

DAA LABORATORY 6

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SY Btech Comp eng.

TASK 1:

Aim: Consider grades received by 20 students, like AA, AB, BB, ..., FF of each student. Computer the Longest common sequence of grades among students.

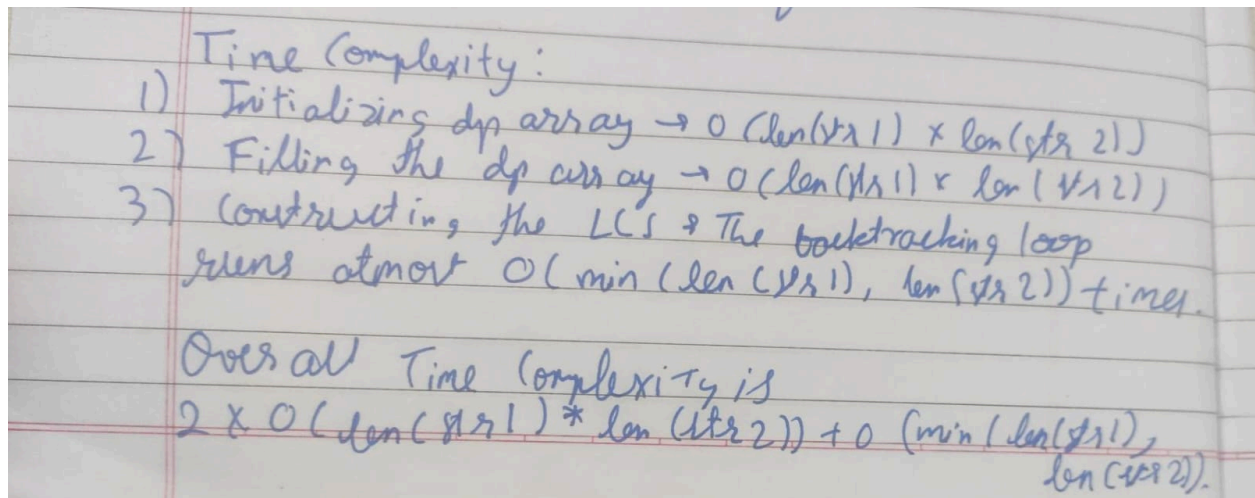
Algorithm:

```
function lcs (str 1, str 2):  
    initialize 2D list 'dp' of size (len(str 1)+1,  
        len(str 2)+1) to all elements 0  
    i → from 1 to len (str 1)  
    j from 1 to len (str 2)  
    if str 1[i-1] == str 2[j-1]:  
        dp[i][j] = dp[i-1][j-1] + 1  
    else  
        dp[i][j] = max(dp[i-1][j], dp[i][j-1])
```

```
initialize a list 'lcs-seq'  
i = len(str 1), j = len (str 2)  
while i > 0 and j > 0  
    if str 1[i-1] == str 2[j-1]:  
        append str 1[i-1] to lcs-seq  
        decrease i and j by 1  
    else if  
        dp[i-1][j] > dp[i][j-1]  
        i--  
    else  
        j--
```

```
return reverse (lcs-seq)
```

Time Complexity:



Positive Testcases:

1)

```
Student ID, Grades
S1, CDABABFFFFFFFFFFFABCDABCCCDDBC AAAAFFCDFFBCCC
S2, FFFFC AABCCDCDABCCBCABFFABCDDBBFFBCABFFBB
S3, CDABCCCCABABABCCABABBCCCCDCDDAA AAFABFF
S4, BBBBFFABBBABAABCAABBBFFFFBCCDCDFFABAACCCC
S5, AACDABFFCDBBAAFFAAAABBBBCFFCCBBBBBCCDFFAB
S6, AAABABCDFFCDABABBCBCBCBBBCAAAACDFFAABCAB
S7, CDABBCABAAAACDCCCCBBBCBBCCAAFFBBBCCDBCCD
S8, AAAABBAABCCDABAABCBCCDDBBBBBCBBFFBCBBCDCC
S9, FFAAABBBBCDCDCDBCBCBBFFCCCCBBBBBBBBBBB CAAAA
S10, BBBCCDAACCCDFFFFABBCABCD CDABCCCCABAACCBC
S11, BBCDBBCCFFFFABBBBBBBCBCC CABBBBCBBB BCDDBB
S12, CCCDCCBBCCCCFFAABCCDAABBBCCDCDBB BCFABCC
S13, CDABFFBBFFCDBCABBBBCBCFFABCCCCABCCAACDBC
S14, BBBCCDBCAABCABBCDFFCCFFCDABCCBCCCCFFBCBC
S15, ABCCABBCAACDAAFFFFCCFFBBBBBCCCCBCBBBBABAA
S16, BBBCBCCDCCCCBBCDCCCCCABFFFFFAAFFFB CAAFF
S17, CCAACCABAACCAABBBCCCFFAABCCDBCBB CDCCABBC
S18, CDBCBCBCBCFFBBCDAACDCB BCDCCFFBBB CAACCB
S19, CDABCCAAFFBBCDBBFFAACDBBAAAABCBCFFBBAACD
S20, AAAACDCDCCCCCFFABBCBBBCBCC CABBBBCCCBBC
```

Longest Common Subsequence of Grades for All Students in Test Case 1: CFFB

2)

```
Student ID, Grades
S1, CDABABFFFFFFFFFFABCDABCCCDDBCAAAFFCDFFBCCC
S2, FFFFCCAABCCDCDABCCBCABFFABCDDBBFFBCABFFBB
S3, CDABCCCCABABABCCABABBCCCCDCCCDAAAFFABFF
S4, BBBBFFABBBABAABCAABBBFFFFBCCDCDFFABAACCCC
S5, AACDABFFCDBBAAFFAAAABBBCFFCCBBBBBBCCDFFAB
S6, AAABABCDFFCDABABBCBCBCBBBCAAAACDFFAABCAB
S7, CDABBCABAAAACDCCCCBBBCBBCCAAFFBBBCCDBCCD
S8, AAAABBAABCCDABAABCBCCDDBBBBBBCBBFFBCBBCDCC
S9, FFAAABBBBCDCDCDBCBCBBFFCCCCBBBBBBBBBBBCAAAA
S10, BBBCCDAACCCDFFFFFABBCABCD CDABCCCCABAACCBBC
S11, BBCDBBCCFFFFFABBBBBBBCBCCCABBBBCBBBBBCDCDBB
S12, CCCDCCBBCCCCCFFAABCCDAABBBCCDCDBBBBCFFABCC
S13, CDABFFBBFFCDBCABBBBCBCFFABCCCCABCCAACDBC
S14, BBBCCDBCAABCABBCCDFFCCFFCDABCCBCCCCFFBCBC
S15, ABCCABBCAACDAAFFFFCCFFBBBBBCCCCBCBBBBBABAA
S16, BBBCBCCDCCCCBBCDCCCCCCCABFFFFFAAFFFBFAAFF
S17, CCAACCABAACCAABBBCCCCFFAABCCDBCBBBCDCCABBC
S18, CDBCBCBCBCFFBBCDAACDCCBBCDCCFFBBBBAACCBBC
S19, CDABCCAAFFBBCDBBFFAACDBBAAAABCBCFFBBAACD
S20, AAAACDCDCCCCCFFABBCBBBCBCCCABBBBCCCBBC
```

Longest Common Subsequence of Grades for All Students in Test Case 2: BCBCAB

3)

Student ID, Grades

S1, A A F F F C D B B A B C D A B B C B C F F C D A A B B A B A A A A C C A A A B
S2, B C A B C D B B B C C D C D F F C C C D A A B C A A B C A B C D B B B C F F C C
S3, C C B C A B A A F F A B C C C D C D A A A A B B A B B B C C C C F F B B C C B B
S4, F F B B C C A A C D C D C D C D B B A A A B A B B C B C B B A A B C C D F F A B
S5, B B B B F F B C F F C C A B C C A A C D F F B C F F B C A A B B B C B B B C C D
S6, B C B C F F C C B B C D A A B C C C A A B C C D C C C C A B C C A B A B B C A B
S7, B B C C B B C D A B C D B B C C C C C C B B F F B B A A A A B C A B C D C D C C
S8, F F F F C C B B A B F F B B B B C D B C A B B C A B B B F F B C B C B C C C F F
S9, A A F F A B A A B B B C C C C C C C C C D B C B B C D F F C D A A B B C C B B
S10, A A F F C D A B F F C D B B C D B C C C A B F F F F A B A A A A A B C C B C B B
S11, F F A A B C B B A A A B C C C D A B A B C C A B B B A B B B A B B C C D A B C C
S12, C D A A B C A B B B F F B C B B A A C C F F F F A A A B A B B C B B C D B B B C
S13, A A A A A B F F A A C D B C B B B B A A A A A B C D C C C D B C A A C C A A C C
S14, C D F F C D C C F F B C A B F F C D C D B C F F C D C D B C A B A B A B F F A A
S15, C D A A A A C D F F C C B B A A B B A B A B A A A B C C B B B C C D A A A B A B
S16, C C B B A A A B C C B C F F C C C D B B A A C D C C A B C D F F B C A B A B F F
S17, C C B B C D C D C D A B C C B B A B C D B B A A C D A B A B A A B B A B A B B C
S18, B B A A C D A A A A A A C D B B F F F F B B A B A A C D C C B C B B B B C C B B
S19, B B B C C C B C B B B B A A F F B B C D C C B B C C A B A B A A A A A B B B C D
S20, A B A A F F A B A B C C C D C C F F C C C C A B C D A B F F B B C D C C A B C C

Longest Common Subsequence of Grades for All Students in Test Case 3: CBBBBCB

4)

Student ID, Grades

S1, CDBBBBCDFFCCAAFFAAABABABBCBCCCBBCDCCBCCC
S2, CCFFFFABAABCBCCDDBCABAAABABABFFFAACCAAAAF
S3, ABCDBBBBCDDBFFCDABAABBCCAACCAABBFBBBBA
S4, CDBCBBABAABCAACDCCABBCFFAAFFABCCAABCBBCC
S5, CDBBAACCCCBBCDDBBBBCCABFFCCBCBCABAACDAABB
S6, CCABAAABCDBBAAABFFCCBCCDABBBAAAAABBBAAAB
S7, AAABCCCDDBCCDCDBBAAFFAACDABFFFFCDAAABBBBCD
S8, AAABAABBBBCFFCD CDCDCDFFBCCCCBCABCCABCCFF
S9, AAFFAAABCD CDCDABBBCCFFCDFFCDBCAACCCCAABC
S10, CDFFAABBFCDFFCDCCCCABCCCDCCAACDCCAACDCD
S11, BBABCDAAACFFFFBBCCCDCAAAACCAAFFABABCDDBC
S12, CCABAAAAABABFFBCABFFCD AABBBBCBCABBCAAAACD
S13, FFCCAACBCAABBBBCABAACDFFAABCAABBCCABBCFF
S14, AABCCDDBFFBCABABCCABBCBCBBBBCCFFBBCCBCBB
S15, ABABBCBCCDFFAAFFABBBAAABCCBBBBAAAAAABBC
S16, BB CDAAFFABBBCCCDCCBCCCBBBCCCB CBABCDABAB
S17, FFCCBCBBCCFFBBBBBBABBBBCDCDBBABFFFFCCCD CD
S18, CDBBAABCAABCCCCDFFFFAAFFCCBBFFCDBBFFBBBC
S19, ABFFBBCDBBABFFCD CDCCFABAAABAABBCBBBBBAB
S20, CDCDAABBABBBAAACDDBBFFCDFFABCDAAACBBBCBCBC

Longest Common Subsequence of Grades for All Students in Test Case 3: CBBBBCB

5)

Student ID, Grades

S1, BBAABBBBCCAABBBBCBBABCDCCAABBBFFABBCABABCC
S2, ABCCCDFFBCABBBAAABABAAAAFFAABCBCFFBCFFAA
S3, BCCDFFCDCDCDABCCBCABBCFFABBBCAABCAAFFCDCC
S4, CDCDCCCCCBCFFBBCCCDCCFFBBCCAABBCDABCDDBB
S5, BB CDABABBBBCCDAAABBBBCBBCDAABBCDAAAAAABC
S6, CCCCCAACDCCABFFAACCAABCBCFFCDFFCDBCAACCCC
S7, CCBBCCBCCDBCBCFFBCCCAABCCDBBFFBCCDCDAAFF
S8, BCAAAAAAFFFFABABABBCCDCDBCFFBCBBCCBB CDCC
S9, ABAABBAABBBBCCBBABFFCCFFBBBCBBBBBBBBBBFF
S10, CDBBAAABABBBCAAABBBCCCB CABABABABBBCAACCBAB
S11, FFBCABBBBBBABABAAFFAAAAABBBBBBABABBCCCBCCD
S12, CCBBAABBBFFBB CDABBBBBB CABFFCDFFCCABCDAAFF
S13, AACDBBABA BCCBCFFBCFFBCBCCDCCFFCDBCCDBCBC
S14, AACDFFAAABBB CDABCDABBBCCBBCCCCAAAAAFAFB
S15, AABCCDCCBCAAFFBCCDBCBBFFABBCBBCCCCABCDFF
S16, CCFFBCABCDAAAAAACCABAAABAAAABBBBBBCBCFFBB
S17, AABBBCCDCCCDAAFFFFBCBCCCB CAABCFFCDBCBBBC
S18, FFFFCCCAACCB CAABCCABBCBBCDFFBCFFBBBBCC
S19, BCCDAAFFFFFBBCCABBCABAABCBCCCAAAABBAACC
S20, CDABBCAABBAABCAABCCCCC DFFBBBBCCCCFFFFF

Longest Common Subsequence of Grades for All Students in Test Case 5: CBBBCC

Negative Testcases:

1)

```
Student ID, Grades
S1, ABFFCDCCAABCFFCDBBCDBBCDFFBBCDCCZ1ABBCFF
S2, BBAACCBABABBBCCCCDAAABCCAXCCCCDFFABAA
S3, Z1BBBCBCCCBBAABCDBCBFFABFFBBCCABABCCCD
S4, CDABBBAAACDCCFFAACCAACCCCDCC2ABBCBCABBCAA
S5, BCBCABABCCABBCFFBCCDBCABBBCCBCABABBCAAE1
S6, AAAAAABABCCBCCDE1CCBBBCBBCDAAAAFFBCBBCD
S7, BCBBBCDAABBCCABAABCBBCCB!FFAABCFFBCBBCCCD
S8, CDBCFFBBAACDBCBCA1AAABBCFFBBBBBCDABBBBCAA
S9, BBFFC2CDCCABCCAACCCDAACCABCDABABCCBCBCFF
S10, FFFFBCCDABCDAAABCCAAABBCDCDAAE1BBAACDFF
S11, CCABCCAABCBCBBBCCDBCAAFFBCCCBBCFFABB!BBFF
S12, AACCAAB!CCFFABCCBBFFABFFCDFFCDFFBBAACDCD
S13, FFABCDABCCCCABCDABFFABFFFFCCAXBAAABCCDCC
S14, CDBBCDBBBCCCBABBBBCCAAAACDCCFFAABBAABBE1
S15, ABAAFFCCCDFFAACDCDBBBBCAAC2BCBBCCBCFFABBB
S16, BCBBBCDCCCCCCCCCAAB!BCCCCCFBCBBAAABBBFF
S17, AAABAABBABB!AAFFAABBBBCDCDBBFFFFBCAACDCD
S18, FFFFFFFAAAABCABABBBCCBCCCCCCCCBBAADDBCAABC
S19, AAAACCABAACCCDDDCDFFABCDDBBAABCCDCCABFFAB
S20, BBABBCFFCCAABCFFAAFFFFFBCAABBA1CDFFCDAA
```

Error for student S2: Invalid grade sequence:

BBAACCBABABBBCCCCDAAABCCAXCCCCDFFABAA. Special characters or invalid grade format detected.

Error detected in Test Case 1. Skipping LCS calculation.

2)

```
S1,CDBCBBBBCCCDAAFFFAAFFFFCDE1AABBBBCBCFFBCCD
S2,CDBBABBBBCABABABAAC2BBCDAAABCCCDABABAB
S3,AACDCCCDFFBBBBAABBAXBBBCBCABFFCCABCDFFBB
S4,ABAABBFCDDBCBBAAAABBBBBBCFFABCDAAABDDCD
S5,BBCCCCBBFFABCDAACCCDBCBBBCDDABBCABABABCD
S6,CDABZ1ABABBBCCCDCCDFBFCFFCDBCABCCCCBCBBAB
S7,FFDDAACDBCAACCBBAACDAAFFFAABBCCABCCCCABBC
S8,CDAAABCDBBFFCDABCCCDABFFFFBBAABAE1BBBBBB
S9,FFABABCDBCAAABFFBACAACDAAAFB!BCBCABBBCC
S10,AAFFABBCFFCDBCAXAAAACCAABCAABBABBBCCCCBB
S11,ABBCAXCDBBBBBBBAABBFCDDBCBBBCBCABABAABBCD
S12,AABCAAABCDAAAABBFEE1ABABBCFFBCBCCDAACCB
S13,BBDDCDBBBBCAABCABABBBABAAAAAABBCAAABCD
S14,BCCCCABCDAAABABBBABABCDZ1CDBBAAABFFABFF
S15,CCBBCCABCCAAABCDCCFFABCDCCCCAXBCCDABBCAB
S16,CCBCCDCCE1CDCCBCBBBCAAAAAAAACCBCCFFCDAAFF
S17,FFBBFFBCAACCBBAAFFFFAACCCDDAAAACCFABBCFF
S18,BCBBBCCDFFCCAABBBCCDFFDDAABBABAAABBCDBC
S19,BCB!CCFFAABBAAFFFFBCCDAABCAABBBBCBCCDBCCD
S20,BBCCCCB!AAAAAABCBBABCCDFFAACDBCABFFBBFF
```

Error for student S2: Invalid grade sequence:

CDBBABBBBCABABABAAC2BBCDAAABCCCDABABAB. Numbers found in the sequence.

Error detected in Test Case 2. Skipping LCS calculation.

3)

```
S1,AAAXFFABAABCFFFFBCCDBCCCBFFFFABFFCDCDF
S2,BBABABFFCCFFAAB!FFCCCDAAFFBBBCABBBAAABFF
S3,CDFFCDAABCCBBBBZ1ABCCBCCCBABBBBCDBBABAAAA
S4,FFCCABFFCCCCAACCBABDDDBCCCCBCFFCDAAABABAA
S5,ABBCE1BCBCBCABAAFFBBBCAAFFCDCDAACDAAFFBC
S6,ABCCBBABABCCCDABA1CCBBABBCBCCDFFB BBBBCCC
S7,CDCDBCCDFFBDDFFBBFFBFCBCCBBBBBBCCDFFCDA
S8,CDFFBABBBABBBABAAAXAAFFBBABAACDABCCABAA
S9,CDCCCDAAACDBBFFCDFFFFABAABCDDCCBBAABBCDCC
S10,BBCCFFBCBBBCBBFFBCBCBCDDCCCDFFABABBBFFAB
S11,BBABFFFFABCDAAAADDABFFCCCCFFABCDCCCDAAFF
S12,CCDBCABFFBCFFBCCDCDCCCDAAFFCCABCDAAAXCD
S13,ABABCDDBCFFAACDAAFFDDFFCDBBCCBBAACDABCC
S14,BBBBCCBCBBFFAABCC2CDFFBCCDABBBABCCBBABAB
S15,BBBCCCCCAAFFAACCCFFCDBCFFABFFBCB!FFABCCCD
S16,FFBBABFFBBBCABFFCCABZ1BCBBBBBBBAAAACDABCC
S17,BBAABDDFFBCCDCCCAABCBBBBAACDFFCDAACDCD
S18,ABAAABAACDBCABCCBCBCBCCABCCBBABB!ABCDCC
S19,FFFFFFBBCDCDFFABBCBCFFCCBBCDCCCCABAADDFF
S20,BBCCCCFFBBFFAACCCDB!ABABBCAACDAACDBBABAB
```

Error for student S2: Invalid grade sequence:

BBABABFFCCFFAAB!FFCCCDAAFFBBBCABBBAAABFF. Special characters or invalid grade format detected.

Error detected in Test Case 3. Skipping LCS calculation.

4)

Student ID, Grades

S1, FFFFFFFFBCAACCCDAAE1FFABCDFFCCBCCDBBCCAB
S2, AAABAAABCCAABCFFA1BCBBCCCDCCDFCCBCCCBBBC
S3, BCABCCABBCAABBBBCDCCABBBFFAACCFZ1FFCCCD
S4, AAFCDABCCCCCDBCCCE1CCCDCCABABBBFFCCBBBC
S5, CCDDFFBBCCAAAAABAAFFCDAXAACCBFFFCDBCBCFF
S6, BCCDAAABBBBBBFFFFCDBBCDCCAABBABFFAXCDBBFF
S7, BBBCABFFCCBCAABBCCFFFFCDAABCA1FFABABAABC
S8, Z1FFAACDCDAAABBBBAABCBBAAACCB BBBBCDBCABFFAA
S9, FFBCABCCCCBBCCABBBABFFBBBBBBCE1AAABBBABBB
S10, BCFFCDFFAACDCDBCAACCCCBCCDFCCABBBAACDE1
S11, CCCCFFBCFFBBFFABBCCCBCCDAAAACCAXBCABCDAA
S12, BBCCCCFFBCCCAABCDDCCCCABCDCCABAAABAAAAAB
S13, ABA1ABBBBBBABFFCDCDCDCCCCFFFFCDABBBABCD
S14, ABABCD CDABAXAAABCD CD CDABBCFFCDBBBBBBBAAFF
S15, ABABBCBCABCDAAAAABAABCCDCCAAAAAABBZ1ABAA
S16, BBBBAADDFFFFBBCCAAFFAAFFCDABABFFBCBCBBCD
S17, BCABAABBCDBCAAFFBBCDBCAAFFBCDDABCCBCABAA
S18, CCABAAAACCBBAABCFFBCAAAXBCBBABFFFFCDBCAB
S19, CDBCC2ABABBBABBCABCD CDBBFFFFABBCAAFFCCBB
S20, ABABBBCCCDCCFFBCBBCDFFABABAAA1FFABFFBBFF

Error for student S2: Invalid grade sequence:

AAABAAABCCAABCFFA1BCBBCCCDCCDFCCBCCCBBBC. Numbers found in the sequence.

Error detected in Test Case 4. Skipping LCS calculation.

5)

Student ID, Grades

S1, AACDFFFFABFFCDCCABAAABBCC2ABAABCAAAACCF
S2, FFCDAABCAAABBBCCBCAAABAAAXABCDBBAABCBBCC
S3, FFBCBBCDABCDABAABCABBBAACCFCDABBBZ1BCBC
S4, AABBBBCB!FFAAAAFFABCDDBCBCFFABABBBBCDBBBBCD
S5, CDBCABCCABFFCDBBCDBCCCCCCCCFFABAABCCDCCC2
S6, ABAACCBCFFBBA1BBCDFFFFBBABABCCCCCDABCD
S7, CCCDAABCAABBBBBBBAACCF FCCABBBCCZ1ABBCABBB
S8, FFBBFFCDABBBABCCABABCDAAACCABBBFFBCBBAAE1
S9, CCB!CDCDABABAABBCDAABBCCFFBBBBBFABCDAAABC
S10, ABCCABAAABBBABFFCDCCDFABBCBBABA1CDAABBAA
S11, FFBBAAABBCBCFFCDABBCCCBCCCCABCCCDFFAADD
S12, CDAACCCCBABFFB!CDAACDABFFFFBBABBCCCBBCFF
S13, CCABBCABBBBBBABAXCDBCCDCCCCCDBCBBBCABAACC
S14, CDBCFFFFABFFFFABAABBAABCDAAABBCFFAXCDBC
S15, FFAABBBBCBBABCCCCFFCDCDCCAAABAABCABFFAAA1
S16, FFCCBBBBBBBBBCAAE1AAAABBBCAACDCCBCABBBABFF
S17, BBBCCDDCCFFBCFFBCCDBCBCBBBBBCCCCCBCAABCAB
S18, ABCCFFBCCDCCCCBBABAABCBCFFBCBCBBFFAXCDAA
S19, CDBBBBAABBCCFFABAAAAFFBCFFCDBBAAAABBABB!
S20, ABFFFFBCCDAAAACDCDAAFFFFBCBCCCCDFCCZ1AB

Error for student S2: Invalid grade sequence:

FFCDAABCAAABBBCCBCAAABAAAXABCDBBAABCBBCC. Special characters or invalid grade format detected.

Error detected in Test Case 5. Skipping LCS calculation.

TASK 2:

Aim: Consider meteorological data like temperature, dew point, wind direction, wind speed, cloud cover, cloud layer(s) for each city. This data is available in two dimensional array for a week. Assuming all tables are compatible for multiplication. You have to implement the matrix chain multiplication algorithm to find fastest way to complete the matrices multiplication to achieve timely predication.

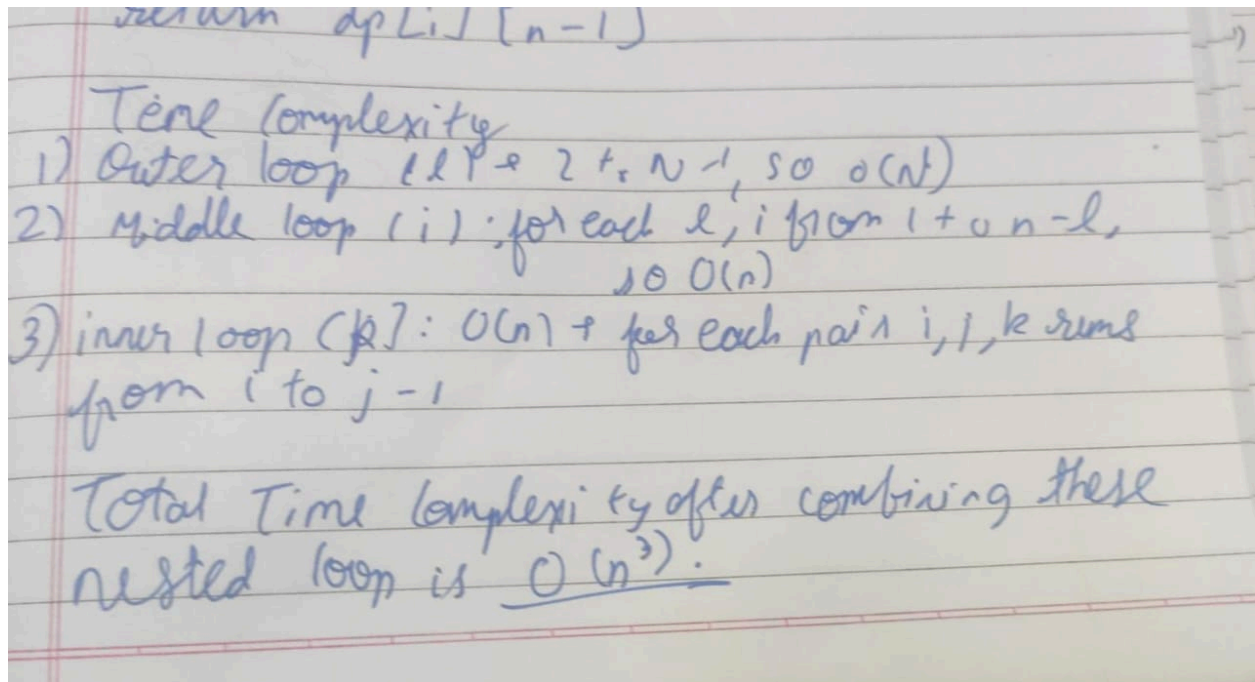
Algorithm:

```
function mem(n, arr[])
    if n < 2
        return "error: there must least be at least two matrices"
    if arr.length is not N+1
        return "error; dimension array must be N+1"
    for each d in arr:
        if d <= 0
            return "error: matrix dimension must be +ve values"

    initialize dp of size N x N with all elements set to 0
    for l from 2 to n-1
        for i from 1 to n-l
            j = i+l-1
            dp[i][j] = ∞
            for k from i to j-1
                q = dp[i][k] + dp[k+1][j] + arr[i-1]*arr[k]*arr[j]
            dp[i][j] = min(dp[i][j], q)

    return dp[i][n-1]
```

TIME COMPLEXITY:



TESTCASES:

POSITIVE:

1)

```
test_cases = [  
    # Valid test cases (positive test cases) for meteorological data (assuming 5 cities)  
    ([7, 5, 4, 6, 7, 8], 5), # Example with matrix dimensions: 7x5, 5x4, 4x6, 6x7, 7x8  
    ([3, 7, 5, 10, 15], 4), # Example with matrix dimensions: 3x7, 7x5, 5x10, 10x15  
    ([2, 4, 5, 6, 8], 4), # Example with matrix dimensions: 2x4, 4x5, 5x6, 6x8  
    ([4, 8, 6, 7, 9], 4), # Example with matrix dimensions: 4x8, 8x6, 6x7, 7x9  
    ([7, 3, 6, 4, 8], 4), # Example with matrix dimensions: 7x3, 3x6, 6x4, 4x8
```

Output:

Test case with $N=5$ and $arr=[7, 5, 4, 6, 7, 8]$: 504
Test case with $N=4$ and $arr=[3, 7, 5, 10, 15]$: 255
Test case with $N=4$ and $arr=[2, 4, 5, 6, 8]$: 100
Test case with $N=4$ and $arr=[4, 8, 6, 7, 9]$: 360
Test case with $N=4$ and $arr=[7, 3, 6, 4, 8]$: 156

NEGATIVE:

```
# Invalid test cases (negative test cases)
([3, 7, 4, 7, 5], 5),    # Invalid: Missing one dimension for multiplication (4 matrices)
([2, 5, 6], 1),         # Invalid: Not enough matrices for multiplication
([10, 20, 30], 2),      # Invalid: Matrix dimensions array length doesn't match the number of matrices
([10, 20], 1),          # Invalid: One matrix (should have 2 for multiplication)
([10, -20, 10], 2),     # Invalid: Negative dimension value
([0, 20, 10], 2),       # Invalid: Zero dimension value
```

Output:

```
Test case with N=5 and arr=[3, 7, 4, 7, 5]: Error: The dimensions array length must be N+1
Test case with N=1 and arr=[2, 5, 6]: Error: There must be at least two matrices for multiplication
Test case with N=2 and arr=[10, 20, 30]: 0
Test case with N=1 and arr=[10, 20]: Error: There must be at least two matrices for multiplication
Test case with N=2 and arr=[10, -20, 10]: Error: Matrix dimensions must be positive values
Test case with N=2 and arr=[0, 20, 10]: Error: Matrix dimensions must be positive values
```

CONCLUSION:

In these tasks, the **Matrix Chain Multiplication** algorithm and the **Longest Common**

Subsequence (LCS) approach demonstrated the importance of efficient computation in data analysis. Matrix Chain Multiplication optimized the order of multiplications for meteorological data, crucial for achieving timely weather predictions by minimizing computational effort. Meanwhile, LCS enabled us to identify common grading patterns among students, valuable for spotting trends in academic performance. Both techniques showcase how foundational algorithms enhance efficiency and reveal insights across diverse domains, from education to weather forecasting.