

INSTRUCTOR:  
XIAOPING SHI



IRVING K. BARBER FACULTY OF SCIENCE  
UBC, OKANAGAN CAMPUS

This exercise set has an additional 7 questions, for a total of 20 points. These questions, in addition to those on other practice sets, are representative of what might be seen on Quiz 2.

READ THE QUESTIONS CAREFULLY
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Notes and electronic devices are allowed, but they MUST be kept in airplane mode. You may use the back of a page if you run out of room on the front.

SURNAME, GIVEN NAME (print) \_\_\_\_\_

STUDENT NUMBER. \_\_\_\_\_

Signature: \_\_\_\_\_

Possible multiple choice—pick the MOST accurate answer

1. (2 marks) Suppose we fit a multiple linear regression  $y = a + b_1x_1 + b_2x_2 + \varepsilon$ , where  $X_1$  is a numeric predictor and  $X_2$  is a binary predictor. We can interpret this model as:
  - (a) a single line with slope  $b_1$ .
  - (b) two lines with the same slope  $b_1$  but one with intercept  $a$  and the other with intercept  $a + b_2$ .
  - (c) two lines with the same intercept  $a$  but one with slope  $b_1$  and the other with slope  $b_1 + b_2$ .
  - (d) two lines with the different slopes, one with slope  $b_1$  and the other with  $b_1 + b_2$ , and with different intercepts, one with  $a$  and the other with  $a + b_2$ .
  - (e) None of the above.

Sol. b.

2. (2 marks) Regarding the multiple linear regression  $y = a + b_1x_1 + b_2x_2 + b_3x_1x_2 + \varepsilon$ , which of the following statements are true?
  - (a)  $E(\varepsilon) = 0$ .
  - (b)  $E(y) = a$  when  $x_1 = 0$ .
  - (c) The change in  $E(y)$  is  $b_1$  when there is a 1 unit increase in  $x_1$ .
  - (d) The change in  $E(y)$  is  $b_2$  when there is a 1 unit increase in  $x_2$ .
  - (e) The change in  $E(y)$  is  $b_1 + b_3$  when there is a 1 unit increase in  $x_1$ .

Sol. a.

3. (2 marks) Suppose we fit a model of the form  $y = a + b_1x + b_2x^2 + \varepsilon$ , where  $\varepsilon$  is assumed to be normal distributed. Which of the following R codes are correct?
  - (a) `lm(y~x+x^2)`.
  - (b) `lm(y~x+I(x^2))`.
  - (c) `glm(y~x+I(x^2), family = binomial)`.
  - (d) `glm(y~x+I(x^2), family = poisson)`.

Sol. b

4. (2 marks) Suppose we fit a model of the form  $\log(E(y)) = a + b_1x + b_2x^2$ , where  $y$  is a count variable. Which of the following R codes are correct?
  - (a) `lm(y~x+x^2)`.
  - (b) `lm(y~x+I(x^2))`.
  - (c) `glm(y~x+I(x^2), family = binomial)`.
  - (d) `glm(y~x+I(x^2), family = poisson)`.

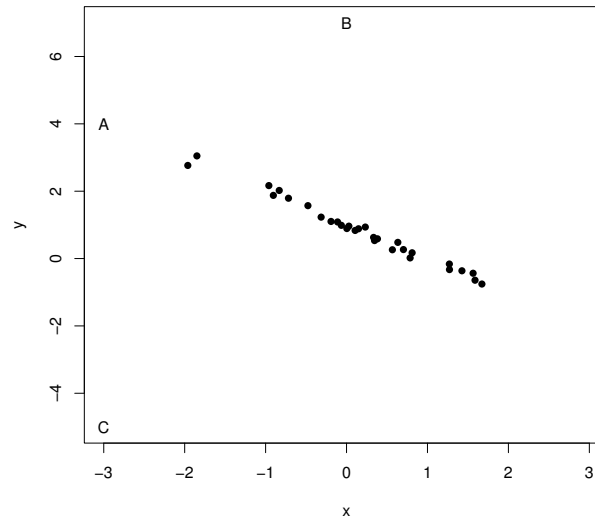
Sol. d.

5. (2 marks) Suppose we fit a model of the form  $\text{logit}(P(Y = 1)) = a + b_1x + b_2x^2$ , where  $y$  takes 1 or zero. Which of the following R codes are correct?

- (a)  $\text{lm}(y \sim x + x^2)$ .
- (b)  $\text{lm}(y \sim x + I(x^2))$ .
- (c)  $\text{glm}(y \sim x + I(x^2), \text{family} = \text{binomial})$ .
- (d)  $\text{glm}(y \sim x + I(x^2), \text{family} = \text{poisson})$ .

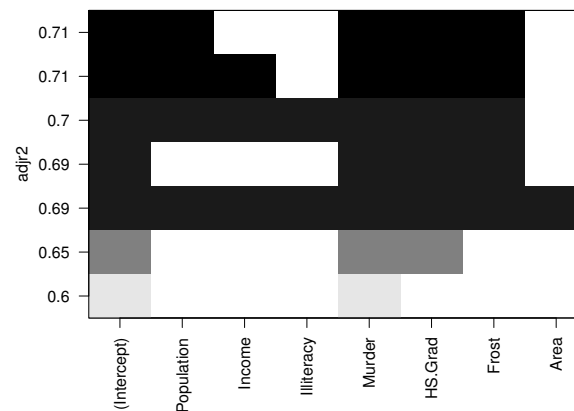
Sol. c.

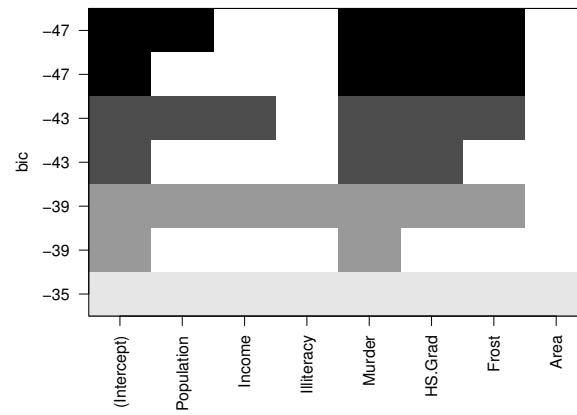
6. (6 marks) Match the points indicated by letters in the following scatterplot to the appropriate terms.



- 2 (a) Outliers SOL. B,C
- 2 (b) Influential points SOL. B,C
- 2 (c) High leverage points SOL. A,C

7. (4 marks) Consider the following partial R output of a multiple linear regression model.





- 2 (a) What's the best model based on adjusted  $R^2$ ? Sol. Population+Murder+HS.Grad+Frost
- 2 (b) What's the best model based on BIC? Sol. Population+Murder+HS.Grad+Frost