CHM202

Energetics and dynamics of chemical reactions

Solutions Assignment – V

Q.1 Methane gas is heated from 25 °C until the volume has doubled. The pressure is constant at 1 bar. The variation in molar heat capacity with temperature has been measured and the results of those experiments can be summarized by the equation-

$$C_P = a + bT$$

where a = 22.34 JK⁻¹mol⁻¹ and b = 48.1×10^{-3} JK⁻²mol⁻¹ . Calculate ΔH and ΔU per mol. Assume the system follows the ideal gas behaviour.

Sol.

The final volume is twice of the initial volume and pressure is constant,

so,
$$V_2 = 2V_1$$
 and $P_2 = P_1$

The initial temperature is $T_1 = 298 K$, so the final temperature can be found (assuming ideal gas behavior)

$$\frac{T_2}{T_1} = \frac{P_2 V_2}{P_1 V_1} = 2$$

$$T_2 = 2T_1 = 596 K$$

$$\Delta T = 298 K$$

$$\Delta H = \left(\frac{\partial H}{\partial T}\right)_P dT = \int_{T_1}^{T_2} C_P(T) dT = \int_{T_1}^{T_2} (a + bT) dT$$

$$= \left[aT + \frac{b}{2}T^2\right]_{T_1}^{T_2}$$

$$= 6.657 kJ mol^{-1} + 6.407 kJ mol^{-1}$$

$$= 13.06 kJ mol^{-1}$$

The change in internal energy

$$\Delta U = \Delta H - p\Delta V = \Delta H - p\Delta T$$

= (13.06 - 2.48)kJ mol⁻¹ = 10.59kJ mol⁻¹

- **Q.2** Compute change in Gibbs free energy for the process $H_2O(l, -10 \,^{\circ}C) = H_2O(s, -10 \,^{\circ}C)$. Specific heat of water and ice over the temperature range is 18 and 9 Cal.mol⁻¹K⁻¹, respectively and $\Delta H_{fus_{273}} = 1440 \,^{\circ}Cal. \,^{\circ}Mol^{-1}$. Predict whether the change is spontaneous or not.
- **Sol.** For the given transformation, $\Delta H \& \Delta S$ are calculated separately. From these values, ΔG can be calculated as follow:

$$\Delta G = \Delta H - T\Delta S$$

$$\Delta H_{273} - \Delta H_{263} = \int_{273}^{263} (C_{P_S} - C_{P_l}) dT = (9 - 18) \ Cal. \ mol^{-1}(263 - 273)$$

$$= 90 \ Cal. \ mol^{-1}$$

$$\Delta H_{263} = \Delta H_{273} - 90 \ Cal. \ mol^{-1} = 1350 \ Cal. \ mol^{-1}$$

To calculate ΔS , the following reversible path is considered:

$$H_2O(l, -10^{\circ}C) \xrightarrow{\Delta S_1} H_2O(l, 0^{\circ}C) \rightleftharpoons H_2O(s, 0^{\circ}C) \xrightarrow{\Delta S_3} H_2O(s, -10^{\circ}C)$$

$$\Delta S_1 = nC_{P_l} \ln \frac{T_f}{T_i} = 18 \ Cal. \ K^{-1} \ln \frac{273}{263} = 0.672 \ Cal. \ K^{-1}$$

$$\Delta S_2 = \frac{\Delta H}{T} = \frac{1440}{273} \ Cal. \ K^{-1} = 5.275 \ Cal. \ K^{-1}$$

$$\Delta S_3 = 9 \times \ln \frac{273}{263} \ Cal. \ K^{-1} = 0.336 \ Cal. \ K^{-1}$$
So $\Delta S = \Delta S_1 + \Delta S_2 + \Delta S_3 = 6.283 \ Cal. \ K^{-1}$

$$\Delta G = \Delta H_{263} - T\Delta S = 1350 - 263 \times 6.283 \ Cal = -302.43 \ Cal$$
As ΔG is negative, the process is a spontaneous process.

Q.3 Calculate entropy change per litre of the solution when pure N₂, H₂, NH₃ gases are mixed to form a solution having the final composition 15% N₂, 55% H₂ and 30% NH₃ (all at STP).

Sol.:

This is a case of free mixing and we know that for free mixing
$$45 = -\sum x_i R \ln x_i$$
 per mole. Here $x_1 = \text{Mole-fraction}$.

In the given problem,

 $X_{N_2} = 0.15$; $X_{H_2} = 0.55$ and $X_{NH_3} = 0.30$.

So, $45 = -0.15 \times 1.987 \ln(0.15) + -0.55 \ln \times 1.987 \ln(0.55)$
 $-0.3 \times 1.987 \ln(0.30)$
 $= (0.565 + 0.653 + 0.718) (al/mole$
 $= 1.936$ Cal/mole

As they are STP, I mole = 22.4 litre

So $45/\text{litre} = 0.086$ Caldeg litre.

Q.4 Establish the condition for spontaneous vaporization of water, given $\Delta H = 9590 \text{ Cal.mol}^{-1}$ and $\Delta S = 26 \text{ e.u.}$ for the process.

Sol.: For spontaneous vaporization, $\Delta G < 0$

or
$$\Delta H - T\Delta S < 0$$

 $\Delta H < T\Delta S$
 $T\Delta S > \Delta H$

$$T > \frac{\Delta H}{\Delta S} = \frac{9590}{26} \,^{\circ} K$$
$$T > 368.85 \,^{\circ} K$$

So, here for spontaneous vaporization T should be greater than 368.85 °K.

Q.5 Describe a reversible process by which one mole of water at 100 °C can be converted to vapour at 0.5 atm and 100 °C. Calculate ΔH and ΔG for the process. How far these quantities would be affected if the operation were performed irreversibly? Assume water vapour behave ideally and latent heat of vaporization of water = 540 Cal.gm⁻¹.

Sol.:

The given change can be brought about reversibely in two steps. In the first stage, water at 100°c and 1 atm is supplied its latent heat so that it is converted to its vapour at 100°c and 1 atm and then it is isothermally reversibly expanded to 0.5 atm i.e. 1 mole water 150. revisible 1 mole votour 150. rev | mole vapour (100°c, 1 atm) | expansion (100°c); 0.5 atm) | Step-II | Step-II In Step-I; SH1 = 18 × 540 = 9720 cal and s62, = 0; as itis reversible equilibrium between liquid and vapour. In Step-II: 4 Hz = O [Isothermal expansion] and $46z_2 = RT \ln \frac{P_2}{P_1} = 1.987 \times 373 \ln \frac{0.5}{1} = -513.73 \text{ Cal}$ So, total 4H = 9720+0=9720 cal. and total 16 = 0 - 513.73 = -513.73 cal. As H and Gr one state functions, their values will remain same in irreversible path.

Q.6 Calculate the change in Gibbs potential when 36 gm water initially at 100 °C and 10 atm pressure are converted to vapour at 100 °C and 0.01 atm pressure. Assume water vapor behave ideally.

Sol.:

Q.7 One mole of benzene at the normal boiling point of 352.2 K vaporizes into a gaseous state at a pressure of 0.1 atm. Calculate ΔS and ΔG . Given the enthalpy of vaporization is 7364 Cal.mol⁻¹.

Sol: Let first one mole of Benzene be vaporized at its normal boiling point i.e. 352.2 K and 1 atm and then the vapor is isothermally expanded to 0.1 atm.

Then in the first step

$$\Delta S_1 = \frac{\Delta H}{T_h} = \frac{7364}{352.2} Cal. K^{-1} = 20.91 Cal. K^{-1}$$

And $\Delta G_1 = 0$ as vaporization at normal boiling point is a reversible process where liquid and vapor are in equilibrium.

In the second step,

$$\Delta S_2 = R \ln \frac{P_1}{P_2} = 1.987 \ln \frac{1}{0.1} = 4.58 \, Cal. \, K^{-1}$$

and

$$\begin{split} \Delta G_2 &= RT \ln \frac{P_2}{P_1} = 1.987 \times 352.2 \times \ln \frac{0.1}{1} Cal = -1615.97 \ Cal \\ \text{So } \Delta S &= \Delta S_1 + \Delta S_2 = 20.91 + 4.58 \ Cal. \ K^{-1} = 25.49 \ Cal. \ K^{-1} \\ \text{and } \Delta G &= \Delta G_1 + \Delta G_2 = -1615.97 \ Cal \end{split}$$

Q.8 Determine the change in entropy when 1 kg ice at 0 °C and 1 atm is heated to 373 °C and 2 atm pressure. Given $\Delta H_{fus_{273}} = 80 \text{ Cal. g}^{-1}$; $\Delta H_{Vap_{373}} = 540 \text{ Cal. g}^{-1}$; $C_{P_L} = 18 \text{ Cal. K}^{-1} mol^{-1}$ and $C_{P_V} = 8 \text{ Cal. K}^{-1} mol^{-1}$.

Sol.:

The change of state can be carried out reversibly as follows, ice (o°c, 1 atm)
$$\frac{dS_1}{dS_2}$$
, water (o°c, 1 atm) $\frac{dS_2}{dS_3}$, water (100°c, 1 atm) $\frac{dS_2}{dS_3}$, water (100°c, 1 atm) $\frac{dS_3}{dS_3}$ $\frac{dS_1}{dS_1} = \frac{dH_1}{dS_3} = \frac{1000 \text{gm} \times 80 \text{calgm}^{-1}}{273 \text{ K}} = 293.04 \text{ cal K}^{-1}$ $\frac{dS_2}{dS_3} = \frac{1000 \text{ mot}}{18} (18 \text{ cal K}^{-1} \text{mot}^{-1}) \ln \frac{373}{273} = 312.11 \text{ cal K}^{-1}$. $\frac{dS_3}{dS_3} = \frac{dH_1}{dS_3} = \frac{1000 \times 540}{373} \text{ cal K}^{-1} = \frac{1447.72 \text{ cal K}^{-1}}{373} = \frac{1000 \times 540}{373} = \frac{1447.72 \text{ cal K}^{-1}}{373} = \frac{1000 \text{ mot}}{373} = \frac{1000 \times 540}{373} = \frac{1000 \times 540}{300} =$

Q.9 One mole of $O_2(C_V = \frac{5}{2}R)$ initially at 546K and 10 atm expands adiabatically against a constant pressure of 1 atm until the volume becomes doubled. Calculate ΔU , ΔH and ΔS for the process. **Sol.:**

The process is an adiabatic irreversible process. So, Ty is calculated by using the expression, Popp (V2-V1) = - Cr(Ty-Ti) or Popp V1 = - 5 R(T4 - 546) [: 1 2 = 2 V1] or latin RTi = - 5 R (Ty - 546) or 546 K = - 5 (Ty - 546) :. Ty = 524.16 K 40 = mCv (T4-Ti) = (1mol) (5 x8.314 JK mol) (524.16 - 546)K = -453.94J 4H = mG(Ty-Ti) = 7 ×8.314 (524.16-546) J = -635.52 J 45 = n Er ln Tf + n R ln \frac{\frac{\gamma_2}{\gamma_1}}{\gamma_1}, = $\left(\frac{5}{2} \times 8.314\right) \ln \frac{524.16}{546} + \left(\frac{5}{2} \times 8.314\right) \ln 2J \kappa^{2}$ = 4.914 JK = 48 sum = 0 as the process is adiabatic. : 4 Suriverse = 4.914 JK This proves that in an irreversible process & Suniverse is positive. **Q.10** One mole of an ideal gas $(C_V = \frac{5}{2}R)$ is taken reversibly from 400K, 5 atm to 600K, 2 atm. Calculate ΔU , ΔH and ΔG for the process. Given: $\bar{S}_{298}^0 = 4J^{-1}K^{-1}mol$).

Sol.: SH is independent of the path of transformation. So, to calculate SH let us consider the transformation as follows. gas (400K, 5 atm) _ + gas (600K, 5 atm) _ + gas (600K, 8H, = mCp (T2-T1) = (= ×8.314 J K moi) (600 - 400) K = 5819 · 8 J 5/1/2 = 0 as for an ideal gas at constant temperature 5/1/20. 1H = 1H, + 1H2 = 5819.85+0 = 5819.85 as = n Cplu T2 - n Rlu P2 = {1 (= x 8.314 J K') ln 600 - 21 x 8.314 J K'ln = } = $\left(\frac{7}{2} \times 8.314 \ln \frac{600}{400} - 8.314 \ln \frac{2}{5}\right) J \vec{k}' = 19.42 J \vec{k}$ = 50-51 Again, for the transformation of state from 298K, I atm to 400K, 5 atm. - 5, = (-4.81+4) JK = -0.81 JK Sz = 19-42+5, = (19.42-0-81) JK = 18.61 JK NOW, 462 = 4H - 4(TS) = 4H - (T2S2 - T, S1) = 5819.8 J - (600 x18.61+400 x0.81) J = - 56 70.2 J.

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Energetics and dynamics of chemical reactions

Solutions Assignment -VI

Q.1 When a certain liquid freezes at -3.65 °C its density changes from 0.789 g cm⁻³ to 0.801 g cm⁻³. Its enthalpy of fusion is 8.68 kJ mol⁻¹. Calculate the freezing point of the liquid at 100 MPa. **Sol.** The change in molar entropy of the system will be

$$\Delta_{fus}S = \frac{\Delta_{fus}H}{T_f}$$

Fusion is accompanied by a molar enthalpy change $\Delta_{fus}H$ occurs at a temperature T. So, the Clapeyron equation becomes

$$\frac{\Delta P}{\Delta T} = \frac{\Delta_{fus}S}{\Delta_{fus}V}$$

$$\Delta T = \frac{\Delta_{fus}V}{\Delta_{fus}S} \times \Delta P = \frac{T_f \Delta_{fus}V}{\Delta_{fus}H} \times \Delta P$$
$$= \frac{T_f \Delta P}{\Delta_{fus}H} \times M \times \Delta \left(\frac{1}{\rho}\right)$$

Here $T_f = -3.65 + 273.15 = 269.50K$

$$\Delta T = \left(\frac{269.50K \times 100 \text{ MPa}}{8.68 \text{ kJ } mol^{-1}}\right) \times \text{M} \times \left(\frac{1}{0.789 \text{ g cm}^{-3}} - \frac{1}{0.801 \text{ g cm}^{-3}}\right)$$

$$= (3.1048 \times 10^{6} \text{KPa } J^{-1} mol) \times \text{M} \times (0.018987 \text{g}^{-1} \text{ cm}^{3}) \times \left(\frac{m^{3}}{10^{6} \text{ cm}^{3}}\right)$$

$$= (0.058951 \text{ KPa } J^{-1} m^{3} \text{g}^{-1} mol) \times \text{M}$$

$$= (0.058951 \text{ Kg}^{-1} mol) \times \text{M}$$

Since the initial density is given as 0.789 g cm^{-3} , so $M = 46.07 \text{ g mol}^{-1}$.

$$\Delta T = (0.058951 \, Kg^{-1} mol) \times 46.07 \, g \, mol^{-1} = 2.716 \, K$$

So the freezing point of the liquid 100 MPa is

$$T_f = 269.50 K + 2.716 K = 272.22 K$$

Q.2 The partial molar volumes of two liquids A and B in a mixture in which the mole fraction of A is 0.3713 are 188.2 cm³ mol⁻¹ and 176.14 cm³ mol⁻¹, respectively. The molar masses of A and B are 241.1 gmol⁻¹ and 198.2 gmol⁻¹. What is the volume of a solution of mass 1.000 kg?

Sol. Total volume
$$V = n_A V_A + n_B V_B = n(x_A V_A + x_B V_B)$$

Total Mass $m = n_A M_A + n_B M_B = n(x_A M_A + (1 - x_A) M_B)$
Where $n = n_A + n_B$

$$n = \frac{m}{x_A M_A + (1 - x_A) M_B}$$

$$= \frac{1 \ kg(10^{3} g/kg)}{0.3713 \times (241.1 \ gmol^{-1}) + (1 - 0.3713) \times 198.2 \ gmol^{-1}} = \frac{10^{3} \ g}{214.1287 \ gmol^{-1}}$$
$$= 4.67 \ mol$$

$$V = n(x_A V_A + x_B V_B)$$

= 4.67 mol × [(0.3713 × 188.2 cm³ mol⁻¹) + (1 – 0.3713) × 176.14 cm³ mol⁻¹]
= 4.67 × 180.6178 cm³ = 843.49 cm³

- **Q.3** Consider a container of volume 250 cm³ that is divided into two compartments of equal size. In the left compartment there is argon at 100 kPa and 0 °C while in the right compartment there is neon at the same temperature and pressure. Determine the entropy and Gibbs energy of mixing when the partition is removed. Assume that the gases are perfect.
- **Sol.** The Gibbs energy of mixing

$$\Delta_{mix}G = nRT(x_A \ln x_A + x_B \ln x_B)$$
Here $n_{Ar} = n_{Ne}$; $x_{Ar} = x_{Ne} = 0.5$
So, $n = n_{Ar} + n_{Ne} = \frac{pV}{RT}$

$$\Delta_{mix}G = pV\left(\frac{1}{2}\ln\frac{1}{2} + \frac{1}{2}\ln\frac{1}{2}\right) = -pV \ln 2$$

$$= -(100 \times 10^3 \text{Pa}) \times 250cm^3 \times \left(\frac{m^3}{10^6 \text{ cm}^3}\right) \ln 2 = 25 \text{ Pa } m^3 \times 0.69314$$

$$= -17.329 \text{ Pa } m^3 = -17.329 \text{ J}$$

The entropy of mixing

$$\Delta_{mix}S = \frac{-\Delta_{mix}G}{T} = \frac{17.329 \text{ J}}{273 \text{ K}} = 0.06348 \text{ JK}^{-1} = 6.348 \times 10^{-2} \text{ JK}^{-1}$$

Q.4 At 373.6 K and 372.6 K , the vapor pressure of water is 1.018 and 0.982 atm, respectively. Evaluate the molar entropy of vaporization and ΔV , the change of volume per mole when liquid water vaporises at 373 K. Assume the vapor behaves ideally.

From Clausius - Clapeyron equation
$$\ln \frac{P_2}{P_1} = \frac{Lv}{R} \frac{T_2 - T_1}{T_1 T_2}$$

$$30, \ln \frac{1.018}{0.982} = \frac{Lv}{1.987} \times \frac{1}{(373.6 \times x372.6)}$$

$$= 1 K$$

$$30, molar entropy of vaporisation = \frac{Lv}{T_6}$$

$$= \frac{9958.57}{373.6} = 26.65 \text{ cal } \text{$$

Also,
$$\frac{dP}{dT} = \frac{Lv}{T(Vg - V_L)}$$

$$(Vg - V_L) = \frac{Lv}{T(dP/dT)}$$
Here $L_V = 9958.57$ Cal = 411.511 literatm [:1 literatm = 24.2 Cal]
$$\frac{dP}{dT} = \frac{4P}{4T} = \frac{1.018 - 0.982}{373.6 - 372.6} = 0.036$$
 atm K^{-1}

$$So, Vg - V_L = \frac{411.511}{373.6 \times 0.036} = 30.5965$$
 literamole.

Q.5 Heavy water boils at 101.42 °C and its molal elevation constant (K_b) is 10% higher than that of pure water. (a) How does its latent heat compare with that of pure water?, (b) What will be vapor pressure of pure D_2O if its $L_V = 9960Cal. mol^{-1}$?

Sol.:

We know from Cerbbs Helmholtz equation;
$$\chi_{B} = \frac{\Delta_{rap} H}{R} \left(\frac{1}{T^{*}} - \frac{1}{T} \right)$$
Now amount of solute present is so small we assume that $T \approx T^{*}$

$$\frac{1}{T*} - \frac{1}{T} = \frac{T - T*}{T + T*} = \frac{T - T*}{T*2} = \frac{dT_b}{T*2}$$

$$\chi_{B} = \frac{\Delta v_{ap} H}{R + 2} \Delta v_{b}$$

$$= \frac{\Delta v_{b}}{K_{b}}$$

$$K_{b} = \frac{R + 2}{\Delta v_{ap} H} = elevation of boiling point constant$$

XB is mole fraction of solute & molality (Cm)

Elevation of boiling point: aTb = Kb. Cm

Kb = Ebullioscopic (Motal elevation of b. pt.) const.

Similarly,

Depoession of freezing point STy = Ky. Cm

Depoession of freezing point 4 of the latent heat of fusion/gm

$$K_f = \frac{RT_f^2}{1000 \text{ M}}$$
 $K_f = \text{Cryscopic} (\text{Model depression of fr. point) count.}$

$$\frac{K_{b_1}}{K_{b_2}} = \frac{T_{b_1}^2}{T_{b_2}^2} \frac{l_{v_2}}{l_{v_i}} \text{ For } D_{20} \quad K_{bD_{20}} = 1.1 \text{ Kb}_{H_{20}}$$

$$50, \frac{1}{1.1} = \frac{(373)^2}{(374.42)^2} \frac{lw_2}{lv_1}$$

or
$$\frac{lv_2}{lv_1} = 0.9160$$

From Clausius Clapeyron equi

$$\ln \frac{760}{P_1} = \frac{9960}{1.987} \times \frac{374.42 - 373}{373 \times 374.42}$$

So, vapour pressure of D20 at 100°C is 722.23 mm.

Q.6 An aqueous solution contains 5% by weight of urea and 10% by weight of glucose. What will be its freezing point? [Given: $K_f = 1.86$ °C g mol⁻¹].

Sol.:

Moles of wrea in 1000 gm water =
$$\frac{50}{60} = 0.833$$

 $EMOl.$ wf. of wrea = $60\,\text{J}$
Moles of glucose in 1000 gm water = $\frac{100}{180} = 0.555$
 $EMol.$ wf. of glucose = $180\,\text{J}$
Total moles of solute = $(0.833 + 0.555) = 1.388$
 $1000\,\text{gm}$ solvent
This is molal cone. = $Cm = 1.388$
So, $\Delta T_f = K_f.Cm$
or $\Delta T_f = 1.86 \times 1.388 = 2.58\%$
So, freezing point of solution will be -2.58% .

Q.7 Blood is said to be isotonic with 0.85% NaCl solution at 40 °C. Assuming complete dissociation of *NaCl*; calculate total concentration of various solutes in blood. What is its approximate freezing point? [Given: Cryoscopic constant $K_f = 1.86$ °C g mol⁻¹].

Sol.:

As well completely dissociates into two ions its establishment
$$\pi = 2 \times \frac{9}{V} \frac{RT}{M}$$

Here $g = 0.85g$; $V = 100 \text{ ce.} = 0.1 \text{ litre}$ MNac = 58.5
 $T = 313 \text{ K}$

So, $\pi = 2 \times \frac{0.85}{0.1} \times \frac{0.082 \times 313}{58.5} = 7.46 \text{ atm}$

As it is instenic with blood at 40°C; blood also has 7.46 atm osmotic pressure. So, if $C(M)$ is cone. of dissolved solutes then

$$C = \frac{\pi}{RT}$$

$$Or C = \frac{7.46}{0.082 \times 313} = 0.29 \text{ (M)}$$
For aqueous solution molar cone can be approximated taken as molal cone.

So, molal cone. = 0.29 (Cm)

Now, $4T_f = k_f \cdot \text{Cm} = 1.86 \times 0.29 = 0.54 ^{\circ}\text{C}$

So, free zing point of blood will be $-0.54 ^{\circ}\text{C}$.

Q.8 A mixture which contains 0.550 gm of camphor and 0.045 gm of an organic solute (containing 93.46% *C* and 0.6.54% *H*) freezes at 157 °C. Find out the molecular formula of the organic compound. [Given freezing point and Cryoscopic constant for camphor are 178.4 and 37.7 °C g mol⁻¹, respectively].

Sol.:

We know
$$4T_j = K_j \cdot C_m$$
 $K_j = Cryscopic \text{ (Motal depression of free zing point) Constant} = 37.7 & kg. mole!$
 $= 37.7 \times kero ^c c \text{ gmmole!}$
 $C_m = \text{Motal conc.} = \frac{a \times 1000}{b \times M}$
 $a \text{ gm solute (Mot. wt. M) has been dissolved in b gm solvent.}$
 $a = 0.045 \text{ gm b} = 0.55 \text{ gm g Camphor}$
 $4T_j = (178.4 - 157)^c = 21.4^c c$
 $\therefore 4T_j = K_j \cdot \frac{a \times 1000}{b \times M}$
 $21.4 = \frac{37.7 \times 1000 \times 0.045 \times 10^3}{0.55 \times M}$

or $M = \frac{1.696 \times 10^3}{11.77} = 144.14$

Now % of $C = 93.46$ and % of $C = 6.54$
 $\therefore \text{ Atomic valie of } C: H \text{ is } \frac{93.46}{72} : \frac{6.54}{1}$
 $= 7.78 : 6.54$

So, emperical formula is
$$(C_{7.78} + 6.54)_n = 144.14$$

i. $100 n = 144.14$ or $n = 1.44$
So, no. of Catoms per molecule = $7.78 \times 1.44 = 11.20 \approx 11$
So, no. of H atoms v $v = 6.54 \times 1.44 = 9.41 \approx 9$
Hence the formula is = $C_{11}H_9$ (1-methylnaphthalene)

Q.9 If boiling point of an aqueous solution is 100.1 °C, what is its freezing point? Given l_f and l_V for water are 80 Cal.gm⁻¹ and 540 Cal.gm⁻¹, respectively.

Solis
Elevation of briling point
$$\Delta T_b = K_b \cdot C_m$$
 and for the same solved depression of freezing point $\Delta T_f = K_f \cdot C_m \cdot S_0$,

$$\frac{\Delta T_b}{\Delta T_f} = \frac{K_b}{K_f} = \frac{RT_b^2}{1000 lv} \cdot \frac{1000 ly}{RT_f^2}$$
or $\frac{\Delta T_b}{\Delta T_f} = \frac{T_b^2}{T_f^2} \cdot \frac{l_f}{l_f}$

In the given case $\Delta T_b = 0.1 \text{ c}$; $T_b = 373 \text{ k}$, $T_f = 273 \text{ k}$ $M_f = 80 \text{ calgm}^2$, $N_f = 540 \text{ calgm}^2$.

So, $\frac{0.1}{\Delta T_f} = \left(\frac{373}{273}\right)^2 \frac{80}{540}$ or $\Delta T_f = 0.36 \text{ c}$.

So, freezing point is -0.36 c .

Q.10 Chemical potential of O_2 at 300 K is supposed to be 10 kCal. mol⁻¹ at 1 atm. A 1:4 (mole ratio) mixture of O_2 and N_2 is prepared at 1 atm and 300 K. The pressure of the mixture is increased to 5 atm. Calculate the chemical potential of oxygen in the mixture and in the pure state at 5 atm and 300 K.

For pure Oxygen,
$$d\mu_i^* = V_i dP$$

$$\mu_i^*(satm) = \int_{P}^{Satm} dP = RT \ln \frac{S}{I}$$

$$\mu_i^*(1atm) = \int_{I}^{I} dP$$

in the pure state at 5 atm, 300K is

chemical potential of 02 in the pure state at 5 atm, 300K is

$$\mu_{02}(satm) = \mu_{02}(1atm) + RT \ln 5$$

= 10 Kcalmet + (1.987 cal K mot) (300K) ln 5

= 10.96 K cal mot)

gn the mixture,

 $\mu_{02}(satm) = \mu_{02}(satm) + RT \ln x_{02}$
 $\mu_{02}(satm) = \mu_{02}(satm) + RT \ln x_{02}$

= 10.96 Kcalmot + (1.987 cal K mot) (300K) ln =

= 10.96 Kcalmot .

Q.11 Calculate the change in free energy when 2 moles of H_2 , 3 moles of O_2 and 5 moles of N_2 are mixed at 1 atm, 300 K. Also determine ΔG when the pressure of the mixture is increased to 5 atm. Calculate ΔS_{mix} and ΔH_{mix} . **Sol.**:

Here
$$x_{H2} = \frac{1}{5}$$
, $x_{O2} = \frac{3}{10}$, $x_{N2} = \frac{1}{2}$
 46 mixture = $R + \sum m_i \ln x_i$
= $(1.987 \text{ cal } \text{k}^{\dagger} \text{mol}^{\dagger}) (300 \text{k}) \left[2 \ln \frac{1}{5} + 3 \ln \frac{3}{10} + 5 \ln \frac{1}{2} \right]$ mole
= -6.138 Keal
 46 mixture is independent of pressure.
 45 mix = $-\left[\frac{\partial (46 \text{mix})}{\partial T} \right] = -R \sum n_i \ln x_i = 20.46 \text{ cal } \text{k}^{\dagger}$

:.
$$4 \text{Hmix} = 4 \text{Gemix} + T 4 \text{Smix}$$

= $6.138 \text{ Keal} - \frac{20.46 \times 300}{1000} \text{ Keal}$
= $0.$