Problem Set 3

1. From the equation the value of B is 20.56 cm⁻¹.

Use this value to plot the energy levels in question 1a, which will be located at 0, 2B, 6B, 12 B and 20B.

The spectral lines occur at 2B, 4B, 6B and 8B which is required to plot the spectrum in 1b.

Use this value of B and the reduced mass of HF to get the value of the bond length, r, in 1c. Calculations of this type were done in earlier assignments.

Equation 2, gives you the value of B to be 20.56 cm^{-1} and the centrifugal distortion constant D to be $2.13 \times 10^{-3} \text{ cm}^{-1}$.

Use this equation to plot the energy levels and spectrum in 1d and 1e.

To calculate the vibrational frequency in problem 1d, use the equation

$$\omega_e^2 = 4B^3/D$$

= 4 x (20.56)³/(2.13 x 10⁻³)
=1.632 x 10⁷
 $\omega_e = 4039.9 \text{ cm}^{-1}$

2. The energy level equation for the harmonic oscillator is

$$G(v) = \omega_e (v + \frac{1}{2})$$
 and

For the anharmonic oscillator the energy level equation is

$$G(v) = \omega_e (v + \frac{1}{2}) + \omega_e x_e (v + \frac{1}{2})^2$$

Use these equations to plot the energy levels and the spectra for problems 2 and 3...

Use the selection rules $\Delta v = \pm 1$ for the harmonic oscillator.

For the anharmonic oscillator, in addition to the $\Delta v = \pm 1$, other overtone transitions involving $\Delta v = \pm 2$, $\Delta v = \pm 3$,... are also possible, though with progressively weaker intensities. The fundamental with the $\Delta v = \pm 1$, from v = 0 to v = 1, will be the strongest.

Hot bands involve transitions, from higher vibrational levels, such as from v=1, v=2 etc. These also have weak intensities due to the smaller populations in these levels relative to the population in v=0.