Price Impact Models and Applications

Introduction to Algorithmic Trading

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Plan

Last Week

Preview of the two modules, trading data.

For this Week

An introduction to kdb+ and q:

- (a) Setting up q
- (b) Hello world!
- (c) Loading a database
- (d) Data grammar and basic data manipulation
- (e) Advantages and pitfalls of q

Next Week

Mathematical foundation of price impact models.

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Kdb+ Documentation (Recommended)

Kx website

- (a) references: code.kx.com/q/ref
- (b) course: kx.com/academy
- (c) guide for quants: code.kx.com/q/learn/brief-introduction

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Introduction

Why Kdb+ and Q?

Novotny et al. (Nomura, 2019)

"The kdb+ database and its underlying programming language, q, are the standard tools that financial institutions use for handling high-frequency data."

Efinancialcareers.com (2019)

"if you want to be assured of a job in finance, it will benefit you to learn the coding languages K and Q. K and Q underpin the Kdb+ database system which is used increasingly by banks, hedge funds and high frequency trading houses"

Efinancialcareers.com (2021)

"Developers proficient in both Q and kdb+, the database system that goes with it, tend to be both hard to find and in constant demand globally."

What are Kdb+ and Q?*

Kx systems develops Kdb+

Kx systems describe kdb+ on their web page "Developing with kdb+ and the q language":

- (1) "a high-performance cross-platform historical-time series columnar database
- (2) an in-memory compute engine
- (3) a real-time streaming processor
- (4) an expressive query and programming language called q"

An example

```
select avg slippage by date from orderTable where date > 2020.12.31
```

What do Firms Use Kdb+ for?

Real time trading (3)

Real-time analytics, trading data, algorithms, and signal generation.

Historical replay (1)

Historical monitoring, performance analysis (TCA), and signal research and backtests.

Never underestimate a real-time Graphical User Interface (GUI) for stakeholders:

"Though I did ultimately improve the model, the traders benefited most from the friendly user interface I programmed into it. This simple ergonomic change had a far greater impact on their business." (Derman, Goldman 2004)

Case-study: Almgren's Quantitative Brokers

Real Time Trading Signals, Almgren (2018)

Almgren outlines Quantitative Brokers' trading technology: www.youtube.com/watch?v=s4IdoWUhRDA.

"Signal generator (Kdb+)

The signal generator receives market data, performs computations to predict prices, and feeds the results to the algorithmic engine to improve trade execution."

Essential argument (1)+(3)

Quantitative Brokers uses the same code to generate signals in research and production: signals' reproducibility and accuracy are crucial.

Competitive Edge of Kdb+: Core Performance (1/2)

Native vectorization (2)

Q natively optimizes data structures and functions for vector and time series manipulation.

Automatic parallelization (1)+(2) Q automatically parallelizes operations. For example,

select avg slippage by date from tbl

automatically parallelizes by date.

Competitive Edge of Kdb+: Core Performance $(2/2)^*$

On disk operations (2)

Q can do (some) computations without loading the data in memory. For example,

```
smallTbl lj bigTbl
```

joins bigTbl onto smallTbl even if bigTbl does not fit in memory.

Competitive Edge of Kdb+: Data Locality (1/2)

Data locality is an essential principle for dealing with large datasets.

Models should run computations where one stores the data.

Why data locality matters (1)+(2)

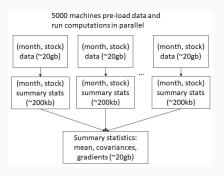
Massive data incurs an upfront transfer cost before any computation can start. This data marshaling cost is prohibitive for the iterative coding style of researchers and traders.

Example in Python: www.dask.org
The Python package Dask implements Pandas grammar with data locality as a core principle.

Competitive Edge of Kdb+: Data Locality (2/2)

Distribute to local data (1)+(2).

Loading data in and out of memory can be expensive. Data locality pre-loads specific data sections on given servers. The central controller distributes computations to servers where the data is local.



When to Use Kdb+ and When to Use Python?

A prerequisite

Both $kd\dot{b}+$ and python must be properly set up to allow for seamless integration with high frequency data.

- (a) For kdb+, this involves a distributed database.
- (b) For Python, this involves a distribution package such as Dask.

Use kdb+ (or C++)

when you want to be close to production: e.g., GUIs, low-latency signals, and live testing require a close connection to production data to remain accurate.

Use python (or R)

when you want to leverage off-the-shelf machine learning packages: e.g., do you want to code neural networks from scratch?

Most quantitative trading teams mix both low and high-level languages.

First Steps in Kdb+

Download and Install the Personal License

```
Kx's general introduction
code.kx.com/q/learn/startingkdb
Download the 32-Bit Personal Edition of kdb+
kx.com/developers/download-licenses
By default, q installs in folders:
// unix
^{\sim}/q/132
// mac
^{\sim}/q/m32
// windows
c:\q\w32
```

Run Hello World!

Run the executable in a shell.

```
c:\q\w32>q.exe
KDB+ 3.6 2019.04.02 Copyright (C) 1993-2019 Kx Systems
w32/ 16()core 4095MB webst desktop-jfb94cd 10.0.0.213 NONEXPIRE

Welcome to kdb+ 32bit edition
For support please see http://groups.google.com/d/forum/personal-kdbplus
Tutorials can be found at http://code.kx.com
To exit, type \\
To remove this startup msg, edit q.q
q)
```

Figure 1: Q's command line.

"Hello World!" tests the installation.

```
show "Hello World!"
```

Save and Run a Script

For sizable scripts, running from terminal is cumbersome. Two solutions:

- (a) Use an IDE: e.g., Qpad, JupyterQ, or Visual Studio with a q plugin.
- (b) Write your script in a .q file and load it.

Example for (b)

```
show "Hello World!"
```

Listing 1: test.q

```
q)\l test.q
"Hello World!"
q)
```

Figure 2: Loading a q-script.

Debug Mode and Exit

Q automatically enters debug mode upon errors.

```
\begin{array}{c} \text{$\backslash$ terminal when not in debug mode} \\ q) \\ \text{$\backslash$ terminal when in debug mode} \\ q)) \end{array}
```

The backslash command exits debug mode, and double backslash exits q altogether.

```
q)f:{1+`}
q)f[1]
'type
  [1] f:{1+`}
q))\
q)\\
c:\q\w32>
```

Figure 3: Example q error.

Loading Data

Load a Database

Same command as loading a script will "load" a database folder into your Q session. In practice

- (a) An object appears for each table in the database.
- (b) You can interact with the object as if it were a table.
- (c) The table is not *actually* loaded in memory: it is only "mapped" for fast reading (2).

q)\l C:\lo q)tbl: sel q)tbl										
date	stock	open	close	dailyTrdLiq	eodImb	eodOfi				
2019.01.02	Α	66.215	65.71	1.88388e+007	-221602	1761854				
019.01.02	AAL	31.525	32.495	3.491806e+007	-394635.8	1.709619e+007				
019.01.02	AAP	156.545	157.965	2.873893e+007	-4987624	2836347				
019.01.02	AAPL	154.915	157.925	8.596159e+008	9295054	1.153468e+008	٠.			

Figure 4: Mapping a database.

Read a File

Reading csvs

The function 0: reads a csv file. See code.kx.com/q/ref/file-text/#load-csv.

```
\msgFile is the file capturing all the messages on the
   public tape
msgFile: '$ (string stockName), "_2012-06-21
   _34200000_57600000_message_1.csv";

\The read function requires column types (f is float, j is
   integer).
msg: 0:[("fjjjjj"; ","); msgFile];

\we manually add column names
msg: ('time'eventType'orderId'size'price'direction)!msg;
```

Database Properties (1/2)

Databases are faster than csvs.

Databases are larger than what fits in memory

You can think of database object as a pointer with (most) table methods (1)+(2).

- (a) Tables only load in memory after an explicit query. Therefore, building concise queries matters (e.g., only load columns you need).
- (b) If aggregating data down (e.g. by stock, date), do this *before* loading the data in memory: kdb+ implements common operations (e.g. averages) on disk before returning the result in memory.
- (c) Data engineers set attributes onto specific table columns to speed up operations. For example, most tables are partitioned by date, sorted by (stock, time). They may also guarantee uniqueness of certain id columns.

Database Properties (2/2)

```
q)select avg mid by stock from bin10 where date = 2019.02.01

stock| mid

------|

A | 76.10731

AAL | 36.28517

AAP | 159.3925

AAPL | 167.2042
```

Figure 5: Sample database query.

Best practices

- (a) Check the table meta information first.
- (b) Always start with a date where clause, e.g., date = x or date within (x y).
- (c) Only load columns you need.
- (d) Consider on disk aggregations.
- (e) Consider on disk joins.



Figure 6: Table meta information.

Data Grammar in Q

What is a Data Grammar?

Quants manipulate sizable data daily

Modern languages break down data manipulation in small actions (verbs) applied to tables (nouns). The precise syntax defines a language's or package's data grammar and aids readability, flexibility, and re-use of code.

Examples in other languages

- (a) An old and well-established data grammar are SQL queries.
- (b) The first package to formalize the idea of data grammar is dplyr from R by Hadley Wickham.
- (c) The most used grammar in data science is pandas.

Introducing Qsql queries

Documentation

code.kx.com/q/basics/qsql

Queries transform tables using two clauses and an action

- (a) Where clauses filter data.
- (b) By clauses group data.
- (c) Actions apply a function to the data.

For instance, the following computes each stock's cumulative sum of trades above 10^4 shares.

select sums trade by stock from tbl where abs[trade] > 1e4

Joining tables

Two tables merge, typically based common columns called keys.

Comparison to Sql queries (4)

Sql is still the standard

The pandas documentation refers to it as a starting point:

"Since many potential pandas users have some familiarity with SQL, this page is meant to provide some examples of how various SQL operations would be performed using pandas."

Qsql mimics sql grammar

The syntax is the same. Q also has a more general but less user-friendly grammar, called functional select. See code.kx.com/q/basics/funsql.

Comparison to Python's Pandas

Where clauses are like filters

```
select from tbl where stock = 'AAPL
tbl[tbl["stock"] = "AAPL"]
```

By clauses are like groupby

```
select avg return by stock from tbl
tbl.groupby("stock").agg({"return": np.mean})
```

Joins are like merges

```
tbl1 lj 'stock xkey tbl2
pd.merge(tbl1, tbl2, on="stock", how = "left")
```

Comparison to R's Dplyr

Where clauses are like filters

```
select from tbl where stock = 'AAPL
tbl %>% filter(stock == "AAPL")
```

By clauses are like group_by

```
select avg return by stock from tbl
tbl %>% group_by(stock) %>% summarize(mean(return))
```

Joins are like left_join

```
tbl1 lj 'stock xkey tbl2
tbl1 %>% left_join(tbl2, by = "stock")
```

Multiple Where Clauses

start with the date clause!

Q interprets where clause chains as "and" statements. Where clauses are (nearly the only thing in q) evaluated left to right:

```
\good practice
select from tbl where date within (2019.01.01 2019.01.31),
    stock = 'AAPL

\bad practice
select from tbl where stock = 'AAPL, date within (2019.01.01
    2019.01.31)
```

By Clause Example

Example: binning fill data into 10 second intervals.

Time	Stock	Trade	Midprice	Spread						
9:30:01	AAPL	-70	154.77	0.18]					
9:30:03	AAPL	100	154.74	0.16		TimeBin	Stock	Trade	MidStart	Spread
9:30:07	AAPL	-100	154.705	0.10		9:30:00	AAPL	-70	154.77	0.18
9:30:12	AAPL	234	154.705	0.025		9:30:10	AAPL	224	154.705	0.10
9:30:13	AAPL	-10	154.78	0.02						

```
\the pattern (x xbar y) bins the vector y every x units. See
    code.kx.com/q/ref/xbar
select sum trade,
    midStart: first midPrice,
    first stock, first spread
    by timeBin: 10 xbar time from tbl
```

Update vs Select for By Clauses.

Select statements return one row per group

```
Q)select avg size by stock from tbl where time < 10:00:00
stock | Size |
AAPL | 87.62302
AMZN | 86.2926
GOGG | 97.90174
INIC | 372.7882
MSST | 408.5571
```

Update statements return one vector per group*

```
Object a wg price, sums size by stock from tbl
Time

09:30:00.004 ANPL 18 S31.436

09:30:00.005 ANPL 36 S831.436

09:30:00.005 ANPL 36 S831.436

09:30:00.207 ANPL 36 S831.436

09:30:00.207 ANPL 36 S831.436

09:30:00.207 ANPL 36 S831.436

09:30:00.207 ANPL 37 S831.436

09:30:00.207 ANPL 30 S831.436

09:30:00.207 ANPL 30 S831.436

09:30:00.207 ANPL 30 S831.436

09:30:00.207 ANPL 30 S831.436

09:30:30:00.207 ANPL 30 S831.436

09:30:30:00.207 ANPL 30 S831.436

09:30:30:30.207 ANPL 32 S831.436

09:30:30:30.207 ANPL 32 S831.436

09:30:30:30.207 ANPL 32 S831.436

09:30:30:30.207 ANPL 32 S831.436
```

Join Operators

Three frequent joins

- (a) Comma join joins data by rows or columns.
- (b) Left join joins data by keys.
- (c) As-of join joins data by the previous timestamp.

Comma Join*

Joining rows

The comma operator appends two conforming data structures. For tables, if tbl1 and tbl2 share columns and data types,

tbl1, tbl2

appends tbl2 rows after tbl1 rows.

Joining columns

The following pattern joins two tables' columns. Tbl1 and tbl2 must have the same number of rows.

flip (flip tbl1), (flip tbl2)

Left Join (1/2)

Documentation

code.kx.com/q/ref/lj

Example

Left join merges two tables based on shared columns, called keys. Rows from the two tables with matching keys merge into one row. For instance

```
trades lj 'stock'date xkey volatility
```

adds a volatility table to the trades table, matching on stock and date.

Left Join (2/2)

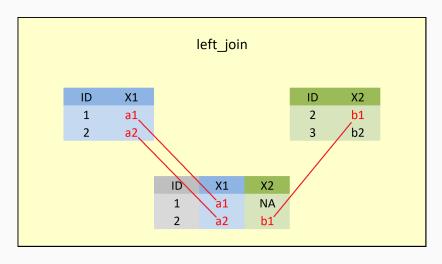


Figure 7: Source: statisticsglobe.com

As-of Join (1/2)

Documentation

code.kx.com/q/ref/aj

Asynchronous timeseries are common in trading

For example, let tbl1 represent trades on AAPL and tbl2 trades on GOOG. Trades on AAPL and GOOG are unlikely to happen exactly simultaneously. Therefore, using time as a key variable leads to few matches when using precise timestamps.

The last trade on AAPL as of the trade time on GOOG

aj['time; tbl1; tbl2]

For instance, this may produce

timeGOOG	- 1	midGOOG	timeAAPL	midAAPL	nidAAPL	
	-					
10:01:09.001	- 1	94.37	10:01:08.967	142.68		
10:01:15.127	- 1	94.36	10:01:08.967	142.68		
10:02:05.900	- 1	94.39	10:02:02.186	141.65		

As-of Join (2/2)



Figure 8: Additional example. Source: version1.com

A helpful practice for live trading*

Always add a column that gives the as-of time from the other table: this indicates how "stale" the as-of information is. It is particularly useful when considering algorithms' latency requirements.

Advantages and Pitfalls of Q

Basic Operations (1/4)

A common source of bugs

For performance reasons, q evaluates statements from right to left, regardless of the standard order of operations. This property leads to counter-intuitive results.

```
q)1+5*1
6
q)5*1+1
10
```

Figure 9: Counter-intuitive q example.

Basic Operations (2/4)

List of q operators code.kx.com/q/ref/

abs	cor	ej	gtime	like	mins	prev	scov	system	wavg
acos	cos	ema	hclose	lj ljf	mmax	prior	sdev	tables	where
aj aj0	count	enlist	hcount	load	mmin	rand	select	tan	while
ajf ajf0	cov	eval	hdel	log	mmu	rank	set	til	within
all	cross	except	hopen	lower	mod	ratios	setenv	trim	wj wj1
and	CSV	exec	hsym	Isq	msum	raze	show	type	wsum
any	cut	exit	iasc	Itime	neg	read0	signum	uj ujf	xasc
asc	delete	exp	idesc	Itrim	next	readl	sin	ungroup	xbar
asin	deltas	fby	if	mavg	not	reciprocal	sqrt	union	xcol
asof	desc	fills	ij ijf	max	null	reval	SS	update	xcols
atan	dev	first	in	maxs	or	reverse	ssr	upper	xdesc
attr	differ	fkeys	insert	mcount	over	rload	string	upsert	xexp
avg	distinct	flip	inter	md5	parse	rotate	sublist	value	xgroup
avgs	div	floor	inv	mdev	peach	rsave	sum	var	xkey
bin binr	do	get	key	med	pj	rtrim	sums	view	xlog
ceiling	dsave	getenv	keys	meta	prd	save	SV	views	xprev
cols	each	group	last	min	prds	scan	svar	vs	xrank

```
q)a:1
q)a=1
1b
```

Figure 10: Variable assignement vs equality.

Basic Operations (3/4)

Terseness

Q scripts are straightforward to write.

- (a) many high-performance, inbuilt base operators
- (b) expressive data grammar, ideal for scripting
- (c) overloaded functions mean that related operations "feel" similar
- (d) most tasks can be written in a few lines of q

Excessive terseness

It is hard to read q code. Even the original coder will forget what the cryptic one-liner does two weeks from now!

Basic Operations (4/4)

Best practices

- (a) when possible, write qsql
- (b) when not possible, still write qsql (in a comment)
- (c) wrap unreadable q snippets in functions. Document functions
- (d) use dictionaries as function arguments when you need extra flexibility (advanced)

Data Types: Atoms

What is an atom?

Atoms represent an indivisible data unit of a single type. code.kx.com/q/basics/datatypes/.

Casting types in q

One changes an object's type using the \$ operator and checks an object's type using the function "type", which returns the type's integer representation.

```
q)type 5
-7h
q)'float$5
5f
g)type `float$5
-9h
```

Figure 11: Type example.

Data Types: Lists

A list is a collection of objects

Vectors are lists of atoms with a single type. Q vectorizes essential functions and operations: when performed on vectors, these functions significantly outperform traditional loops.

```
q)1 2 3 4
1 2 3 4
q)1 + til 4
1 2 3 4
```

Figure 12: Vector example.

Mixed lists are lists of varying types.

One uses mixed lists as function arguments and avoids their use for massive datasets.

Data Types: Dictionaries

Dictionaries take in two lists: keys and values.

Q assumes keys are unique, and the dictionary defines a map from keys to values.

```
q)(`a`b`c)!(1 1 3)
a| 1
b| 1
c| 3
q)dic: (`a`b`c)!(1 1 3)
q)dic[`b]
1
```

Figure 13: Dictionary example.

Strings and Symbols*

Strings In a stri

In q, strings are atomic character lists; therefore, a string list is nested.

Symbols

Symbols are an enumeration type: q internally encodes them with integers but displays symbols like strings with a backtick prefix.

- (a) Symbols perform better with assignments and searches.
- (b) Symbols are expensive to modify.

One converts strings to symbols with the '\$ operator and symbols to strings with the "string" function.

```
q)a: "Hello World!"
q)a
"Hello World!"
q)b:"§a
q)b
"Hello World!
q)b
"Hello World!
q)string b
"Hello World!"
```

Figure 14: String example.

Functions and Loops

Q implements loops by wrapping an operation in a function and iterating the function over a list. This pattern is like R's lapply and python's map.

```
/define a function that displays its arg and returns arg+1
f:{[arg]
  show arg;
  :arg+1; / colon acts as the return operator in this
    context
  };
/test on an atom
f [0]
/loop over a list
f each 0 1 2
/common iteration pattern
f each til 3
```

Function Projections

A common pattern in q is *projection*, where one projects a function with multiple arguments down to a single argument by *freezing* other arguments.

```
\the following function adds two numbers together
g:{[a;b]
  :a+b:
 };
\f is a projection of g, with the first argument fixed to 1
f: g[1;];
\we can now loop over the second argument
f each til 3
\one can loop g without defining the projection f
g[1; ] each til 3
```

Examples

Computing Daily Market Stats

```
\computing daily stats on disk. Of a replaces NAs in vector
   x with Os.
stats: select vol: sdev Of^(neg 1) + mid% prev mid,
              imbalance: sum Of^trade*mid,
              adv: sum Of abs trade*mid
              by date, stock from bin10;
\avoid look-ahead bias by shifting data. A trading month has
    roughly 20 days.
stats: update vol: prev mavg[20; vol],
              imbalance: prev mavg[20; imbalance],
              adv: prev mavg[20; adv]
              by stock from stats;
\loading a month of intraday trading data
tbl: select from bin10 where date within (2019.01.01
   2019.01.31);
\joining the daily stats with the trading data
tbl: tbl lj 'date'stock xkey update stats;
```

Computing Cumulative Sums and Moving Averages

```
\many signals are moving averages of past trades. It helps
   to normalize variables using adv!
tbl: update cumulativeImb: sums trade%adv,
            imb1min: ema[1%6; trade%adv],
            imb5min: ema[1%30: trade%adv].
            imb30min: ema[1%180; trade%adv],
            imb60min: ema[1%360: trade%adv]
            by date, stock from tbl;
\note the key use of update to parallelize computations by
   date and stock!
\to enable parallel computing, you must specify the number
   of cores when you start q. For instance, to enable
   parallelization over eight cores, use
q.exe -s 8
```

Computing Returns

Why different return horizons?

Different trading strategies operate on different timescales.

- * E.g. a one minute strategy focuses on one minute alpha forecasts and price impact: the first minute of the day may require a different model from the middle of the day.
- * E.g. a two hour forecast will be less sensitive to the "time of the day". Market news may matter more.

Return Horizons (1/3)

Bad approach to generate returns Computing variables as aggregation functions over the horizon: this loops over the data multiple times!

time	return		time	return		time	return	
09:30	10bps	10min	09:30	10bps	15min	09:30	10bps	
09:35	-5bps	returns	09:35	-5bps	returns	09:35	-5bps	
09:40	3bps		09:40	3bps		09:40	3bps	30min
09:45	8bps		09:45	8bps		09:45	8bps	returns
09:50	-1bps		09:50	-1bps		09:50	-1bps	
09:55	-8bps		09:55	-8bps		09:55	-8bps	
10:00	-13bps		10:00	-13bps		10:00	-13bps	
10:05	2bps		10:05	2bps		10:05	2bps	

Return Horizons (2/3)

Good approach to generate returns

- (a) Use cumulative variables, e.g., prices, impact, cumulative volumes.
- (b) For each horizon, compute horizon-specific difference variables.



Simple shift in Python Pandas

df['ret10min'] = df['price'].shift(2) % df['price'] - 1
df['ret30min'] = df['price'].shift(6) % df['price'] - 1

instead of expensive aggregations

df['ret10min'] = df['ret'].groupby('10min').aggregate('cumulateRet')
df['ret30min'] = df['ret'].groupby('30min').aggregate('cumulateRet')

Return Horizons (3/3)

```
\optional step if you aren't sure the grid is sorted by time
    . Sorting by date, stock accelerates the grouping.
tbl: 'date'stock'time xasc tbl:
\xprev[n; ] shifts data by n steps. Negative n look into the
    future.
\For grids, we look ahead a fixed number of steps on the
   grid within a given (date, stock) group. This assumes
   the grid is sorted by time!
tbl: update retEod: (neg 1) + last[mid]%mid,
            ret1min: (neg 1) + xprev[-6; mid]%mid,
            ret5min: (neg 1) + xprev[-30; mid]%mid,
            ret30min: (neg 1) + xprev[-180; mid]%mid,
            ret60min: (neg 1) + xprev[-360; mid]%mid,
            by date, stock from tbl;
```

Computing Returns for Non-grids (e.g. Intervals)

```
tbl: select startTime: time, mid from events;
\ Step (a): duplicate rows for each horizon to define
    interval end times
tbl: tbl cross ([]horizon: 00:01:00 00:05:00 00:30:00
    01:00:00):
tbl: update endTime: startTime + horizon from tbl;
\ Step (b): Apply an as-of joins to endTimes
tmpTbl: select endTime: time, endMid: mid from events;
tbl: aj['endTime; tbl; tmpTbl];
\ Step (c) Finalize return computation using the start and
    end states
outputTbl: update ret: (neg 1) + endMid%mid from intervalTbl
```

Weekly Summary

Learn qSql queries.

It's a useful data grammar: make sure you are comfortable solving standard data manipulation problems with queries.

Keep kdb+'s idiosyncracies in mind.

The right to left evaluation is an unfortunate reality. The earlier you get used to it, the better.

Take advantage of kdb+'s speed.

If an operation feels slow, you are likely doing it "wrong".

Document your code.

Documenting code is a good practice. It's particularly important for Q, which is a *terse* language.

Questions?

Next week

First module: using price impact models in trading algorithms.

- (a) Mathematical foundation of price impact.
- (b) Example on the Obizhaeva and Wang (OW) model.
- (c) Translate alpha signals into trades.