

# LaTeX Generation From PDF Content

I want to generate a latex file  
All the definitions and notation  
Any proofs and derivations in  
and it should have a detailed

I have also attached a Scribe



Below is the LaTeX code generated based on the lecture material from "L6\_S1\_A.pdf," formatted according to the style of 1

## Code snippet

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\documentclass[11pt]{article}
\usepackage[margin=1in]{geometry}
\usepackage{amsmath, amsfonts, amssymb, amsthm}
\usepackage{graphicx}

\title{CSE 400: Fundamentals of Probability in Computing \ Lecture 6: Discrete RVs, Expectation, and Po}
\author{Group-6 Scribe Refactoring}
\date{February 6, 2026}

\begin{document}

\maketitle

\section{Introduction to Random Variables}
A \textbf{Random Variable (RV)}  $X$  on a sample space  $\Omega$  is defined as a function  $X: \Omega \rightarrow \mathbb{R}$ 

\subsection{Discrete Random Variables}
A random variable is considered \textbf{discrete} if it can take on at most a countable number of possible values.

\begin{itemize}
\item \textbf{Support}: Countable (finite or countably infinite)[cite: 251].
\item \textbf{Probability Mass Function (PMF)}: Defined as  $P_X(x_k) = \Pr(X = x_k)$  for  $k = 1, 2, \dots$ 
\item \textbf{Constraint}: The sum of all probabilities in a PMF must equal 1:  $\sum_{k=1}^{\infty} P_X(x_k) = 1$ 
\end{itemize}

\section{Independent Events}
Two events  $A$  and  $B$  are \textbf{independent} if the occurrence of one does not provide information about the occurrence of the other.

\begin{itemize}
\item \textbf{Mathematical Definition}:  $\Pr(A|B) = \Pr(A)$  and  $\Pr(B|A) = \Pr(B)$ [cite: 583].
\item \textbf{Joint Probability}: For independent events,  $\Pr(A, B) = \Pr(A)\Pr(B)$ [cite: 583, 594].
\item \textbf{Mutual Independence}: Three events  $A$ ,  $B$ , and  $C$  are mutually independent if every pair is independent and  $\Pr(A, B, C) = \Pr(A)\Pr(B)\Pr(C)$ .
\end{itemize}

\section{Derivations and Bayes' Theorem}
\subsection{Bayes' Formula Derivation}
Using the definition of conditional probability  $\Pr(A|B) = \frac{\Pr(A, B)}{\Pr(B)}$ , we derive Bayes' Theorem[cite: 594].

\begin{equation}
\Pr(B_i|A) = \frac{\Pr(A|B_i)\Pr(B_i)}{\sum_{j=1}^n \Pr(A|B_j)\Pr(B_j)}
\end{equation}

Where  $\Pr(B_i)$  is the \textit{a priori} probability and  $\Pr(B_i|A)$  is the \textit{posteriori} probability.

\section{Types of Discrete Random Variables}

\subsection{Bernoulli Random Variable}
Models a single trial with two outcomes: Success (1) or Failure (0)[cite: 670, 679].
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\begin{itemize}
  \item \textbf{PMF}:  $P_X(1) = p$ ,  $P_X(0) = 1-p$ [cite: 691].
  \item \textbf{Examples}: Tossing a coin, spam detection, or demographic classification[cite: 707, 760].
\end{itemize}

\subsection{Binomial Random Variable}
Denoted as  $B(n, p)$ , it represents the number of successes in  $n$  independent trials[cite: 732, 734].
\begin{itemize}
  \item \textbf{PMF Derivation}:  $p(i) = \binom{n}{i} p^i (1-p)^{n-i}$  for  $i=0, 1, \dots, n$ [cite: 747].
  \item \textbf{Usage}: Number of defective items in a sample or correct answers on a test[cite: 761, 762].
\end{itemize}

\subsection{Geometric Random Variable}
Represents the number of trials required to achieve the \textbf{first} success in a sequence of independent trials.
\begin{itemize}
  \item \textbf{PMF}:  $P_X(X=n) = (1-p)^{n-1} p$ [cite: 794].
  \item \textbf{Proof of PMF Summation}:
    \begin{equation}
      \sum_{n=1}^{\infty} \Pr(X=n) = p \sum_{n=1}^{\infty} (1-p)^{n-1} = p \left( \frac{1}{1-(1-p)} \right) = 1
    \end{equation}
  \end{itemize}

\subsection{Poisson Random Variable}
Models the number of rare events occurring in a fixed interval[cite: 260].
\begin{itemize}
  \item \textbf{PMF}:  $p(i) = e^{-\lambda} \frac{\lambda^i}{i!}$  for  $i=0, 1, 2, \dots$ [cite: 837, 840].
  \item \textbf{Constraint Proof}:  $\sum_{i=0}^{\infty} e^{-\lambda} \frac{\lambda^i}{i!} = e^{-\lambda} e^{\lambda} = 1$ .
  \item \textbf{Approximation}: Can approximate  $B(n, p)$  when  $n$  is large and  $p$  is small[cite: 860, 861].
\end{itemize}

\section{Summary for Exam Review}
\begin{itemize}
  \item \textbf{RVs}: Understand mapping from Sample Space to Real Numbers[cite: 183].
  \item \textbf{Discrete vs. Continuous}: Discrete uses PMF (summation); Continuous uses PDF (integration).
  \item \textbf{Independence}: Key requirement for Binomial and Geometric distributions[cite: 723, 776].
  \item \textbf{Bayes' Theorem}: Crucial for updating probabilities based on observed evidence[cite: 400, 401].
  \item \textbf{Key Distributions}:
    \begin{itemize}
      \item \textbf{Bernoulli}: 1 trial, 2 outcomes[cite: 668, 670].
      \item \textbf{Binomial}:  $n$  trials, counting successes[cite: 732].
      \item \textbf{Geometric}: Waiting for the first success[cite: 779].
      \item \textbf{Poisson}: Rare events over time/space[cite: 260, 830].
    \end{itemize}
  \end{itemize}
\end{document}

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Would you like me to create a table comparing the Mean ( $\mu$ ) and Variance ( $\sigma^2$ ) for each of these discrete random variables?