Software Systems Verification and Validation



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Faculty of Mathematics and Computer Science Babeş-Bolyai University

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Software Systems Verification and Validation

"Tell me and I forget, teach me and I may remember, involve me and I learn."

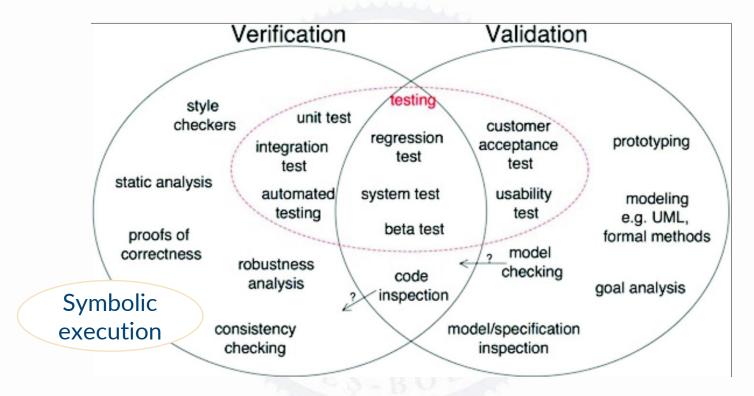
(Benjamin Franklin)

(Next)/Today Lecture

Correctness



What we will learn!



• http://www.easterbrook.ca/steve/2010/11/the-difference-between-verification-and-validation/

Outline

- Correctness
- Floyd's Method -Inductive assertions, Partial correctness, Termination
- Hoare Logic, Semantics of Hoare triples, Partial correctness, Total correctness
- Dijkstra's Language, Guarded commands, Nondeterminacy, Formal Derivation of Programs
- Developing correct programs from specification, Refinement, Rules of Refinement, Examples
- Static analysis, JML- Java Modeling Language, ESC/Java2- Extended Static Checker for Java
- Questions

Program verification methods - Correctness

- Lecture 1 Verification and Validation
 - Verification/Validation
 - reviews products to ensure their quality → correctness
 - · static and dynamic analysis techniques
 - A correct program is one that does exactly what it is intended to do, no more and no less.
 - A formally correct program is one whose correctness can be proved mathematically.
 - This requires a language for specifying precisely what the program is intended to do.
 - · Specification languages are based in mathematical logic.
 - Until recently, correctness has been an academic exercise. Now it is a key element of critical software systems.

Program verification - correctness

- 1. proof-based, computer-assisted, program-verification approach, mainly used for programs which we expect to terminate and produce a result
- 2. model-based, automatic, property-verification approach, mainly used for concurrent, reactive systems (originally used in a post-development stage) model checking (Lecture 9)
- 3. Developing correct algorithms from specification (Carroll Morgan, "Programming from Specification)

Correctness-by-Construction.

Originally intended as a mere means of programming algorithms that are correct by construction - -Dijkstra (1968), Hoare (1971),

the approach found its way into commercial development processes of complex systems - Hall (2002), Hall and Chapman (2002)

2012, The Correctness-by-Construction Approach to Programming, Authors: Kourie, Derrick G., Watson, Bruce W.

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2023, Automated Software Engineering Conference, The 5th International Workshop on Automated and verifiable Software system DEvelopment (ASYDE)

Topic: Correct-by-construction software development

(https://conf.researchr.org/track/ase-2023/ase-2023--workshop--asyde#the-5th-international-workshop-on-automated-and-verifiable-software-system-development-aside)

Correctness Tools

Theorem provers (PVS), Modeling languages (UML and OCL), Specification languages (JML), Programming language support (Eiffel, Java, Spark/Ada), Specification Methodology (Design by contract)

· Methods for prooving program correctness

- Floyd's Method Inductive assertions
- · Hoare Semantics of Hoare triples

Aplicability

- · Partial correctness of the program
- Termination of the program
- Total correctness = Partial correctness + Termination of the program

Uses

- The condition satisfied by the initial values of the program.
- The condition to be satisfied by the output of the program.
- Source code of the program.

Method:

- Cut the loops
- Find an appropriate set of inductive assertions.
- Construct the verification/termination conditions.
- **Theorem**: If all verification conditions are true, then the program is partially correct, i.e., whenever it terminates the result is correct.
- Remark. The method is useful when it is combined with termination.



Robert W Floyd (June 8, 1936 -September 25, 2001)

Partial correctness - steps

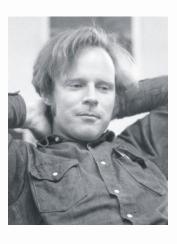
- Cutting points are chosen inside the algorithm
 - 1 point at the beginning of the algorithm, 1 point at the end;
 - 2 At least 1 point for each *loop* statement
- For each cutting point an assertion (invariant predicate) is chosen.
 - 1 Entry point $\varphi(X)$;
 - 2 Ending point $\psi(X, Z)$.
- Construction of the verification conditions
 - Path from *i* to $j \alpha$;
 - P_i and P_i are assertions in i and j;
 - $R_{\alpha}(X,Y)$ predicate that gives the condition for path α ;
 - $r_{\alpha}(X,Y)$ function that gives the transformations of the variables Y from path α ;
- Theorem: If all the verification conditions are true then *P* is partial correct.



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Partial correctness - example

```
• Algorithm for z=x^y z:=1;\ u:=x;\ v:=y; A: \varphi(X)::=(v>0 \land (y\geq 0)) While (v>0) execute B: \eta(X,Y)::=z*u^v=x^y If (v \text{ is even}) then u:=u*u;\ v:=v/2; else v:=v-1;\ z:=z*u; end If end While end Alg; C: \psi(X,Z)::=z=x^y
```



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Termination- steps

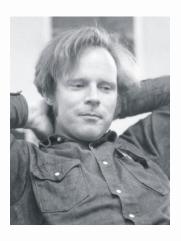
- Cut the loops and find "good" inductive assertions.
- Choose a well-formed set M (i.e., an ordered set without infinite strictly decreasing sequences)
- To demonstrate that some termination conditions hold: passing from one cutting point to another the values of some functions in the well-ordered set decrease.
- In point i a function is chosen $u_i: D_X \times D_Y \to M$ and the termination condition on α is: $\forall X \forall Y (\varphi(X) \land R_{\alpha}(X,Y) \to (u_i(X,Y) > u_i(X,r_{\alpha}(X,Y))))$.
- **Remark**. If partial correctness was demonstrated then the termination condition can be: $\forall X \forall Y (P_i(X) \land R_{\alpha}(X,Y) \rightarrow (u_i(X,Y) > u_i(X,r_{\alpha}(X,Y))))$.
- Theorem: If all the termination conditions hold then the program *P* terminates.



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Termination- example

```
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- The meaning of a statement is described by a triple
 - $\{\varphi\}$ P $\{\psi\}$, where φ is called the precondition and ψ is called the postcondition.

{P} S {Q}

"when started in a state satisfying P, any terminating execution of S ends in a state satisfying Q"

If P does not terminate, we make no guarantees.

- Partial correctness
 - $\models_{par} \{\varphi\}P\{\psi\}$
 - only if P actually terminates.
- Total correctness
 - $\models_{tot} \{\varphi\}P\{\psi\}$
 - the program P is guaranteed to terminate.



The Grand Verification Challenge Hoare 2003

Develop a compiler which verifies that the program is correct

https://vimeo.com/39256698

Charles Antony Richard Hoare (11 January 1934, Colombo, Sri Lanka)



An Advanced Study Institute of the NATO Security Through Science Committee

the Institut fľr Informatik, Technische UniversitĤt Mļnchen, Germany,

Software System Reliability and Security

August 1 to August 13 2006

M. Broy (director)
O. Kupferman (director)
C.A.R. Hoare (co-director)
A. Pnueli (co-director)

Katharina Spies (secreta

The Summer School is also substantially supported by the DAAD under the program "Deutsche Sommerakademie 2006", and the town and the county of Marktoberdorf





Partial correctness



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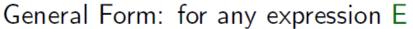
Charles Antony Richard Hoare (11 January 1934, Colombo, Sri Lanka)

Rules

- Assignment
- Sequencing
- Conditional
- Loop

Partial correctness

Assignment



• $\{P\} \ X := E\{Q\} \ provided[P \Rightarrow \langle X \leftarrow E \rangle (Q)]$

- Consider the triple $\{P\}X := Y + 2\{Q\}$
 - Given predicate Q, for what predicate P does this hold?
 - for any P such that $[P \Rightarrow \langle X \leftarrow Y + 2 \rangle (Q)]$
- Examples
 - $\{P_0\} X := Y + 2 \{X \le Y + 2\}$ $P_0 \equiv true$
 - $\{P_1\} X := Y + 2 \{X < 0\}$ $P_1 \equiv (Y + 2 < 0)$
 - $\{P_2\} X := Y + 2 \{Y < 0\}$ $P_2 \equiv (Y < 0)$
 - $\{P_3\} X := X + 2 \{X \text{ is even}\}\$ $P_3 \equiv (X \text{ is even})$



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Partial correctness

Sequencing

We can conclude

$$\{P\}$$
 S; $T\{Q\}$
if we can find a predicate R such that $\{P\}$ S $\{R\}$ and $\{R\}$ $T\{Q\}$

Examples

- $\{P_0\} X := 2 * X; X := X + 1\{X > 0\}$ $P_0 \equiv (2 * X + 1 > 0)]$
- $\{P_1\} X := Y; Y := 3 \{X + Y < 5\}$ $\{P_1 \equiv (Y + 3 < 5)]$



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Partial correctness

Conditional

• We can conclude $\{P\}$ IF (C) THEN S ELSE T END $\{Q\}$ provided we can show $\{P \land C\}$ S $\{Q\}$ and $\{P \land \neg C\}$ T $\{Q\}$



```
• \{?\} \{((x > y) \Rightarrow Q_0) \land ((x \le y) \Rightarrow Q_1)\}

IF (x > y) THEN Q_0: \{(m|x - y) \land (m|y)\}

x := x - y

ELSE Q_1: \{(m|x) \land (m|y - x)\}

y := y - x

END

Q: \{(m|x) \land (m|y)\}

• So our final proof obligations are
```

 $[(x > y) \Rightarrow (m|x - y) \land (m|y) \text{ and}$ $[(x < y) \Rightarrow (m|x) \land (m|y - x)]$

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5/19/2023

4 m b 4 A b

Partial correctness

Loop

- How can we conclude
 {P} WHILE (G) DO S END {Q}
 At the end of the loop (assuming it terminates), we know ¬G
 But in general we dont know how often S is executed...
- Suppose we have a predicate J that is preserved by S $\{J\}S\{J\}$ such a J is called a loop invariant Then, at the end of the loop, we can conclude $J \land \neg G$ To establish the postcondition, we need J such that $[J \land \neg G \Rightarrow Q]$
- We can conclude
 {P} WHILE (G) DO S END {Q}
 provided we can find a loop invariant J such that

$$[P \Rightarrow J]$$

$$[J \land \neg G \Rightarrow Q]$$

$$\{G \land J\}S\{J\}$$

J holds at loop entry
J establishes Q at loop exit
J is preserved by each iteration



- The Grand Verification Challenge Hoare 2003
- Develop a compiler which verifies that the program is correct

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• Exponentiation using multiplication

•
$$\{(A > 0) \land (B \ge 0)\} \ S \ \{R = A^B\}$$

```
\{(A > 0) \land (B \ge 0)\}\

R := ?; b := 0 R := 1

WHILE (b \ne B) DO J : R = A^b

R := ?; R := R * A;

b := b + 1

END

\{R = A^B\}
```

- The meaning of a statement is described by a triple
 - $\{\varphi\}$ P $\{\psi\}$, where φ is called the precondition and ψ is called the postcondition.



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```
{P} S {Q}
```

"when started in a state satisfying P, any terminating execution of S ends in a state satisfying Q"

- If P does not terminate, we make no guarantees.
 - Partial correctness
 - $\models_{par} \{\varphi\}P\{\psi\}$
 - only if P actually terminates.
 - Total correctness
 - $\models_{tot} \{\varphi\}P\{\psi\}$
 - the program P is guaranteed to terminate.
- The "total correctness" interpretation also requires termination
 - "when started in a state satisfying P, any execution of S must terminate in a state satisfying Q "

Termination

Rules

- Assignment
- Sequencing
- Conditional
- Loop
 - Assignment $\{P\} \ X := E \ \{Q\} \ provided \ [P \Rightarrow \langle X \leftarrow E \rangle(Q)]$
 - Sequencing $\{P\}$ S; $T\{Q\}$ provided $\{P\}$ S $\{R\}$ and $\{R\}$ T $\{Q\}$ for some R
 - Conditional $\{P\} \ IF \ (G) \ THEN \ S \ ELSE \ T \ END \ \{Q\} \ provided \\ \{P \land G\} \ S \ \{Q\} \ and \ \{P \land \neg G\} \ T\{Q\}$
 - Note: Same as the rules for partial correctness!



The Grand Verification Challenge Hoare 2003

Develop a compiler which verifies that the program is correct

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- Total correctness rule for loops
- Consider{P} WHILE (G) DO S END {Q}
- How do we show that the loop terminates?
- One method find an integer expression V such that the value of V is nonnegative (that is $V \ge 0$), and the value of V (strictly) decreases in every iteration that is, $\{V = K\}$ S $\{V < K\}$
- Such an expression is called a "loop variant"



The Grand Verification Challenge Hoare 2003

Develop a compiler which verifies that the program is correct

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Exponentiation using multiplication

- $\{(A > 0) \land (B \ge 0)\}\$ S $\{R = A^B\}$
- Recall loop invariant $J: R = A^b \land (B \ge b)$;

$$\{(A>0)\land (B\geq 0)\}$$

$$R := 1; b := 0$$

WHILE
$$(b \neq B)$$
 DO $J: R = A^b \land (B \geq b);$

$$R := R * A$$
:

$$b := b + 1$$

END

$$\{R=A^B\}$$

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Guarded command

- "guarded command" a statement list prefixed by a boolean expression: only when this boolean expression is initially true, is the statement list eligible for execution
- ullet < guarded command >::=< guard >o< guarded list >
- < guard >::=< boolean expression >
- < guarded list >::=< statement > {; < statement >}
- < guarded command set >::= < guarded command > $\{\Box < guarded \ command > \}$
- \bullet < alternative construct >::= **if** < guarded command set > **fi**
- ullet < repetitive construct >::= do < guarded command set > do
- < statement >::=< alternative construct > |
 < repetitive construct > | "other statements"



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Nondeterminacy

• Example 1 if $x \ge y \to m := x$ $\Box y \ge x \to m := y$

• Example 2 - compute k s.t. for fixed value n and fixed function f(i) (defined for $0 \le i < n$), k will eventually satisfy $0 \le k < n$ and $(\forall i : 0 \le i < n : f(k) \ge f(i))$.

$$k := 0; \ j := 1;$$

do $j \neq n \rightarrow \text{if } f(j) \leq f(k) \rightarrow j := j + 1$
 $\Box f(j) \geq f(k) \rightarrow k := j; \ j := j + 1$
fi

od



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

Weakest pre-conditions

- Hoare introduced sufficient pre-conditions such that the mechanism will not produce the wrong result but may fail to terminate.
- Dijkstra introduced necessary and sufficient preconditions such that the mechanism are guaranteed to produce the right result.
 - = weakest pre-conditions
- wp(S, R), where S denotes a statement list, R some condition on the state of the system.
- wp called a "predicate transformer" because it associates a pre-condition to any post-condition R.



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Properties of wp

- 1 Law of the Excluded Miracle For any S, for all states: wp(S, F) = F
- Por any S and any two post-conditions, such that for all states $P \Rightarrow Q$, for all states: $wp(S, P) \Rightarrow wp(S, Q)$
- To any S and any two post-conditions P and Q, for all states: wp(S, P) and wp(S, Q) = wp(S, P) and wp(S, Q)
- For any deterministic S and any post-conditions P and Q, for all states:

$$(wp(S, P) \text{ or } wp(S, Q)) \Rightarrow wp(S, P \text{ or } Q)$$



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Assignment and concatenation operator

- Assignment
 - The semantics of x := E are given by: $wp("x := E", R) = R_E^x$, R_E^x -denotes a copy of the predicate defining R in which each occurrence of the variable x is replaced by E.
- Concatenation operator; The semantics of the; operator are given by: wp("S1; S2", R) = wp(S1, wp(S2, R)).



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The Alternative Construct

- Let IF denote: **if** $B_1 o SL_1 \square ... \square B_n o SL_n$ **fi** Let BB denote: $(\exists i : 1 \le i \le n : B_i)$, then, by definition $wp(IF, R) = (BB \text{ and } (\forall i : 1 \le i \le n : B_i \Rightarrow wp(SL_i, R)))$.
- Theorem 1 From $(\forall i: 1 \leq i \leq n: (Q \text{ and } B_i) \Rightarrow wp(SL_i, R)$ for all states we can conclude that $(Q \text{ and } BB) \Rightarrow wp(IF, R)$ holds for all states.)
- Let t denote some integer function, and wdec(S, t)
- Theorem 2 From $(\forall i : 1 \le i \le n : (Q \text{ and } B_i) \Rightarrow wdec(SL_i, t))$ for all states we can conclude that $(Q \text{ and } BB) \Rightarrow wdec(IF, t)$ hold for all states.
- By definition, $wdec(S, t) = (tmin(X) \le t(X) 1) = (tmin(X) < t(X)).$



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The Alternative Construct - example

- The formal requirements for performing m := max(x, y) is: $R : (m = x \text{ or } m = y) \text{ and } m \ge x \text{ and } m \ge y.$
- Assignment m := x for m = x? $wp("m := x", R) = (x = x \text{ or } x = y) \text{ and } x \ge x \text{ and } x \ge y = x \ge y$
- Theorem 1: $\mathbf{if} x > y \rightarrow m := x \mathbf{fi}$
- But $B \neq T$, so we weakening BB means looking for alternatives which might introduce new guards.
- Alternative: "m := y" that introduces the new guard $wp("m" := y, R) = y \ge x$ if $x \ge y \to m := x$ $\Box y \ge x \to m := y$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Repetitive Construct

- Let DO denote: $\mathbf{do}B_1 \to SL_1 \square ... \square B_n \to SL_n \mathbf{do}$ Let $H_0 = (R \text{ and non } BB)$ and for k > 0, $H_k(R) = (wp(IF, H_{k-1}(R)))$ or $H_0(R)$ then, by definition: $wp(DO, R) = (\exists k : k \ge 0 : H_k(R))$.
- Theorem 3
 If we have all the states $(P \text{ and } BB) \Rightarrow (wp(IF, P) \text{ and } wdec(IF, t) \text{ and } t \ge 0)$ we can conclude that we have for all states $P \Rightarrow wp(DO, P \text{ and non } BB)$
- T is the condition satisfied by all states, and wp(S, T) is the weakest pre-condition guaranteeing proper termination of S.
- Theorem 4 From $(P \text{ and } BB) \Rightarrow wp(IF, P)$ for all states, we can conclude that we have for all states $(P \text{ and } wp(DO, T) \Rightarrow wp(DO, P \text{ and non } BB))$



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

The Repetitive Construct - example

- The greatest common divisor: x = gcd(X, Y)
- Choose an invariant relation and variant function.
 establish the relation P to be kept invariant
 do "decrease t as long as possible under variance of P" od
- invariant relation (established by x := X; y := Y): P : gcd(X, Y) = gcd(x, y) and x > 0 and y > 0
- $(P \text{ and } B) \Rightarrow wp("x, y : E1, E2", P))$ = (gcd(X, Y) = gcd(E1, E2) and E1 > 0 and E2 > 0).
 - gcd(X, Y) = gcd(E1, E2) is implied by P
 - invariant for (x, y): wp("x := x y, P) = (gcd(X, Y) = gcd(x y, y)and x y > 0 and y > 0), and guard x > y
 - decrease of the variant function t = x + y $wp("x := x - y", t \le t_0) = (x \le t_0)$ tmin = x, wdec("x := x - y", t) = (x < x + y) = y > 0



Edsger Wybe Dijkstra (May 11, 1930 - August 6, 2002)

- x := X; y := Y**do** $x > y \to x := x - y$ **od**
- But P and BB are not allowed to conclude $x = \gcd(X, Y)$ the alternative y := y x requires a guard y > x
- x:=X; y:=Ydo $x > y \rightarrow x:=x-y$ $\Box y > x \rightarrow y := y - x$ od

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(https://conf.researchr.org/track/ase-2023/ase-2023--workshop--asyde#the-5th-international-workshop-on-automated-and-verifiable-software-system-development-aside)

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Questions

Developing correct programs from specification[Mor98]

Refinement

• Input data: X $\varphi(X)$ Output data: Z $\psi(X, Z)$

- Abstract program
 - $Z: [\varphi, \psi]$
- Refinement

$$P_1 \prec P_2 \prec ... \prec P_{n-1} \prec P_n$$

- Rules of refinement
 - Assignment rule
 - Sequential composition rule
 - Alternation rule
 - Iteration rule

Carroll Morgan

https://my.c se.unsw.edu. au/staff/staf f_details.php ?ID=carrollm

Developing correct programs from specification[Mor98]

Rules of Refinement

- Assignment rule: $[\varphi(v/e), \psi] \prec v := e$
- Sequential composition rule $(\gamma middlepredicate)$ $[\eta_1, \eta_2] \prec [\eta_1, \gamma]$ $[\gamma, \eta_2]$
- Alternation rule, $G = g_1 \vee g_2 \vee ... \vee g_n$ $[\eta_1, \eta_2] \prec$ if $g_1 \to [\eta_1 \wedge g_1, \eta_2]$ $\Box g_2 \to [\eta_1 \wedge g_2, \eta_2]$ \vdots $\Box g_n \to [\eta_1 \wedge g_n, \eta_2]$

```
• Iteration rule G = g_1 \vee g_2 \vee ... \vee g_n
[\eta, \eta \wedge \neg G] \prec
do g_1 \rightarrow [\eta \wedge g_1, \eta \wedge TC]
\Box g_2 \rightarrow [\eta \wedge g_2, \eta \wedge TC]
\vdots
\Box g_n \rightarrow [\eta \wedge g_n, \eta \wedge TC]
do
```

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 - the approach found its way into commercial development processes of complex systems Hall (2002), Hall and Chapman (2002)
 - 2012, The Correctness-by-Construction Approach to Programming, Authors: Kourie, Derrick G., Watson, Bruce W.
 - 2015, Experience with correctness-by-construction, B.W. Watson a, D.G. Kourie b, L. Cleophas b,*
 - 2016, Correctness-by-Construction and Post-hoc Verification: Friends or Foes?, Maurice H. ter Beek1(B), Reiner H"ahnle2, and Ina Schaefer3
- Correctness Tools
 - Theorem provers (PVS), Modeling languages (UML and OCL), Specification languages (JML), Programming language support (Eiffel, Java, Spark/Ada), Specification Methodology (Design by contract)
- · Methods for prooving program correctness
 - Floyd's Method Inductive assertions
 - Hoare Semantics of Hoare triples
 - Dijkstra's Language- Guarded commands, Nondeterminacy and Formal Derivation of Programs

Program verification methods - Correctness

- Software engineering problem: building/maintaining correct systems.
 - How?
 - Specification
 - Tools
- Formal Methods in Software Engineering
 - Formal languages guarantee
 - Precision (no ambiguity)
 - Certainty (modeling errors)
 - Automation (automatic verification tools).
- Things to do:
 - 1) make a formal model
 - 2) specify properties for the model
 - 3) **verify/check** the properties

- Formal methods and JML (Java Modeling Language):
 - 1) formal model is Java programming language
 - 2) the properties are specified in JML
 - 3) Properties may be
 - Tested using jmlrac
 - · Checked using ESC2Java

What is JML?

- Gary T. Leavens's JML group at the University of Central Florida
- http://www.eecs.ucf.edu/~leavens/JML//index.shtml
- a behavioral interface specification language
- used to specify the behavior of Java modules
- combines
 - design by contract approach
 - the model-based specification approach
 - some elements of the refinement calculus

Tools for using JML

- Runtime assertion checkers (e.g. jmlc/jmlrac)
- Static checkers (ESC2Java)

- Test generation (e.g. jmlunit)
- Formal verification tools (e.g. KeY)
- Design tools (e.g. AutoJML)

Tools for JML

Runtime assertion checking with jmlc/jmlrac

- Special compiler inserts runtime tests for all JML assertions. Any assertion violation results in a special exception.
- checks specs at run-time
- only tests correctness of specs.
- Find violations at runtime.

JML web page

 http://www.eecs.ucf.edu/~lea vens/JML//index.shtml

Extended static checking with ESC/Java

- Automatically tries to prove simple JML assertions at compile time.
- checks specs at compile-time
- proves correctness of specs.
- Warn about likely runtime exceptions and violations.

ESC/Java2 web page
http://www.kindsoftware.com/products/opensource/ESCJava2/download.html

Design by contract

Contract?

Method contract

Precondition

Specifies "caller's responsibility"

- Constraints on parameter values and target object's state.
- Valid object's states, in which a method can be called. *Intuitively*
- Expression that must hold at the entry to the method.

Postcondition

Specifies "implementation's responsibility"

- Constraints on the method's return value and side effects.
- Relation between initial and final state of the method. *Intuitively*
- Expression that must hold at the exit from the method.

Class contract

Invariant

- Specifies caller's responsibility at the entry to a method and implementation's responsibility at the exit from a method.
- Valid states of class instances (values of fields).

Intuitively

• Expression that must hold at the entry and exit of each method in the class.

Tools for JML

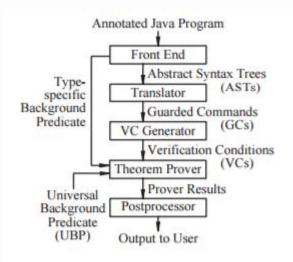
Runtime assertion checking with jmlc/jmlrac

- Special compiler inserts runtime tests for all JML assertions. Any assertion violation results in a special exception.
- checks specs at run-time
- only tests correctness of specs.
- Find violations at runtime.

jmlc and jmlrac - by example

- Compile and Run
- Compile
- jmlc FileName.java
- Run
- jmlrac FileName listOfParam
- Demo 01: Factorial
- Demo02: Integer sqrt

Faculty of Mathematics and Computer Science Babeş-Bolyai University



- Unsound?
- Incomplete?

Tools for JML

Extended static checking with ESC/Java

Automatically tries to prove simple JML assertions at compile time.

- ESC/Java2 by example
- Run
- escj FileName.java
- Demo 01: Fast exponentiation
- Demo 02: MyArray
- Demo 03: MySet

- checks specs at compile-time
- proves correctness of specs
- Warn about likely runtime exceptions and violations.

Next Lecture

Snyk Invited Lecture

Test-Driven Development (TDD) and its Role in Web and Internet Security

Presenter:

Matt Gibbs,

VP of Engineering at Snyk,

Former VP of Engineering at GitHub,

Microsoft Veteran

Tuesday

23 May 2023, 8-10 am

Room: 2/I

(Main Building)

Outline



- Correctness
- Floyd's Method -Inductive assertions, Partial correctness, Termination
- Hoare Logic, Semantics of Hoare triples, Partial correctness, Total correctness
- Dijkstra's Language, Guarded commands, Nondeterminacy, Formal Derivation of Programs
- Developing correct programs from specification, Refinement, Rules of Refinement, Examples
- Static analysis, JML- Java Modeling Language, ESC/Java2- Extended Static Checker for Java

Questions

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Software Systems Verification and Validation

"Tell me and I forget, teach me and I may remember, involve me and I learn."

(Benjamin Franklin)