Instructions. This exam is open book and open note—you may freely use your notes, lecture notes, or textbook while working on it. You may *not* consult any living resources such as other students or web forums. The exam must be submitted by **5:00 PM on Thursday, November 11th, 2021.** If you do not attend class in person, you may email your scanned or typeset solution **in PDF format** to the professor using the subject line [COSC 211] Midterm 02.

In order to receive full credit, be sure to show your work for each problem (where applicable)—an answer without justification is not guaranteed to receive any credit.

Affirmation. I attest that that work presented here is mine and mine alone. I have not consulted any disallowed resources while taking this exam.

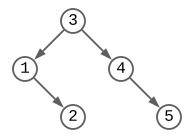
Name:			
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Problem 1. Consider an SSet implementation using an *unbalanced* binary search tree (BST).

(a) Starting from an initially empty BST, in the space below draw the tree depicting the state of the BST after adding the elements 10, 15, 20, 5, 25, 3, 7, 12, 11, 16, 17 in that order (i.e., after calling add(10), add(15), add(20), etc.).

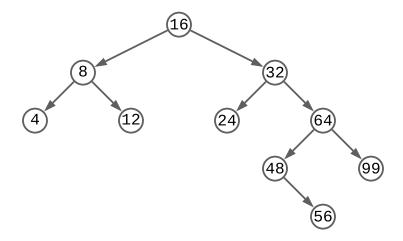
(b) In the space below, draw the resulting BST after performing the operation remove (15).								

(c) Starting from an empty BST, the following state is the result of adding the elements 3, 1, 4, 2, 5 in that order:



In the space below, list all orderings of the numbers 1 through 5 such that adding the elements in that order to an initially empty BST would result in the same state depicted above.

Problem 2. The following BST is *not* an AVL (height balanced) tree:



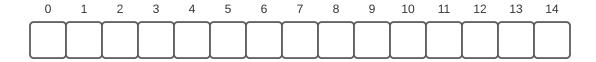
- (a) On the tree above, indicate the height of each node, and find all nodes that are not height balanced.
- (b) The AVL property of the tree above can be restored by performing a single restructure operation. In the space below, draw the (AVL) tree resulting from performing this restructure operation.

Problem 3. Consider the following binary heap, represented as an array:

			3										
1	5	3	21	13	7	11	23	25	17	19	9	15	

(a) In the space below, express the heap above as a complete binary tree.

(b) What is the *array* resulting from the operation add(2)?



(c) Starting from the original heap, what is the array resulting from the removeMin() operation?

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