11.9.3.7

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Exercise 9.3

7. Find the sum to indicated number of terms in each of the geometric progressions in 0.15, 0.015, 0.0015...20 terms.

Solution:

Parameter	Description	Value
n	No. of terms in the G.P	20
x(0)	first term in the G.P	0.15
r	common ratio in the G.P	0.1
	TABLE I	

VARIABLES AND THEIR DESCRIPTIONS

$$x(n) = x(0)r^n \tag{1}$$

$$X(z) = \frac{x(0)}{1 - rz^{-1}} \qquad |z| > |r| \tag{2}$$

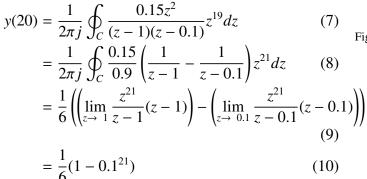
$$U(z) = \frac{1}{1 - z^{-1}}, \qquad |z| > 1 \tag{3}$$

$$y(n) = x(n) * u(n)$$
(4)

$$Y(z) = X(z)U(z) \tag{5}$$

$$= \left(\frac{0.15}{1 - 0.1z^{-1}}\right) \left(\frac{1}{1 - z^{-1}}\right) \quad |z| > 1 \qquad (6)$$

Using Contour integration



$$= \frac{1}{6}(1 - 0.1^{21}) \tag{10}$$
$$= 0.16667 \tag{11}$$

:. Sum of 20 terms of the given GP is 0.16667

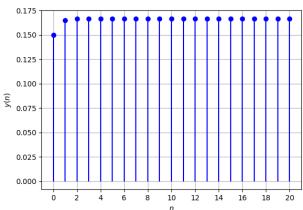


Fig. 0. Stem plot of y(n)