

$$\frac{d[A]}{dt} = -k[A]^n$$

$$\int_{[A]_0}^{[A]} \frac{d[A]}{[A]^n} = -k \int_0^t dt$$

$$\left(\frac{1}{(-n+1)} \frac{1}{[A]^{n-1}} \right) \Big|_{[A]_0}^{[A]} = \frac{1}{-n+1} \left(\frac{1}{[A]^{n-1}} - \frac{1}{[A]_0^{n-1}} \right) = -kt$$

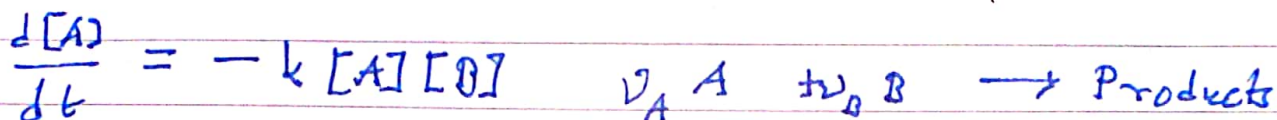
$$\boxed{\frac{1}{n-1} \left(\frac{1}{[A]^{n-1}} - \frac{1}{[A]_0^{n-1}} \right) = kt} \quad \left| \quad n \neq 1 \right.$$

$$\left. \begin{array}{l} t = t_{1/2} \\ [A] = [A]_0/2 \end{array} \right\} \rightarrow \frac{1}{n-1} \left(\frac{2^{n-1}}{[A]_0^{n-1}} - \frac{1}{[A]_0^{n-1}} \right) = kt_{1/2}$$

$$\frac{1}{[A]_0^{n-1}} \times \frac{2^{n-1} - 1}{n-1} = kt_{1/2}$$

$$\frac{d[A]}{dt} = -k[A]^2 \Rightarrow \sum_{n=2}^{\infty} \boxed{\left(\frac{1}{[A]} - \frac{1}{[A]_0} \right) = kt}$$

①



$$\begin{aligned} -\frac{dx}{dt} &= -k([A]_0 - x)([B]_0 - x) \\ \frac{dx}{dt} &= k([A]_0 - x)([B]_0 - x) \end{aligned} \quad \left| \begin{array}{l} t=0 \quad [A]_0 \quad [B]_0 \\ t=t \quad [A] \quad [B] \\ [A] = [A]_0 - \nu_A x \\ [B] = [B]_0 - \nu_B x \end{array} \right. \quad \left| \begin{array}{l} [A] = [A]_0 - \nu_A x \\ [B] = [B]_0 - \nu_B x \end{array} \right.$$

$$\frac{dx}{([A]_0 - x)([B]_0 - x)} = k dt$$

$$\frac{1}{([A]_0 - [B]_0)} \frac{([A]_0 - x) - ([B]_0 - x)}{([A]_0 - x)([B]_0 - x)} dx = k dt$$

$$\frac{1}{([A]_0 - [B]_0)} \left[\int_0^x \frac{dx}{[B]_0 - x} - \int_0^x \frac{dx}{[A]_0 - x} \right] = \int_0^t k dt$$

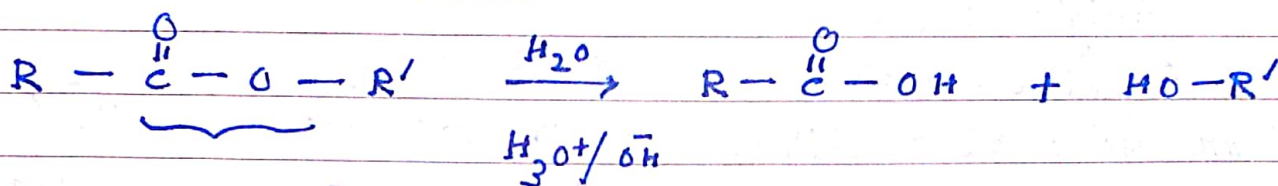
$$\frac{1}{[A]_0 - [B]_0} \left(-\ln \frac{[B]_0 - x}{[B]_0} + \ln \frac{[A]_0 - x}{[A]_0} \right) = kt$$

$$\frac{1}{[A]_0 - [B]_0} \left(-\ln \frac{[B]}{[B]_0} + \ln \frac{[A]}{[A]_0} \right) = kt$$

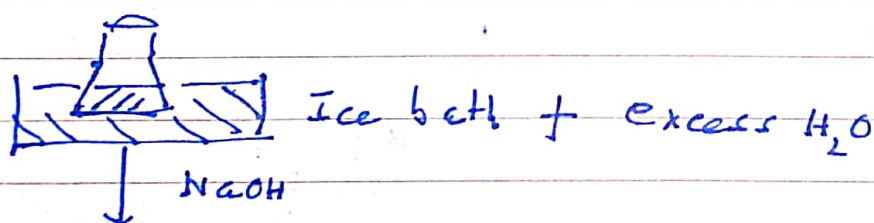
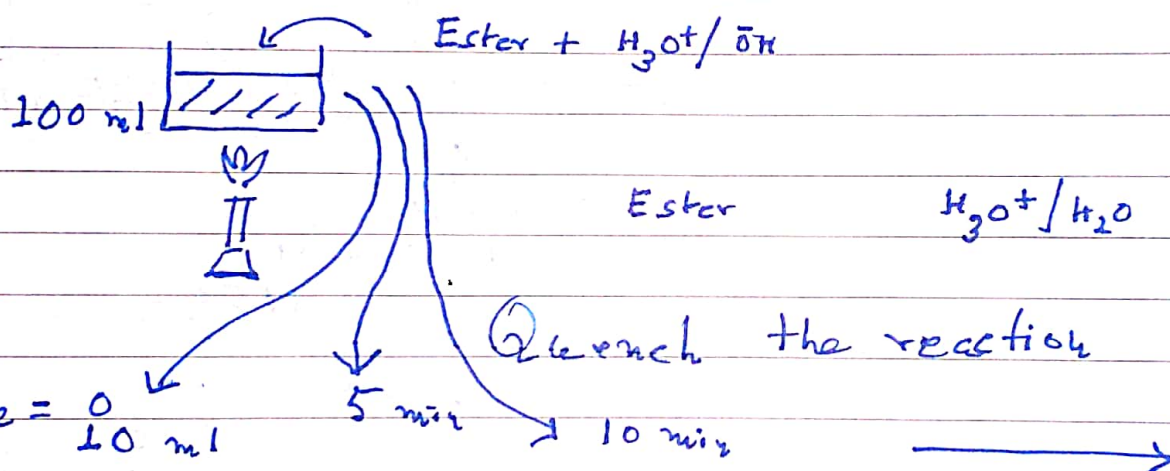
$$\boxed{\frac{1}{[A]_0 - [B]_0} \ln \frac{[A]/[A]_0}{[B]/[B]_0} = kt}$$

(2)

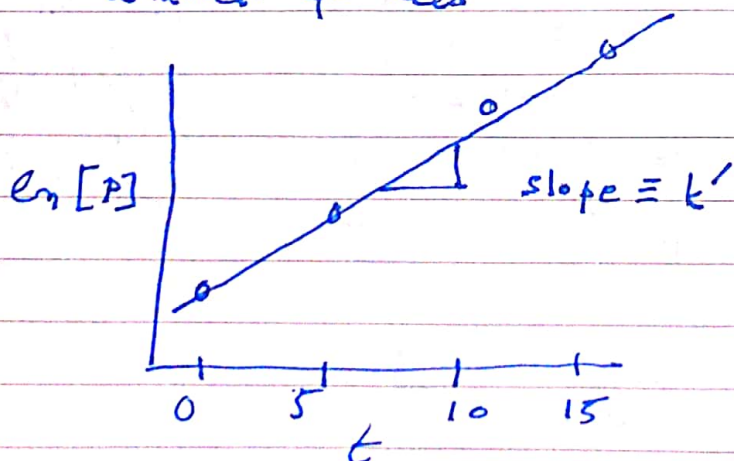
Hydrolysis of esters



$$\text{Rate} = k [\text{Ester}] [\text{H}_2\text{O}] \approx k' [\text{Ester}]$$



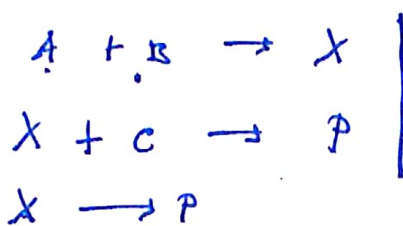
amount of acid



$$\frac{d[A]}{dt} = -k' [A]$$

$$\frac{d[P]}{dt} = k' [A]$$

$$\frac{d[A]}{dt} = -k[A][B][C] \dots$$

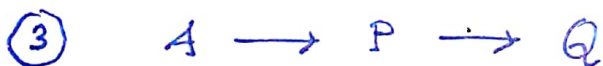
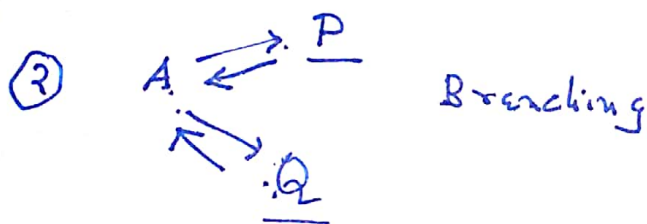


Mechanism

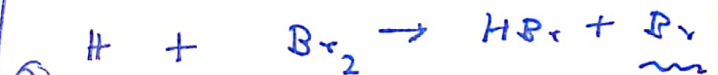
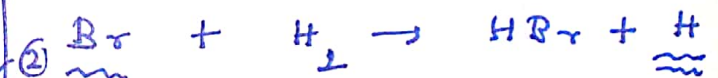
Composite reaction
(Multi-step process)



Elementary reaction
(Single step process)

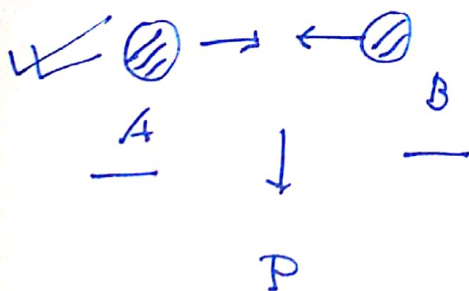


Rate $\propto [H_2][Br_2]$ X



Rate $= k_2 [Br] [H_2]$

k rate constant



$k = k(T)?$

$k = A e^{-E_a/kT}$
ln k

Arrhenius

