Assignment 4: Solution.

The change of state can be carried out neversibly as follows: Ice (o°C, latm) _____ Dates (o°C, latm) _____ Dates (100°C, latm) Vapoux (273°C, 2 atm) (DS4 Vapoux (100°C, latm) $\Delta S_1 = \frac{\Delta H_f}{T} = \frac{1000 \text{gm} \times 80 \text{cal. gm}^{-1}}{273 \text{k}} = 293.04 \text{ cal. k}^{-1}$ DS2 = ncplnt2 = (1000 mol) (18 cal K-1 mol-1) In 373 273 = 312.11 cal. k-1 = 1447.72 (al. K-1 DS4 = nG ln Is - nRln B = 1000 mot \[8calk^-1. \ln\frac{546}{373} - 1.987 \calk^-1 \, mot^-1 \ln\frac{2}{1} \] = 92.84 cal. K-1 Total DS = DS1 + DS2 + DS3 + DS4 = (293.04 + 312.11 + 1447.72 + 92.84) Cal K-1 = 2145.71 cal. KT

As,
$$\Delta G = \Delta H - T\Delta S$$
 263
 $\Delta H_{263} = \Delta H_{273} + \int_{273} (\bar{c}_{P_3} - \bar{c}_{P_L}) dT$

$$\therefore \Delta H_{263} = -1440 \text{ cal. } \text{mol}^{-1} + (9-18)(263-273) \text{ cal. } \text{mol}^{-1}$$

Have (e, -10°c)
$$\xrightarrow{SS_1}$$
 Have (e, 0°c) $\xrightarrow{SS_2}$ Have (s, 0°c) $\xrightarrow{SS_3}$ Have (s, -10°c)

$$\Delta S_{1} = m \bar{c}_{P_{L}} \ln \frac{T_{f}}{T_{i}} = (18 \text{ (al. } \text{k}^{-1})) \ln \frac{373}{263}$$

$$\Delta S_2 = \frac{\Delta H}{T} = -\frac{1440}{273} \text{ cal. } k^{-1} = -5.275 \text{ cal. } k^{-1}$$

$$\Delta S_3 = (9 (al \cdot k^{-1}) (n (\frac{273}{263})) = -0.336 (al k^{-1})$$

$$\Delta S = \Delta S_1 + \Delta S_2 + \Delta S_3$$

$$= (0.672 - 5.275 - 0.336) \text{ (al } k^{-1}$$

$$= -4.94 \text{ (al } k^{-1}$$

As, DGP,T is negative, the process is a spontaneous Process.

Ans3: Efficiency of engine =
$$\frac{T_2-T_1}{T_2}$$

= $\frac{400-300}{400}$ = 0.25 [Engine]
Coefficient of performance (Ψ) = $\frac{T_1}{T_2-T_1}$ [For Ref.]

$$=\frac{273}{3m\cdot 3-273}=10$$

Work done by engine per Sec = $2 \times 10^3 \text{ J}$ Heat Extracted to prepare 3kg ice at $0^\circ \text{C} = 3 \times 10^3 \times 334.72 \text{ J}$ = $1004.16 \times 10^3 \text{ J}$

: Quantity of heat to be extracted per sec to prepare

3kg ice per min = 1004.16 × 103 Js-1

60

= 16.736 × 103 J. Sec-1

Quantity of heat actually extracted per sec. =

Hence, rate of heat leakage to the refrigerator = = (20 - 16.736) × 103 J Sec-1

= 3.264 × 103 J sec-1

Amount of Heat needed for the engine per minute
$$= \frac{W}{7} = \frac{2 \times 60 \times 10^3 \text{ J}}{0.25} = 480 \times 10^3 \text{ J}.$$

$$Ans 4$$
: As, $(8s)_{T} = (8p)_{V}$

(a) For a vander Waals gas
$$P = \frac{nRT}{V-nb} - \frac{n^2a}{V^2} = \frac{RT}{V_m-b} - \frac{a}{V_m^2}$$

$$\left(\frac{SS}{SV}\right)_T = \left(\frac{SP}{ST}\right)_V = \left(\frac{R}{V_m-b}\right)$$

(b) For a Dieterici gas:
$$P = \frac{RTe^{-a|RTV_{m}}}{V_{m}-b}$$

$$\frac{\left(\frac{8S}{SV}\right)_{T}}{\left(\frac{SP}{ST}\right)_{V}} = \frac{R\left(\frac{1+a}{RV_{m}T}\right)e^{-a|RV_{m}T}}{V_{m}-b}$$

For an Isothermal Doocess,

$$\Delta s = \int_{V_i}^{V_f} ds = \int_{SV_T}^{V_f} \frac{(8s)}{sv} dv$$
So we can simply compare $\left(\frac{8s}{sv}\right)_T$ expressions for the three gases.

$$P = \frac{nRT}{V} = \frac{RT}{Vm}$$
 so $\left(\frac{gs}{sv}\right)_T = \left(\frac{gp}{sT}\right)_V = \frac{R}{Vm}$

(85) is certainly greater for a vander woods gas than for a perfect gas, for the denominator is smaller for the for a perfect gas, for the denominator is smaller for the vander woods gas to van der woods gas. To compare the vander woods gas to the Dieterici gas, we assume that both have the same the Dieterici gas, we assume that both have the same Parameter b. (That is reasonable, for b is an excluded volume in both equation of state). In that case,

$$\frac{\left(\frac{8S}{SV}\right)_{T, \text{ Die.}}}{SV_{m}-b} = \frac{R\left(1+\frac{a}{RV_{m}T}\right)e^{-a/RV_{m}T}}{V_{m}-b}$$

=
$$\left(\frac{8S}{SV}\right)_{T, VdW} \left(1 + \frac{a}{RV_{m}T}\right) e^{-a/RV_{m}T}$$

Now, notice that the additional factor in $(\frac{85}{8V})_T$, Die.

the form $(1+x)e^{-x}$, where x>0. This factor is always less than 1. Clearly, $(1+x)e^{-x} < 1$ for large x, for then the exponential dominates. But $(1+x)e^{-x} < 1$ even for somall x, as can be seen by using the power series expansion for the exponential: $(1+x)(1-x+x^2/2+...)$ $= 1-\frac{x^2}{2}+......$ So $(\frac{85}{8V})_T$, $x < \frac{85}{8V}$

To Summerize, for isothermal expansion: [DSvdw > Die and DSvdw > Ds perfect The companison between a perfect gas and a Dieterici gas depends on particular values of constants a and b and on the physical conditions. Asns 5. As, S = S(T,P) $ds = \frac{8s}{sT} dT + \frac{8s}{sP} dP$ As, $\left(\frac{\delta S}{ST}\right)_{0} = \frac{CP}{T}$ Also, $\left(\frac{8S}{SP}\right)_{T} = -\left(\frac{8V}{ST}\right)_{p}$ & $\alpha = -\frac{1}{V}\left(\frac{SV}{ST}\right)_{p}$ =) $dq_{sev} = TdS = C_p dT - T\left(\frac{SV}{ST}\right) dP$ $C_S = \left(\frac{89}{8T}\right)_s = C_P - T_{V_X}\left(\frac{SP}{ST}\right)_s$ Cs = Cp - XV × Dtrs H Dtrs V. Ans6. (i) According to Trouton's rule

Ansb. (i) According to Trouton's rule

DvapH = 85Jk-1mol-1 x Tb

= 85Jk-1mol-1 x 342.2K

= 29.1 kJmol-1

ii) Use the integrated form of the Clausius - Clapeyon eq. 1.

Nearranged to

$$ln\left(\frac{R}{P_{i}}\right) = \frac{\Delta vapH}{R} \left[\frac{1}{T_{i}} - \frac{1}{T_{2}}\right]$$

At $T_{i} = 342.2 \, \text{k}$, $P_{i} = 1.0 \, \text{atm} \left[\text{Normal Boiling Point}\right]$;

thus at 25°C.

 $ln\left(\frac{P_{2}}{1.0 \, \text{atm}}\right) = \left(\frac{2.91 \times 10^{4} \, \text{Jmol}^{-1}}{8.314 \, \text{J k}^{-1} \, \text{mol}^{-1}}\right) \times \left(\frac{1}{342.2 \, \text{k}} - \frac{1}{248.2 \, \text{k}}\right)$
 $lnP_{2} = -1.51$
 $P_{2} = e^{-1.51} = 0.22 \, \text{atm}$.

At 60°C $ln\left(\frac{P_{2}}{2}\right) = \left(\frac{2.91 \times 10^{4} \, \text{Jmol}^{-1}}{2.91 \times 10^{4} \, \text{Jmol}^{-1}}\right) \times \left(\frac{1}{240.2 \, \text{k}} - \frac{1}{3332.2 \, \text{k}}\right)$

At 60°C,
$$en\left(\frac{P_2}{Iatm}\right) = \left(\frac{2.91 \times 10^4 Jmol^{-1}}{8.3145 Jk^{-1} mol^{-1}}\right) \times \left(\frac{1}{342.2k}, \frac{-1}{333.2k}\right)$$