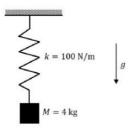
1

XE 71

EE23BTECH11048-Ponugumati Venkata Chanakya*

QUESTION: A spring mass system is shown in the figure. Take the value of acceleration due to gravity as $g = 9.81m/s^2$. The static deflection due to weight and the time period of the oscillations, respectively, are

(GATE 2023 XE)



Solution:

1) Static deflection due to weight(sdw) let x be sdw.

At mean position in equilibrium

$$Mg = kx \tag{1}$$

$$4 \cdot 9.81 = 100x \tag{2}$$

$$39.24 = 100x \tag{3}$$

$$x = 0.3924m (4)$$

$$x = 39.24cm$$
 (5)

2) Time period of oscilattion

$$F = -kx \tag{6}$$

$$ma = -kx \tag{7}$$

$$m\left(\frac{d^2x}{dt^2}\right) = -kx\tag{8}$$

Taking Laplace transform:

$$m(s^{2}X(s) - sf(0) - f^{1}(0)) = -kX(s)$$
 (9)

$$X(s) = \frac{m(sf(0) + f^{1}(0))}{k + ms^{2}}$$
(10)

Taking Inverse Laplace Transform: Initial Conditions be at extreme point of SHM

$$x(t) = a \sin\left(\sqrt{\frac{k}{m}}t + \phi\right) \tag{11}$$

$$x(t) = 0.3924 \left(\sin\left(\sqrt{\frac{100}{5}}t + \frac{\pi}{2}\right)$$
 m (12)

$$x(t) = 39.24 \sin(5t + \frac{\pi}{2}) \text{ cm}$$
 (13)

The static deflection due to weight and the time period of the oscillations, respectively are 39.24 cm and $\frac{2\pi}{5}$ s

