

# Mobile Manipulation Calibration

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## 1 Introduction

The frames of interest are listed in Table 1.

Table 1: Coordinate frames.

Name	Subscript
World	$w$
Mobile base	$b$
Base of arm	$a$
End effector	$e$
Tool	$t$

The pose  $\mathbf{T}_{wt}$  of an arbitrary tool attached to the end effector can be computed using the sequence of transforms

$$\mathbf{T}_{wt} = \mathbf{T}_{wb}(\mathbf{q}_b)\mathbf{T}_{ba}\mathbf{T}_{ae}(\mathbf{q}_a)\mathbf{T}_{et}, \quad (1)$$

where  $\mathbf{T}_{wb}$  depends on the base configuration  $\mathbf{q}_b = [x_b, y_b, \theta_b]^T$  and  $\mathbf{T}_{ae}$  depends on the arm configuration  $\mathbf{q}_a$ .

## 2 Base Calibration

We need to calibration the Vicon measured base poses  $\hat{\mathbf{q}}_b$  so that the origin of  $\mathbf{T}_{wb}$  is correct. We have

$$\mathbf{T}_{wb}(\mathbf{q}_b) = \begin{bmatrix} \mathbf{C}_z(\theta_b) & \mathbf{r}_b \\ \mathbf{0}^T & 1 \end{bmatrix}, \quad (2)$$

where  $\mathbf{C}_z(\theta) \in SO(3)$  is a rotation about the  $z$ -axis and  $\mathbf{r}_b = [x_b, y_b, z_b]^T$  with  $z_b$  a constant. Our goal in this section is to calibrate the origin  $(x_b, y_b)$  so that it is located at the point of rotation of  $\theta_b$ .

Starting at an arbitrary configuration  $\mathbf{q}_{b,0}$ , we will move the base to a sequence of desired yaw angles  $\theta_{b,i}^d$  and obtain the corresponding measured configurations  $\hat{\mathbf{q}}_{b,i}$ . We would like to find an offset  $\Delta \mathbf{r}_b$  such that

$$\mathbf{r}_{b,i}^d = \hat{\mathbf{r}}_{b,i} + \Delta \mathbf{r}_b \quad (3)$$

is satisfied as closely as possible for each  $i$ . We will do so by solving the least squares problem

$$\operatorname{argmin}_{\Delta \mathbf{r}_b} \frac{1}{2} \sum_i \|\mathbf{r}_{b,0} - \hat{\mathbf{r}}_{b,i} - \Delta \mathbf{r}_b\|^2, \quad (4)$$

where we've used the fact that  $\mathbf{r}_{b,i}^d = \mathbf{r}_{b,0}$ .

### 3 Arm-End Effector-Tool Calibration

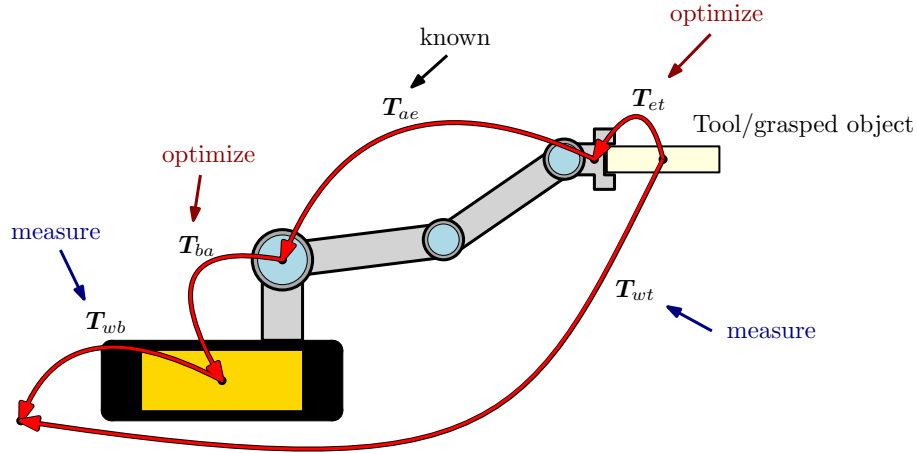


Figure 1: Frames on the robot being calibrated.

Having calibrated the base pose  $T_{wb}$ , we now wish to calibrate (static) the transforms between the base and arm  $T_{ba}$  and the EE and tool  $T_{et}$ . We will assume that factory calibration for the arm transform  $T_{ae}(\mathbf{q}_a)$  is good enough.

To do so, we will collect a sequence of pairs  $(\mathbf{q}_{a,i}, \hat{T}_{wt,i})$  by moving the arm to the sequence of configurations  $\mathbf{q}_{a,i}$ . We will then solve the (nonlinear) least squares problem<sup>1</sup>

$$\operatorname{argmin}_{T_{ba}, T_{wt}} \frac{1}{2} \sum_i \|\Xi(T_{wt}(\mathbf{q}), \hat{T}_{wt})\|^2. \quad (5)$$

<sup>1</sup>We may have nominal guesses for the transforms, in which case we would actually optimize over (for example)  $\Delta T_{ba}$ , where  $T_{ba} = \Delta T_{ba} \bar{T}_{ba}$  with nominal guess  $\bar{T}_{ba}$ .

over the manifold  $SE(3)$ , where  $\mathbf{T}_{wt}$  is computed using (1) and

$$\Xi(\mathbf{T}_1, \mathbf{T}_2) = \log(\mathbf{T}_1^{-1} \mathbf{T}_2)^\vee \quad (6)$$

is the error between the poses.