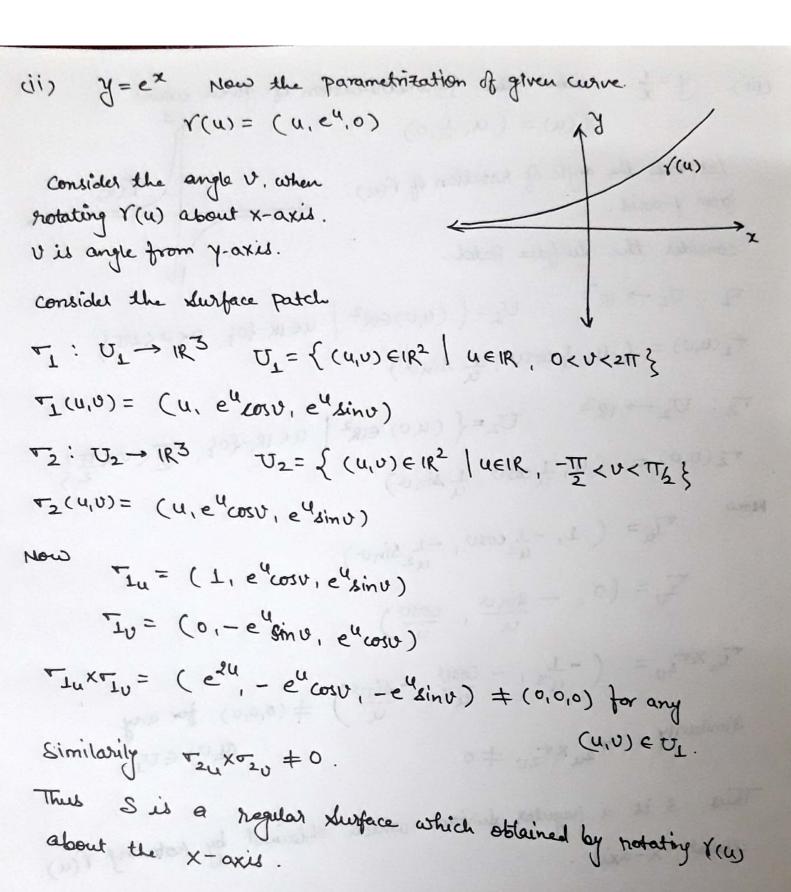
Assignment #8 Ans[1] (i) S: x2+y2-=2=1 consider the Surface Patch of S $\nabla_1: U_1 \longrightarrow IR^3$ where $U_1 = \{(u,v) \in IR^2 \mid u^2 + v^2 > 1\}$ $\frac{1}{2}(u,v) = \left(u,v,\sqrt{u^2+v^2-1}\right)$ T2: U1 → 183 $\sqrt{\frac{2}{2}}(u,v) = (u,v,-\sqrt{u^2+v^2-1})$ 53: U2 → 1R3 where U2 = { (4,0) €1R2 | u2-v2<1} $\sqrt{3} (u,v) = (u, \sqrt{1+v^2-u^2}, v)$ $\overline{\tau}_{u} = (1,0, \frac{u}{\sqrt{u^{2}+v^{2}-1}}), \quad \overline{\tau}_{v} = (0,1, \frac{v}{\sqrt{u^{2}+v^{2}-1}})$ $\overline{J}_{u} \times \overline{J}_{v} = \left(\frac{-u}{Ju^{2}+v^{2}-1}, \frac{v}{Ju^{2}+v^{2}-1}, 1 \right) + (0.0,0) \text{ for any}$ $(u,v) \in \mathbb{R}^{2}.$ similarly = x = 20 + 0 & = 3u × = 3u + 0. Thus S is a regular surface. S: { (x,y, Z) \in 183 | x2+y2-Z2-1=0} here $f(x,y,Z) = x^2+y^2-Z^2-1$ for level surface representation. clearly $\nabla f = (f_x, f_y, f_z) = (2x, 2y, 2z) \neq 0$ for any so S is a smooth surface also. hence every regular surface patch of (x, y, z) ES. s will be allowable.

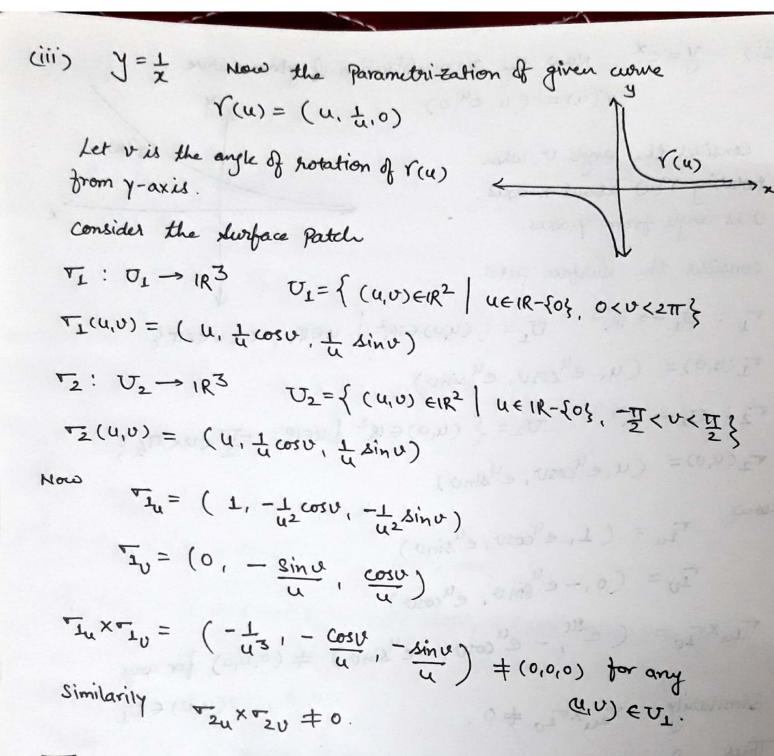
(ii) S: x2+4x2=4 consider the surface Patch of S U_= { (u,v) \in 12 | 0 < u < 2TT, v \in } TI: UI - IR3 $\tau_{\perp}(u,v) = (2\cos u, \sin u, v)$ TE: UZ - IR3 UZ={(U,U) EIR2 | - #< 4<#, VEIR} $\sqrt{2}(u,v) = (2\cos u, \sin u,v)$ $T_u = (-2\sin u, \cos u, 0), T_v = (0, 0, 1)$ Tux Tu = (cosu, & sinu, 0) = (0,0,0) for any UEU1. Similarity for \$20 x 020 \$ (0,0,0) for any $u \in U_2$. hence S is a regular surface. Now S: $\{(x,y,z) \in \mathbb{R}^3 \mid f(x,y,z) = x^2 + 4y^2 - 4 = 0\}$ $\nabla f = (f_x, f_y, f_z) = (lx, 8y, 0) \neq (0,0,0)$ for any $(x, y, z) \in S$. Thus S is a smooth surface hence allowable surface patches are there. (TI, TZ are also allowable). (iii) See it in the book, cylinder with axis as x-axis S: y2+ =2=1 U1= { (0,0) EIR2 | 0< u <217, veir} T (u,u): U_ ~ K3 $\mathcal{I}(u,v) = (v, \cos u, \sin u)$ 5, (4,0): U2 → 1R3 U2={ (u,v) e12 | -11 < u< 11, v e12} √2 (4,0) = (V, cosu, Linu) check! Regularity. $\nabla f = (0,24,27) \neq (0,0,0)$ for any point $(x,4,7) \in S$. S is smooth.

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(iv) S: Z= x2+242
        consider the surface patch of S
     T: U1 → 183 U1 = { (u,v) ∈ 182 | U ∈ 18, v ∈ 18 } = 182
     \sqrt{(u,v)} = (u,v,u^2+2v^2)
 Now Tu = (1,0,24), Tu = (0,1,40)
    Tu×Tv = (-2u, -4v,+1) ≠ (0,0,0) for any (1,v) ∈12.
    So S is a regular surface.
      S: { (x,y, Z) e1R3 | f(x,y,Z) = 22+242-Z=0 }.
      \nabla f = (2x, 2y, -1) \neq (0, 0, 0) for any (x, y, 7) \in S.
    Thus S is smooth hence or is allowable.
(V) S: y= sinx consider the surface patch of s
      T: U_ → 1R3 U_= { (u,u) ∈ 1R2 \ o < u < 21T, v ∈ 1R }
     T1(u,v) = (u, sinu,v)
     T2: U2 → 1R3 U2={ (4,0) €1R2 | -#<4<\frac{11}{2}, U€1R}
      45(n'n) = (n'yinn'n)
           T_u = (1, +\cos u, 0), \quad T_v = (0, 0, 1)
  T_{1}X_{4}T^{0} = (co2n'-1'0) + (0'0'0) for and (d'n) \in \Omega^{T}.
    Similarily 52 X 520 = 0
   Thus Sis a fregular surface.
    S: { (x, y, Z) e 1 R3 | f(x, y, Z) = y-sinx = 0 }
    \nabla f = (-\cos x, 1, 0) + (0,0,0) for any (x, y, z) \in S.
    to Sis smooth. Thus or is allowable.
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Ans [2] (i) y= 1+x2 Now the Parametrization of given curve $Y(u) = (u, 1+u^2, 0)$ consider the angle v from y-axis when hotating about x-axis. Consider the Surface patch TI: UI -> IR3 UI = {(u,v) \in IR2 | u \in IR, O < U < 2 TT } ~ I(u,v) = (u,(1+u2) cosv, (1+u2) sinv) T2: U2 → 1R3 U2= {(u,v) ∈ 1R2 | u ∈ 1R, -T< v < T/2} $\frac{1}{2}(u,v) = (u,(1+u^2)\cos v,(1+u^2)\sin v)$ Tu = (1, 24 cosv, 24 sinv) $\nabla_{1v} = \left(0, -\left(1+u^2\right) \sin \theta, \left(1+u^2\right) \cos v\right)$ $T_{u} \times T_{v} = (2u(1+u^{2}), -(1+u^{2})\cos v, -(1+u^{2})\sin v) + (0,0,0)$ for any (u,v) & UI similarily =2 × =2 + 0. Thus S is a negular surface which obtained by notating V(U)

about the X-axis.





Thus I is a regular surface which obtained by notating r(u) about X-axis.