

## ch-17

I] Inserting  $n$  elements using

a] Aggregate Method:-

- the table doubles in size when it runs out of space

- so, if the original size is 1, after insertion it doubled to size 2, after 2 more inserting, it doubles to size 4, etc.

- In general, after  $k$  doublings, the size is  $2^k$ .

Pseudo code:-

Initialize table with capacity = 1

For  $i = 1$  to  $n$

if table is Full

new table = create new table with size  $2 \times$  current size

copy elements from old table to new table

table = new table

insert element  $a_i$  into table



$$\text{Let } k = \log(n+1) - 1$$

$$\begin{aligned}\text{Total cost} &= O(n) * k \\ &= O(n \log n)\end{aligned}$$

Amortized cost per insertion  $= O(\log)$

Runtime per insertion is  $O(\log n)$

$$\text{Total time is } O(n) * \log(n+1)$$

b) Accounting Method

charge 2 units for each insertion.

when the table doubles in size, from  $m$  to  $2m$ , credit  $m$  units.

The credit exactly pay for the copy cost  $O(1) + O(m)$

$$\text{Total credit is } M + 2M + 4M + \dots + n/2 * m = O(n^2)$$



Pseudo code

initialize table with capacity =  $\sqrt{n}$

For  $i = 1$  to  $n$

if table is Full!

new table = create Newtable with  
size  $2 \times \text{current size}$

Copy elements from old table to  
new table

table = newtable

② insert element  $+ i$  into table

initialize charges = 0

initialize credits = 0

For  $i = 1$  to  $n$ :

charges  $++ 2$

if table doubled in size from  $m$   
to  $2m$

credits  $+= m$

Total charges =  $2 \times n = O(n)$

Total credits =  $m + 2m + \dots + n/2^k m = O(n)$

Amortized cost per insertion =  $\text{Total} / n$   
 $= O(n) / n$   
 $= O(1)$



Runtime per insertion =  $O(1)$

Total time =  $O(n^2)$