

3.
$$\iint_{R} \frac{1}{(2x+3y)^{3}} dA \qquad R: 0 \le x \le 1$$

$$= \int_{1}^{2} \left(\int_{0}^{1} \frac{dx}{(2x+3y)^{3}} \right) dy$$

$$= \int_{1}^{2} \left(\int_{1}^{1} \frac{dx}{(2x+3y)^{3}} \right) dy$$

$$= \int_{1}^{2} \left[\frac{-1}{2(2x+3y)} + \frac{1}{6y} \right] dy$$

$$= \int_{1}^{2} \left[\frac{1}{2(2x+3y)} + \frac{1}{2y} \right] dy$$

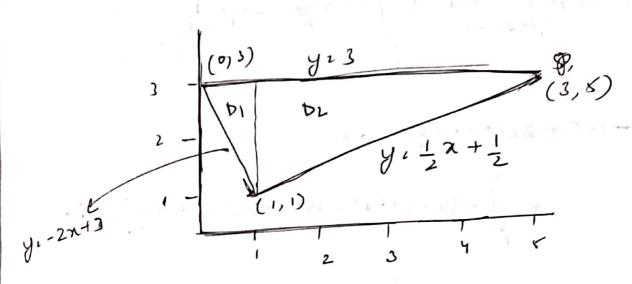
$$= \int_{1}^{2} \left[\ln \left(\frac{3}{2} \right) - \ln \left(\frac{3}{2} \right) \right] dy$$

$$= \int_{1}^{2} \left[\ln \left(\frac{3}{2} \right) - \ln \left(\frac{3}{2} \right) \right] dy$$

$$= \int_{1}^{2} \left[\frac{1}{2} \cos^{2} y \right]^{3} dy,$$

$$= \int_{1}^{2} \left[\frac{1}{2} \cos^{2} y \right]^{3} dy$$

SS (6xt-40y) dA, D is the triangle with vertices (0,3), (1)1), (5,3)



$$D_{1} = \{(x,y) \mid 0 \le x \le 1, -2x + 3 \le y \le 3\}$$

$$D_{2} : \{(x,y) \mid 1 \le x \le x, \frac{1}{2}x + \frac{1}{2} \le y \le 3\}$$

$$D_{3} : D_{4} : D_{5} : D_{$$

The intou triangle has an area D, bor last of wintegration, I have divided to into D, & Dz

Now, we have bound limits separately for each ougin, so we can would it in the usual form now

$$\int \int (6x^{2} - 40y) dA \cdot dx = \int \int (6x^{2} - 40y) dy dx + \int \int (6x^{2} - 40y) dy dx$$

$$= \int -2x + 3 \qquad \qquad 1 = \frac{1}{2}x + \frac{1}{2}$$

$$\int_{0}^{1} \left(6x^{2}y - 20y^{2}\right) \Big|_{-2x+1}^{3} dx + \int_{0}^{3} \left(6x^{2}y - 20y^{2}\right) \Big|_{\frac{1}{2}}^{3} x + \frac{1}{2}$$

$$\int_{0}^{2} \left(12x^{3} + 180 + 20(+2x+3)^{2}\right) dx$$

$$+ \int_{0}^{2} -3x^{2} + 18x^{2} - 180 + 20(\frac{1}{2}x + \frac{1}{2})^{2} dx$$

$$\frac{1}{2} \left[3x^{4} - 180x - \frac{10}{3}(3-2x)^{3}\right]_{0}^{1} + \left(-\frac{3}{4}x^{4} + 6x^{2} - 180x + \frac{1}{40}\left(\frac{1}{2}x + \frac{1}{2}\right)^{3}\right]_{0}^{2}$$

$$\frac{1}{2} \left[\frac{1}{2}x + \frac{1}{2}\right]_{0}^{3}$$

$$\frac{1}{2} \left[\frac{1}{2}x + \frac{1}{2}\right]_{0}^{3}$$

$$\frac{1}{2} \left[\frac{1}{2}x + \frac{1}{2}\right]_{0}^{3}$$

6.
$$\iint_{D} e^{x^2+y^2} dA = S \quad D - unit \ disk$$

$$envised at ordgin.$$

$$\lambda = reo30$$

$$\lambda = reo30$$

$$\lambda = r \cdot dr \cdot d\theta$$

$$[Remembut this for mean time]$$

$$\lambda = r^2 + y^2 = r^2 (eor^2\theta + inr^2\theta)$$

$$= r^2.$$

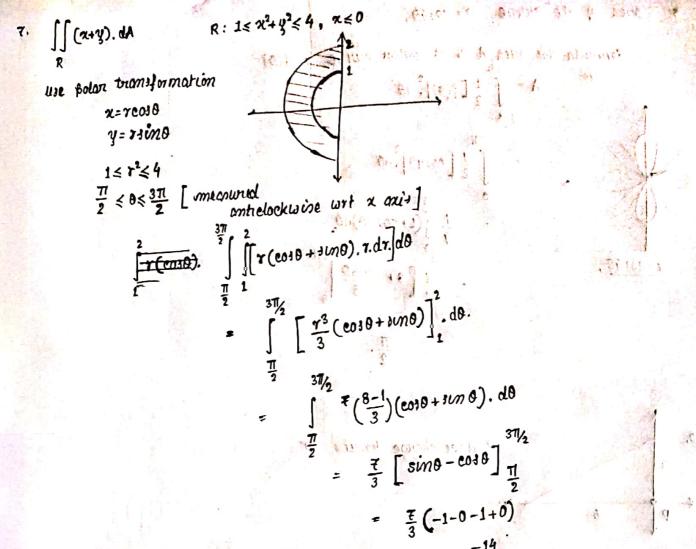
$$S = \int_{0}^{2\pi} \left(\int_{0}^{2\pi} e^{x^2} r \cdot dr \right) \cdot d\theta$$

$$= r^2 \cdot du = 2r \cdot dr.$$

$$\int_{0}^{2\pi} \left(\int_{0}^{2\pi} e^{x^2} r \cdot dr \right) \cdot d\theta$$

$$= \int_{0}^{2\pi} \left[\frac{e^u}{2} \right] \cdot d\theta$$

$$= \left(\frac{e^u}{2} \right) \cdot d\theta$$



8. 5.
$$\iint (4-n^2-y^2) dA$$
 R-evicle of radius 2.
 $R = 7 \times 10^{10}$ $R = 10^{10}$ $R = 7 \times 10^{10}$ R

9. Area of the eurove $T = \cos 40$.

9. Area of the eurove $T = \cos 40$. $A = \int_{0}^{1} \frac{1}{2} \left[4(0)^{-1} \right]^{2} d\theta$ $= \int_{0}^{1} \frac{1}{2} \left[\cos 4\theta \right]^{2} d\theta$ $= \int_{0}^{1} \frac{1}{4} \left[(1 + \cos 380) d\theta \right]$ $= \frac{1}{4} \int_{0}^{1} (1 + \cos 380) d\theta$ $= \frac{1}{4} \int_{0}^{1} (1 + \cos 380) d\theta$ $= \frac{1}{4} \left[\theta + \frac{\sin 80}{8} \right]_{0}^{2}$