Solution to HW6

1) Suppose d: I-DR is such a curve. Then Xz is also constant. Therefore, if I is the turning angle He have del = constant. = c say.

Case 1: C=0

Then of is constant

is a constant =) T= (cosq(s), sinq(s)) vector.

If = (01, 92) then

 $d(b) = (a_1 b + b_1, a_2 b + b_2)$ for some

constants b, bz.

Note: (a1, a2) + (0,0) there there

since affar=1.

clearly & is confained in the plane

az (x-b) = a1 (y-b2).

Case2: C +0

4= Cb+Co for some constant co

=) T(b) = (cos(cs+co), bin(cs+co))

-) d(b) = (= fin(est(a)), - = cos(est(a))

for some constants e, ez Clearly of is contained in the circle

(x-e1)2+(y-c2)2= 1/2

2) $x_{\beta} = \cos \beta \Rightarrow \frac{dq}{dh} = \cos \beta$ =) $\varphi(8) = 95ins + co for some constant co$ =) T(15) = (cos(sins+co), sin (sins+co)) P=(0,0) is on the curve. If length is measured from P then 7(0) = (cosco, sinco) = (1,0) Hence, we can take co=0. $\Rightarrow d(b) = \left(\int_{0}^{\infty} \cos(\sin u) du, \int_{0}^{\infty} \sin u (\sin u) du\right)$ 3) Let $e_1 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$, $e_2 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$, $e_3 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$. (x) Aei = ith column vector of A. From AAt= I deduce that SAe1, Aez, Aezz is an orthonormal laris of R3.

Griven U, WER3 write V= a, e, +92ez + 93e3, W- bjeifbreze b3e3, ai, bi ER and then use that Ut) Au is a linear map. (il) => (i): Apply (ii) for V, W = {e1, e2, e3}, Then use (x). (ii) =) (iii): Innediate (iii) =) (iii): Compute A(V+W), A(V+W) 4. (i) Check if for U, W = {e1, e2, e3} or {i', I', I'} and then use linearity. (ii) Do it yourself.

5- (i)
$$d(t) = (t, t, t^{3})$$

=) $d'(t) = (1, 2t, 3t^{3}) = d'(6) = (1, 0, 0) = \overline{t}^{3}$
 $d'''(t) = (0, 2, 6t)$
 $d'''(t) = (0, 0, 6)$
 $d'''(t) = \overline{t}^{3}$

=) $\overline{n}(0) = \overline{b}(0) \times \overline{T}(0) = \overline{k} \times \overline{t}^{3} = \overline{J}^{3}$
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 $\overline{n}(0) = \overline{n}(1) \times \overline{n}(0) = 2\overline{n}(1) \times \overline{n}$