

1) Node

```
{  
    int val;  
    Node * next;  
}
```

Main()

```
{  
    Bool ret;  
    ret = Bad (head, head.next);  
}
```

Bool Bad (Node n1, Node n2)

```
{  
    if (n1 == n2)  
        return true;  
    else if (n2 == null)  
        return false;  
    else if (n2.next == null)  
        return false;  
    else return Bad (n1.next, n2.next.next);  
}
```

2) Algorithm :-

```
bool heap (node *root)
{
```

```
    int i = 0
```

```
    isheap (root, i, sizeof(root));
```

```
}
```

```
bool isheap (node *root, int i, int n)
```

```
{
```

```
    if (root == null)
```

```
        return true;
```

```
    if (i > n)
```

```
        return false;
```

```
    if ((root->lchild && root->lchild->val > root->val)
```

```
        || (root->rchild && root->rchild->val > root->val))
```

```
    {
```

```
        return false;
```

```
    }
```

```
    return isheap (root->lchild, 2*i+1, n) &&
```

```
        isheap (root->rchild, 2*i+2, n);
```

```
}
```

```
int size (node *root)
```

```
{
```

```
    if (root == null)
```

```
    {
```

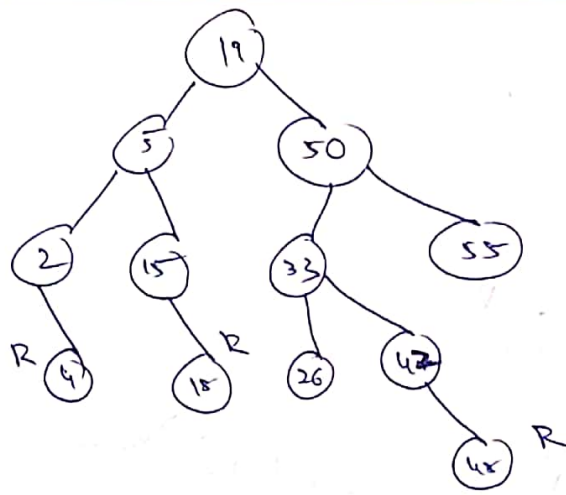
```
        return 0;
```

```
    }
```

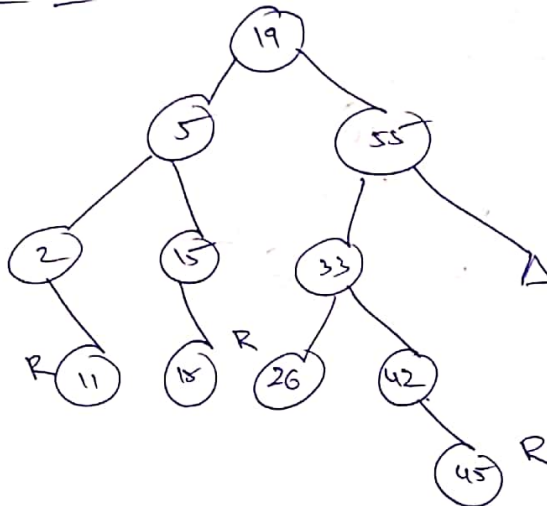
```
    return 1 + size (root->lchild) + size (root->rchild)
```

```
}
```

3) (a)

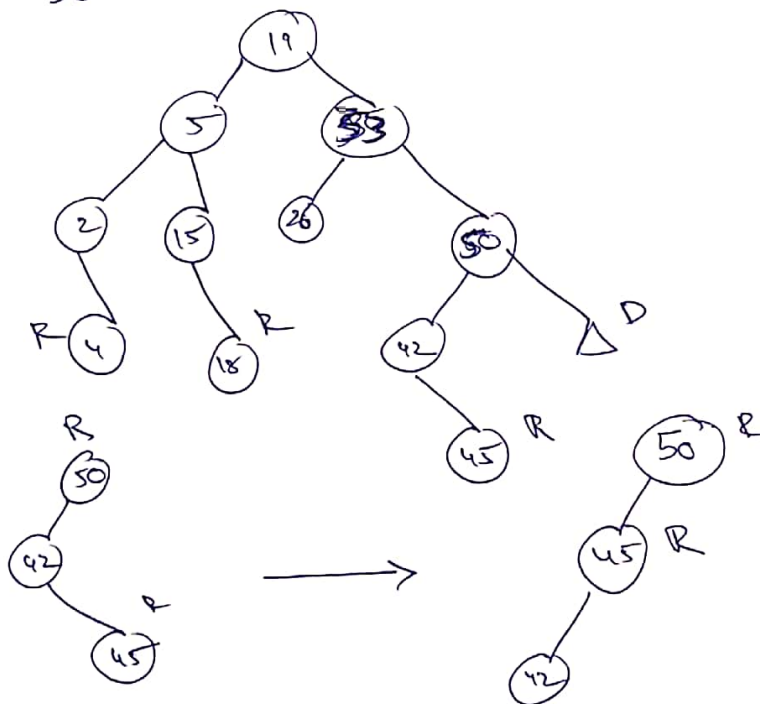


Delete 55 :-

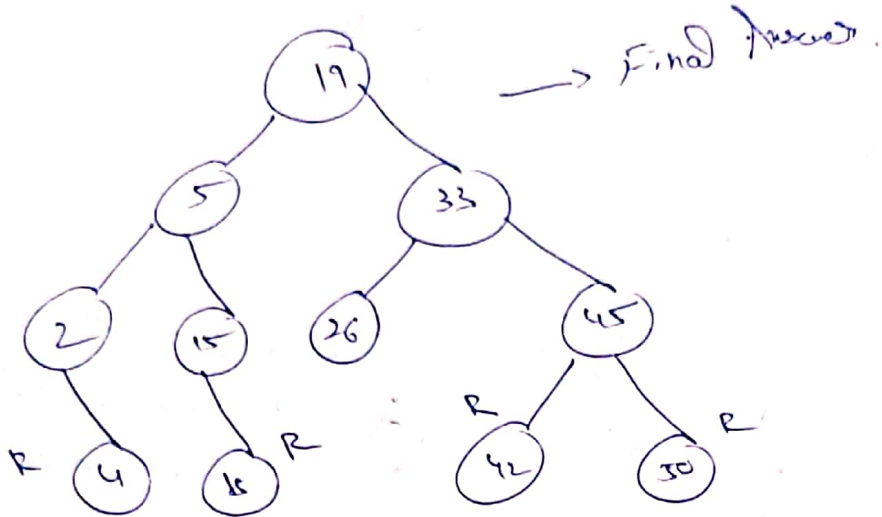
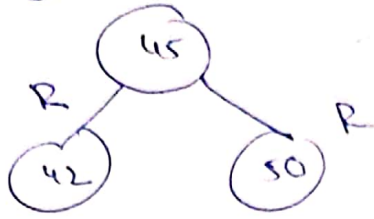


Replace with null
we have an imbalance
of black nodes.
So put black triangle.

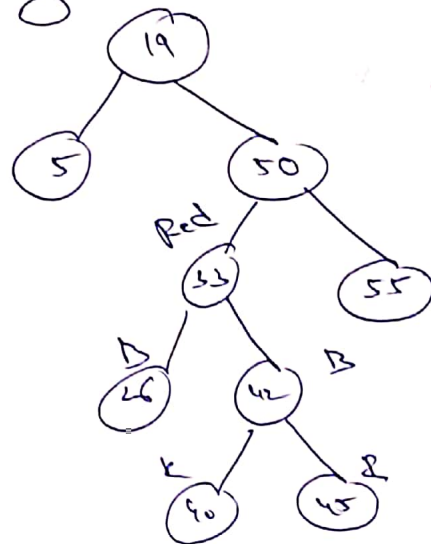
→ Also check sibling and nephew. Since sibling is Red, rotate. null node and it remains to the right of 50 with the black square.



It is in zig-zag
↳ Straight it up.

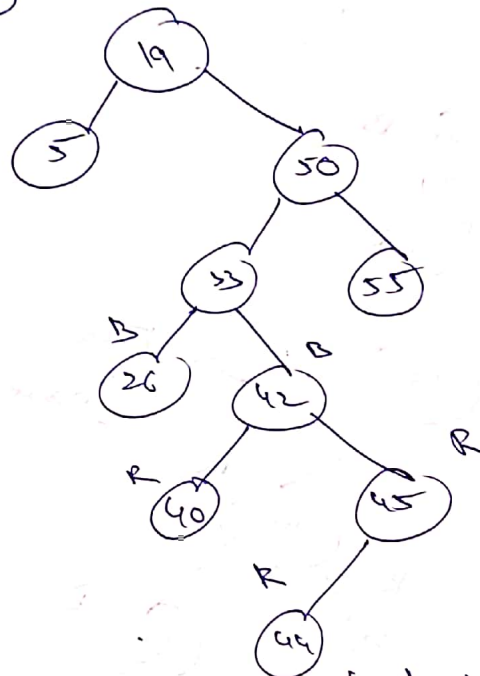


3)(b) Inserting 40

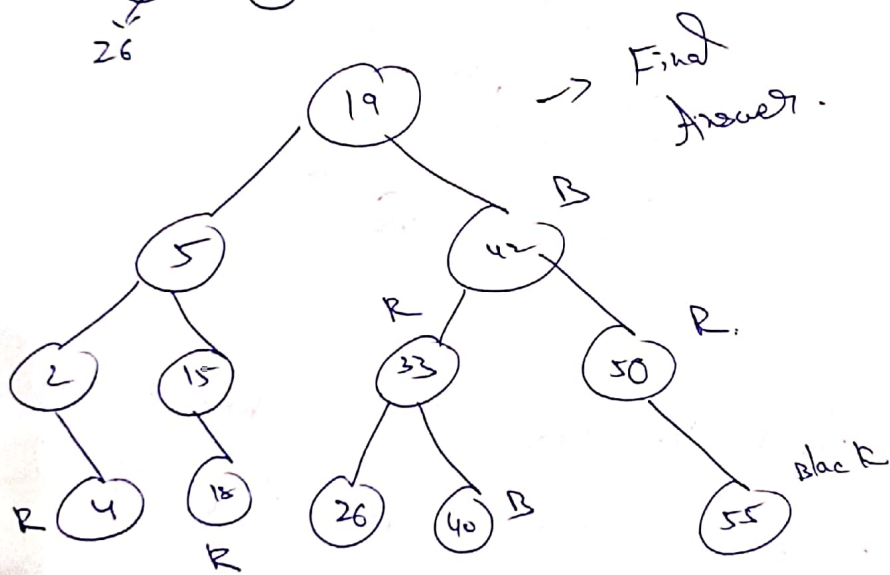
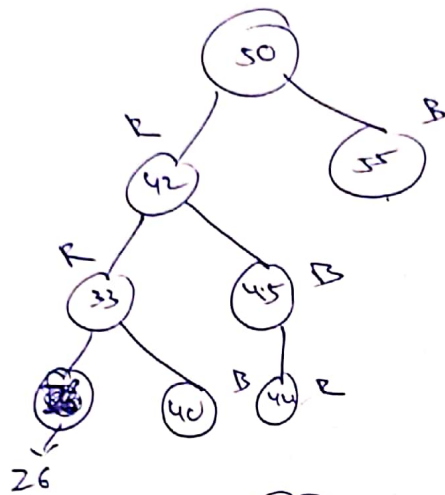
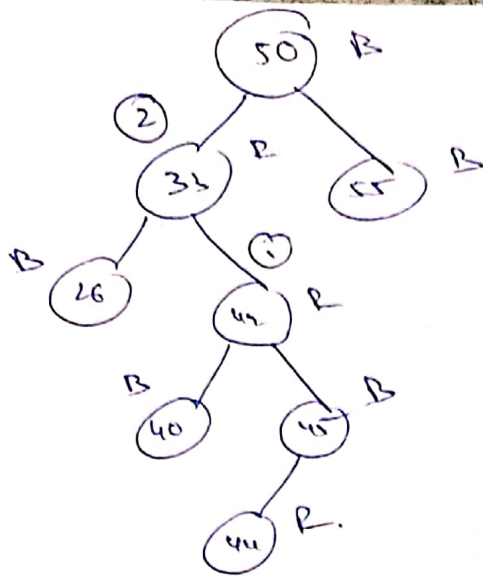


→ new node Red.

Inserting 44



Check the node if it is Red or Black.
 → Since the node is red change the parents to black ~~parents~~ and grand parents to red.



4) $1 \rightarrow -1 \rightarrow -2 \rightarrow 6 \rightarrow 10$

$2 \rightarrow -1 \rightarrow 8$

$3 \rightarrow -1 \rightarrow 6$

$4 \rightarrow -1 \rightarrow -2 \rightarrow 10$

$5 \rightarrow -1 \rightarrow 4$

$6 \rightarrow -1 \rightarrow -2 \rightarrow -3 \rightarrow -4 \rightarrow -5$

$7 \rightarrow -1 \rightarrow 1$

$8 \rightarrow -1 \rightarrow -2 \rightarrow 10$

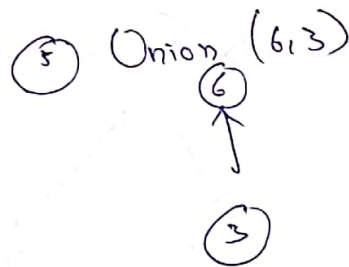
$9 \rightarrow -1$

$10 \rightarrow -1 \rightarrow -2 \rightarrow -4 \rightarrow -6 \rightarrow -8$

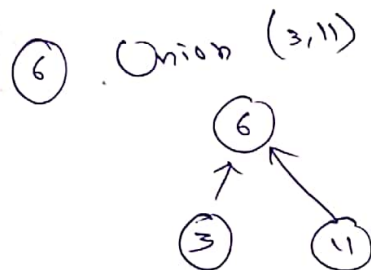
$11 \rightarrow -1 \rightarrow 6$

$12 \rightarrow -1 \rightarrow 10$

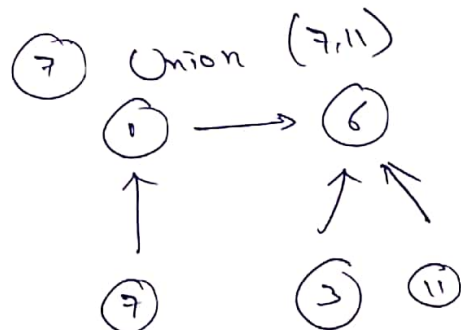
① Union (4,5)



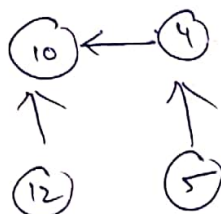
② Union (10,12)

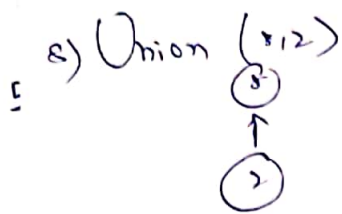


③ Union (1,7)

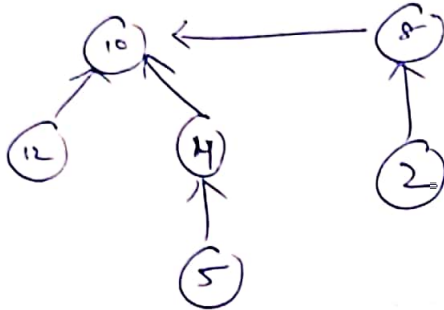


④ Union (12,5)

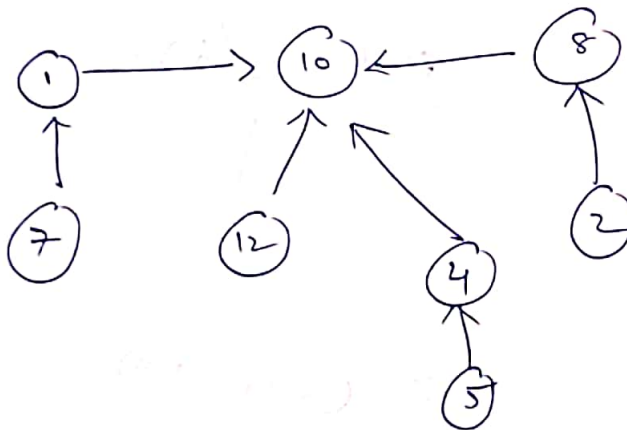




9) Union (12, 2)



10) Union (7, 12)



5) Given

3776, 1248, 0159, 0378, 0127, 0047, 4495, 0077,
3218, 0119, 0061, 1416, 3225

RADIX Sort LSD :
We need to Sort for maximum of 4 times.

0

1 0061,

2

3

4

5 4495, 3225

6 3776, 1416,

7 0127, 0047, 0077

8 1248, 0378, 3218

9 0159, 0119,

After 1 iteration we have

0061, 4495, 3225, 3776, 1416, 0127, 0047, 0077, 1248,
0378, 3218, 0159, 0119

0

1 ~~3225~~ 1416, 3218, 0119

2 3225, 0127,

3

4 0047, 1248

5 0159

6 0061,

7 3776, 0077, 0378,

8

9 4495

After second iteration we have

1416, 3218, 0119, 3225, 0127, 0047, 1248, 0159, 0061,
3776, 0077, 0378, 4495

0 ~~0047~~ 0047, 0061, 0077

1 0119, 0127, 0159

2 3218, 3225, 1248

3 0378

4 1416, 4495

5

6

7 3776,

8

9

After third iteration

0047, 0061, 0077, 0119, 0127, 0159, 3218, 3225, 1248,
0378, 1416, 4495, 3776

0 0047, 0061, 0077, 0119, 0127, 0159, 0378

1 1248, 1416

2

3 3218, 3225, 3776

4 4495

5

6

7

8

9

After 4th iteration, we get the sorted array.

0047, 0061, 0077, 0119, 0127, 0159, 0378, 1248, 1416,

3218, 3225, 3776, 4495

6) Given
Table size ~~10~~ = 7

164, 378, 289, 94, 821, 632, 200, 120

$$\begin{aligned} \Rightarrow 164 &= 11 \div 7 = 4 \\ 378 &= 18 \div 7 = 4 \rightarrow \text{Already occupied} \Rightarrow 4+1 \\ 289 &= 19 \div 7 = 5 \rightarrow \text{Already occupied} \Rightarrow 5+1 \end{aligned}$$

0
1
2
3
4 164
5 378
6 289

For inserting 94, the load factor will be greater than 0.5, so increasing table size to next prime number after doubling $\Rightarrow 17$ Final answer.

$$\begin{aligned} 164 &\Rightarrow 11 \div 17 = 11 \\ 378 &\Rightarrow 18 \div 17 = 1 \\ 289 &\Rightarrow 19 \div 17 = 2 \\ 94 &\rightarrow 13 \div 17 = 13 \\ 821 &\Rightarrow 11 \div 17 = 11 \rightarrow \text{occupied} \\ &\Rightarrow 11+1 \\ 632 &\rightarrow 11 \div 17 = 11 \rightarrow \text{occupied} \\ &\Rightarrow 11+1 = 12 \rightarrow \text{occupied} \\ &\Rightarrow 11+2 = 13 \rightarrow \text{occupied} \\ &\Rightarrow 11+3 = 14 \\ 200 &\rightarrow 2 \div 17 = 2 \rightarrow \text{occupied} \\ &\Rightarrow 2+1 = 3 \\ 120 &\rightarrow 3 \div 17 = 3 \rightarrow \text{occupied} \\ &\Rightarrow 3+1 = 4 \end{aligned}$$

0
1 378
2 289
3 200
4 120
5
6
7
8
9
10
11 $\rightarrow 164$
12 $\rightarrow 821$
13 $\rightarrow 94$
14 $\rightarrow 632$
15
16

7) Sort the edge distance of vertices on ascending order.

$$(h, g) = 1$$

$$(g, f) = 2$$

$$(c, i) = 2$$

$$(a, b) = 4$$

$$(c, d) = 4$$

$$(i, g) = 6$$

$$(h, i) = 7$$

$$(c, d) = 7$$

$$(b, c) = 8$$

$$(a, h) = 8$$

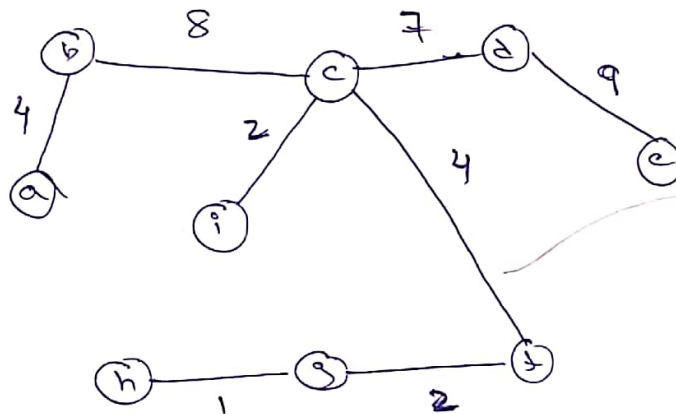
$$(d, e) = 9$$

$$(e, f) = 10$$

$$(b, h) = 11$$

$$(d, f) = 14$$

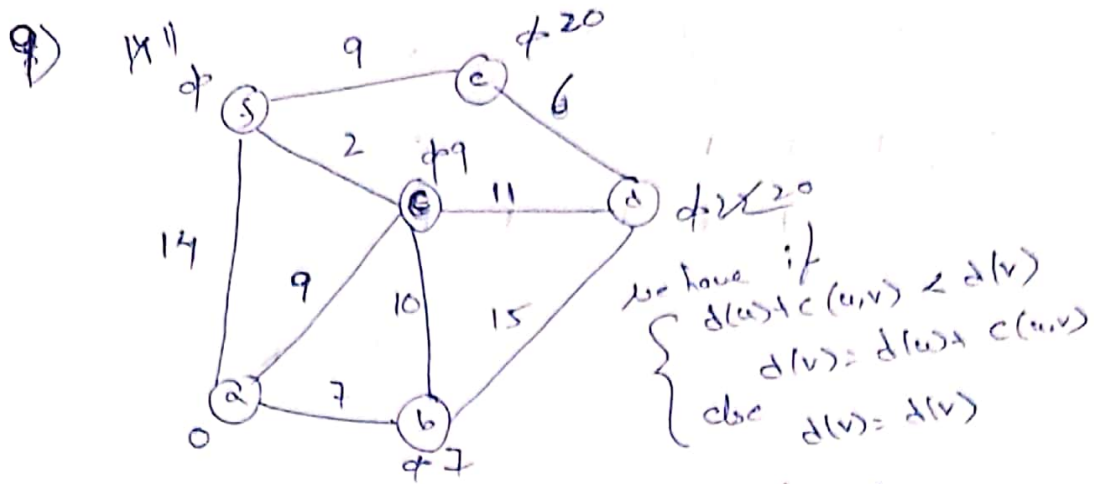
Now start joining vertices by considering minimum edge weights which doesn't form any loops



8) Incidence Matrix representation.

	e_1	e_2	e_3	e_4	e_5	e_6	e_7
v_1	1	1	1	0	0	0	0
v_2		1	1	1		1	1
v_3							
v_4							
v_5							

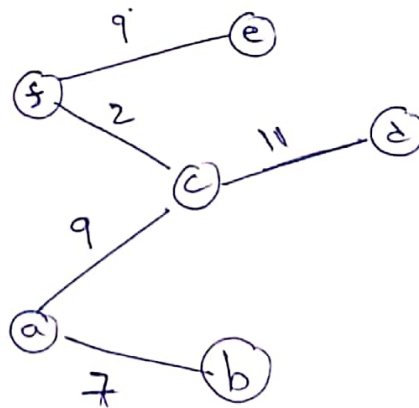
	e_1	e_2	e_3	e_4	e_5	e_6	e_7	e_8
v_1	1	1	1	0	0	0	0	0
v_2	0	1	1	1	0	1	1	0
v_3	0	0	0	1	1	0	0	0
v_4	0	0	0	0	0	0	1	1
v_5	0	0	0	0	1	1	0	0



	a	b	c	d	e	f
	0	∞	∞	∞	∞	∞ \rightarrow initially
a	0	7	9	∞	∞	14
b	0		9	20	∞	14
c	0			20	∞	11
d				20	20	11
e					20	
f						

\therefore the shortest path from a is

a - 0
 b - 7
 c - 9
 d - 20
 e - 20
 f - 11



10) * Degree:-

↳ In graphs, the degree of the vertex of a graph is nothing but the number of edges that are incident to the vertex.

⇒ The degree of a vertex is denoted by Δ .

* In-degree:-

⇒ The number of incoming edges to a vertex (v) is called In-degree.

* Out-degree:-

⇒ The no. of outgoing edges from a vertex is called "out degree".

11) Algorithm:-

↳ Start from a random vertex (v) of a graph and

perform DFS (G, v)

→ If DFS (G, v) didn't reach other vertex in the graph G , then there exists some vertex u , such that there is no directed path from v to u . so it is not strongly connected.

→ If the DFS (G, v) reach to every other vertex, then there is a directed path from vertex v to every other vertex in graph G .