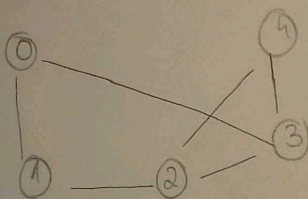


Practical Work 5. Find a Hamiltonian cycle in an undirected graph. If it exists.



Hamiltonian Cycle ( $N$ , adj-matrix, path, current-position)

$N=5$ ; path = [0, -1, -1, -1, -1], current-position = 1

HamiltonianCycle(5, adj-matrix, [0, -1, -1, -1, -1], 1)

current-position =  $N \Leftrightarrow 1 = 5$  (False)

for vertex in range (1, 5):

vertex = 1

isNext(adj-matrix, [0, -1, -1, -1, -1], 1, 1) = true

path[1] = 1

HamiltonianCycle(5, adj-matrix, [0, 1, -1, -1, -1], 2)

2 = 5 (False)

for vertex in range (1, N)

vertex = 1

isNext(adj-matrix, [0, 1, -1, -1, -1], 2, 1) = false

vertex = 2

isNext(adj-matrix, [0, 1, -1, -1, -1], 2, 2) = true

path[2] = 2

HamiltonianCycle(5, adj-matrix, [0, 1, 2, -1, -1], 3)

3 = 5 (False)

for vertex in range (1, 5):

vertex = 1

isNext(adj-matrix, [0, 1, 2, -1, -1], 3, 1) = false

vertex = 2

isNext(adj-matrix, [0, 1, 2, -1, -1], 3, 2) = false

vertex = 3

isNext(adj-matrix, [0, 1, 2, -1, -1], 3, 3) = ~~false~~ true

vertex Input file  
5 6 edges  
0 1 2 cost

1 2 3

2 3 0

3 4 2

4 2 0

0 3 1

Adjacency matrix

	0	1	2	3	4
0	0	1	0	1	0
1	1	0	1	0	0
2	0	1	0	1	1
3	1	0	1	0	1
4	0	0	1	1	0

path[3]=3

isHamiltonCycle(5, adj-matrix, [0, 1, 2, 3, -1], 4)

4=5 (False)

for vertex in range(1, 5):

vertex=1

isNext(adj-matrix, [0, 1, 2, 3, -1], 4, 1)=false

vertex=2

isNext(adj-matrix, [0, 1, 2, 3, -1], 4, 2)=false

vertex=3

isNext(adj-matrix, [0, 1, 2, 3, -1], 4, 3)=false

vertex=4

isNext(adj-matrix, [0, 1, 2, 3, -1], 4, 4)=true

path[4]=4

isHamiltonCycle(5, adj-matrix, [0, 1, 2, 3, 4], 5)

5=5 (True)

adj-matrix[0][4]=0 (False)

→ isHamiltonCycle(5, adj-matrix, [0, 1, 2, 3, 4], 5) = ~~false~~ false

path[4]=-1

→ isHamiltonCycle(5, adj-matrix, [0, 1, 2, 3, -1], 4) = false

vertex=4

isNext(adj-matrix, [0, 1, 2, -1, -1], 3, 4)=true

path[4]=4

isHamiltonCycle(5, adj-matrix, [0, 1, 2, 4, -1], 4)

4=5 (false)

for vertex in range(1, 5)

isNext(adj-matrix, [0, 1, 2, 4, -1], 4, 1)=false

isNext(adj-matrix, [0, 1, 2, 4, -1], 4, 2)=false



isNext(adj-matrix, [0, 1, 2, 4, ~~4~~], 4, 3) = true

path[4] = 3

HamiltonianCycle(5, adj-matrix, [0, 1, 2, 4, 3], 5)

5 = 5

adj-matrix[0][3] = true

→ HamiltonianCycle(5, adj-matrix, [0, 1, 2, 4, 3], 5) = true

→ HamiltonianCycle(5, adj-matrix, [0, 1, 2, 4, -1], 4) = True

→ HamiltonianCycle(5, adj-matrix, [0, 1, 2, -1, -1], 3) = True

→ HamiltonianCycle(5, adj-matrix, [0, 1, -1, -1, -1], 2) = True

→ HamiltonianCycle(5, adj-matrix, [0, 1, -1, -1, -1], 1) = True

⇒ A Hamiltonian cycle ~~cont~~ contained in the Graph is: 0 1 2 4 3 0