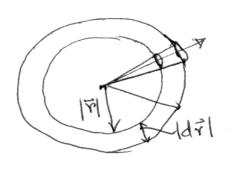
Average Therem:

Consider the 2 whenthe spheres with radii road redr.



Average of ϕ over $S: \phi = \frac{1}{A} \int \phi \, dA$ where $A: area of the sphere = 4\pi r^2$

& dA = r2 dr = r sint do dq.

Since or is constant over the sphere, it can be taken out of the integral and we get,

中= 上(F) d2

Similarly average of \$ over \$:

\$\forall '= \frac{1}{45} \int \phi(\vec{r} + d\vec{r}) d\varepsilon.

: Differer, \$ - 4 = \frac{1}{45} \left(\bar{47} + d\bar{17} \right) - \phi(\bar{17}) \right] d\D.

Non, $\Phi(\tilde{v} \in d\tilde{v}) = \varphi(\tilde{v}) + \frac{24}{3r} dr + \frac{21}{3r} dr + \frac{29}{32} dr + ---$

οιπα, σφ. dr = (R=4+9=4+2=4). (Ran+yay+2dx)

= 1 () まゆ、ながかします. (dv=+ d+) = Ly Std. Fdr rds = dy (FA. Frds) = dr 4 Fr Swfa. da Applying divergence meanen, φ'-== dy Sp. (pd) dV = dy SpadV. :9k vq=0=) \$- =0 => \$= = : Average values of of over S & s' one equal. We can keep doing this by taking smaller and Smaller circles until we reach center of sphere. : 9t & setisfies Laplaces, egn, the average value of of over a spherical surface egrals the value of of at the center of the sphere.