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# HW2B

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## q = (50, -45, 30, 20, 10, 0)

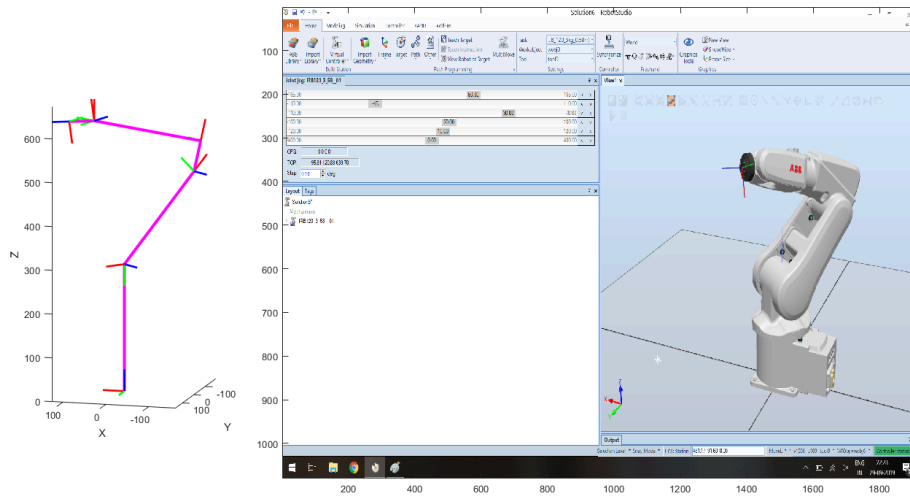
For configuration:

q = (50, -45, 30, 20, 10, 0)

```
subplot(1,4,1);  
[T] = plotArm(50, -45, 30, 20, 10, 0, f);  
subplot(1,4,[2 3 4]);  
image(imread('Images\01.png'));  
set(gcf, 'Position', get(0, 'Screensize'));
```

T =

-0.2119	-0.7767	0.5931	95.8449
0.2715	0.5362	0.7992	120.8760
-0.9388	0.3304	0.0973	633.7005
0	0	0	1.0000



$$\mathbf{q} = (10, 50, -45, 20, 10, 0)$$

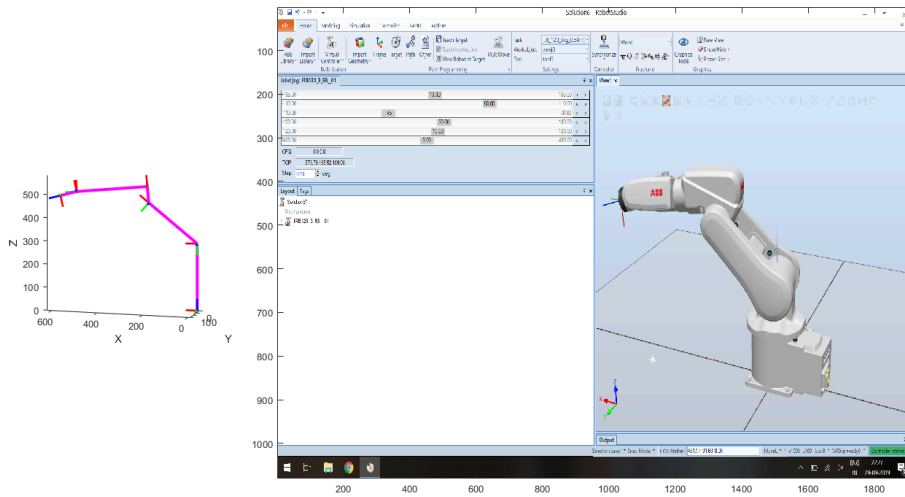
For configuration:

$$\mathbf{q} = (10, 50, -45, 20, 10, 0)$$

```
subplot(1,4,1);
[T] = plotArm(10, 50, -45, 20, 10, 0, f);
subplot(1,4,[2 3 4]);
image(imread('Images\02.png'));
set(gcf, 'Position', get(0, 'Screensize'));
```

$T =$

$$\begin{bmatrix} -0.3083 & -0.1338 & 0.9418 & 573.7904 \\ 0.2877 & 0.9306 & 0.2264 & 105.5169 \\ -0.9068 & 0.3407 & -0.2484 & 489.0814 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$



$q = (50, -45, 30, 50, -20, 40)$

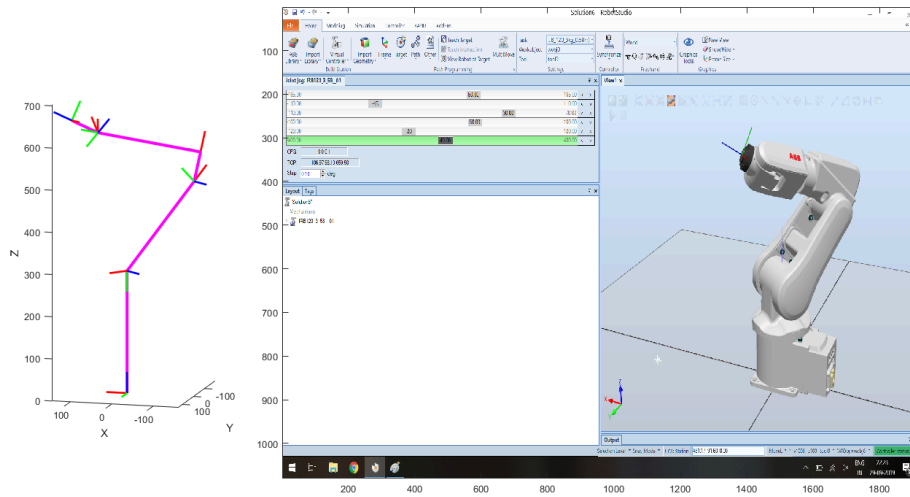
For configuration:

$q = (50, -45, 30, 50, -20, 40)$

```
subplot(1,4,1);
[T] = plotArm(50, -45, 30, 50, -20, 40, f);
subplot(1,4,[2 3 4]);
image(imread('Images\03.png'));
set(gcf, 'Position', get(0, 'Screensize'));
```

$T =$

-0.5812	-0.3215	0.7476	106.9666
0.8080	-0.3369	0.4833	98.1304
0.0965	0.8850	0.4556	659.4977
0	0	0	1.0000



$$\mathbf{q} = (-30, -60, 20, 40, -20, 40)$$

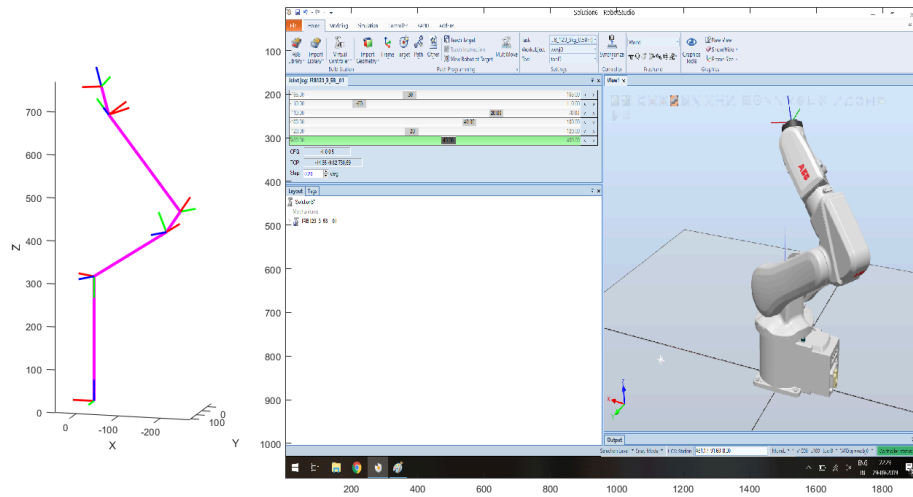
For configuration:

$$\mathbf{q} = (-30, -60, 20, 40, -20, 40)$$

```
subplot(1,4,1);
[T] = plotArm(-30, -60, 20, 40, -20, 40, f);
subplot(1,4,[2 3 4]);
image(imread('Images\04.png'));
set(gcf, 'Position', get(0, 'Screensize'));
```

$T =$

$$\begin{bmatrix} 0.7283 & -0.5782 & 0.3676 & -14.6463 \\ 0.6824 & 0.5631 & -0.4661 & -9.8216 \\ 0.0625 & 0.5903 & 0.8047 & 730.6854 \\ 0 & 0 & 0 & 1.0000 \end{bmatrix}$$



**$q = (0, 32, 45, 30, 56, 40)$**

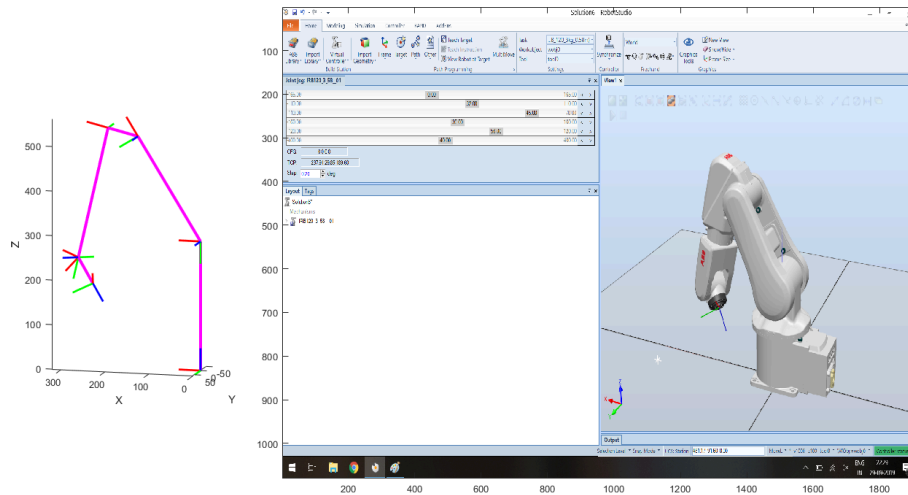
For configuration:

$q = (0, 32, 45, 30, 56, 40)$

```
subplot(1,4,1);
[T] = plotArm(0, 32, 45, 30, 56, 40, f);
subplot(1,4,[2 3 4]);
image(imread('Images\05.png'));
set(gcf, 'Position', get(0, 'Screensize'));
```

$T =$

-0.1912	0.7964	-0.5738	237.9075
0.7709	0.4837	0.4145	29.8454
0.6076	-0.3631	-0.7064	189.6013
0	0	0	1.0000



## Appendix

### Plot Arm Function

```
function [T] = plotArm(val1, val2, val3, val4, val5, val6, f)

syms q1 q2 q3 q4 q5 q6
q = [q1 q2 q3 q4 q5 q6].';
vals = [val1 val2 val3 val4 val5 val6].';
[n_dof,m] = size(q);
Individual_Transforms = sym(zeros(4,4,n_dof));
Transforms = sym(zeros(4,4,n_dof));

thetas = q;
thetas(2,1) = q2 - 90;
thetas(6,1) = q6 + 180;
d = [290 0 0 302 0 72].';
a = [0 270 70 0 0 0].';
alpha = [-90 0 -90 90 -90 0].';

for i = 1:n_dof
    Individual_Transforms(:, :, i) = ...
        dhpam2matrix(thetas(i,1), d(i,1), a(i,1),
        alpha(i,1));
    if i == 1
        Transforms(:, :, 1) = Individual_Transforms(:, :, 1);
    else
        Transforms(:, :, i) = ...
            Transforms(:, :, i-1)*Individual_Transforms(:, :, i);
    end
end
```

```
T01 = Individual_Transforms(:, :, 1);
T12 = Individual_Transforms(:, :, 2);
T23 = Individual_Transforms(:, :, 3);
T34 = Individual_Transforms(:, :, 4);
T45 = Individual_Transforms(:, :, 5);
T56 = Individual_Transforms(:, :, 6);

T06 = Transforms(:, :, 6);

solution = double(simplify(fk_solve(Transforms, q, vals, 0)));
T = solution(:, :, 6)
indTransforms = double( ...
    simplify(fk_solve(Individual_Transforms, q, vals,
    0)));

f = drawManip(solution, indTransforms, 'ABB_Robot');

end
```

## dhparam2matrix Function

```
function [trans] = dhparam2matrix(theta, d, a, alpha)
    %DHPARAM2MATRIX This function returns a Homogenous Transformation
    matrix
    % given the input parameters a, alpha, theta and d derived from
    the
    % DH Parameters of the robot.
    % Please enter all values in degrees and not radians.

    cos_alpha = @cosd;
    sin_alpha = @sind;
    cos_theta = @cosd;
    sin_theta = @sind;

    a11 = cos_theta(theta);
    a12 = -sin_theta(theta)*cos_alpha(alpha);
    a13 = sin_theta(theta)*sin_alpha(alpha);
    a14 = a*cos_theta(theta);
    a21 = sin_theta(theta);
    a22 = cos_theta(theta)*cos_alpha(alpha);
    a23 = -cos_theta(theta)*sin_alpha(alpha);
    a24 = a*sin_theta(theta);
    a31 = 0;
    a32 = sin_alpha(alpha);
    a33 = cos_alpha(alpha);
    a34 = d;
    scl = 1;

    trans = [a11 a12 a13 a14;
             a21 a22 a23 a24;
```

```
        a31 a32 a33 a34;  
        0   0   0   scl];  
end
```

## fk\_solve Function

```
function [T] = fk_solve(Transforms, states, vals, n)  
%FK_SOLVE This function substitutes the states in the transformation  
%matrix  
%with the values specified while maintaining the joint constraints  
%imposed  
%by the ABB Arm  
% @param transforms is the 4x4xm transformation matrices to solve  
% @param states are the states  
% @param vals are the values required  
% @param n is the T of n wrt 0 with substituted values.  
%  
  
q = vals;  
  
if abs(q(1,1)) > 165  
    disp('Joint 1 has reached max limit')  
    if q(1,1) > 0  
        q(1,1) = 165;  
    else  
        q(1,1) = -165;  
    end  
end  
  
if abs(q(2,1)) > 110  
    disp('Joint 2 has reached max limit')  
    if q(2,1) > 0  
        q(2,1) = 110;  
    else  
        q(2,1) = -110;  
    end  
end  
  
if q(3,1) > 70 || q(3,1) < -110  
    disp('Joint 3 has reached max limit')  
    if q(3,1) > 0  
        q(3,1) = 70;  
    else  
        q(3,1) = -110;  
    end  
end  
  
if abs(q(4,1)) > 160  
    disp('Joint 4 has reached max limit')  
    if q(4,1) > 0  
        q(4,1) = 160;
```



```
        else
            q(4,1) = -160;
        end
    end

    if abs(q(5,1)) > 120
        disp('Joint 5 has reached max limit')
        if q(5,1) > 0
            q(5,1) = 120;
        else
            q(5,1) = -120;
        end
    end

    if abs(q(6,1)) > 400
        disp('Joint 6 has reached max limit')
        if q(6,1) > 0
            q(6,1) = 400;
        else
            q(6,1) = -400;
        end
    end

    Transforms = subs(Transforms,[states], [q]);
    if n == 0
        T = Transforms(:, :, :);
    else
        T = Transforms(:, :, n);
    end
end
end
```

## drawManip Function

```
function [f] = drawManip(Transformations, indTransforms, Name)
%DRAWMANIP Summary of this function goes here
% Detailed explanation goes here
[l,m,n] = size(Transformations);
f = gcf;
az = -165;
el = 11;
rotate3d on
grid on
xlabel('X');
ylabel('Y');
zlabel('Z');
R1 = [1 0 0;
      0 1 0;
      0 0 1];
x = [0, Transformations(1,4,1)];
y = [0, Transformations(2,4,1)];
z = [0, Transformations(3,4,1)];
```

```
plot3(x, y, z, 'm', 'LineWidth', 3);
hold on
drawAxisLines(f, R1, [0;0;0]); % indTransforms(1:3,1:3,1)
    Transformations(1:3,4,1)
view(az, el);
axis('equal');
for i = 2:n
    x = [Transformations(1,4,i-1), Transformations(1,4,i)];
    y = [Transformations(2,4,i-1), Transformations(2,4,i)];
    z = [Transformations(3,4,i-1), Transformations(3,4,i)];
    %
    drawAxisLines(f, indTransforms(1:3,1:3,i), Transformations(1:3,4,i))

    drawAxisLines(f, Transformations(1:3,1:3,i-1), Transformations(1:3,4,i-1));
    plot3(x, y, z, 'm', 'LineWidth', 3);
end

drawAxisLines(f, Transformations(1:3,1:3,i), Transformations(1:3,4,i));

hold off
end
```

## drawAxisLines Function

```
function [p] = drawAxisLines(fig, rot, p_in)
%DRAWAXISLINES Summary of this function goes here
% Detailed explanation goes here
x = [1 0 0].';
y = [0 1 0].';
z = [0 0 1].';
rX = rot*x;
rY = rot*y;
rZ = rot*z;
rX = 50*(rX(:,1)) + p_in;
rY = 50*(rY(:,1)) + p_in;
rZ = 50*(rZ(:,1)) + p_in;
ax_x = [p_in(:,1), rX(:,1)];
ax_y = [p_in(:,1), rY(:,1)];
ax_z = [p_in(:,1), rZ(:,1)];
hold on
xlabel('X');
ylabel('Y');
zlabel('Z');
plot3(ax_x(1,:), ax_x(2,:), ax_x(3,:), 'r', 'LineWidth', 2);
hold on
plot3(ax_y(1,:), ax_y(2,:), ax_y(3,:), 'g', 'LineWidth', 2);
plot3(ax_z(1,:), ax_z(2,:), ax_z(3,:), 'b', 'LineWidth', 2);
end
```

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