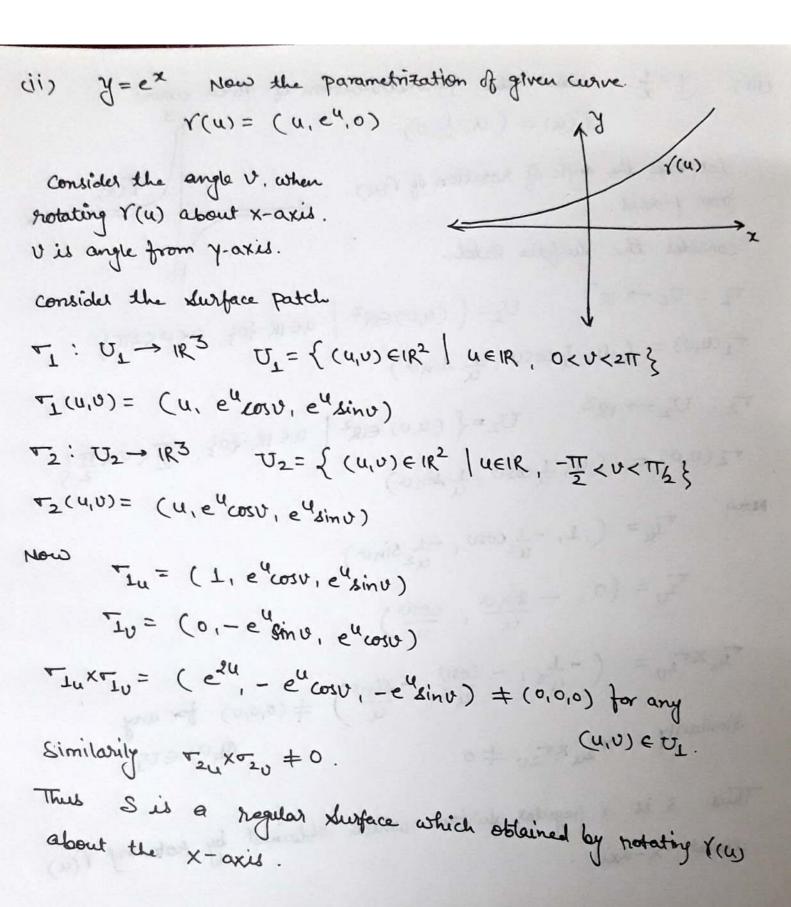
Assignment #8 Ans[1] (i) S: x2+y2-=2=1 consider the surface patch of S $\nabla_{\mathbf{I}}: U_{\mathbf{I}} \longrightarrow \mathbb{R}^{3}$ where $U_{\mathbf{I}} = \{(u,v) \in \mathbb{R}^{2} \mid u^{2} + v^{2} > 1\}$ $\frac{+z}{\sqrt{1}}(u,v) = \left(u,v,\sqrt{u^2+v^2-1}\right)$ T2: U1 → 183 $\sqrt{\frac{2}{2}}(u,v) = (u,v,-\sqrt{u^2+v^2-1})$ 53: U2 → 1R3 where U2 = { (4,0) ∈1R2 | u2-v2<1} $\sqrt{3} (u,v) = (u, \sqrt{1+v^2-u^2}, v)$ $\nabla_{L_{u}} = (1,0,\frac{u}{\sqrt{u^{2}+v^{2}-1}}), \quad \nabla_{L_{v}} = (0,1,\frac{v}{\sqrt{u^{2}+v^{2}-1}})$ similarily = 2 × 2 v + 0 & 3 u × 3 v + 0. Thus S is a regular surface. S: { (x,y, Z) \in 183 | x2+y2-Z2-1=0} here $f(x,y,Z) = x^2+y^2-Z^2-1$ for level surface representation. clearly $\nabla f = (f_x, f_y, f_z) = (2x, 2y, 2z) \neq 0$ for any so S is a smooth surface also. hence every regular surface patch of (x, y, z) ES. s will be allowable.

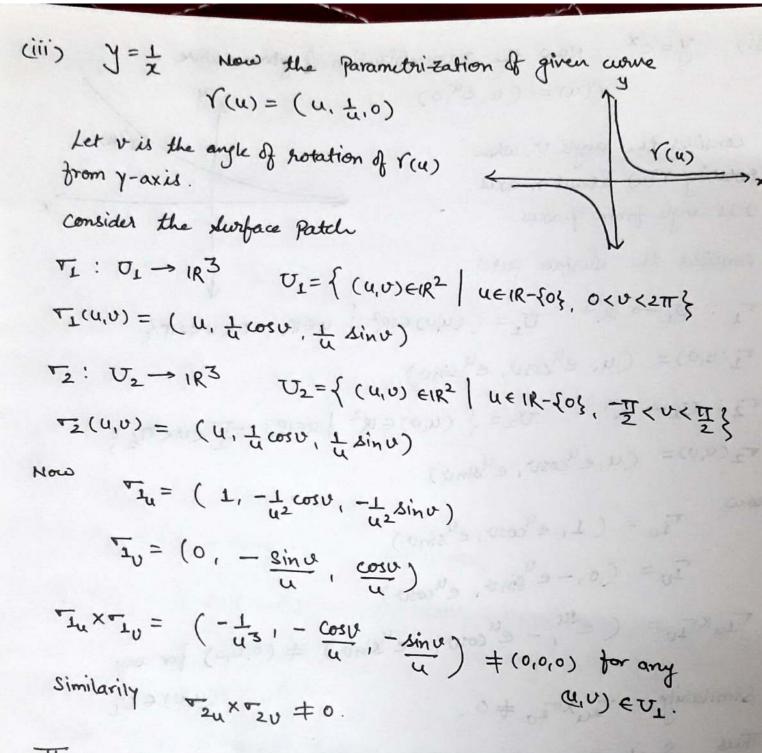
(ii) S: $x^2 + 4y^2 = 4$ consider the surface Patch of S U_= { (u,v) \in 12 | 0 < u < 2TT, v \in } TI: UI - IR3 $\tau_{\perp}(u,v) = (2\cos u, \sin u, v)$ Te: U2 - 1R3 UZ={(U,U) EIR2 | - IZ < U < II, UEIR} $\sqrt{2}(u,v) = (2\cos u, \sin u,v)$ $T_u = (-2\sin u, \cos u, 0), \quad T_v = (0, 0, 1)$ Tux Tu = (cosu, esinu, 0) = (0,0,0) for any UEU1. Similarity for \$20 x 020 \$ (0,0,0) for any $u \in \mathcal{U}_2$. hence S is a regular surface. Now S: $\{(x,y,z) \in \mathbb{R}^3 \mid f(x,y,z) = x^2 + 4y^2 - 4 = 0\}$ $\nabla f = (f_x, f_y, f_z) = (lx, 8y, 0) \neq (0,0,0)$ for any $(x, y, z) \in S$. Thus S is a smooth surface hence allowable surface patches are there. (\$1, \$72 are also allowable). (iii) see it in the book . cylinder with axis as x-axis S: y2+=2=1 U1= { (4,0) EIR2 | O<4<211, UEIR } T (u,u): U_ ~ K3 $\mathcal{I}(u,v) = (v, \cos u, \sin u)$ 5, (4,0): U2 → 1R3 02={ (u,v) e12 | -11 < u < 11 , v e1 } ₹2(4,0) = (V, cosu, Linu) check! Regularity. $\nabla f = (0,24,27) \neq (0,0,0)$ for any point $(x,4,7) \in S$. S is smooth.

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(iv) S: Z= x2+242
       consider the surface patch of S
     T1: U1 → 183 U1= { (4,0) €182 | UEIR, VEIR } = 182
     \forall (u,v) = (u,v,u^2+2v^2)
 NOW TU = (1,0,24), TU = (0,1,40)
    Tu×Tv = (-2u, -4v,+1) ≠ (0,0,0) for any (ti,v) ∈ 12.
    So S is a regular surface.
      S: { (x,y, \tau) \engline 1R3 | f(x,y,\tau) = 22+242-\tau=0 \frac{1}{5}.
      \nabla f = (2x, 2y, -1) \neq (0, 0, 0) for any (x, y, 7) \in S.
    Thus S is smooth hence or is allowable.
(V) S: y= sinx consider the surface patch of s
      T: U_ → 1R3 U_= { (u,v) ∈ 1R2 \ o < u < 21T, v ∈ 1R }
     T1(u,v) = (u, sinu,v)
     45(n'n) = (n'pinn'n)
           \sigma_{L_u} = (1, +\cos u, 0), \quad \sigma_{L_v} = (0, 0, 1)
  L^{Tn} \times_{\Delta} T^{n} = (\cos n' - 1'0) + (0'0'0) + \cos n (n'n) \in \Omega^{T}
    Similarily F2, X = 20 = 0
   Thus Sis a fregular surface.
    S: { (x, y, Z) e 1 R3 | f(x, y, Z) = y-sinx = 0 }
     \nabla f = (-\cos x, 1, 0) \neq (0,0,0) for any (x, y, z) \in S.
    to Sis smooth. Thus or is allowable.
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Ans [2] (i) y= 1+x2 Now the Parametrization of given when $Y(u) = (u, 14u^2, 0)$ consider the angle v from y-axis when hotating about x-axis. Consider the Surface patch TI: UI -> IR3 UI = {(u,v) \in IR2 | u \in IR, O < U < 2 TTZ ~ I(u,v) = (u,(1+u2) cosv, (1+u2) sinv) T2: U2 → 1R3 U2= {(u,v) ∈ 1R2 | u ∈ 1R, -1T< v < T/2} $\sqrt{2}(u,v) = (u,(1+u^2)\cos v,(1+u^2)\sin v)$ Tu = (1, 24 coso, 24 sino) $\nabla_{10} = (0, -(1+u^2) \sin \theta, (1+u^2) \cos \theta)$ Tux Tu = (24 (1+42), - (1+42) cosv, - (1+42) sinv) + (0,0,0) for any (u,v) & UI similarily \$20×520 = 0. Thus S is a regular surface which obtained by rotating V(u)

about the x-axis.





Thus S is a regular surface which obtained by notating r(u) about X-axis.