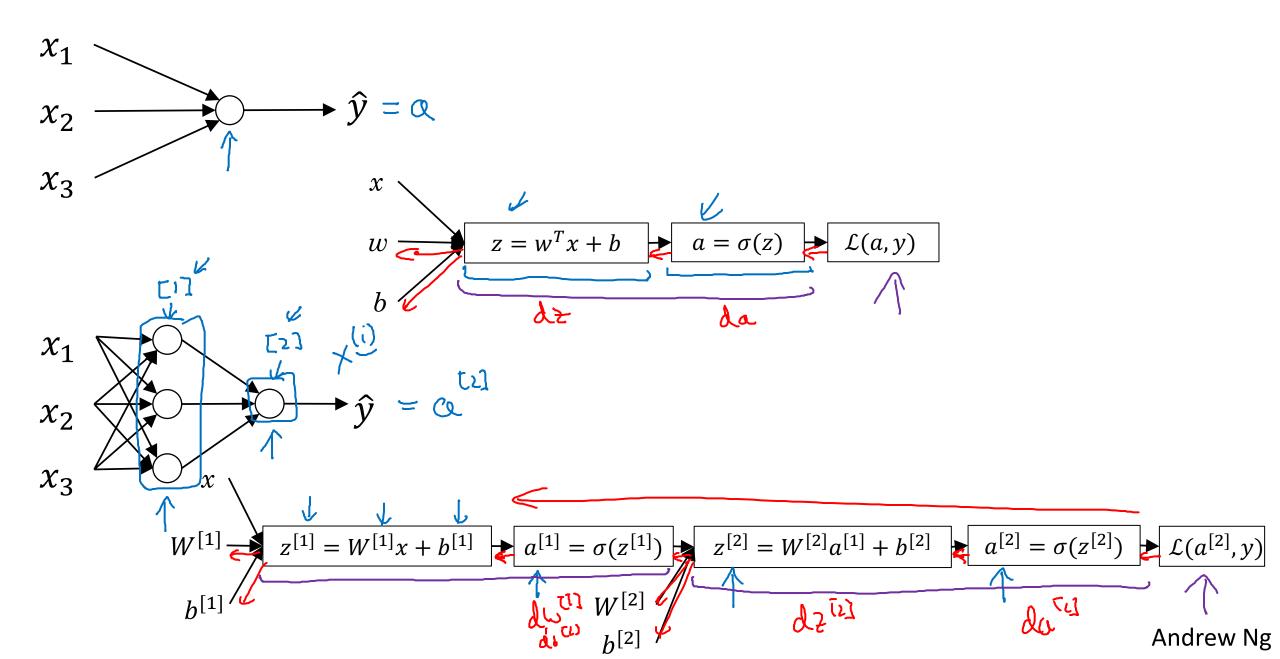


## One hidden layer Neural Network

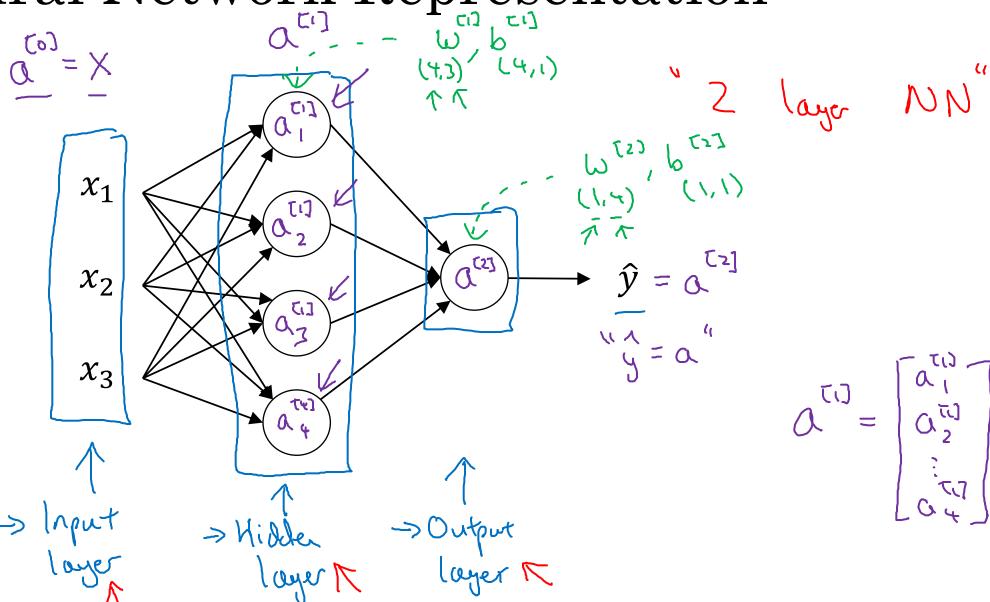
# Neural Networks Overview

#### What is a Neural Network?





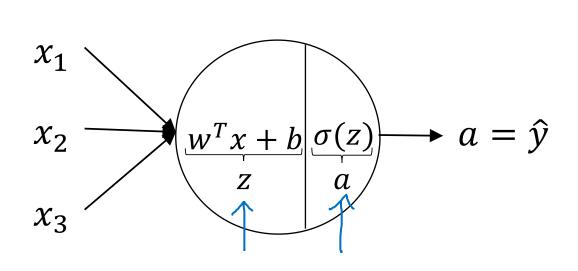
## One hidden layer Neural Network

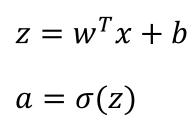


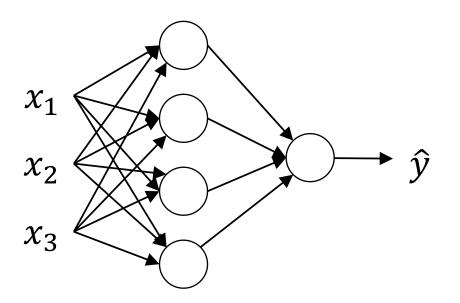


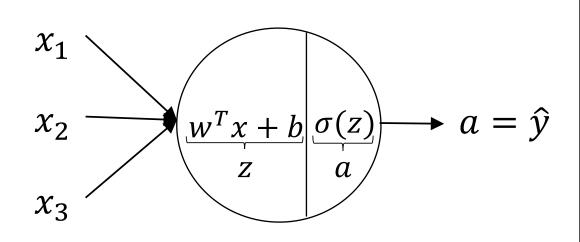
## One hidden layer Neural Network

Computing a Neural Network's Output

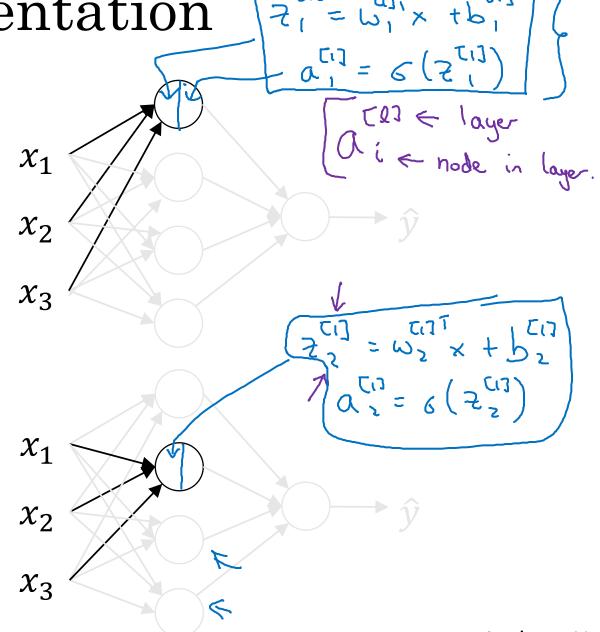


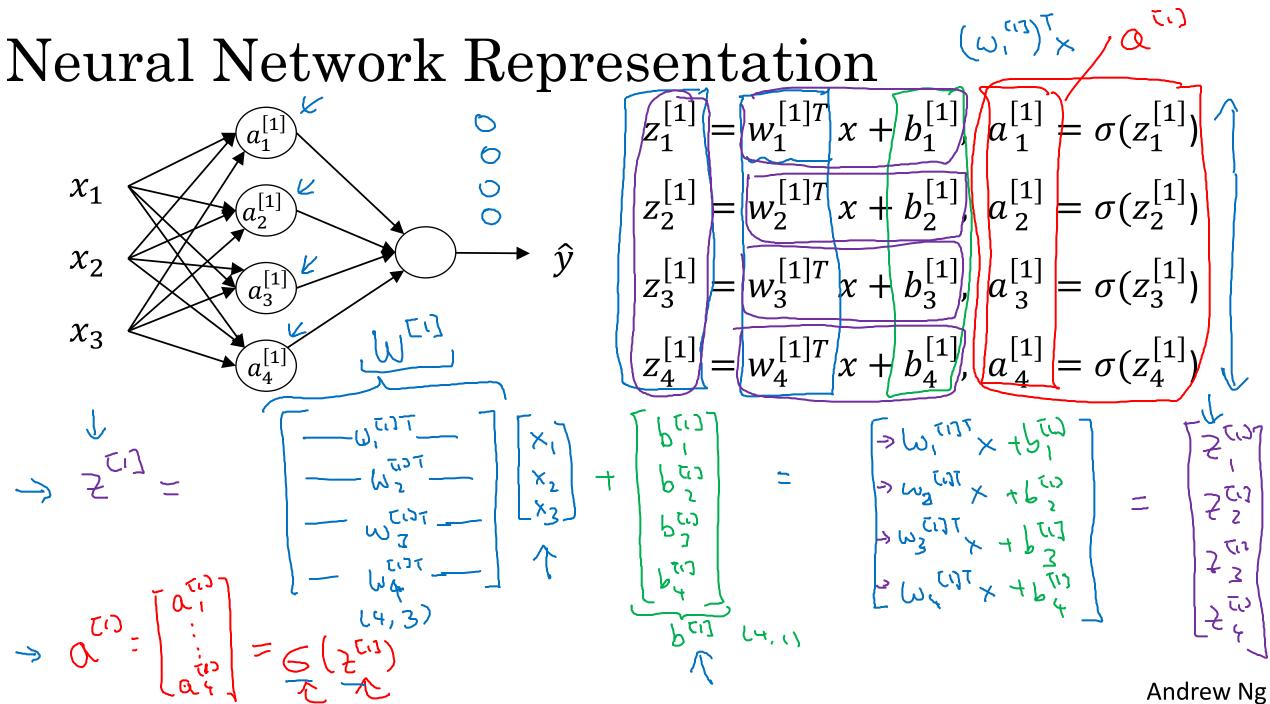




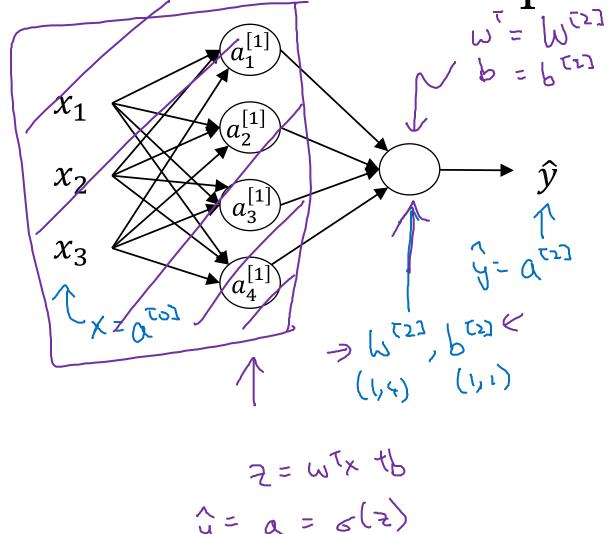


$$z = w^T x + b$$
$$a = \sigma(z)$$





Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$a^{[1]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

$$a^{[2]} = \sigma(z^{[2]})$$

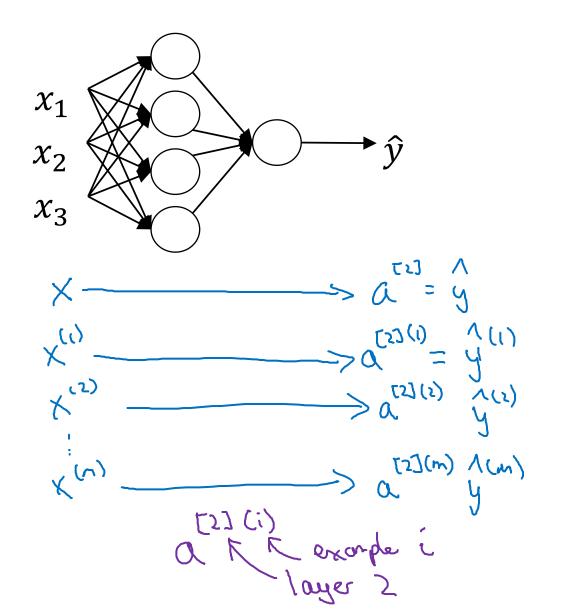
$$a^{[2]} = \sigma(z^{[2]})$$

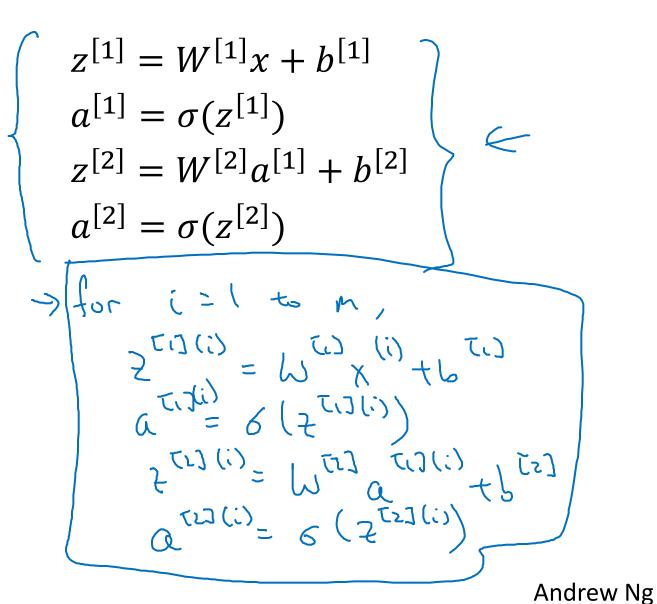


## One hidden layer Neural Network

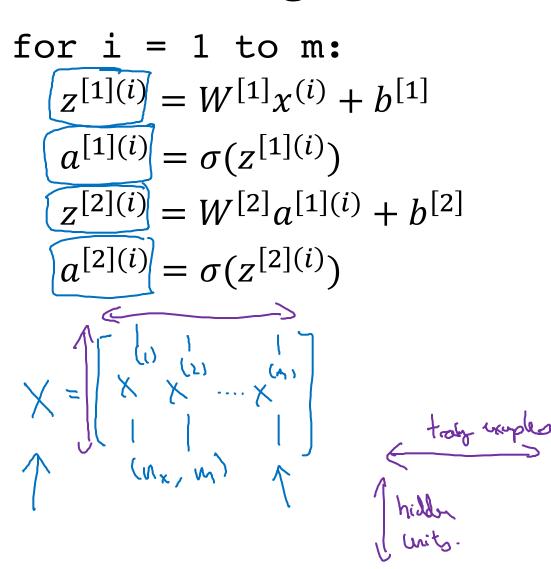
Vectorizing across multiple examples

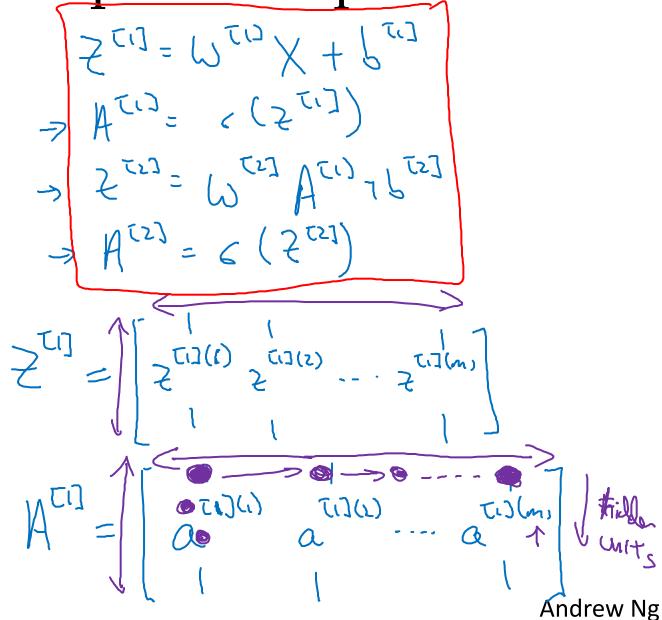
#### Vectorizing across multiple examples





Vectorizing across multiple examples



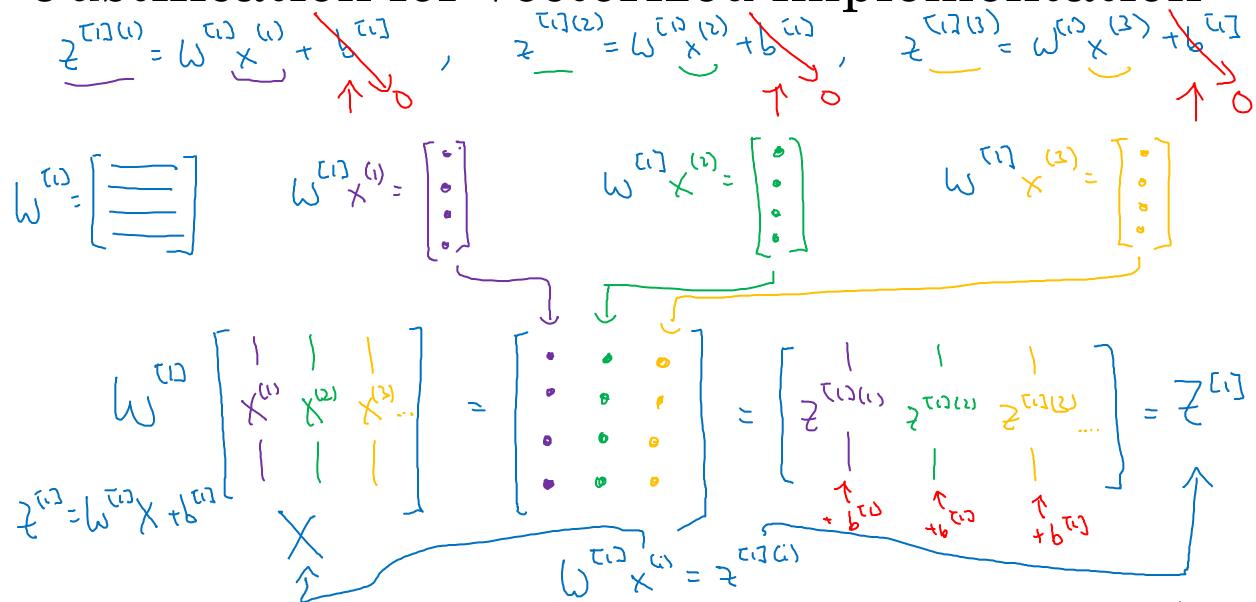




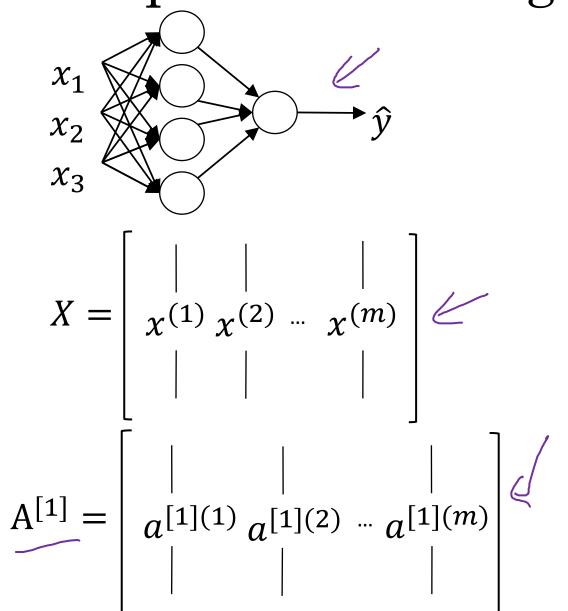
## One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



#### Recap of vectorizing across multiple examples



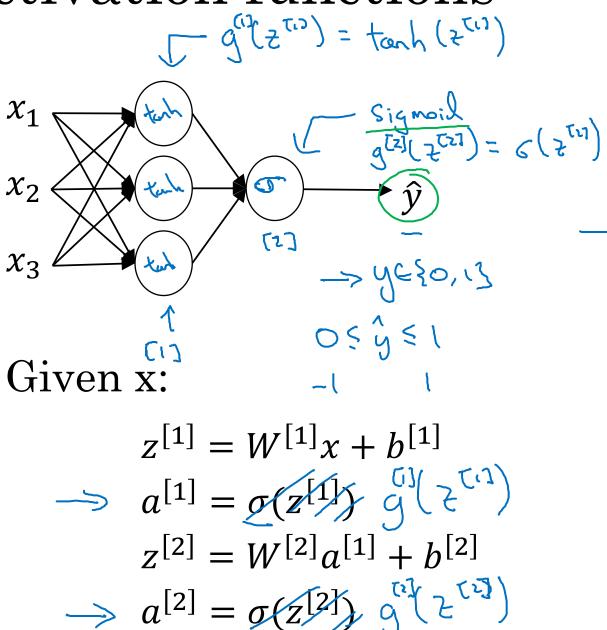
```
for i = 1 to m
                                     + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
                                    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
                                  \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
                            \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                                                                                                                                                                                                                      \chi = \alpha^{(0)} \quad \chi = \alpha^{(0)} \quad \chi^{(0)} = \alpha^{(0)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
         A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
     A^{[2]} = \sigma(Z^{[2]})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Andrew Ng
```

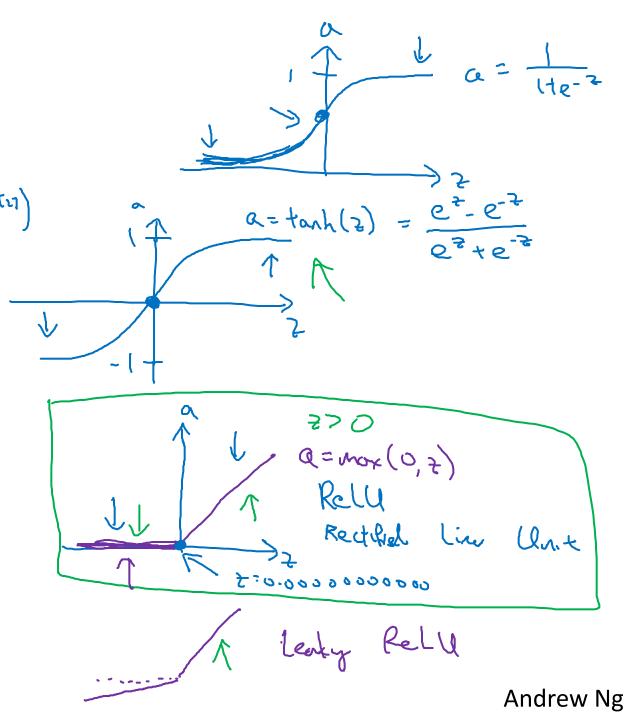


## One hidden layer Neural Network

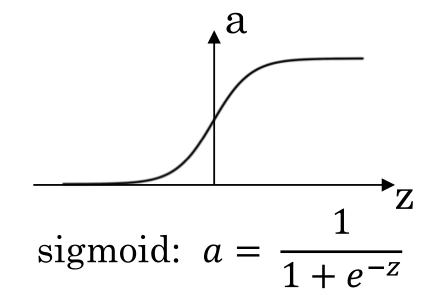
#### Activation functions

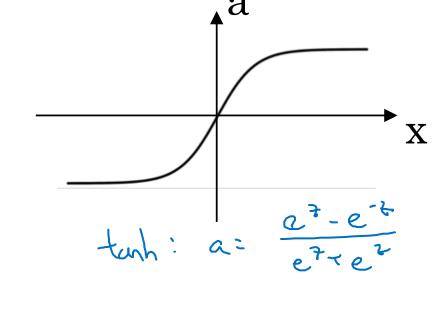
#### Activation functions

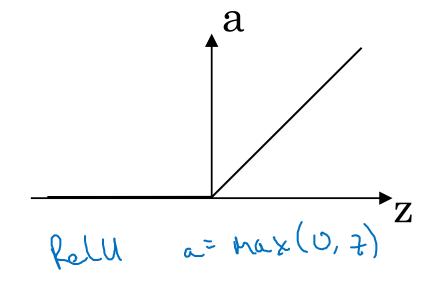


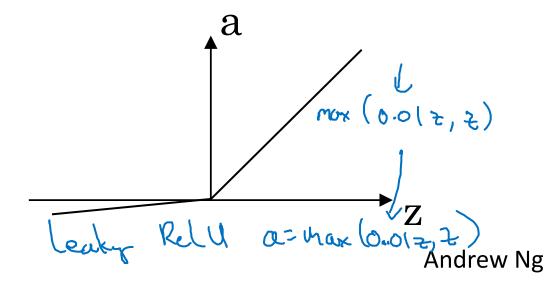


#### Pros and cons of activation functions







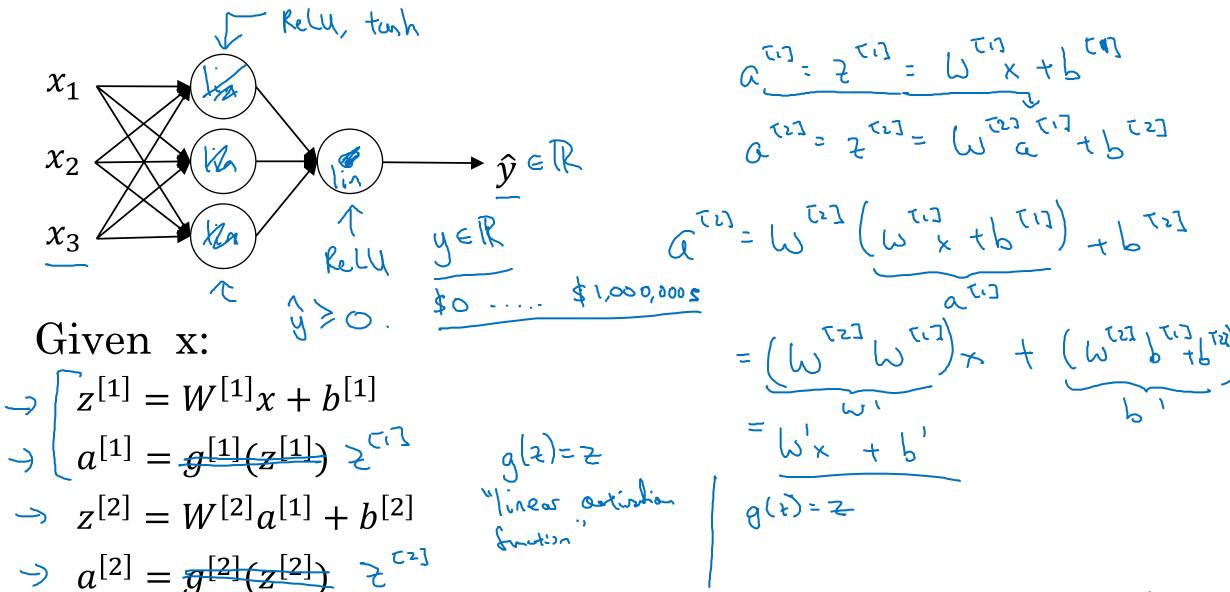




## One hidden layer Neural Network

Why do you need non-linear activation functions?

#### Activation function





## One hidden layer Neural Network

## Derivatives of activation functions

#### Sigmoid activation function

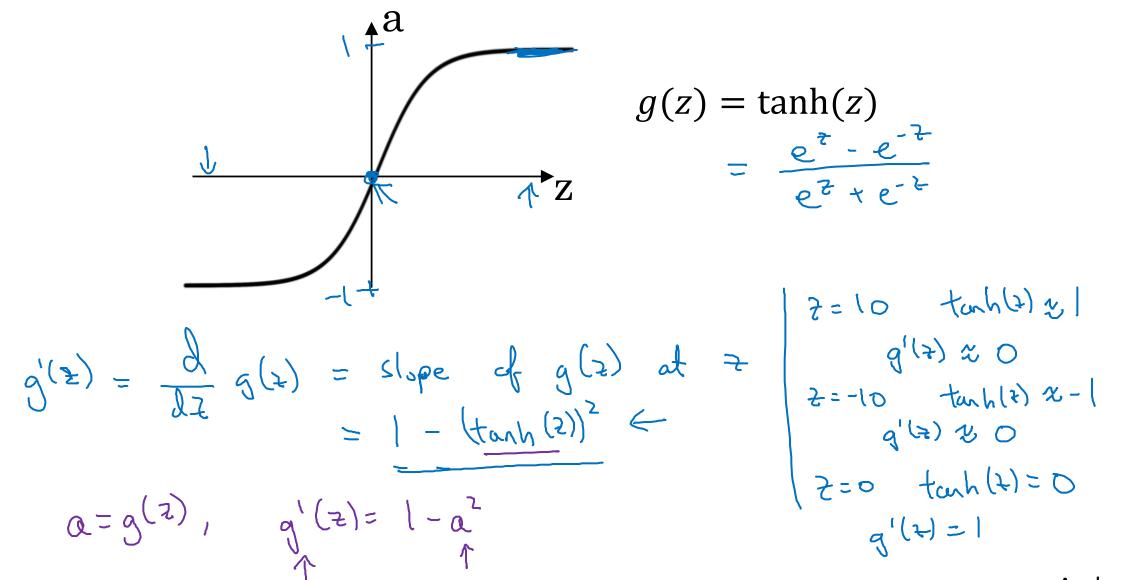
$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

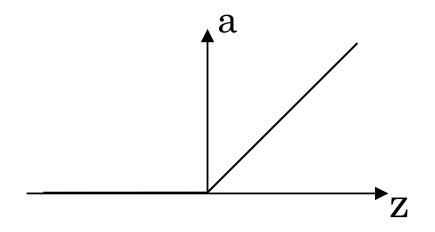
$$a = g(z) = \frac{1}{(1 + e^{-z})}$$

$$= \frac{1$$

#### Tanh activation function



#### ReLU and Leaky ReLU



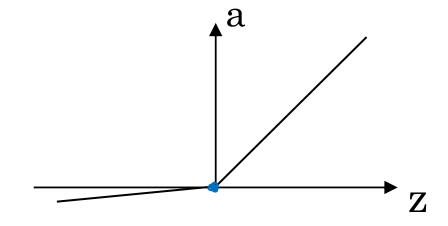
#### ReLU

$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } 2 < 0 \\ 1 & \text{if } t \geq 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 1 & \text{if } t \geq 0 \\ 1 & \text{if } t \geq 0 \end{cases}$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{on } t \neq 0 \\ 1 & \text{otherwise} \end{cases}$$



#### Leaky ReLU

$$g(z) = \max(0.01z, z)$$
 $g'(z) = \{0.01 : t > 0.00\}$ 
 $f(z) = \{0.01 : t > 0.00\}$ 



## One hidden layer Neural Network

# Gradient descent for neural networks

#### Gradient descent for neural networks

Parameters: 
$$(J^{(1)})$$
  $b^{(2)}$   $(J^{(2)})$   $(J^{(2$ 

#### Formulas for computing derivatives

Formal propagation:
$$Z_{(1)} = P_{(1)}(S_{(1)}) = e(S_{(2)})$$

$$Y_{(1)} = P_{(2)}(S_{(2)}) = e(S_{(2)})$$

$$Y_{(2)} = P_{(2)}(S_{(2)}) = e(S_{(2)})$$

$$Y_{(2)} = P_{(2)}(S_{(2)}) = e(S_{(2)})$$

Andrew Ng

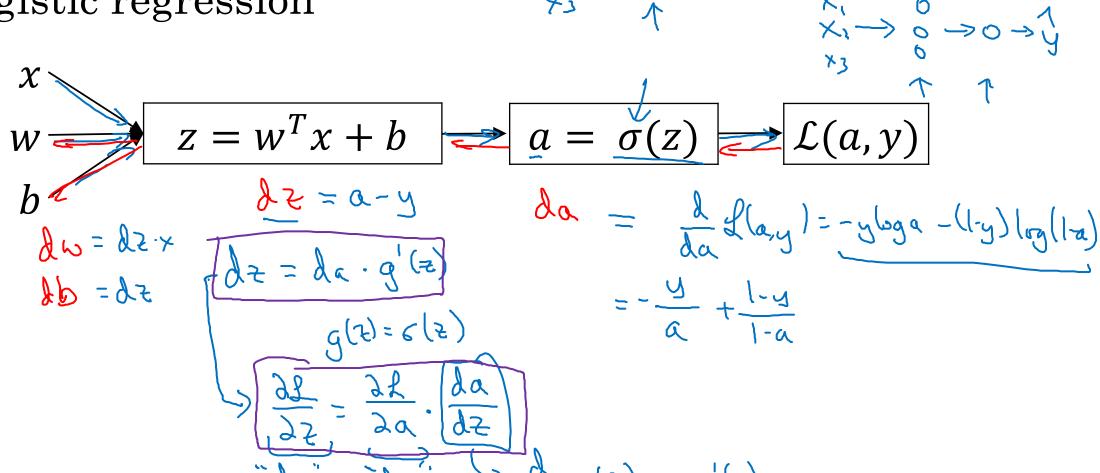


## One hidden layer Neural Network

Backpropagation intuition (Optional)

#### Computing gradients

Logistic regression



Neural network gradients  $z^{[2]} = W^{[2]}x + b^{[2]}$ duri = de a Tos -> > db = dztz] K  $\left( \begin{array}{ccc} n & \zeta & \zeta & \zeta & \zeta \end{array} \right)$ 

#### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$ 
 $db^{[2]} = dz^{[2]}$ 
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$ 
 $dW^{[1]} = dz^{[1]}x^T$ 
 $db^{[1]} = dz^{[1]}$ 

Vectorized Implementation:

$$z^{(1)} = (\omega^{(1)} \times + b^{(1)})$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

#### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dw^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$db^{[1]} = dz^{[1]}$$

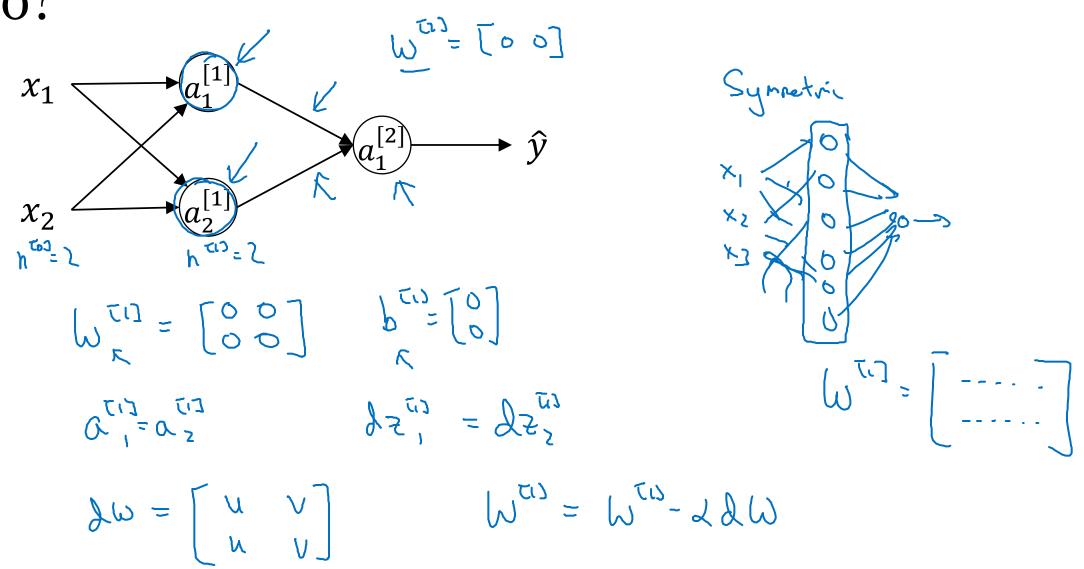
$$db^{[1]} = \frac{1}{m}np. sum(dz^{[1]}, axis = 1, keepdims = True)$$



## One hidden layer Neural Network

#### Random Initialization

## What happens if you initialize weights to zero?



#### Random initialization

