

# Context Free Grammars

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Continued

$G = (V, \Sigma, R, S)$  where -  $V$  a finite set called the set of variables -  $\Sigma$  a finite set of characters -  $S \in V$  start variables -  $R$  is a set of rules  $A \rightarrow$  string of variables and/or letters from  $\Sigma$

Rules

supp. rule  $A \rightarrow 0A1$  And if  $w1 = 01A11 \Rightarrow w2 = 010A111$  where  $w2$  is derived from  $w1$ .

Also,

$w1 \Rightarrow w2 \Rightarrow w3 \Rightarrow w4 \Rightarrow \dots \Rightarrow wn$

Then  $w1 \Rightarrow^* wn$

Given a CFG  $G = (V, \Sigma, R, S)$ , then the language generated by it is  $LG = \{ w \mid w \in \Sigma^* \text{ and } S \Rightarrow^* w \}$

Example

In the previous case of the Grammar of arithmetic over add and sub, -  $\Sigma$  was  $\{0\dots9, (, ), +, -\}$  -  $V$  was  $\{E, N\}$  -  $R$  was -  $E \rightarrow E+E \mid E-E \mid (E) \mid N$  -  $N \rightarrow 0 \mid \dots \mid 9 \mid NN$  -  $S = E$

Parse Tree

Stack

FILO - First in Last out. You push into the stack, but you must pop out the last element only.

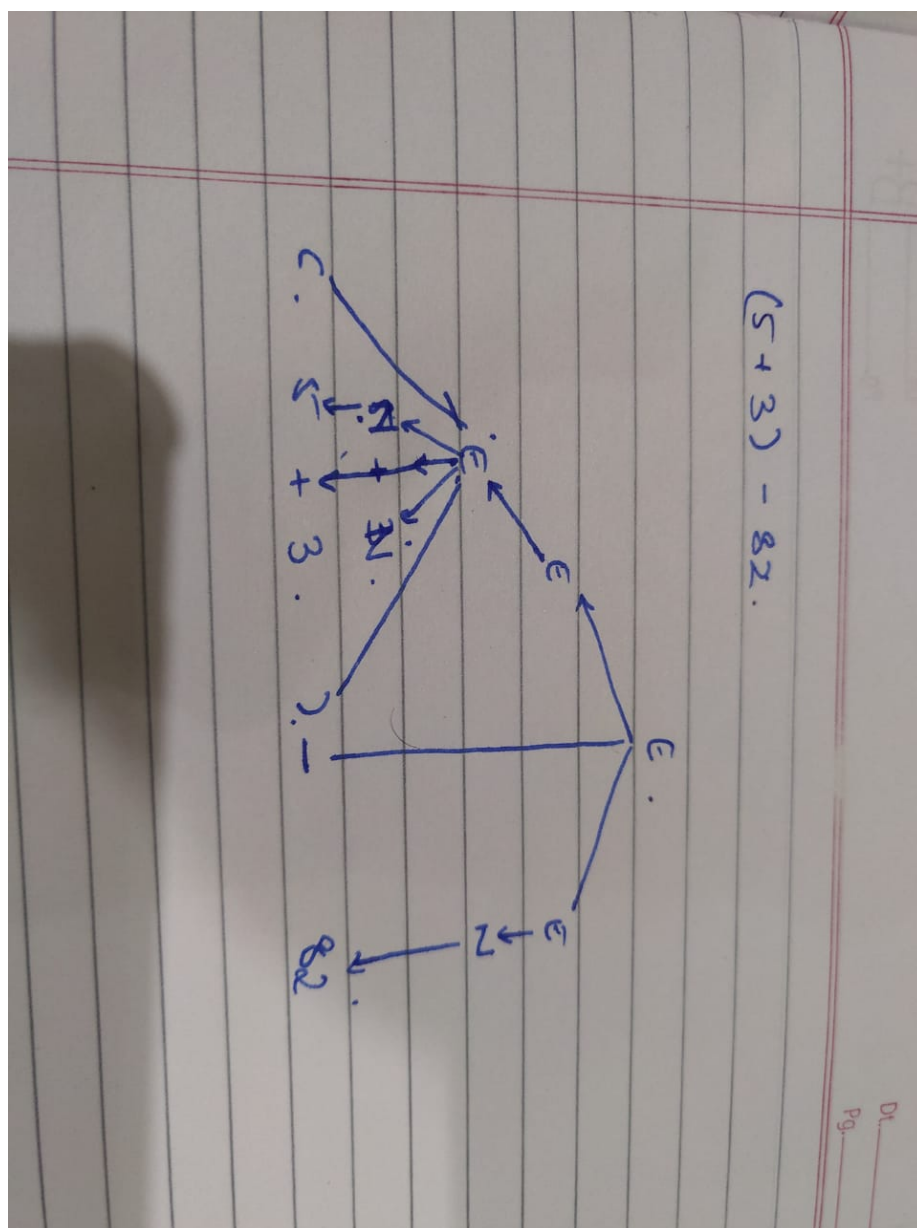


Figure 1: parsetree.jpg

Parse to check if Expr.

Let St be a St.

1. Push E to St
2. Pop