

### BSTNode:

info: TElem  
left:  $\uparrow$  BSTNode  
right:  $\uparrow$  BSTNode

### BinarySearchTree:

root:  $\uparrow$  BSTNode

**function** search\_rec (node, elem) **is:**

*//pre: node is a BSTNode and elem is the TElem we are searching for*

**if** node = NIL **then**

    search\_rec  $\leftarrow$  false

**else**

**if** [node].info = elem **then**

        search\_rec  $\leftarrow$  true

**else if** [node].info < elem **then**

        search\_rec  $\leftarrow$  search\_rec([node].right, elem)

**else**

        search\_rec  $\leftarrow$  search\_rec([node].left, elem)

**end-if**

**end-function**

- Complexity of the search algorithm:  $O(h)$  (which is  $O(n)$ )

**function** search (tree, elem) **is:**

*//pre: tree is a BinarySearchTree and elem is the TElem we are searching for*

currentNode  $\leftarrow$  tree.root

found  $\leftarrow$  false

**while** currentNode  $\neq$  NIL and not found **execute**

**if** [currentNode].info = elem **then**

        found  $\leftarrow$  true

**else if** [currentNode].info < elem **then**

        currentNode  $\leftarrow$  [currentNode].right

**else**

        currentNode  $\leftarrow$  [currentNode].left

**end-if**

**end-while**

search  $\leftarrow$  found

**end-function**

**function** initNode(e) **is:**

*//pre: e is a TComp*

*//post: initNode  $\leftarrow$  a node with e as information*

allocate(node)

[node].info  $\leftarrow$  e

[node].left  $\leftarrow$  NIL

[node].right  $\leftarrow$  NIL

initNode  $\leftarrow$  node

**end-function**

**function** insert\_rec(node, e) **is:**

*//pre: node is a BSTNode, e is TComp*

*//post: a node containing e was added in the tree starting from node*

**if** node = NIL **then**

node  $\leftarrow$  initNode(e)

**else if** [node].info  $\leq$  e **then**

[node].left  $\leftarrow$  insert\_rec([node].left, e)

**else**

[node].right  $\leftarrow$  insert\_rec([node].right, e)

**end-if**

insert\_rec  $\leftarrow$  node

**end-function**

- Complexity:  $O(n)$

**function** minimum(tree) **is:**

*//pre: tree is a BinarySearchTree*

*//post: minimum  $\leftarrow$  the minimum value from the tree*

currentNode  $\leftarrow$  tree.root

**if** currentNode = NIL **then**

@empty tree, no minimum

**else**

**while** [currentNode].left  $\neq$  NIL **execute**

currentNode  $\leftarrow$  [currentNode].left

**end-while**

minimum  $\leftarrow$  [currentNode].info

**end-if**

**end-function**

**function** parent(tree, node) **is:**

*//pre: tree is a BinarySearchTree, node is a pointer to a BSTNode, node  $\neq$  NIL*

*//post: returns the parent of node, or NIL if node is the root*

$c \leftarrow \text{tree.root}$

**if**  $c = \text{node}$  **then** *//node is the root*

    parent  $\leftarrow$  NIL

**else**

**while**  $c \neq \text{NIL}$  **and**  $[c].\text{left} \neq \text{node}$  **and**  $[c].\text{right} \neq \text{node}$  **execute**

**if**  $[c].\text{info} \geq [\text{node}].\text{info}$  **then**

$c \leftarrow [c].\text{left}$

**else**

$c \leftarrow [c].\text{right}$

**end-if**

**end-while**

    parent  $\leftarrow c$

**end-if**

**end-function**

- Complexity:  $O(n)$

**function** successor(tree, node) **is:**

*//pre: tree is a BinarySearchTree, node is a pointer to a BSTNode, node  $\neq$  NIL*

*//post: returns the node with the next value after the value from node*

*//or NIL if node is the maximum*

**if**  $[\text{node}].\text{right} \neq \text{NIL}$  **then**

$c \leftarrow [\text{node}].\text{right}$

**while**  $[c].\text{left} \neq \text{NIL}$  **execute**

$c \leftarrow [c].\text{left}$

**end-while**

        successor  $\leftarrow c$

**else**

$p \leftarrow \text{parent}(\text{tree}, c)$

**while**  $p \neq \text{NIL}$  **and**  $[p].\text{left} \neq c$  **execute**

$c \leftarrow p$

$p \leftarrow \text{parent}(\text{tree}, p)$

**end-while**

        successor  $\leftarrow p$

**end-if**

**end-function**