





PyBOP: A Python package for battery model optimisation and parameterisation

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Summary

The Python Battery Optimisation and Parameterisation (PyBOP) package provides a set of methods for the parameterisation and optimisation of battery models, offering both Bayesian and frequentist approaches with example workflows to assist the user. PyBOP can be used for parameter identification of various models, including the electrochemical and equivalent circuit models provided by the popular open-source package PyBaMM ([Sulzer et al., 2021](#)). Similarly, PyBOP can be used for design optimisation under user-defined operating conditions for a given parameter. PyBOP allows the user to parameterise battery models using a variety of methods and provides diagnostics on the performance and convergence of the optimisation. The identified parameters can be used for prediction, on-line control and design optimisation, all of which support improved battery utilisation and development.

Statement of need

PyBOP is designed to provide a user-friendly, object-oriented interface for the optimisation of battery models which have been implemented in existing battery modelling software, e.g. PyBaMM ([Sulzer et al., 2021](#)). PyBOP is intended to serve a broad audience of students, engineers, and researchers in both academia and the battery industry. PyBOP prioritises clear and informative diagnostics and workflows for both new and experienced users, while also leveraging advanced optimisation algorithms provided by SciPy ([Virtanen et al., 2020](#)), PINTS ([Clerx et al., 2019](#)), and internal implementations such as the adaptive moment estimation with weight decay (AdamW), as well as Cuckoo search.

PyBOP supports the Battery Parameter eXchange (BPX) standard ([Korotkin et al., 2023](#)) for sharing battery parameter sets. These parameter sets are costly to obtain due to a number of factors: the equipment and time spent on characterisation experiments, the requirement of battery domain knowledge, and the computational cost of parameter estimation. PyBOP reduces the barrier to entry and ongoing costs by providing an accessible workflows that efficiently connects battery models with numerical optimisers, as well as explanatory examples of battery parameterisation and design optimisation.

This package complements other tools in the field of lithium-ion battery modelling built around PyBaMM, such as `liionpack` for simulating battery packs ([Tranter et al., 2022](#)) as the identified parameters are easily exportable from PyBOP into packages aimed at predictive forward modelling.

39 Architecture

40 PyBOP is a Python package packaged through PyPI, which currently supports Python versions
41 3.9 — 3.12. The package composes the popular battery modelling package PyBaMM for forward
42 modelling, while providing classes for parameterisation and optimisation. As shown in Figure 1,
43 PyBOP composes the battery modelling package PyBaMM, enabling a consistent interface and
44 robust objection construction process. With the forward model interface construction for
45 parameter identification and optimisation, PyBOP provides statistical methods and optimisation
46 algorithms to interface cleanly with the forward model predictions. Furthermore, identifiability
47 metrics are provided for the estimated parameters through Hessian approximation of the
48 cost/likelihood functions in the frequentist workflows and posterior moments in the Bayesian
49 workflows.

PyBOP's interface to supporting funding agencies, alongside a visualisation of the general
workflow for parameterisation and optimisation

Figure 1: PyBOP's interface to supporting funding agencies, alongside a visualisation of the general workflow for parameterisation and optimisation

50 PyBOP formulates the optimisation workflow through four main classes, namely the model,
51 problem, cost, and optimiser or sampler, as shown in Figure 2. Each of these objects
52 represent a base class with children classes constructing differing functionality for specialised
53 parameterisation or optimisation workflows. For example, the model class offers children classes
54 for differing physics-based battery models, as well as emperical models. This allows for the
55 underlying PyBaMM model to be constructed and validated for the different requirements between
56 the physics-based models and the emperical. For a given set of model equations provided
57 from PyBaMM, initial conditions, spatially discretisation, and numerical solver initialisation is
58 completed. By composing PyBaMM models directly into PyBOP, the underlying model structure
59 can be modified, and optimally constructed for the optimisation tasks. One such example of
60 this, is the spatially rediscretiation that is performed with geometric parameters are optimised.
61 In this situation, PyBOP aims to minimally reconstruct the PyBaMM model while maintaining the
62 problem, cost, and optimisation objects, providing improved performance benefits to end-users.
63 In the typical optimisation workflow, the classes in Figure 2 are constructed in sequence.

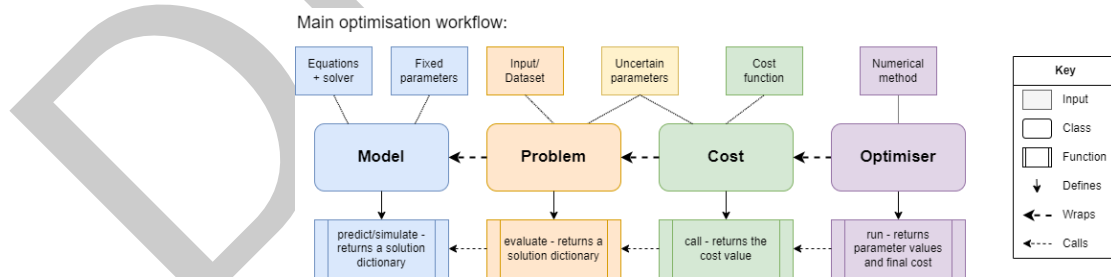


Figure 2: The core PyBOP architecture, showcasing the base class interfaces. Each class provide direct mapping to a classical step in the optimisation workflow.

64 The currently implemented subclasses for the model, problem, and cost classes are listed in
65 Table 1. From this point onwards, the parameterisation and optimisation tasks will simply be
66 referred to as an optimisation task. This simplification can be justified by inspecting Equation 4
67 and Equation 5 and confirming parameterisation can be viewed as an minimising optimisation
68 task for a distance-based cost function.

Table 1: List of available model, problem and cost classes.

Battery Models	Problem Types	Cost / Likelihood Functions
Single particle model (SPM)	Fitting problem	Sum of squared error
SPM with electrolyte (SPMe)	Design problem	Root mean squared error
Doyle-Fuller-Newman (DFN)	Observer	Gaussian log likelihood
Many particle model (MPM)		Maximum a posteriori
Multi-species multi-reaction (MSMR)		Unscented Kalman filter
Weppner Huggins		Gravimetric energy density
Equivalent circuit model (ECM)		Volumetric energy density

Likewise, the current optimisation algorithms available for usage in optimisation tasks in presented in Table 2. The cost functions in Table 1 are grouped by problem type, while the model and optimiser classes can be selected in combination with any problem-cost pair.

Table 2: List of available optimisers. (*) Scipy Minimize provides gradient and non-gradient methods.

Gradient-based	Non-gradient-based
Adaptive moment estimation with weight decay (AdamW)	Covariance matrix adaptation evolution strategy (CMA-ES)
Improved resilient backpropagation (iRProp-)	Exponential natural evolution strategy (xNES)
Gradient descent	Separable natural evolution strategy (sNES)
SciPy minimize (*)	Particle swarm optimization (PSO)
	SciPy differential evolution
	Nelder-Mead
	Cuckoo search

As previously discussed, PyBOP offers Bayesian inference methods such as Maximum a Posteriori (MAP) presented alongside the frequentist methods in Table 2. A full Bayesian framework is available from a Markov-chain Monte Carlo implemented within PyBOP, capable of providing uncertainty on the inferred parameters. These samplers are currently composed within PyBOP from the Pints' library, with a base class implemented for interoperability and direct application to the PyBOP model, problem, and likelihood classes. The currently support MCMC samplers is shown in Table 3.

Table 3: List of available Monte Carlo samplers.

Gradient-based	Non-gradient-based
Adaptive Moment Estimation with Weight Decay (AdamW)	Covariance Matrix Adaptation Evolution Strategy (CMA-ES)
Improved Resilient Backpropagation (iRProp-)	Exponential Natural Evolution Strategy (xNES)
Gradient Descent	Separable Natural Evolution Strategy (sNES)
SciPy Minimize (*)	Particle Swarm Optimization (PSO)
	SciPy Differential Evolution
	Nelder-Mead
	Cuckoo Search

- Performance (multiprocessing)
- Construction of PyBaMM models (geometric and non-geometric identification)
- Feasability checks on identified parameters

- 82 ▪ Spatial identification methods?
- 83 ▪ Documentation supported at X
- 84 ▪ Benchmarks provided at X
- 85 ▪ Plotting available via Plotly (cost landscapes, gradient landscapes)
- 86 ▪ Test suite provided by pytest (~98% coverage)
- 87 ▪ Standalone implementations (Bring your own model)

88 Background

89 Battery models

90 In general, battery models can be written in the form of a differential-algebraic system of
91 equations:

$$\frac{dx}{dt} = f(t, x, y, u(t), \theta), \quad (1)$$

$$y(t) = g(t, x, y, u(t), \theta), \quad (2)$$

93 with initial conditions

$$x(0) = x_0(\theta). \quad (3)$$

94 Here, t is time, $x(t)$ are the spatially (discretised) states, $y(t)$ are the outputs (for example
95 the terminal voltage), $u(t)$ are the inputs (e.g. the applied current) and θ are the unknown
96 parameters.

97 Common battery models include various types of equivalent circuit model (e.g. the Thévenin
98 model), the Doyle–Fuller–Newman (DFN) model (Doyle et al., 1993; Fuller et al., 1994)
99 based on porous electrode theory and its reduced-order variants including the single particle
100 model (SPM) (Planella et al., 2022), as well as the multi-scale, multi-reaction (MSMR) model
101 (Verbrugge et al., 2017).

102 Simplified models that retain good prediction capabilities at a lower computational cost are
103 widely used, for example within battery management systems, while physics-based models are
104 required to understand the impact of design parameters on battery performance.

105 Examples

106 Parameterisation

107 Battery model parameterisation is difficult due to the high ratio of the number of parameters
108 to measurable outputs (Andersson et al., 2022; Miguel et al., 2021; Wang et al., 2022). A
109 complete parameterisation often requires a step-by-step identification of smaller groups of
110 parameters from a variety of different datasets (Chen et al., 2020; Chu et al., 2019; Kirk et al.,
111 2023).

112 A generic data fitting optimisation problem may be formulated as:

$$\min_{\theta} \mathcal{L}_{(y_i)}(\theta) \quad \text{subject to equations (1)-(3)} \quad (4)$$

113 in which $\mathcal{L} : \theta \mapsto [0, \infty)$ is a cost (or likelihood) function that quantifies the agreement
114 between the model and a sequence of data points (y_i) measured at times t_i . For gradient-based
115 optimisers, the Jacobian of the cost function with respect to the unknown parameters, $(\frac{\partial \mathcal{L}}{\partial \theta})$ is
116 used as a directional metric for the algorithm when exploring the parameter space.

117 By way of example, we next demonstrate the fitting of some synthetic data for which we know
118 the true parameter values.

Design optimisation

Design optimisation is supported within PyBOP to guide future development of the battery design by identifying parameter variations which may unlock improvements in battery performance. This optimisation task can be viewed similarly to the parameterisation workflows described above, however, with the aim of increasing the distance metric instead of minimising it. In the case of design optimisation for maximising gravimetric energy density, PyBOP minimises the negative of the cost function, where the cost metric is no longer a distance between two time-series vectors, instead it is the integrated energy from the vector normalised with the corresponding cell mass. This is typically quantified for operational conditions such as a 1C (the applied current required to discharge the cell in one hour) capacity.

Design optimisation can be written in the form of a constrained optimisation problem as:

$$\min_{\theta \in \Omega} \mathcal{L}(\theta) \quad \text{subject to equations (1)-(3)} \quad (5)$$

in which $\mathcal{L} : \theta \mapsto [0, \infty)$ is a cost function that quantifies the desirability of the design and Ω is the set of allowable parameter values.

As an example, let us consider the target of maximising gravimetric energy density subject to constraints on the geometric electrode parameters (Couto et al., 2023).

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References

- Andersson, M., Streb, M., Ko, J. Y., Löfqvist Klass, V., Klett, M., Ekström, H., Johansson, M., & Lindbergh, G. (2022). Parametrization of physics-based battery models from input-output data: A review of methodology and current research. *Journal of Power Sources*, 521(November 2021), 230859. <https://doi.org/10.1016/j.jpowsour.2021.230859>
- Chen, C.-H., Brosa Planella, F., O'Regan, K., Gastol, D., Widanage, W. D., & Kendrick, E. (2020). Development of experimental techniques for parameterization of multi-scale lithium-ion battery models. *Journal of The Electrochemical Society*, 167(8), 080534. <https://doi.org/10.1149/1945-7111/ab9050>
- Chu, Z., Plett, G. L., Trimboli, M. S., & Ouyang, M. (2019). A control-oriented electrochemical model for lithium-ion battery, Part I: Lumped-parameter reduced-order model with constant phase element. *Journal of Energy Storage*, 25(August), 100828. <https://doi.org/10.1016/j.est.2019.100828>
- Clerx, M., Robinson, M., Lambert, B., Lei, C. L., Ghosh, S., Mirams, G. R., & Gavaghan, D. J. (2019). Probabilistic inference on noisy time series (PINTS). *Journal of Open Research Software*, 7(1), 23. <https://doi.org/10.5334/jors.252>
- Couto, L. D., Charkhgard, M., Karaman, B., Job, N., & Kinnaert, M. (2023). Lithium-ion battery design optimization based on a dimensionless reduced-order electrochemical model. *Energy*, 263(PE), 125966. <https://doi.org/10.1016/j.energy.2022.125966>
- Doyle, M., Fuller, T. F., & Newman, J. (1993). Modeling of Galvanostatic Charge and Discharge of the Lithium/Polymer/Insertion Cell. *Journal of The Electrochemical Society*, 140(6), 1526–1533. <https://doi.org/10.1149/1.2221597>

- Fuller, T. F., Doyle, M., & Newman, J. (1994). Simulation and optimization of the dual lithium ion insertion cell. *Journal of The Electrochemical Society*, 141(1), 1. <https://doi.org/10.1149/1.2054684>
- Kirk, T. L., Lewis-Douglas, A., Howey, D., Please, C. P., & Jon Chapman, S. (2023). Nonlinear electrochemical impedance spectroscopy for lithium-ion battery model parameterization. *Journal of The Electrochemical Society*, 170(1), 010514. <https://doi.org/10.1149/1945-7111/acada7>
- Korotkin, I., Timms, R., Foster, J. F., Dickinson, E., & Robinson, M. (2023). Battery parameter eXchange. In *GitHub repository*. The Faraday Institution. <https://github.com/FaradayInstitution/BPX>
- Miguel, E., Plett, G. L., Trimboli, M. S., Oca, L., Iraola, U., & Bekaert, E. (2021). Review of computational parameter estimation methods for electrochemical models. *Journal of Energy Storage*, 44(PB), 103388. <https://doi.org/10.1016/j.est.2021.103388>
- Planella, F. B., Ai, W., Boyce, A. M., Ghosh, A., Korotkin, I., Sahu, S., Sulzer, V., Timms, R., Tranter, T. G., Zyskin, M., Cooper, S. J., Edge, J. S., Foster, J. M., Marinescu, M., Wu, B., & Richardson, G. (2022). A Continuum of Physics-Based Lithium-Ion Battery Models Reviewed. *Progress in Energy*, 4(4), 042003. <https://doi.org/10.1088/2516-1083/ac7d31>
- Sulzer, V., Marquis, S. G., Timms, R., Robinson, M., & Chapman, S. J. (2021). Python Battery Mathematical Modelling (PyBaMM). *Journal of Open Research Software*, 9(1), 14. <https://doi.org/10.5334/jors.309>
- Tranter, T. G., Timms, R., Sulzer, V., Planella, F. B., Wiggins, G. M., Karra, S. V., Agarwal, P., Chopra, S., Allu, S., Shearing, P. R., & Brett, D. J. I. (2022). Liionpack: A python package for simulating packs of batteries with PyBaMM. *Journal of Open Source Software*, 7(70), 4051. <https://doi.org/10.21105/joss.04051>
- Verbrugge, M., Baker, D., Koch, B., Xiao, X., & Gu, W. (2017). Thermodynamic model for substitutional materials: Application to lithiated graphite, spinel manganese oxide, iron phosphate, and layered nickel-manganese-cobalt oxide. *Journal of The Electrochemical Society*, 164(11), E3243. <https://doi.org/10.1149/2.0341708jes>
- Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., Burovski, E., Peterson, P., Weckesser, W., Bright, J., van der Walt, S. J., Brett, M., Wilson, J., Millman, K. J., Mayorov, N., Nelson, A. R. J., Jones, E., Kern, R., Larson, E., ... SciPy 1.0 Contributors. (2020). SciPy 1.0: Fundamental Algorithms for Scientific Computing in Python. *Nature Methods*, 17, 261–272. <https://doi.org/10.1038/s41592-019-0686-2>
- Wang, A. A., O’Kane, S. E. J., Brosa Planella, F., Houx, J. L., O’Regan, K., Zyskin, M., Edge, J., Monroe, C. W., Cooper, S. J., Howey, D. A., Kendrick, E., & Foster, J. M. (2022). Review of parameterisation and a novel database (LiionDB) for continuum Li-ion battery models. *Progress in Energy*, 4(3), 032004. <https://doi.org/10.1088/2516-1083/ac692c>