# HOMEWORK 3 KNN, PERCEPTRON, LINEAR REGRESSION<sup>1</sup>

CMU 10-601: MACHINE LEARNING (FALL 2018)

piazza.com/cmu/fall2018/10601bd OUT: Thursday, Sep 20th, 2018

DUE: Friday, Sept 28th, 2018, 11:59pm TAs: Brynn Edmunds, Zhuoran Liu, Emilio Arroyo-Fang, George Xu

## START HERE: Instructions

Homework 3 covers topics on KNN, perceptron, and linear regression. The homework includes multiple choice, True/False, and short answer questions.

- Collaboration policy: Collaboration on solving the homework is allowed, after you have thought about the problems on your own. It is also OK to get clarification (but not solutions) from books or online resources, again after you have thought about the problems on your own. There are two requirements: first, cite your collaborators fully and completely (e.g., "Jane explained to me what is asked in Question 2.1"). Second, write your solution independently: close the book and all of your notes, and send collaborators out of the room, so that the solution comes from you only. See the Academic Integrity Section on the course site for more information: http://www.cs.cmu.edu/~mgormley/courses/10601bd-f18/about.html#7-academic-integrity-policies
- Late Submission Policy: See the late submission policy here: http://www.cs.cmu.edu/~mgormley/courses/10601bd-f18/about.html#6-general-policies
- Submitting your work:
  - Gradescope: For written problems such as short answer, multiple choice, derivations, proofs, or plots, we will be using Gradescope (https://gradescope.com/). Please use the provided template. Submissions can be handwritten onto the template, but should be labeled and clearly legible. If your writing is not legible, you will not be awarded marks. Alternatively, submissions can be written in LaTeX. Regrade requests can be made, however this gives the TA the opportunity to regrade your entire paper, meaning if additional mistakes are found then points will be deducted. Each derivation/proof should be completed on a separate page. For short answer questions, you should not include your work in your solution. If you include your work in your solutions, your assignment may not be graded

<sup>&</sup>lt;sup>1</sup>Compiled on Friday 28<sup>th</sup> September, 2018 at 16:36

correctly by our AI assisted grader. In addition, please tag the problems to the corresponding pages when submitting your work.

For multiple choice or select all that apply questions, shade in the box or circle in the template document corresponding to the correct answer(s) for each of the questions. For  $\LaTeX$  use  $\blacksquare$  and  $\blacksquare$  for shaded boxes and circles, and don't change anything else.

# Instructions for Specific Problem Types

For "Select One" questions, please fill in the appropriate bubble completely:
Select One: Who taught this course?
• Matt Gormley
○ Marie Curie
○ Noam Chomsky
If you need to change your answer, you may cross out the previous answer and bubble in the new answer:
Select One: Who taught this course?
• Matt Gormley
○ Marie Curie ▼ Noam Chomsky
For "Select all that apply" questions, please fill in all appropriate squares completely:
Select all that apply: Which are scientists?
■ Stephen Hawking
■ Albert Einstein
■ Isaac Newton
$\square$ I don't know
Again, if you need to change your answer, you may cross out the previous answer(s) and bubble in the new answer(s):
Select all that apply: Which are scientists?
■ Stephen Hawking
■ Albert Einstein
■ Isaac Newton ■ I don't know

For questions where you must fill in a blank, please make sure your final answer is fully included in the given space. You may cross out answers or parts of answers, but the final answer must still be within the given space.

Fill in the blank: What is the course number?

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# 1 K-Nearest Neighbors [30 pts]

1. [3pt] Consider the description of two objects below:

	Object A	Object B
Feature 1	3	9.1
Feature 2	2.1	0.7
Feature 3	4.8	2.2
Feature 4	5.1	5.1
Feature 5	6.2	1.8

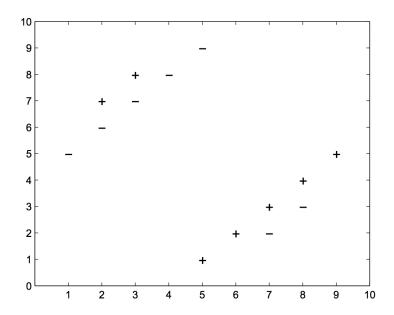
We can reason about these objects as points in high dimensional space.

Consider the two different distance functions below. Under which scheme are they closer in 5-D space?

(a) Euclidean Distance: 
$$d(x,y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$$

(b) Manhattan Distance: 
$$d(x,y) = \sum_{i=1}^{n} |x_i - y_i|$$

- Euclidean Distance
- O Manhattan Distance



2. [3pt] Consider a k-nearest neighbors binary classifier which assigns the class of a test point to be the class of the majority of the k-nearest neighbors, according to a Euclidean distance metric. Using the data set shown above to train the classifier and choosing k = 5, which is the classification error on the training set? Assume that a point can be its own neighbor.

Answer as a decimal with precision 4, e.g. (6.051, 0.1230, 1.234e+7)

0.2857

3. [3pt] In the data set shown above, what is the value of k that minimizes the training error? Note that a point can be its own neighbor.

1

4. [3pt] Assume we have a training set and a test set drawn from the same distribution, and we would like to classify points in the test set using a k-NN classifier. In order to minimize the classification error on this test set, we should always choose the value of k which minimizes the training set error.

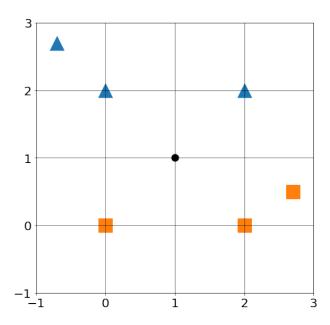
Select one:

○ True

• False

5. [3pt] Consider a binary k-NN classifier where k=4 and the two labels are "triangle" and "square".

Consider classifying a new point  $\mathbf{x} = (1, 1)$ , where two of the  $\mathbf{x}$ 's nearest neighbors are labeled "triangle" and two are labeled "square" as shown below.



Which of the following methods can be used to break ties or avoid ties on this dataset?

- (a) Assign x the label of its nearest neighbor
- (b) Flip a coin to randomly assign a label to  ${\bf x}$  (from the labels of its 4 closest points)
- (c) Use k = 3 instead
- (d) Use k = 5 instead

- O a only
- Ob only
- $\bigcirc$  b,c,d
- b,d
- Od only
- $\bigcirc$  a,b,c,d
- O None of the above

6. [3pt] Consider the following data concerning the relationship between academic performance and salary after graduation. High school GPA and university GPA are two numerical variables (predictors) and salary is the numerical target. Note that salary is measured in thousands of dollars per year.

Student ID	High School GPA	University GPA	Salary
1	2.2	3.4	45
2	3.9	2.9	55
3	3.7	3.6	91
4	4.0	4.0	142
5	2.8	3.5	88
6	3.5	1.0	2600
7	3.8	4.0	163
8	3.1	2.5	67
9	3.5	3.6	unknown

Among Students 1 to 8, who is the nearest neighbor to Student 9, using Euclidean distance?

Answer the Student ID only.



7. [3pt] In the data set shown above, our task is to predict the salary Student 9 earns after graduation. We apply k-NN to this regression problem: the prediction for the numerical target (salary in this example) is equal to the average of salaries for the top k nearest neighbors.

If k = 3, what is our prediction for Student 9's salary?

Round your answer to the nearest integer. Be sure to use the same unit of measure (thousands of dollars per year) as the table above.

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8. [3pt] Suppose that the first 8 students shown above are only a subset of your full training data set, which consists of 10,000 students. We apply KNN regression using Euclidean distance to this problem and we define training loss on this full data set to be the mean squared error (MSE) of salary.

Now consider the possible consequences of modifying the data in various ways. Which of the following changes **could** have an effect on training loss on the full data set as measured by mean squared error (MSE) of salary? Select all that apply.

	measured by mean squared error (MSE) of salary? Select all that apply.
	Select all that apply:
	$\blacksquare$ Rescaling only "High School GPA" to be a percentage of 4.0
	■ Rescaling only "University GPA" to be a percentage of 4.0
	$\square$ Rescaling both "High School GPA" and "University GPA", so that each is a percentage of 4.0 (scale by the same percentage).
	$\square$ None of the above.
9. [3pt] In this question, we would like to compare the differences among KN perceptron algorithm, and linear regression. Please select all that apply in the fol options.	
	Select all that apply:
	$\blacksquare$ For classification tasks, both KNN and the perceptron algorithm can have linear decision boundaries.
	$\Box$ For classification tasks, both KNN and the perceptron algorithm always have linear decision boundaries.
	$\blacksquare$ All three models can be susceptible to overfitting.
	$\Box$ In all three models, after the training is completed, we must store the training data to make predictions on the test data.
	$\square$ None of the above.

10.	[3pt] Please select all that apply about kNN in the following options.
	Select all that apply:
	$\blacksquare$ Large $k$ gives a smoother decision boundary
	$\blacksquare$ To reduce the impact of noise or outliers in our data, we should increase the value $k$ .
	$\square$ If we make $k$ too large, we could end up overfitting the data.
	$\blacksquare$ We can use cross-validation to help us select the value of $k$ .
	$\square$ We should never select the $k$ that minimizes the error on the validation dataset.

 $\square$  None of the above.

# 2 Perceptron [30 pts]

1. [3pt] Consider running the Perceptron algorithm on some sequence of examples S (an example is a data point and its label). Let S' be the same set of examples as S, but presented in a different order.

True or False: the perceptron algorithm is guaranteed to make the same number of mistakes on S as it does on S'.

### Select one:

O True

• False

2. [3pt] Suppose we have a perceptron whose inputs are 2-dimensional vectors and the vector component is either 0 or 1, i.e.,  $x_i \in \{0,1\}$ . The prediction function  $y = \text{sign}(w_1x_1 + w_2x_2 + b)$ , and

$$sign(z) = \begin{cases} 1, & \text{if } z \ge 0\\ 0, & \text{otherwise.} \end{cases}$$

Which of the following functions can be implemented with the above perceptron? That is, for which of the following functions does there exist a set of parameters w, b that correctly define the function. Select all that apply.

## Select all that apply:

- $\blacksquare$  AND function, i.e., the function that evaluates to 1 if and only if all inputs are 1, and 0 otherwise.
- OR function, i.e., the function that evaluates to 1 if and only if at least one of the inputs are 1, and 0 otherwise.
- $\square$  XOR function, i.e., the function that evaluates to 1 if and only if the inputs are not all the same. For example

$$XOR(1,0) = 1$$
, but  $XOR(1,1) = 0$ .

 $\square$  None of the above.

3. [3pt] Suppose we have a dataset  $\{(\mathbf{x}^{(1)}, y^{(1)}), \dots, (\mathbf{x}^{(N)}, y^{(N)})\}$ , where  $\mathbf{x}^{(i)} \in \mathbb{R}^M$ ,  $y^{(i)} \in \{+1, -1\}$ . We would like to apply the perceptron algorithm on this dataset. Assume there is no bias term. How many parameter values is the perceptron algorithm learning?

Select one:

- $\bigcirc N$
- $\bigcirc N \times M$
- $\bullet$  M
- 4. [3pt] Which of the following are true about the perceptron algorithm? Select all that apply.

Select all that apply:

- $\Box$  The number of mistakes the perceptron makes is proportional to the size of the dataset.
- $\square$  The perceptorn algorithm converges on any dataset.
- Perceptron algorithm can be used in the context of online learning.
- $\Box$  For linearly spearable data, the perceptron algorithm finds the separating hyperplane with the largest margin.
- $\square$  None of the above.
- 5. [3pt] Suppose we have the following data:

$$\mathbf{x}^{(1)} = [1, 2]$$
  $\mathbf{x}^{(2)} = [-1, 2]$   $\mathbf{x}^{(3)} = [-2, 3]$   $\mathbf{x}^{(4)} = [1, -1]$   $y^{(1)} = 1$   $y^{(2)} = -1$   $y^{(3)} = -1$   $y^{(4)} = 1$ 

Starting from  $\mathbf{w} = [0, 0]$ , what is the vector  $\mathbf{w}$  after running the perceptron algorithm with exactly one pass over the data? Assume we are running the perceptron algorithm without a bias term. If the value of the dot product of a data point and the weight vector is 0, the algorithm makes the prediction 1.

- $\bullet \ [1,-2]$
- $\bigcirc$  [2,0]
- $\bigcirc$  [-1,1]
- $\bigcirc$  [1, -3]

6. [3pt] Please refer to previous question for the data. Assume we are running perceptron in the batch setting. How many passes will the perceptron algorithm make before converging to a perfect classifier, i.e., one that does not make false prediction on this dataset?

Select one:

- 2
- $\bigcirc$  3
- $\bigcirc$  5
- O Infinitely many (the algorithm does not converge)
- 7. [3pt] We can view the perceptron algorithm as trying to minimize which of the following objective functions with stochastic gradient descent? Assume that we apply the notation where  $x_0 = 1$ .  $\theta_0$  is the bias term, and N is the number of data points. Note the function

$$f(x) = (x)_{+} = \begin{cases} x, & \text{if } x \ge 0\\ 0, & \text{otherwise} \end{cases}$$

Select one:

$$\bigcirc J(\boldsymbol{\theta}) = \sum_{i=1}^{N} -y^{(i)} \left(\boldsymbol{\theta} \cdot \mathbf{x}^{(i)}\right)$$

$$\bigcirc J(\boldsymbol{\theta}) = \sum_{i=1}^{N} y^{(i)} \left( \boldsymbol{\theta} \cdot \mathbf{x}^{(i)} \right)$$

• 
$$J(\boldsymbol{\theta}) = \sum_{i=1}^{N} \left( -y^{(i)} \left( \boldsymbol{\theta} \cdot \mathbf{x}^{(i)} \right) \right)_{+}$$

$$\bigcirc J(\boldsymbol{\theta}) = \sum_{i=1}^{N} \left( y^{(i)} \left( \boldsymbol{\theta} \cdot \mathbf{x}^{(i)} \right) \right)_{+}$$

8. [3pt] Continuing with the above question, what is the gradient of the correct loss function when the current data we are seeing is  $(\mathbf{x}^{(i)}, y^{(i)})$ ?

$$\bullet \begin{cases}
-y^{(i)}\mathbf{x}^{(i)}, & \text{if } -y^{(i)}\left(\theta \cdot \mathbf{x}^{(i)}\right) \ge 0 \\
0, & \text{otherwise.} 
\end{cases}$$

$$\bigcirc -y^{(i)}\mathbf{x}^{(i)}$$

$$\bigcirc y^{(i)}\mathbf{x}^{(i)}$$

$$\bigcirc \begin{cases} y^{(i)}\mathbf{x}^{(i)}, & \text{if } -y^{(i)}\left(\theta \cdot \mathbf{x}^{(i)}\right) \geq 0\\ 0, & \text{otherwise.} \end{cases}$$

<ul> <li>Select all that apply:</li> <li>☐ If the minimum distance from any data point to the separating hyperplane of the data is increased, the mistake bound will also increase.</li> <li>☐ If the maximum distance from any data point to the origin is increased, then the mistake bound will also increase.</li> <li>☐ If the maximum distance from any data point to the mean all data points increased, then the mistake bound will also increase.</li> </ul>	
the data is increased, the mistake bound will also increase.  □ If the maximum distance from any data point to the origin is increased, the the mistake bound will also increase.  ■ If the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the maximum distance from any data point to the mean all data points in the mean all data points in the maximum distance from any data point to the mean all data points in the mean all data points in the maximum distance from the mean all data points in the maximum distance from the mean all data points in the maximum distance from the mean all data points in the maximum distance from the mean all data points in the mean all data poin	
the mistake bound will also increase.  If the maximum distance from any data point to the mean all data points in	
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increased, then the inistance bound will also increase.	
$\Box$ The mistake bound is linearly inverse-proportional to the minimum distance of any data point to the separating hyperplane of the data.	
$\square$ None of the above.	
10. [3pt] Suppose we have data whose elements are of the form $[x_1, x_2]$ , where $x_1 + x_2 =$ We do not know the label for each element. Suppose the perceptron algorithm star with $\boldsymbol{\theta} = [1, 2]$ , which of the following values will $\boldsymbol{\theta}$ never take on in the process running the perceptron algorithm on the data?	
Select one:	
$\bigcirc$ [3, 0]	
$\bigcirc$ [-2, 5]	
$\bigcirc$ [1, 2]	
$\bullet$ [2, 3]	

# 3 Linear Regression [40 pts]

1. [4pt] Suppose you have data  $(x^{(1)}, y^{(1)}), \ldots, (x^{(n)}, y^{(n)})$  and the solution to linear regression on this data is  $y = w_1x + b_1$ . Now suppose we have the dataset  $(x^{(1)} + \alpha, y^{(1)} + \beta), \ldots, (x^{(n)} + \alpha, y^{(n)} + \beta)$  where  $\alpha > 0, \beta > 0$  and  $w_1\alpha \neq \beta$ . The solution to the linear regression on this dataset is  $y = w_2x + b_2$ . Please select the correct statement about  $w_1, w_2, b_1, b_2$  below. Note that the statement should hold no matter what values  $\alpha, \beta$  take on within the specified constraints.

#### Select one:

- $\bigcirc w_1 = w_2, b_1 = b_2$
- $\bigcirc w_1 \neq w_2, b_1 = b_2$
- $\bullet \ w_1 = w_2, b_1 \neq b_2$
- $\bigcirc w_1 \neq w_2, b_1 \neq b_2$
- 2. [4pt] We would like to fit a linear regression estimate to the dataset

$$D = \{ (\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), \cdots, (\mathbf{x}^{(N)}, y^{(N)}) \}$$

with  $\mathbf{x}^{(i)} \in \mathbb{R}^M$  by minimizing the ordinary least square (OLS) objective function:

$$J(\mathbf{w}) = \frac{1}{2} \sum_{i=1}^{N} \left( y^{(i)} - \sum_{j=1}^{M} w_j x_j^{(i)} \right)^2$$

Specifically, we solve for each coefficient  $w_k$   $(1 \le k \le M)$  by deriving an expression of  $w_k$  from the critical point  $\frac{\partial J(\mathbf{w})}{\partial w_k} = 0$ . What is the expression for each  $w_k$  in terms of the dataset  $(\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), \cdots, (\mathbf{x}^{(N)}, y^{(N)})$  and  $w_1, \cdots, w_{k-1}, w_{k+1}, \cdots, w_M$ ?

$$\bullet \ w_k = \frac{\sum_{i=1}^{N} x_k^{(i)} (y^{(i)} - \sum_{j=1, j \neq k}^{M} w_j x_j^{(i)})}{\sum_{i=1}^{N} (x_k^{(i)})^2}$$

$$\bigcirc w_k = \frac{\sum_{i=1}^N x_k^{(i)} (y^{(i)} - \sum_{j=1, j \neq k}^M w_j x_j^{(i)})}{\sum_{i=1}^N (y^{(i)})^2}$$

$$\bigcirc w_k = \sum_{i=1}^N x_k^{(i)} (y^{(i)} - \sum_{j=1}^M w_j x_j^{(i)})$$

$$\bigcirc \ w_k = \frac{\sum_{i=1}^N x_k^{(i)} (y^{(i)} - \sum_{j=1, j \neq k}^M w_j x_j^{(i)})}{\sum_{i=1}^N (x_k^{(i)} y^{(i)})^2}$$

3. [3pt] Continuing from the above question, how many coefficients do you need to estimate? When solving for these coefficients, how many equations do you have?

Select one:

- $\bigcirc N$  coefficients, M equations
- $\bigcirc M$  coefficients, N equations
- $\bullet$  M coefficients, M equations
- $\bigcirc N$  coefficients, N equations
- 4. [4pt] We are trying to derive the closed form solution for linear regression:

In the following, each row in X denotes one data point and Y is a column vector.

First we take the derivative of the objective function  $L = \frac{1}{2}(\mathbf{X}\mathbf{w} - Y)^T(\mathbf{X}\mathbf{w} - Y)$  with respect to  $\mathbf{w}$  and set it to zero, arriving at equation (\*).

Then after some algebraic manipulation, we get the solution  $\mathbf{w} = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T Y$ . What should equation (\*) be?

Select one:

- $\bullet (\mathbf{X}\mathbf{w} Y)^T \mathbf{X} = 0$
- $\bigcirc (\mathbf{X}\mathbf{w} + Y)^T \mathbf{X} = 0$
- $\bigcirc \mathbf{X}^T \mathbf{X} \mathbf{w} + Y^T \mathbf{X} = 0$
- $\bigcirc YX^TXw + X = 0$
- 5. [3pt] Suppose we are working with datasets where the number of features is 3. The optimal solution for linear regression is always unique regardless of the number of data points that are in this dataset.

- True
- O False

6. [3pt] Identifying whether a function is a convex function is useful because a convex function's local minimum has the nice property that it has to be the global minimum. Please select all functions below that are convex functions. Note dom(f) denotes the domain of the function f.

## Select all that apply:

$$\blacksquare f(x) = x, dom(f) = \mathbb{R}$$

$$\Box f(x) = x^3 + 2x + 3, dom(f) = \mathbb{R}$$

$$\Box f(x) = \log x, dom(f) = \mathbb{R}_{++}$$
 (the set of positive real numbers)

$$\blacksquare f(x) = |x|, dom(f) = \mathbb{R}$$

$$\blacksquare f(x) = ||\mathbf{x}||_2, dom(f) = \mathbb{R}^n$$

- $\square$  None of the above.
- 7. [3pt] Typically we can solve linear regression problems in two ways. One is through direct methods, e.g. solving the closed form solution, and the other is through iterative methods, e.g. using stochastic or batch gradient descent methods. Consider a linear regression on data (**X**, **y**). We assume each row in **X** denotes one input in the dataset. Please select all options that are correct about the two methods.

### Select all that apply:

- $\square$  If the matrix  $\mathbf{X}^T\mathbf{X}$  is invertible, the exact solution is always preferred for solving the solution to linear regression as computing matrix inversions and multiplications are fast regardless of the size of the dataset.
- $\blacksquare$  Assume N is the number of examples and M is the number of features. The computational complexity of N iterations of batch gradient descent is  $\mathcal{O}(MN)$ .
- When the dataset is large, stochastic gradient descent is often the preferred method because it gets us reasonably close to the solution faster than both the direct method and batch gradient descent.
- $\square$  None of the above.

8. [3pt] A data scientist is working on a regression problem on a large data set. After trying stochastic gradient descent (gradient is evaluated on a portion of the data set in each step) and batch gradient descent (gradient is evaluated on the entire data set in each step), the scientist obtained the values of the loss function for the two methods with respect to training time. Note that the same learning rate is used in both cases.

Time in hours	Stochastic GD	Batch GD
1	102.34	120.12
2	80.45	92.37
3	65.23	73.64
4	56.77	58.23
5	52.33	49.21
6	50.74	45.98
7	49.88	43.64

Select all the choices consistent with this table.

### Select all that apply:

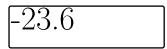
more accurate gradient direction than batch gradient descent.
$\square$ Within the first 3 hours, the table suggests that batch gradient descent makes more progress in finding the optimum of the objective function than stochastic gradient descent.
■ In general, stochastic gradient descent does not necessarily take a descent step in each step. However, stochastic gradient descent takes much less time to evaluate per step. In this table, during the first hour, stochastic gradient descent makes more update steps to the weights while batch gradient descent makes less updates. Hence it is reasonable that using batch gradient descent likely results in a higher value for the loss function (worse performance) than that of stochastic gradient descent at the 1 hour time point.
$\square$ None of the above.

☐ The table shows, in practice, that stochastic gradient descent can compute a

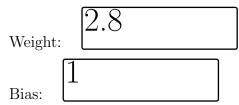
9. [3pt] Consider the following dataset:

If we initialize the weight as 2.0 and bias term as 0.0, what is the gradient of the loss function with respect to the weight w, calculated over all the data points, in the first step of the gradient descent update? Note that we do not introduce any regularization in this problem and and our objective function looks like  $\frac{1}{N} \sum_{i=1}^{N} (wx_i + b - y_i)^2$ , where N is the number of data points, w is the weight, and b is the bias term.

Fill in the blank with the gradient on the weight you computed, rounded to 2 decimal places after the decimal point.



10. [4pt] Based on the data of the previous question, please compute the direct solution of the weight and the bias for the objective function defined in the previous question, rounded to 2 decimal places after the decimal point.



11. [3pt] Using the dataset and model given in question 9, perform two steps of batch gradient descent on the data. Fill in the blank with the value of the weight after two steps of batch gradient descent. Let the learning rate be 0.01. Round to 2 decimal places after the decimal point.

$\boxed{2.42}$	

12. [3pt] Using the dataset and model given in question 9, which of the following learning rates leads to the most optimal weight and bias after performing two steps of batch gradient descent? (Hint: The most optimal learned parameters are the parameters that lead to the lowest value of the objective function.)

 $\bigcirc$  1

 $\bigcirc$  0.1

• 0.01

 $\bigcirc$  0.001

### Collaboration Questions Please answer the following:

After you have completed all other components of this assignment, report your answers to the collaboration policy questions detailed in the Academic Integrity Policies found here.

- 1. Did you receive any help whatsoever from anyone in solving this assignment? Is so, include full details.
- 2. Did you give any help whatsoever to anyone in solving this assignment? Is so, include full details.
- 3. Did you find or come across code that implements any part of this assignment? If so, include full details.

### Solution

Anuj Pahuja and I discussed some ideas related to overfitting of models, particularly if and when linear regression models overfit, and why they do that.