



Some administration first

before we really get started ...





The overall goal of this course is for you to:

How to choose and use appropriate algorithms and data structures to help solve data science problems

This course covers basic algorithms and data structures that will enable you to develop your own algorithms that are faster, efficient, and scalable in real-world.

Admin stuff...



Course syllabus:

<u>Github</u>





Weekly lab assignments are worth 30% of your overall grade.

Lab assignments may take more than the two hours lab time. You have one week to submit them.

- No late labs will be accepted.
- A lab may be submitted in any time before the due date.

Lab assignments are done individually.

The lab assignments are critical to learning the material and are designed both to prepare you for the exams and build up your skills!





Cheating is strictly prohibited and is taken very seriously by UBC.

A guideline to what constitutes cheating:

- Labs
 - Submitting code produced by others.
 - Working in groups to solve questions and/or comparing answers to questions once they have been solved (except for group assignments).
 - Discussing detailed HOW to solve a particular question instead of WHAT the question involves.
- Exams
 - Only materials permitted by instructor should be in the exam.

Academic dishonesty may result in a "F" for the course and removal from the MDS program.





Attend *every* class:

- Read notes before class as preparation and try the questions.
- Participate in class exercises and questions.

Attend and complete all labs:

Labs practice the fundamental employable skills as well as being for marks.

Practice on your own. Practice makes perfect.

- Do more questions than in the labs.
- Read the additional reference material and perform practice questions.

Systems and Tools



Course material is on GitHub.

https://github.com/ubco-mds-2023/data_532

Marks are distributed on Canvas.

Labs are submitted on Canvas using GitHub Classroom assigments.





For any computational task on data you need an algorithm to solve it, and you need to store the data in a suitable data structure to access the data. If the data are large, you need these algorithms and data structures to be efficient.

At the end of this course, you should be able:

- Select a suitable basic algorithm and data structure for a given task
- Design efficient algorithms for simple computational tasks





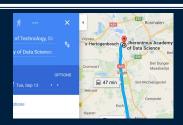
- Importance of algorithms and their applications
- Learn about complexity of algorithms
- Understand the idea of searching
 - Linear Search
 - Binary Search





Route planning shortest-path algorithms





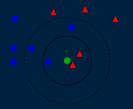
Search engines matching and ranking algorithms

Al Al

Data Analysis e.g., k-means clustering algorithm, k-nearest neighbor algorithm, ...







Algorithms run everywhere: cars, smartphones, laptops, servers, climate-control systems, elevators ...





How do you "teach" a computational device to perform an algorithm?

Computers do not have intuition or spatial insight

"An algorithm is a set of steps to accomplish a task that is described **precisely** enough that a computer can run it."

Algorithms



Algorithm

a well-defined computational procedure that takes some value, or a set of values, as input and produces some value, or a set of values, as output.

Algorithm

sequence of computational steps that transform the input into the output.

Algorithms & Data Structures

fast algorithms require the data to be stored in a suitable way.

Data structures



Data Structure

They are essential ingredients in creating fast and powerful algorithms.

They help manage and organize data.

A way to store and organize data to facilitate access and modifications

Abstract Data Type (ADT)

An ADT is an abstraction of the data structure which provides only the interface to which a data structure must adhere to.

Data structures



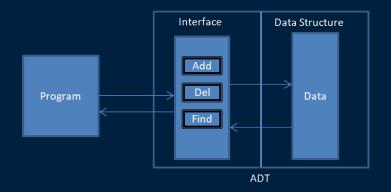
Abstract data type

describes external functionality (which operations are supported) to operate on a data structure

Implementation

a way to realize the desired functionality

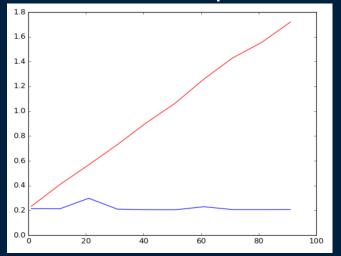
how is the data stored (array, linked list, ...)







If you often need to search your data, simply storing it in an array/list will considerably slow down the computations



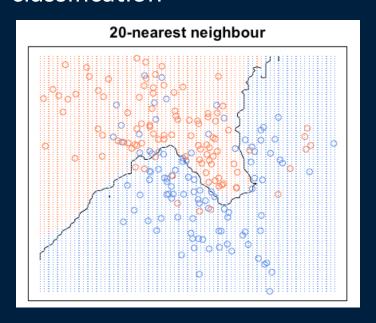
Worst case search

```
In [5]: timeit.timeit(stmt='1 in A', setup='A = list(range(2, 300))')
Out[5]: 4.774117301917343
In [6]: timeit.timeit(stmt='1 in A', setup='A = set(range(2, 300))')
Out[6]: 0.0499541983165841
```





Algorithms for finding the k nearest neighbors are used for analysis tasks like classification



Example: The KNN Algorithm

- 1. Load the data
- 2. chose K value
- 3. For each example in the data
- 3.1 Calculate the distance between the query example and the current example from the data.
- 3.2 Add the distance and the index of the example to an ordered collection
- 4. Sort the ordered collection of distances and indices from smallest to largest (in ascending order) by the distances
- 5. Pick the first K entries from the sorted collection
- 6. Get the labels of the selected K entries
- 7. If regression, return the mean of the K labels
- 8. If classification, return the mode of the K labels

Simplest version of KNN is brute-force algorithm

Which algorithm/implementation is suitable for your data?





http://scikit-learn.org/stable/modules/neighbors.html

1.6.4. Nearest Neighbor Algorithms

1.6.4.1. Brute Force

Fast computation of nearest neighbors is an active area of research in machine learning. The most naive neighbor search implementation involves the brute-force computation of distances between all pairs of points in the dataset: for N samples in D dimensions, this approach scales as $O[DN^2]$. Efficient brute-force neighbors searches can be very competitive for small data samples. However, as the number of samples N grows, the brute-force approach quickly becomes infeasible. In the classes within ${\tt sklearn.neighbors}$, brute-force neighbors searches are specified using the keyword ${\tt algorithm} = {\tt 'brute'}$, and are computed using the routines available in ${\tt sklearn.metrics.pairwise}$.

1.6.4.2. K-D Tree

To address the computational inefficiencies of the brute-force approach, a variety of tree-based data structures have been invented. In general, these structures attempt to reduce the required number of distance calculations by efficiently encoding aggregate distance information for the sample. The basic idea is that if point A is very distant from point B, and point B is very close to point C, then we know that points A and C are very distant, without having to explicitly calculate their distance. In this way, the computational cost of a nearest neighbors search can be reduced to $O[DN\log(N)]$ or better. This is a significant improvement over brute-force for large N.

An early approach to taking advantage of this aggregate information was the KD tree data structure (short for K-dimensional

Which of the algorithms would you choose?



A) Brute-force

B) K-D Tree

C) A combination of the two algorithms depending on your problem

D) Doesn't matter both will solve the problem



K-D tree performs well enough when D < 20. With larger D, it again takes longer time. This is known as "curse of dimensionality"

Unless you do the brute force on a GPU, overall, the KD-Tree should be faster



What do we expect from an algorithm?



What do we expect from an algorithm?

Computer algorithms solve computational problems

Computational problems have well-specified input and output

Question: Is the following problem well-specified?
 "Given a collection of values, find a certain value x."

array: sequential collection of elements, which allows constant-time access to an element by its index. (*Note: We (and Python) use as first index 0, in some textbooks, they start at 1.*)

35	30	19	30	8	12	11	17	2	5
0	1	2	3						

"Given an array A of elements and another element x, output either an index i for which A[i] = x, or Not-Found"

There are 2 requirements on the algorithm:

- 1. Given an input the algorithm should produce the correct output
- 2. The algorithm should use resources efficiently

Correctness



Given an input the algorithm should produce the correct output

What is a correct solution? For example, the shortest-path ... but given traffic, constructions ... input might be incorrect Not all problems have a well-specified correct solution

we focus on problems with a clear correct solution

Randomized algorithms and approximation algorithms special cases with alternative definition of correctness

Efficiency



The algorithm should use resources efficiently

The algorithm should be reasonably fast (elapsed time)

The algorithm should not use too much memory

Other resources: network bandwidth, random bits, disk operations ...

we focus on time

How do you measure time?





A) Use my wrist watch

B) Use a sand clock

C) Use the clock on the computer

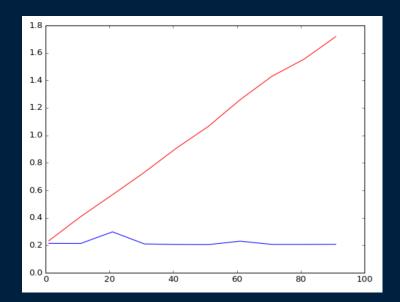
D) Implement the algorithm and measure time

E) Theoretical analysis of the algorithm

Experiments?



```
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```



Efficiency



The algorithm should use resources efficiently

How do you measure time?

Extrinsic factors: computer system, programming language, compiler, skill of programmer, other programs ...

implementing an algorithm, running it on a particular machine and input, and measuring time gives very little information

Efficiency analysis



Two components:

- 1. Determine running time as function T(n) of input size n
- 2. Characterize rate of growth of T(n)

Focus on the order of growth ignore all but the most dominant terms

Examples

Algorithm A takes 50n + 125 machine cycles to search a list

- 50n dominates 125 if $n \ge 3$, even factor 50 is not significant the running time of algorithm A grows linearly in n

Algorithm B takes $20n^3 + 100n^2 + 300 n + 200$ machine cycles

the running time of algorithm B grows as n³

Recall (maybe): Logarithms



log n denotes log, n

We have for a, b, c > 0:

1.
$$\log_c$$
 (ab) = \log_c a + \log_c b

2.
$$\log_{c}(a^{b}) = b \log_{c} a$$

3.
$$\log_a b = \log_c b / \log_c a$$

Comparing orders of growth



log³⁵n vs. √n?

- logarithmic functions grow slower than polynomial functions
- $\lg^a n$ grows slower than n^b for all constants a > 0 and b > 0

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n^{100} vs. 2^{n}?
```

- polynomial functions grow slower than exponential functions
- n^a grows slower than bⁿ for all constants a > 0 and b > 1





An algorithm runs in O(g) time if the number of steps it executes on an input of size n is at most proportional to g(n) when n is large.

Notes about the use of onotation:

Constant factors are not important

So $O(n^2)$ is the same as $O(5n^2)$ or $O(n^2/2)$.

Added/subtracted lower order terms can also be ignored

So $O(n^2 + 5n + 4)$ and $O(n^2 + n\log n - 2)$ are the same as $O(n^2)$.

Time Complexity



Some typical time complexities (ordered from slower to larger growth):

- O(1): constant
- O(log n): logarithmic
- O(n): linear
- O(n log n)
- O(n²): quadratic
- O(n³): cubic
- O(n^k): polynomial
- O(2ⁿ), O(3ⁿ), O(kⁿ): exponential
- O(n!): factorial



In general: Order of growth of some common functions

$$O(1) < O(\log n) < O(n) < O(n * \log n) < O(n^2) < O(n^k) < O(2^n) < O(n!)$$

Exercise



Compare growth rates

Practice Exercises 1

Exercise 1

Rank the following functions of n by order of growth (starting with the slowest growing). Functions with the same order of growth should be ranked equal.

 $\log n^3$, n , $n \log n$, 4^n , $\log \sqrt{n}$, $n + \log n^4$, $2^{\log 16}$, n^{-1} , 16 , $n^{\log 4}$

Some typical time complexities:

- O(1): constant
- O(log n): logarithmic
- O(n): linear
- O(n log n)
- O(n²): quadratic
- O(n³): cubic
- O(n^k): polynomial
- $O(2^n)$, $O(3^n)$, $O(k^n)$: exponential

What is the run-time complexity of an algorithm with following g(n)?



$$g(n) = n^2 + (n \log n)^4 + 2^n + (n!)$$

- A) n²
- B) 2ⁿ
- C) n!
- D) $n^2 + 2^n$





A complete description of an algorithm consists of three parts:

- 1. the algorithm
 - expressed in whatever way is clearest and most concise,
 - can be English and / or "readable code",
 - readable: pseudo-code or python code
 - code will nearly always need a short high-level description in words
- 2. a proof of the algorithm's correctness
- 3. a derivation of the algorithm's running time



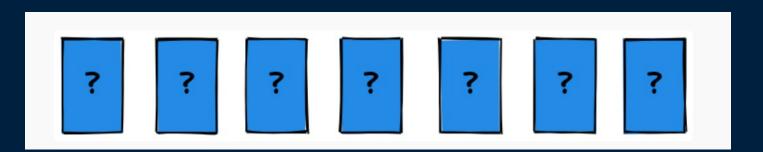
Searching Algorithms

Search



Problem

Emily possesses a set of cards labeled with numerical values. She organizes these cards in a descending order and places them facedown in a row on a table. She presents a challenge to Chris: to identify the card with a specified number by flipping over the minimal number of cards. Develop a function to help Chris in locating the desired card.







Linear-Search(A, n)

Input and Output specification

Input:

- A: an array
- n: the given number whose position in A needs to be determined
- x: the value to be searched for

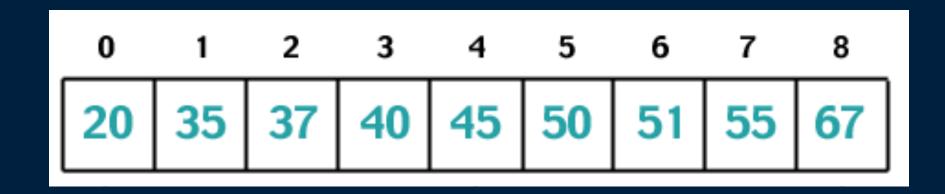
Output: Either an index i for which A[i] = x, or -1 (Not Found)

- 1.Set x to Not-Found
- 2.For each index i, going from 0 to n-1, in order:
 - A. If A[i] = n, then set answer to the value of i
- 3. Return the value of x as the output





Search for the number 51?



Binary Search Contd...

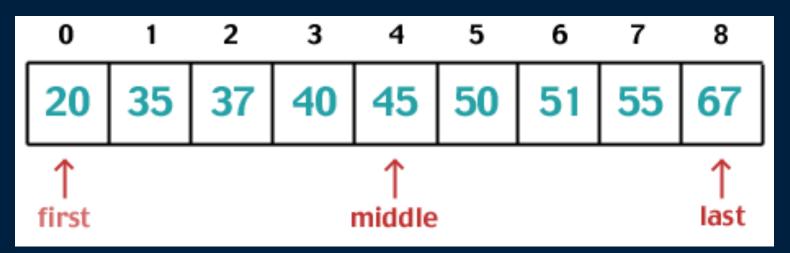


Compare 51 with middle

if 51 == middle then "Hurray"

if 51 < middle then between first and middle

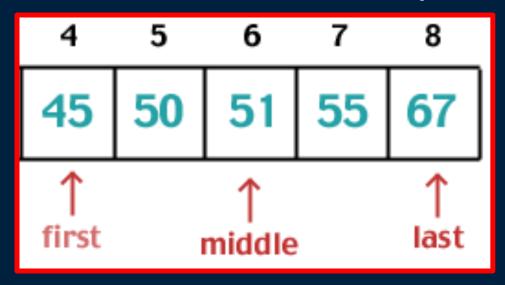
if 51 > middle then between middle and last







Compare 51 with middle if 51 == middle then "Hurray"







- A) O(n)
- B) O(log n)
- C) $O(\sqrt{n})$
- D) O(1)





- Understand notion of algorithm and data structure
- Analyze algorithm for time complexity, correctness, and efficiency
- Compare algorithms on the basis on Big O
- Design a linear search algorithm
- Improve the linear search algorithm
- Learn the Binary Search algorithm

