

Revised

U.S.N.

B.M.S. College of Engineering, Bengaluru-560019

Autonomous Institute Affiliated to VTU

December 2019 / January 2020 Semester End Main Examinations

Programme: B.E.

Branch: CSE/ISE

Course Code: 19MA3BSSDM

Course: STATISTICS & DISCRETE MATHEMATICS

Semester: III

Duration: 3 hrs.

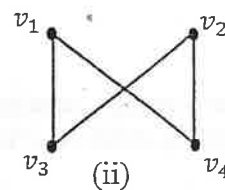
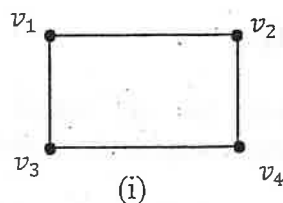
Max Marks: 100

Date: 17.12.2019

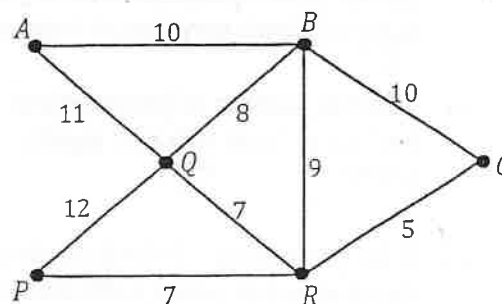
- Instructions: 1. Answer any FIVE full questions, choosing one full question from each unit.
2. Missing data, if any, may be suitably assumed.
3. Use of Statistical tables is permitted.

UNIT-1

- 1 a) Draw a diagram of the graph $G = (V, E)$ in each of the following cases: 6
- $V = \{A, B, C, D\}$, $E = \{AB, AC, AD, CD\}$
 - $V = \{v_1, v_2, v_3, v_4, v_5\}$, $E = \{v_1v_2, v_1v_3, v_2v_3, v_4v_5\}$
 - $V = \{P, Q, R, S, T\}$, $E = \{PS, QR, QS\}$
 - $V = \{v_1, v_2, v_3, v_4, v_5, v_6\}$, $E = \{v_1v_4, v_1v_6, v_4v_6, v_3v_2, v_3v_5, v_2v_5\}$
- b) Define isomorphism of graphs. Verify that the two graphs shown below are isomorphic or not. 7



- c) Using Kruskal's algorithm, find a minimal spanning tree for the weighted graph shown below: 7

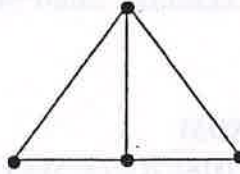


OR

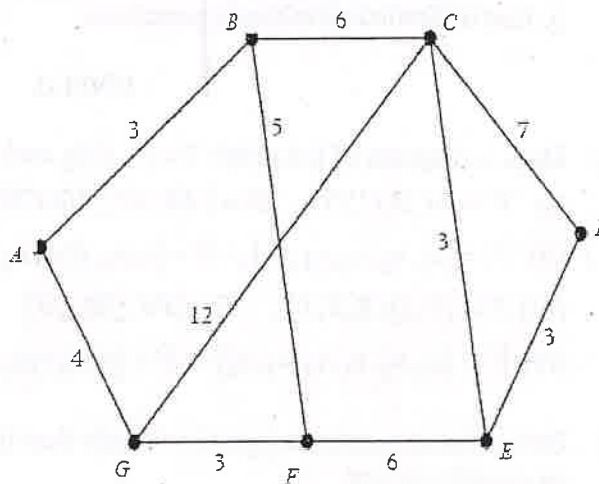
- 2 a) Let G be a simple graph with n vertices and m edges where m is at least 3. 6
- If $m \geq \frac{1}{2}(n-1)(n-2) + 2$, then prove that G is a Hamilton graph.

Important Note: Completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Revealing of identification, appeal to evaluator will be treated as malpractice.

- b) Write the adjacency matrix for the given graph and also find all the spanning trees of the graph. 7



- c) The diagram below shows roads connecting villages. The numbers on each arc represent the distance, in miles, along each road. Use Dijkstra's algorithm to find the minimum distance from vertex B to vertex D. 7



UNIT-2

- 3 a) How many arrangements are there for all letters in the word SOCIOLOGICAL? In how many of these arrangements A and G are adjacent? 6
- b) A certain question paper contains three parts A, B and C with four questions in part A, five questions in part B and six questions in part C. It is required to answer seven questions selecting at least two questions from each part. In how many different ways can a student select his seven questions for answering? 7
- c) Find the number of permutations of the English letters that contain (i) exactly two (ii) at least two (iii) exactly three of the patterns CAR, DOG, PUN and BYTE. 7

UNIT-3

- 4 a) If the probability of a bad reaction from a certain injection is 0.001, determine the chance that out of 2,000 individuals more than two will get a bad reaction. 6
- b) In a test on 2000 electric bulbs, it was found that the life of particular make, was normally distributed with an average life of 2040 hours and standard deviation of 60 hours. Estimate the number of bulbs likely to burn for 7

- (i) more than 2150 hours (ii) more than 1920 hours but less than 2160 hours

- c) A joint probability distribution is given by the following table:

Y \ X	-3	2	4
1	0.1	0.2	0.2
3	0.3	0.1	0.1

Find $COV(X, Y)$ and $\rho(X, Y)$.

UNIT-4

- 5 a) A coin was tossed 400 times and the head turned up 216 times. Test the hypothesis that the coin is unbiased at 5% level of significance.
- b) Two horses A and B were tested according to the time (in seconds) to run a particular race with the following results:

Horse A	28	30	32	33	33	29	34
Horse B	29	30	30	24	27	29	

Test whether you can discriminate between the two horses based on the average time taken to run a particular race at 5% level of significance.

- c) A set of five similar coins is tossed 320 times and the result is

No. of Heads	0	1	2	3	4	5
Frequency	6	27	72	113	71	32

Test the hypothesis that the data follows a binomial distribution at 5% level of significance.

OR

- 6 a) A certain stimulus administered to each of the 12 patients resulted in the following increase of blood pressure : 5, 2, 8, -1, 3, 0, -2, 1, 5, 0, 4, 6. Can it be concluded that the stimulus will be in general accompanied by an increase in blood pressure at 5% level of significance.
- b) Can we conclude that the two population variances are equal for the following data of post graduates passed out from a *State* and *Private* university?

State:	8350	8260	8130	8340	8070	
Private:	7890	8140	7900	7950	7840	7920

- c) A company claims that alloying reduces resistance of electric wire by more than 0.05 ohm. To test this claim samples of standard wire and alloyed wire are tested yielding the following results:

Type of wire	Sample Size	Mean resistance (ohms)	Standard deviation (ohms)
Standard	32	0.136	0.004
Alloyed	32	0.083	0.005

Can the claim be substantiated at 0.05 level of significance?

UNIT-5

- 7 a) A student's study habits are as follows; if he studies one night, he is 70% sure not to study the next night. On the other hand, if he does not study one night, he is 60% sure not to study the next night. In the long run how often does he study? 6
- b) The pattern of sunny and rainy days on the planet Rainbow is a homogeneous Markov chain with two states. Every sunny day is followed by another sunny day with probability 0.8. Every rainy day is followed by another rainy day with probability 0.6. i) Today is sunny on Rainbow. What is the chance of rain the day after tomorrow? ii) In the long run, what is the probability that it will be rainy on the planet Rainbow? 7
- c) Let us consider a small post office in a village where on the average 70 customers arrive according to a Poisson process during a day. Let us assume that the service times are exponentially distributed with the rate of 10 clients per hour and the office operates 10 hours daily. Find the mean queue length and the probability that the number of waiting customer is greater than 2. What is the mean waiting time and the probability that the waiting time is greater than 20 minutes? 7



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Q. No.	Course : <u>Statistics & Discrete Mathematics</u> Course Code : <u>19MA3BSSDM</u> Signature of the Paper Setter : <u>[Signature]</u> Signature of the Paper Scrutinizer : _____ Date : <u>22/11/2019</u> SCHEME OF VALUATION Date : _____	Marks
1.a)	<p>(i)</p> <p>(i) (ii) (iii) (iv)</p> <p>(1+1+2+2)</p> <p>b) From the given both the graphs have four vertices and four edges. The following one-to-one correspondence between the vertices of the graphs $u_1 \leftrightarrow v_1, u_2 \leftrightarrow v_4, u_3 \leftrightarrow v_3, u_4 \leftrightarrow v_2$</p> <p>This correspondence gives the following correspondence between the edges:</p> <p>$\{u_1, u_2\} \leftrightarrow \{v_1, v_4\}, \{u_1, u_3\} \leftrightarrow \{v_1, v_3\}$ $\{u_2, u_4\} \leftrightarrow \{v_4, v_2\}, \{u_3, u_4\} \leftrightarrow \{v_3, v_2\}$</p> <p>These represent one-to-one correspondence between the edges of the two graphs under which the adjacent vertices in the first graph correspond to adjacent vertices in the second graph and vice-versa. \therefore the two graphs are isomorphic.</p> <p>Defⁿ \rightarrow 2M</p> <p>c) The given graph has 6 vertices and spanning tree will have 5 edges. Let us put the edges of the graph in the non-decreasing order of their weights and on selecting 5 edges one by</p>	<p>06</p> <p>2M</p> <p>2M</p> <p>1M</p>



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Course Statistics & Discrete - Mathematics Course Code: 19 MA 3BSSDM

Signature of the Paper Setter

Signature of the Paper Scrutinizer

Q. No.

Date: 22/11/2019

SCHEME OF VALUATION

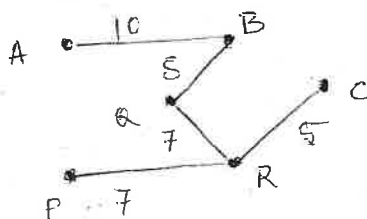
Marks

One is such a way that no cycle is created. The scheme is summarised below:

Edge	CR	PR	QR	BQ	BR	AB	BC	AQ	PQ
Weight	5	7	7	8	9	10	10	11	12
Select	Yes	Yes	Yes	Yes	No	Yes			

3M

Thus, a minimal spanning tree of the given graph contains the five edges CR, PR, QR, BQ, AB. This tree is shown in the following figure. The weight of the tree is 37 units.



4M

(3+4)

2. a) Let u and v be any two non-adjacent vertices in G . Let x and y be their respective degrees. If we delete u, v from G , we get a subgraph with $(n-2)$ vertices. If this subgraph has q edges, then $q \leq \frac{1}{2}(n-2)(n-3)$.

Since u and v are nonadjacent, $m = q + x + y$.
 Thus, $x + y = m - q \geq \left\{ \frac{1}{2}(n-1)(n-2) + 2 \right\} - \left\{ \frac{1}{2}(n-2)(n-3) \right\}$
 $= n$ ✓

(3+3)M

Therefore, the given graph is a Hamiltonian graph.

~~The converse of the result proved is not~~



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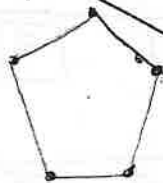
Date: 22/11/2019

SCHEME OF VALUATION Date:

Marks

always true. Because, a 2-regular graph with five vertices is Hamiltonian but the inequality does not hold.

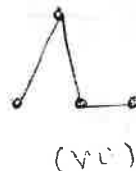
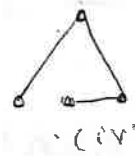
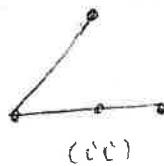
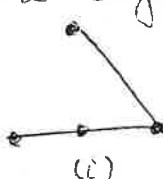
Ex.



(4+2)

2M

2.b) In the given graph, there are four vertices. Its spanning tree must include all these four vertices and three of the edges. Each such tree is got by deleting two edges from the graph. There are eight such trees are shown below:



3M

4M

Adjacency matrix

c) Step 1: Given a connected, weighted graph G with n vertices, assign n names (say: V_1, V_2, \dots, V_n or A, B, C & so on) to these vertices and prepare a $n \times n$ table in which the weights of all edges are shown. The entries in the table will be symmetric w.r.t. diagonal and no entries appear on the diagonal. Increase the weights of the non-existing edges as 0.

3M

A B C D
0 1 1 1
1 0 0 0
1 1 0 1
1 0 1 0

2c)

	A	B	C	D	E	F	G	
B	∞	0	∞	∞	∞	∞	∞	$A: \text{Min}(\infty, 5)$
A	3	0	6	∞	∞	5	∞	$C: \text{Min}(\infty, 6)$ $F: \text{Min}(\infty, 5)$
F	3	0	6	∞	∞	5	7	$G: \text{Min}(\infty, 7)$
C	3	0	6	∞	11	5	7	$G: \text{Min}(7, 8)$ $E: \text{Min}(\infty, 11)$
G	3	0	6	13	9	5	7	$G: \text{Min}(3, 13)$ $D: \text{Min}(\infty, 13)$ $E: \text{Min}(11, 9)$
E	3	0	6	13	9	5	7	$F: \text{Min}(\infty, 12)$
D	3	0	6	12	9	5	7	$D: \text{Min}(13, 12)$

Shortest path:

$B \rightarrow C \rightarrow E \rightarrow D$

Shortest distance = 12 (6 + 1) Marks



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	<p><u>Step-2:</u> Start from the vertex v_1 (or A) and connect it to its nearest neighbours in the v_1-row say v_k now, consider the edge $\{v_1, v_k\}$ and connect it to its closest neighbours. Let this vertex be v_m.</p> <p><u>Step-3:</u> Start from the vertex v_m and repeat the process of Step 2. Stop the process when all the n vertices have been connected by $(n-1)$ edges. These $(n-1)$ edges constitute a maximal spanning tree. (3+2+2)</p>	<p>2M</p> <p>2M</p>
3a)	<p><u>Unit -2</u></p> <p>The given word has 12 letters of which 3 are O, 2 are C, I, L and 1 each are S, A, G.</p> <p>\therefore the no. of arrangements of these letters is</p> $\frac{12!}{3! 2! 2! 2! 1! 1! 1!} = 99, 79, 200$ <p>of, in an arrangement, A and G are to be adjacent, we treat A & G together as a single letter say X so that we have 3 number of letters say X, 2 each of C, I, L and one each of S & X. These can be arranged in $\frac{11!}{3! 2! 2! 2! 1! 1!}$ ways.</p> <p>In the letters A & G can be arranged among themselves in two ways.</p> <p>\therefore the total no. of arrangements is</p> $\frac{11!}{3! 2! 2! 2! 1! 1!} \times 2 = 16, 63, 200 \text{ ways}$ <p style="text-align: right;">(2+4)</p>	<p>2M</p> <p>4M</p>



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3.b)	<p>The different possible ways in which a student can make a selection are</p> <p>(i) 2 questions from part A, 2 from B and 3 from C</p> <p>(ii) 2 questions from A, 3 from B and 2 from C</p> <p>(iii) 3 questions from A, 2 from B and 2 from C</p> <p>Selection (i) can be made in</p> $C(4,2) \times C(5,2) \times C(6,3) = 6 \times 10 \times 20 = 1200 \text{ ways}$ <p>Selection (ii) can be made in</p> $C(4,2) \times C(5,3) \times C(6,2) = 6 \times 10 \times 15 = 900 \text{ ways}$ <p>Selection (iii) can be made in</p> $C(4,3) \times C(5,2) \times C(6,2) = 4 \times 10 \times 15 = 600 \text{ ways}$ <p>\therefore the total no. of possible selection is</p> $1200 + 900 + 600 = \underline{2700} \text{ ways} \quad (1+5+1)$ <p>c) Let S denote the set of all permutations of the 26 letters. Then $S = 26!$</p> <p>Let A, be the set of all permutations in which CAR appears in which CAR consists of three letters to form single block. $\therefore A = 24!$</p> <p>Similarly $A_2 = A_3 = A_4 = 24!$</p> <p>where A_2, A_3 & A_4 are denotes the words DOG, PUN & BYTE respectively.</p> <p>$A_1 \cap A_2 = A_1 \cap A_3 = A_2 \cap A_3 = 22!$</p> <p>$A_1 \cap A_4 = A_2 \cap A_4 = A_3 \cap A_4 = 21!; A_1 \cap A_2 \cap A_3 = 20!$</p> <p>$A_1 \cap A_2 \cap A_4 = A_1 \cap A_3 \cap A_4 = A_2 \cap A_3 \cap A_4 = 19!$</p> <p>$A_1 \cap A_2 \cap A_3 \cap A_4 = 17!$</p>	<p>1M</p> <p>5M</p> <p>1M</p> <p>2M</p>



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	Course: <u>Statistic and Discrete Mathematics</u>	Course Code: <u>19MA3BSSPM</u>									
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Q. No.	Date: <u>22/11/2019</u>	SCHEME OF VALUATION Date: _____									
		Marks									
	<p> $S_0 = S = 261, S_1 = \sum A_i = 3 \times 241 + 231$ $S_2 = \sum A_i \cap A_j = (3 \times 221) + (3 \times 211)$ $S_3 = \sum A_i \cap A_j \cap A_k = 201 + (3 \times 191), S_4 = A_1 \cap A_2 \cap A_3 \cap A_4 = 171$ </p> <p> $(i) E_2 = S_2 - 3C_1 S_3 + 4C_2 S_4$ $(ii) L_2 = S_2 - 2C_1 S_3 + 3C_2 S_4$ $(iii) E_3 = S_2 - 4C_1 S_4$ </p> <p style="text-align: center;"><u>Unit - 3</u></p> <p> 4 a) Let X denotes the no. of individuals get bad reaction from a certain injection. Given, $p = 0.001, n = 2000$ In the poisson distribution $P(X) = \frac{e^{-\mu} \mu^x}{x!}$, where $\mu = np \Rightarrow \mu = 2$ $\Rightarrow P(X) = \frac{2^x}{x!} e^{-2}$ </p> <p> $P(X > 2) = 1 - P(X \leq 2) = 1 - \{P(X=0) + P(X=1) + P(X=2)\}$ $= 1 - \left[e^{-2} \frac{2^0}{0!} + e^{-2} \frac{2^1}{1!} + e^{-2} \frac{2^2}{2!} \right] =$ $= 1 - 0.6767 = \underline{0.323}$ </p> <p> b) Let X denotes the life of a bulb Given, $\mu = 2040$ hrs, $\sigma = 60$ hrs $Z = \frac{X - \mu}{\sigma} = \frac{X - 2040}{60}$ </p> <table border="1" style="margin-top: 10px; width: 100%; border-collapse: collapse;"> <tr> <td>X</td> <td>2150</td> <td>1920</td> <td>2160</td> </tr> <tr> <td>$Z = \frac{X - 2040}{60}$</td> <td>1.83</td> <td>-2</td> <td>2</td> </tr> </table>		X	2150	1920	2160	$Z = \frac{X - 2040}{60}$	1.83	-2	2	<p>2M</p> <p>3M (2+2+3)</p> <p>3M</p> <p>3M (3+3)</p> <p>3M</p>
X	2150	1920	2160								
$Z = \frac{X - 2040}{60}$	1.83	-2	2								



Date	Page	Topic
10/11/2023	1	Introduction to Engineering
11/11/2023	2	Engineering Drawing
12/11/2023	3	Engineering Mathematics
13/11/2023	4	Engineering Physics
14/11/2023	5	Engineering Chemistry
15/11/2023	6	Engineering Computer Graphics
16/11/2023	7	Engineering Workshop
17/11/2023	8	Engineering Project



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	<p>(i) $P(X > 2150) = P(Z > 1.83) = 0.5 - A(Z=1.83) = 0.0336$</p> <p>∴ The no of bulbs expected to burn for more than 2150 hrs = $0.0336 \times 2000 \approx 67$</p> <p>(ii) $P(1920 < X < 2160) = P(-2 < Z < 2) = 2P(0 < Z < 2) = 0.9544$</p> <p>∴ The no of bulbs expected to burn for more than 1920 but less than 2160 hrs = $0.9544 \times 2000 \approx 1909$ (3+2+2)</p>		2M														
4.c)	<p>The marginal distributions of X & Y are given below</p> <table border="1"> <tr> <td>x_i</td> <td>1</td> <td>2</td> </tr> <tr> <td>$f(x_i)$</td> <td>0.5</td> <td>0.5</td> </tr> </table> <table border="1"> <tr> <td>y_j</td> <td>-3</td> <td>2</td> <td>4</td> </tr> <tr> <td>$g(y_j)$</td> <td>0.4</td> <td>0.3</td> <td>0.3</td> </tr> </table> <p>$\mu_x = \sum x_i f(x_i) = 2, \mu_y = \sum y_j g(y_j) = 0.6$</p> <p>$E(XY) = \sum_i \sum_j x_i y_j f_{ij} = 0$</p> <p>$Cov(X, Y) = E(XY) - \mu_x \mu_y = -1.2$</p> <p>$E(X^2) = \sum x_i^2 f(x_i) = 5, E(Y^2) = \sum y_j^2 g(y_j) = 9.6$</p> <p>$\sigma_x^2 = E(X^2) - (\mu_x)^2 = 1, \sigma_y^2 = E(Y^2) - \mu_y^2 = 9.24$</p> <p>$\rho(X, Y) = \frac{Cov(X, Y)}{\sigma_x \sigma_y} = -0.3947$ (2+2+3)</p>		x_i	1	2	$f(x_i)$	0.5	0.5	y_j	-3	2	4	$g(y_j)$	0.4	0.3	0.3	2M
x_i	1	2															
$f(x_i)$	0.5	0.5															
y_j	-3	2	4														
$g(y_j)$	0.4	0.3	0.3														
5 a)	<p>Unit - 4</p> <p>H₀: coin is unbiased i.e. $p = 1/2$</p> <p>H₁: coin is biased i.e. $p \neq 1/2$</p> <p>Here $n = 400$, no of success = $X = 216$</p>		2M														



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	<p>In the binomial distribution $\mu = np = 400 \times 1/2 = 200$ & $\sigma = \sqrt{npq} = 10$ For two tailed test, under H_0, $Z = \frac{\hat{p} - E(p)}{SE(p)} = \frac{216 - 200}{10} = 1.6 \checkmark$ For two tailed test, from the normal distribution table at 5% l.o.s $Z_{\alpha} = 1.96 \checkmark$ <u>Conclusion</u>: Since $Z_{cal}(1.6) < Z_{tab}(1.96) \therefore H_0$ is accepted at 5% l.o.s. (2+3+1)</p>	<p>3M</p> <p>1M</p>
5.b)	<p>H_0: There is no discriminate between the two horses H_1: There is a discriminate between the two horses Let X & Y be the variables respectively corresponds to horse A & horse B. $n_1 = 7, n_2 = 6, \bar{x} = \frac{\sum x_i}{n_1} = 31.3, \bar{y} = \frac{\sum y_i}{n_2} = 28.2$ $\sum (x_i - \bar{x})^2 = 31.43, \sum (y_i - \bar{y})^2 = 26.84$ $s^2 = \frac{1}{(n_1 + n_2 - 2)} \left[\sum (x_i - \bar{x})^2 + \sum (y_i - \bar{y})^2 \right] = 5.2973$ Under $H_0, t = \left \frac{\bar{x} - \bar{y}}{s \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \right = 2.42$ From t-table (t/2) 0.05 for d.f. = 11 = 2.2 <u>Conclusion</u>: Since $t_{cal}(2.42) > t_{tab}(2.2)$ $\therefore H_0$ is rejected at 5% o.f l.o.s. (1+3+2+1)</p>	<p>1M</p> <p>3M</p> <p>2M</p> <p>1M</p>
c)	<p>H_0: The data follows a binomial distribution H_1: The data doesnot follows a binomial distribution</p>	<p>1M</p>



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Q. No.	<p>Course: <u>Statistics and discrete mathematics</u> Course Code: <u>19MA3BSSDM</u></p> <p>Signature of the Paper Setter _____ Signature of the Paper Scrutinizer _____</p> <p>Date: <u>22/11/19</u></p> <p align="center">SCHEME OF VALUATION</p>	Marks																														
	<p>$p = 1/2 \Rightarrow q = 1/2$ & $n = 320$</p> <table border="0"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td rowspan="2">}</td> </tr> <tr> <td>$f(x)$</td> <td>10</td> <td>50</td> <td>100</td> <td>100</td> <td>50</td> <td>10</td> </tr> </table> <p>$f(x) = n C_x p^x q^{n-x} \times N$</p> <table border="0"> <tr> <td>O_i</td> <td>6</td> <td>27</td> <td>72</td> <td>112</td> <td>71</td> <td>32</td> <td rowspan="2">}</td> </tr> <tr> <td>E_i</td> <td>10</td> <td>50</td> <td>100</td> <td>100</td> <td>50</td> <td>10</td> </tr> </table> <p>$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i} = 78.688$ (78.938)</p> <p>From table, $(\chi^2_{0.05})_{d.f. = 5} = 11.07$</p> <p>Conclusion: $\chi^2_{cal} > \chi^2_{tab} \therefore H_0$ is Rejected at 5% of LOS.</p> <p align="center"><u>OR</u></p> <p>6.a) $H_0: \mu = 1600 \text{ hrs}, H_1: \mu \neq 1600 \text{ hrs}$ $n = 100, \bar{x} = 1580, s = 90, \sigma_{\bar{x}} = s/\sqrt{n} = 9$ }</p> <p>Under $H_0, Z = \frac{\bar{x} - \mu}{\sigma_{\bar{x}}} = 2.22$ }</p> <p>From the table $(Z_{1/2}) = (Z_{0.05/2}) = 1.96$</p> <p>Conclusion: $\therefore Z_{cal} > Z_{tab} \therefore H_0$ is Rejected at 5% LOS (2+3+1)</p> <p>6.a) $H_0: \mu = 0, H_1: \mu \neq 0$ $\bar{x} = \sum \frac{x_i}{n} = 0.6, s^2 = \frac{1}{(n-1)} \sum (x_i - \bar{x})^2 = 3.08, n = 12$ }</p> <p>Under $H_0, t = \frac{ \bar{x} - \mu }{s/\sqrt{n}} = 2.94$ }</p> <p>From t-table $(t_{0.05/2})_{d.f. = 11}$ is 2.201</p> <p>Conclusion: since $t_{cal} > t_{tab} \therefore H_0$ is Rejected at 5% LOS (3+3+1)</p>	x	0	1	2	3	4	5	}	$f(x)$	10	50	100	100	50	10	O_i	6	27	72	112	71	32	}	E_i	10	50	100	100	50	10	<p>2M</p> <p>3M</p> <p>1M</p> <p>2M</p> <p>3M</p> <p>1M</p> <p>3M</p> <p>1M</p>
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6b)

$$H_0 : N.H. : \sigma_1^2 = \sigma_2^2$$

$$H_1 : A.H. : \sigma_1^2 \neq \sigma_2^2$$

$$n_1 = 5 \quad n_2 = 6 \quad \sum x_{1i} = 41150$$

$$\sum x_{1i}^2 = 338727500$$

$$S_1^2 = \frac{63000}{4} = 15750$$

$$\sum x_{2i} = 378316200 \quad \sum x_{2i}^2 = 378316200$$

$$S_2^2 = \frac{54600}{5} = 10920$$

$$F = \frac{S_1^2}{S_2^2} = \frac{15750}{10920} = 1.442$$

(4M)

At 5% $F_{(4,5)} = 5.19$ (1M)

Conclusion: $\therefore F < \text{Table Value}$
accept N.H. The Variances are not
significantly different (1M)

6c) $H_0 : N.H. : \mu_1 - \mu_2 = 0.05$ (1M)

$$H_1 : A.H. : \mu_1 - \mu_2 < 0.05$$

Test statistic: $Z = \frac{(\bar{x}_1 - \bar{x}_2) - \delta}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} = 2.65$ (4M)

$$Z_{0.05} = 1.645$$

Reject H_0 and accept A.H. (1M)
(1M)

Unit - 5

7a)

A: studying

B: not studying

$$P = \begin{matrix} & \begin{matrix} A & B \end{matrix} \\ \begin{matrix} A \\ B \end{matrix} & \begin{bmatrix} 0.3 & 0.7 \\ 0.4 & 0.6 \end{bmatrix} \end{matrix}$$

2M

Q. No.

Marks

Let $V = (x \ y)$ such that
 $VP = V$ where $x + y = 1$

$$\begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} 0.3 & 0.7 \\ 0.4 & 0.6 \end{bmatrix} = \begin{bmatrix} x & y \end{bmatrix}$$

Solving $V = (4/11, 7/11)$

In the long run the student will study $4/11$ or 36.36% of the time.

7b) state space: A: Sunny B: Raining
 A B
 A $\begin{bmatrix} 0.8 & 0.2 \end{bmatrix}$
 B $\begin{bmatrix} 0.4 & 0.6 \end{bmatrix}$

ci) $P^{(0)} = \begin{bmatrix} 1 & 0 \end{bmatrix}$
 $P^{(2)} = P^{(0)} P^2$

$$= \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} 0.72 & 0.28 \\ 0.56 & 0.44 \end{bmatrix} = \begin{bmatrix} 0.72 & 0.28 \end{bmatrix}$$

The chance of rain day after tomorrow is 0.28

cii) Let $V = (x \ y)$ such that
 $VP = V$ where $x + y = 1$

$$\begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} 0.8 & 0.2 \\ 0.4 & 0.6 \end{bmatrix} = \begin{bmatrix} x & y \end{bmatrix}$$

Solving $x = 0.667$ $y = 0.333$

In the long run it will be raining 0.33 or 33% of the times

7c. Let the time unit be an hour then

$$\lambda = 7, \quad \mu = 10$$

(1M)

$$\rho = \frac{\lambda}{\mu} = 0.7$$

Mean queue length $L_q = L_s - \rho$

$$= \frac{\rho}{1-\rho} - \rho = \frac{0.7}{1-0.7} - 0.7 = \frac{0.7}{0.3} - 0.7 = 1.633$$

Mean waiting time in the queue

$$W_q = \frac{\lambda}{\mu(\mu-\lambda)} = \frac{7}{10(10-7)} = \frac{7}{30} = 0.233$$

probability that the number of waiting customer is greater than 2 is

$$P(\geq 3) = \rho^3 = (0.7)^3 = 0.343$$

$$(2+2+2)^M$$

The scheme is discussed by the following members
C.D.R. T. N. Vishalakshi

1) Abhishek

2) Sreyas [SHAZIA P.A]

3) T.S. Mallikarjuna (DR. B. Mallikarjuna)

TO COE,

This scheme and solution is approved for valuation.

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