

## 1

- a)  $\cos x$
- b)  $\sec^2 x$
- c)  $e^x$
- d)  $\frac{1}{x}$
- e)  $5x^4$

## 2

- a)  $2x + 4$
- b)  $\cos(x) - \sin(x)$
- c)  $e^x + 12x^2$

## 3

- a)  $e^x(\sin(x) + \cos(x))$
- b)  $2(\cos^2 x - \sin^2 x)$
- c)  $x \cos(x) + \sin(x)$

## 4

- a)  $\sec^2(x)$
- b)  $\frac{1}{3} \frac{(2x+e^x) \cos(x) + (x^2+e^x) \sin(x)}{\cos^2 x}$

## 5

- a)

$$\begin{aligned} \frac{d}{dx} [\sin(2x)] &= \frac{d[\sin(2x)]}{d(2x)} \times \frac{d(2x)}{dx} \\ &= 2 \cos(2x) \end{aligned}$$

- b)

$$\begin{aligned} \frac{d}{dx} [e^{x^2}] &= \frac{d[e^{x^2}]}{d(x^2)} \times \frac{d(x^2)}{dx} \\ &= 2xe^{x^2} \end{aligned}$$

c)

$$\begin{aligned}
\frac{d}{dx}(3x+4)^{25} &= \frac{d[(3x+4)^{25}]}{d(3x+4)} \times \frac{d(3x+4)}{dx} \\
&= 3.25(3x+4)^{24} \\
&= 75(3x+4)^{24}
\end{aligned}$$

## 6

a)

$$\begin{aligned}
\frac{d}{dx}[\log(x+2+\sqrt{x^2+4x+1})] &= \frac{d[\log(x+2+\sqrt{x^2+4x+1})]}{d(x+2+\sqrt{x^2+4x+1})} \times \frac{d(x+2+\sqrt{x^2+4x+1})}{dx} \\
&= \frac{1}{(x+2+\sqrt{x^2+4x+1})} \times \left(1 + \frac{d(\sqrt{x^2+4x+1})}{dx}\right) \\
&= \frac{1}{(x+2+\sqrt{x^2+4x+1})} \times \left(1 + \frac{d(\sqrt{x^2+4x+1})}{d(x^2+4x+1)} \times \frac{d(x^2+4x+1)}{dx}\right) \\
&= \frac{1}{(x+2+\sqrt{x^2+4x+1})} \times \left(1 + \frac{1}{2\sqrt{x^2+4x+1}} \times (2x+4)\right) \\
&= \frac{1}{(x+2+\sqrt{x^2+4x+1})} \times \left(1 + \frac{(x+2)}{\sqrt{x^2+4x+1}}\right)
\end{aligned}$$

b)

$$\begin{aligned}
\frac{d}{dx}[\sin(x^2 \sin(x))] &= \frac{d[\sin(x^2 \sin(x))]}{d(x^2 \sin(x))} \times \frac{d(x^2 \sin(x))}{dx} \\
&= \cos(x^2 \sin(x)) \times (x^2 \cos(x) + 2x \sin(x)) \\
\frac{d}{dx}[\sqrt{1+(2x+3)^2}] &= \frac{d[\sqrt{1+(2x+3)^2}]}{d[1+(2x+3)^2]} \times \frac{d[1+(2x+3)^2]}{dx} \\
&= \frac{1}{2\sqrt{1+(2x+3)^2}} \times \left(0 + \frac{d(2x+3)^2}{d(2x+3)} \times \frac{d(2x+3)}{dx}\right) \\
&= \frac{1}{2\sqrt{1+(2x+3)^2}} \times (8(2x+3)) \\
&= \frac{4(2x+3)}{\sqrt{1+(2x+3)^2}} \\
\frac{d}{dx} \left[ \frac{\sin(x^2 \sin(x))}{\sqrt{1+(2x+3)^2}} \right] &= \frac{\sqrt{1+(2x+3)^2} \frac{d(\sin(x^2 \sin(x)))}{dx} - \sin(x^2 \sin(x)) \frac{d\sqrt{1+(2x+3)^2}}{dx}}{1+(2x+3)^2}
\end{aligned}$$

Just put the values now. Or you may choose not to. What is important is that get the idea right.

## 7

$$x^2 + 2xy + y^3 = 42$$

Differentiate both sides wrt x

$$\frac{dx^2}{dx} + 2\frac{d(xy)}{dx} + \frac{dy^3}{dx} = 0$$

$$2x + 2\left(x\frac{dy}{dx} + y\right) + \frac{dy^3}{dy} \times \frac{dy}{dx} = 0$$

$$2x + 2x\frac{dy}{dx} + 2y + 3y^2\frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = -\frac{2(x+y)}{(2x+3y^2)}$$

## 8

$$x = \sin(y)$$

Differentiate wrt x

$$1 = \frac{d\sin(y)}{dy} \frac{dy}{dx}$$

$$1 = \cos(y) \frac{dy}{dx}$$

$$\begin{aligned} \frac{dy}{dx} &= \frac{1}{\cos(y)} \\ &= \frac{1}{\sqrt{1-\sin^2(y)}} \\ &= \frac{1}{\sqrt{1-x^2}} \end{aligned}$$

Now you know how the derivative of inverse trigonometric functions is found.

## 9

a)

$$\begin{aligned} \frac{d}{dx}[\tan^{-1}(m \sin(x))] &= \frac{d(\tan^{-1}(m \sin(x)))}{d(m \sin(x))} \times \frac{d(m \sin(x))}{dx} \\ &= \frac{m \cos(x)}{1 + m^2 \sin^2(x)} \end{aligned}$$

b)

$$\frac{d}{dx} \left[ \sin^{-1} \left( \frac{2x}{1+x^2} \right) \right] = \frac{d \left[ \sin^{-1} \left( \frac{2x}{1+x^2} \right) \right]}{d \left( \frac{2x}{1+x^2} \right)} \times \frac{d \left( \frac{2x}{1+x^2} \right)}{dx} \quad (1)$$

Use the derivative of sine inverse for the first derivative and quotient rule for the second derivative.