

LaTeX Generation From PDF Content

I want to generate a latex file
All the definitions and notati
Any proofs and derivations in
and it should have a detailed

I have also attached a Scribe



Below is the LaTeX code generated based on the lecture material from "L6_S1_A.pdf," formatted according to the style of the document.

Code snippet

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\documentclass[11pt]{article}
\usepackage[margin=1in]{geometry}
\usepackage{amsmath, amsfonts, amssymb, amsthm}
\usepackage{graphicx}

\titl{CSE 400: Fundamentals of Probability in Computing \\ Lecture 6: Discrete RVs, Expectation, and PDFs}
\author{Group-6 Scribe Refactoring}
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\begin{document}

\maketitle

\section{Introduction to Random Variables}
A \textbf{Random Variable (RV)} $X$ on a sample space $\Omega$ is defined as a function $X: \Omega \rightarrow \mathbb{R}$.

\subsection{Discrete Random Variables}
A random variable is considered \textbf{discrete} if it can take on at most a countable number of possible values.
\begin{itemize}
    \item \textbf{Support}: Countable (finite or countably infinite)[cite: 251].
    \item \textbf{Probability Mass Function (PMF)}: Defined as $P_X(x_k) = \Pr(X = x_k)$ for $k = 1, 2, \dots$.
    \item \textbf{Constraint}: The sum of all probabilities in a PMF must equal 1: $\sum_{k=1}^{\infty} P_X(x_k) = 1$.
\end{itemize}

\section{Independent Events}
Two events $A$ and $B$ are \textbf{independent} if the occurrence of one does not provide information about the other.
\begin{itemize}
    \item \textbf{Mathematical Definition}: $\Pr(A|B) = \Pr(A)$ and $\Pr(B|A) = \Pr(B)$[cite: 583].
    \item \textbf{Joint Probability}: For independent events, $\Pr(A, B) = \Pr(A)\Pr(B)$[cite: 583, 594].
    \item \textbf{Mutual Independence}: Three events $A, B,$ and $C$ are mutually independent if every pair $(A_i, B_j, C_k)$ is independent.
\end{itemize}

\section{Derivations and Bayes' Theorem}
\subsection{Bayes' Formula Derivation}
Using the definition of conditional probability $\Pr(AB_i) = \Pr(B_i|A)\Pr(A)$, we derive Bayes' Theorem[cite: 583].
\begin{equation}
\Pr(B_i|A) = \frac{\Pr(A|B_i)\Pr(B_i)}{\sum_{j=1}^n \Pr(A|B_j)\Pr(B_j)}
\end{equation}
Where $\Pr(B_i)$ is the \textit{a priori} probability and $\Pr(B_i|A)$ is the \textit{posteriori} probability.

\section{Types of Discrete Random Variables}
\subsection{Bernoulli Random Variable}
Models a single trial with two outcomes: Success (1) or Failure (0)[cite: 670, 679].
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\begin{itemize}
    \item \textbf{PMF}:  $P_X(1) = p$ ,  $P_X(0) = 1-p$ [cite: 691].
    \item \textbf{Examples}: Tossing a coin, spam detection, or demographic classification[cite: 707, 76]
\end{itemize}

\subsection{Binomial Random Variable}
Denoted as  $B(n, p)$ , it represents the number of successes in  $n$  independent trials[cite: 732, 734].
\begin{itemize}
    \item \textbf{PMF Derivation}:  $p(i) = \binom{n}{i} p^i (1-p)^{n-i}$  for  $i=0, 1, \dots, n$ [cite: 747]
    \item \textbf{Usage}: Number of defective items in a sample or correct answers on a test[cite: 761, 76]
\end{itemize}

\subsection{Geometric Random Variable}
Represents the number of trials required to achieve the \textbf{first} success in a sequence of independent trials[cite: 794].
\begin{itemize}
    \item \textbf{PMF}:  $P_X(X=n) = (1-p)^{n-1} p$ [cite: 794].
    \item \textbf{Proof of PMF Summation}:
        \begin{equation}
            \sum_{n=1}^{\infty} \Pr(X=n) = p \sum_{n=1}^{\infty} (1-p)^{n-1} = p \left( \frac{1}{1-(1-p)} \right) = p
        \end{equation}
\end{itemize}

\subsection{Poisson Random Variable}
Models the number of rare events occurring in a fixed interval[cite: 260].
\begin{itemize}
    \item \textbf{PMF}:  $p(i) = e^{-\lambda} \frac{\lambda^i}{i!}$  for  $i=0, 1, 2, \dots$ [cite: 837, 84]
    \item \textbf{Constraint Proof}:  $\sum_{i=0}^{\infty} e^{-\lambda} \frac{\lambda^i}{i!} = e^{-\lambda} \lambda^0 / 0! = e^{-\lambda}$ 
    \item \textbf{Approximation}: Can approximate  $B(n, p)$  when  $n$  is large and  $p$  is small[cite: 866]
\end{itemize}

\section{Summary for Exam Review}
\begin{itemize}
    \item \textbf{RVs}: Understand mapping from Sample Space to Real Numbers[cite: 183].
    \item \textbf{Discrete vs. Continuous}: Discrete uses PMF (summation); Continuous uses PDF (integral)
    \item \textbf{Independence}: Key requirement for Binomial and Geometric distributions[cite: 723, 776]
    \item \textbf{Bayes' Theorem}: Crucial for updating probabilities based on observed evidence[cite: 779]
    \item \textbf{Key Distributions}:
        \begin{itemize}
            \item \textbf{Bernoulli}: 1 trial, 2 outcomes[cite: 668, 670].
            \item \textbf{Binomial}:  $n$  trials, counting successes[cite: 732].
            \item \textbf{Geometric}: Waiting for the first success[cite: 779].
            \item \textbf{Poisson}: Rare events over time/space[cite: 260, 830].
        \end{itemize}
\end{itemize}
\end{itemize}

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Would you like me to create a table comparing the Mean (μ) and Variance (σ^2) for each of these discrete random variables?