```
In [54]:
          %run my_functions_library.ipynb
                                                                      # executing my library file
          import math
          import matplotlib.pyplot as plt
                                                                      # to be used for plotting
        Question 1
In [55]:
          def func_1(x):
              return math.sqrt(1+1/x)
          eps, p, q =10**-6, 1, 4
          MP=[]
                                                                           # creating list for mid-point
          TR=[]
                                                                           # creating list for mid-point
```

```
SMP=[]
                                                    # creating list for mid-point
# Below, I'm adding elements to the above created lists
n1=8
MP.append(int_mid_point(func_1, p, q, n1))
TR.append(int_trapezoidal(func_1, p, q, n1))
SMP.append(int_simpson(func_1, p, q, n1))
MP.append(int_mid_point(func_1, p, q, n2))
TR.append(int_trapezoidal(func_1, p, q, n2))
SMP.append(int_simpson(func_1, p, q, n2))
n3=24
MP.append(int_mid_point(func_1, p, q, n3))
TR.append(int_trapezoidal(func_1, p, q, n3))
SMP.append(int_simpson(func_1, p, q, n3))
# Here I am calculating the actual value of integral
fn_mp=0.619
                                    # for func_1 # feed here maximum of second derivative of function for Mid-point
fn_t=0.619
                                    # for func_1 # feed here maximum of second derivative of function for trapezoidal
                                    # for func_1 # feed here maximum of fourth derivative of function for simpson
fn_s=6.016
N_mp, N_t, N_s = calculate_N(fn_mp, fn_t, fn_s)
MP.append(int_mid_point(func_1, p, q, N_mp))
TR.append(int_trapezoidal(func_1, p, q, N_t))
SMP.append(int_simpson(func_1, p, q, N_s))
# printing the values
print ("{:<30} {:<30} {:<30}".format('No. of iterations', 'Mid-point', 'Trapezoidal', 'Simpson'))</pre>
print()
print ("{:<25} {:<32} {:<30} {:<25}".format(n1, MP[0], TR[0], SMP[0]))</pre>
print ("{:<25} {:<32} {:<30} {:<25}".format(n2, MP[1], TR[1], SMP[1]))</pre>
print ("{:<25} {:<32} {:<30} {:<25}".format(n3, MP[2], TR[2], SMP[2]))</pre>
print()
print ("{:<25} {:<32} {:<30} {:<25}".format('True value', MP[3], TR[3], SMP[3]))</pre>
```

Trapezoidal

3.623956949398562

3.6211354043642174

3.620607687124767

3.6201848732718958

Simpson

3.6203301434402904

3.6201948893527693

3.620186449815972

3.6201849759261933

Question 2

Actual value

No. of iterations

8

16

24

Mid-point

3.6183138593298727

3.619709761707181

3.619972785533525

3.6201836884000755

```
In [77]:
         def func_2(x):
             return x*math.sqrt(1+x)
         eps, p, q = 10**-4, 0, 1
         fn_mp = 1
                                                    # for func_2 # feed here maximum of second derivative of function for Mid-point
         fn_t = 1
                                                    # for func_2 # feed here maximum of second derivative of function for trapezoidal
         fn_s = 1.5
                                                    # for func_2 # feed here maximum of fourth derivative of function for simpson
         N_mp, N_t, N_s = calculate_N(fn_mp, fn_t, fn_s, eps)
         MP=(int_mid_point(func_2, p, q, N_mp))
         TR=(int_trapezoidal(func_2, p, q, N_t))
         SMP=(int_simpson(func_2, p, q, N_s))
         print("Simpson :" )
         print("N = " + str(N_s), " ; integral = " + str(SMP), "\n")
         print("Trapezoidal :" )
         print(" N = " + str(N_t) , " ; integral = " + str(TR) , "\n")
         print("Mid-point : ")
         print("N = " + str(N_mp) , " ; integral = " + str(MP) , "n")
         Simpson :
         N = 4; integral = 0.6438016157592887
        Trapezoidal:
         N = 28; integral = 0.6438718899363646
        Mid-point :
        N = 20; integral = 0.643710311759088 n
```

In [70]:

Question 3

```
def func_3(x):
   return 4/(1+x**2)
print("Please wait\n Processing will take around 10 seconds")
plt.figure(figsize=(12,6))
p, q, N = 0, 1, 10
NN=[]
MC=[]
NN.append(N)
MC.append(int_monte_carlo(func_3,pdf,p,q,N))
x=[0,3000]
y=[math.pi, math.pi]
plt.plot(x,y,'k-', label='Actual value of PI')
for N in range(100, 3001, 100):
   NN.append(N)
   MC.append(int_monte_carlo(func_3,pdf,p,q,N))
plt.plot(NN, MC, 'r-o', label='Monte-carlo points')
print("The value of the integral in the last iteration is = " + str(MC[-1]))
One could also use N=10 and proceed with a step size of 10 as instructed in question 3 but
that will not give any significant improvement.
Hence, I made the plot with step size=100 upto 5000 taking a total of 50 points.
If one still wishes to use step-size = 10 and work for 100 points, then the following code should be used :
x=[0,500]
y=[math.pi, math.pi]
plt.plot(x,y,'r-', label='Actual value of PI')
for N in range(10, 501, 10):
   NN.append(N)
   MC.append(int_monte_carlo(f3,pdf,a,b,N))
plt.plot(NN,MC,'b-o', label='Monte-carlo points')
print("The value of the integral in the last iteration is = " + str(MC[-1]))
1.1.1
plt.grid(b=True, which='major', color='k', alpha=1, ls='-', lw=0.5)
plt.minorticks_on()
plt.grid(b=True, which='minor', color='g', alpha=0.2, ls='-', lw=0.5)
plt.ylim(3.12,3.16)
plt.legend()
plt.show()
```

Actual value of PI Monte-carlo points

3000

3.150 3.145 3.140 3.135 3.130 3.125

1500

The value of the integral in the last iteration is = 3.140063418670694

1000

Question 4

3.120

Please wait

3.155

Processing will take around 10 seconds

```
In [78]:
       def func_4(x):
          return x**3
       def func_5(x):
          return x**2
       eps, p, q = 10**-6, 0, 2
       print("Linear mass density = T = x^2")
       print("Centre of mass = integral(xT) dx / integral(T) dx")
       f4_mp = 12
                                         # for func_4 # feed here maximum of second derivative of function for Mid-point
       f4_t = 12
                                         # for func_4 # feed here maximum of second derivative of function for trapezoidal
       f4_s = 0
                                         # for func_4 # feed here maximum of fourth derivative of function for simpson
       N_mp, N_t, N_s = calculate_N(f4_mp, f4_t, f4_s, eps)
       MP1=(int_mid_point(func_4, p, q, N_mp))
       TR1=(int_trapezoidal(func_4, p, q, N_t))
       SMP1=(int_simpson(func_4, p, q, N_s))
       fn_mp = 2
                                        # for func_5 # feed here maximum of second derivative of function for Mid-point
       fn_t = 2
                                        # for func_5 # feed here maximum of second derivative of function for trapezoidal
                                        # for func_5 # feed here maximum of fourth derivative of function for simpson
       fn_s = 0
       N_mp, N_t, N_s = calculate_N(f5_mp, f5_t, f5_s, eps)
       MP2=(int_mid_point(func_5, p, q, N_mp))
       TR2=(int_trapezoidal(func_5, p, q, N_t))
       SMP2=(int_simpson(func_5, p, q, N_s))
       print("\n Using Mid-point, the centre of mass = " + str(MP1/MP2))
       print("\n Using Trapezoidal, the centre of mass = " + str(TR1/TR2))
       print("\n Using Simpson, the centre of mass = " + str(SMP1/SMP2))
```

```
linear mass density = T = x^2
        Centre of mass = integral(xT) dx / integral(T) dx
         Using Mid-point, the centre of mass = 1.5000030206786539
         Using Trapezoidal, the centre of mass = 1.4999969945303646
         Using Simpson, the centre of mass = 1.5
In [ ]:
```