

# Reducing Energy Bloat in Large Model Training

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## Abstract

Training large AI models on numerous GPUs consumes a massive amount of energy, making power delivery one of the largest limiting factors in building and operating datacenters for AI workloads. However, we observe that not all energy consumed during training directly contributes to end-to-end throughput; a significant portion can be removed without slowing down training. We call this portion *energy bloat*.

In this work, we identify two independent sources of energy bloat in large model training and propose *Perseus*, a training system that mitigates both. To do this, *Perseus* obtains the time-energy tradeoff frontier of a large model training job using an efficient graph cut-based algorithm, and schedules computation energy consumption across time to reduce both types of energy bloat. Evaluation on large models, including GPT-3 and Bloom, shows that *Perseus* reduces the energy consumption of large model training by up to 30% without any throughput loss or hardware modification.<sup>1</sup>

**CCS Concepts:** • Computer systems organization; • Computing methodologies → Machine learning; • Software and its engineering → Power management;

**Keywords:** Energy-efficiency, datacenter power management, straggler, distributed training, large model training

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## 1 Introduction

As deep neural networks (DNNs) continue to grow in model and dataset size [32, 40], the energy consumption of large

model training is increasing as well. For instance, training GPT-3 [8] reportedly consumed 1.3 GWh [63]. Then, this was dwarfed by Amazon’s training of a 200B model, which consumed about 11.9 GWh [29]—enough to power more than 1,000 average US households for a year [2]. Such energy-intensive large model training not only inflates datacenter operational expenses, but also made power delivery a primary challenge in building datacenters today [9, 11, 12, 52, 53].

Despite recent works on accelerating large model training [45, 57, 90], energy optimization remains an open challenge [63, 68]. While energy optimization is well-studied in the hardware community [7, 14, 75, 84], the power bottleneck of recent datacenters [9, 11, 12, 53, 65] shows that efficiency gains from hardware advancement alone are not sufficient to sustain the growing demand for AI compute. In light of this, recent works show that software can play a significant role in energy optimization by capturing application characteristics that general-purpose hardware cannot (e.g., no need to finish computation before the deadline), bringing hardware-agnostic energy-efficiency gains [15, 17, 78, 85, 86].

In this paper, we seek a software method that reduces the energy consumption of large model training without slowdown, thereby also reducing average power draw. To that end, we identify *energy bloat*, the portion of energy consumption that can be removed without slowdown in software systems for large model training. We find two independent sources of energy bloat—*intrinsic* and *extrinsic*—and propose a single optimization framework that minimizes both.

*Intrinsic* energy bloat comes from computation imbalance when a large model is distributed across multiple GPUs with pipeline parallelism (§2.2). Balancing the amount of computation in each pipeline stage is an important problem for distributed execution planning [23, 30, 55, 90], but perfectly balancing every stage is not always possible because layers in a DNN are coarse-grained tensor operations with varying amounts of computation. When stages have unequal computation times, those not on the *critical path* of computation run needlessly fast—that is, they consume energy that does not contribute to the overall training throughput. Such *intrinsic* energy bloat opens up the opportunity to *precisely* slow down each non-critical computation in the pipeline such that the length of the critical path does not change.

*Extrinsic* energy bloat, in contrast, arises when multiple pipelines run in parallel in a synchronous fashion, and one or more pipelines run slower than the rest (§2.3). Root causes behind such slowdowns are varied, including power/thermal throttling [47, 61, 62, 67, 93], I/O bottlenecks in the storage/network [54, 83, 89], and hardware/software failures [25,

<sup>1</sup>*Perseus* is open-source as part of Zeus [86] at <https://ml.energy/zeus>.

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37, 76], and the likelihood of their presence increases with the scale and duration of training [28, 38, 79]. All pipelines running faster than the *straggler pipeline* are needlessly fast, wasting energy that does not affect the overall training throughput. Thus, we can slow down entire pipelines without delaying gradient synchronization.

In this work, we propose *Perseus*, which formulates a unified optimization framework to remove both intrinsic and extrinsic energy bloat from large model training (§3). At its core, Perseus efficiently pre-characterizes the entire time-energy tradeoff frontier of a training iteration, allowing it to minimize intrinsic bloat under normal operation and to mitigate extrinsic bloat arising from stragglers. Existing works fall short on both fronts. EnvPipe [15] is limited to intrinsic bloat reduction with a point solution that leads to suboptimal energy reduction. Zeus [86], in contrast, ignores intrinsic bloat as it only considers single-GPU training, which also renders its time-energy frontier suboptimal for large models.

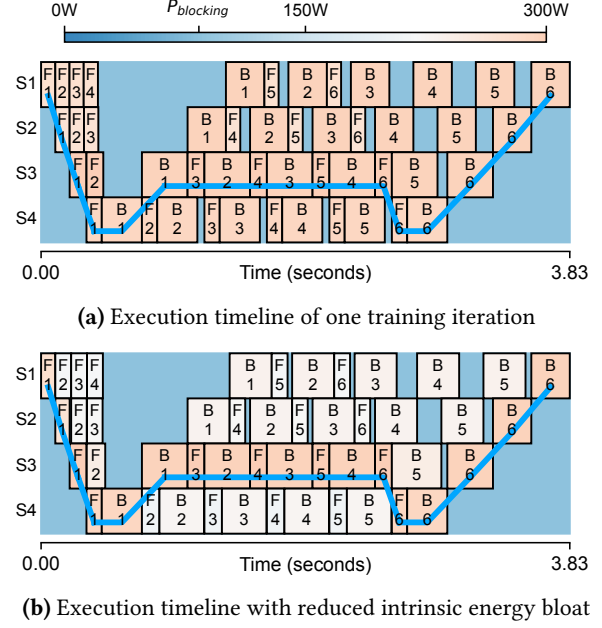
We show that characterizing the optimal time-energy Pareto frontier is NP-hard not only to solve, but also to approximate within any constant factor. Given this impasse, we propose an efficient algorithm that optimally solves a relaxed problem instead (§4). To do so, Perseus represents one training iteration as a directed acyclic graph (DAG) of forward and backward computations in each pipeline stage. Then, Perseus efficiently generates all energy schedules, defined as the planned time and energy consumption of each computation, that are on the time-energy frontier using a graph cut-based algorithm that iteratively *crawls up* the frontier from the bottom. Minimizing intrinsic and/or extrinsic energy bloat is then as simple as choosing the appropriate energy schedule from the pre-characterized time-energy frontier.

Perseus consists of a *client library* and a *server* (§5). The client library integrates with a large model training framework and accelerator to measure computation energy consumption and control accelerator speed. The server produces optimized energy schedules, using the abstract computation DAG and time/energy measurements provided by the client.

Evaluation on large models (GPT-3 [8], BERT [19], T5 [66], Bloom [82], and a scaled-up version of Wide-ResNet [87]), shows that Perseus is able to reduce per-iteration energy consumption by up to 30% with negligible or no slowdown, reducing energy consumption and average power draw (§6).

Overall, we make the following contributions in this paper:

- We identify intrinsic and extrinsic energy bloat in large model training, fundamentally caused by computation time imbalance at different levels.
- We propose Perseus, a software-only energy optimization system that reduces energy bloat through a unified optimization framework and a graph cut-based algorithm.
- We evaluate Perseus on a diverse set of large model workloads and show that it significantly reduces energy bloat, bringing hardware-agnostic energy savings.



**Figure 1.** One training iteration of GPT-3 1.3B with 4 pipeline stages and 6 microbatches on NVIDIA A100 GPUs, drawn to scale. For example, F5 and B5 in the S2 row denote forward and backward for the fifth microbatch on Stage 2. The critical path is traced with a blue line. Colors show power consumption. Other models are visualized in Appendix A.

## 2 Motivation

First, we provide necessary background regarding large model training (§2.1). Then, we introduce intrinsic (§2.2) and extrinsic (§2.3) energy bloat present in large model training, and discuss opportunities for energy reduction (§2.4).

### 2.1 Large Model Training

Large model training is mostly dominated by 3D (data, tensor, and pipeline) parallelism [5, 45, 57, 72, 82]. Especially, pipeline parallelism partitions a large model into multiple *stages* and its training batch into *microbatches*, and pipelines forward and backward computations through the stages. Then, such pipelines are replicated to perform data parallel training. Pipelines can only move on to the next iteration after every pipeline has finished and synchronized gradients.

### 2.2 Intrinsic Energy Bloat

We profile GPT-3 1.3B on NVIDIA A100 GPUs and visualize the timeline of one training iteration in Figure 1a. In addition to the familiar bubbles in the 1F1B schedule [57], we observe *gaps* between forward and backward computations, where the GPU is simply blocking on communication with an adjacent stage. Such gaps exist because the computation time of each pipeline stage is not perfectly balanced. Partitioning stages in a balanced manner is an important problem in

Model	# Parameters	Imbalance Ratio	
		4 stages	8 stages
GPT-3 [8]	3B	1.13	1.25
	7B	1.11	1.23
	13B	1.08	1.17
	175B	1.02	1.03
Bloom [82]	3B	1.13	1.25
	7B	1.13	1.25
	176B	1.05	1.10
BERT [19]	0.1B	1.33	2.00
	0.3B	1.17	1.33
T5 [66]	0.2B	1.19	1.50
	0.7B	1.05	1.11
	2.9B	1.06	1.16
Wide-ResNet50 [87]	0.8B	1.23	1.46
Wide-ResNet101 [87]	1.5B	1.09	1.25

**Table 1.** Forward latency ratio of the longest to the shortest stage on A100 GPUs. 1.00 would mean perfect balance.

distributed execution planning [23, 34, 55, 90], but *perfect* balancing is difficult because DNNs are essentially a sequence of coarse-grained tensor operations with varying sizes.

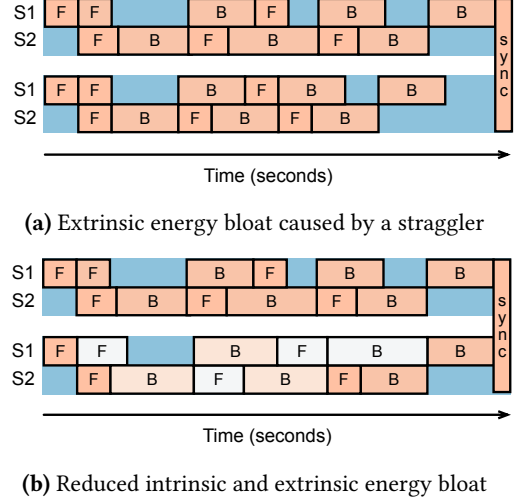
To understand the amount of possible pipeline stage imbalance, we exhaustively searched for the pipeline partition with the smallest imbalance ratio, defined as the ratio of the longest stage forward computation latency to the shortest.<sup>2</sup> Table 1 lists the minimum imbalance ratio for various models, which shows that perfect balance is difficult to achieve. See Appendix B for partitioning details and sources of imbalance.

Given stage imbalance, not all forward and backward computations are on the *critical path* of computation (Figure 1a). This means that non-critical computations running at their maximum speed are not contributing to faster iteration time, and thus simply wasting energy. We call this *intrinsic energy bloat*, which can be reduced by precisely slowing down each non-critical computation without lengthening the critical path (Figure 1b). Although seemingly simple, this problem is not only NP-hard to solve, but also NP-hard to even *approximate* to any constant factor [74].

### 2.3 Extrinsic Energy Bloat

Numerous replicas of the same pipeline run in a data parallel fashion in large model training. Because every pipeline must synchronize gradients at the end, if one pipeline runs slower, *all other* pipelines must wait until the straggler pipeline finishes (Figure 2a). Since the straggler pipeline determines end-to-end iteration time, all other pipelines running at their fastest possible iteration time are wasteful. We call this *extrinsic energy bloat*, because unlike intrinsic energy bloat, its cause is *extrinsic* to the training pipeline. To reduce extrinsic

<sup>2</sup>For Transformer-based models, we partition at the granularity of Transformer layers. For Wide-ResNet, we partition at the granularity of bottleneck layers, which are three convolution layers wrapped with a skip connection.



**Figure 2.** Among two data parallel pipelines, the first one becomes a straggler. The non-straggler pipeline causes extrinsic energy bloat by running as fast as possible (a), which can be reduced by precisely slowing it down (b).

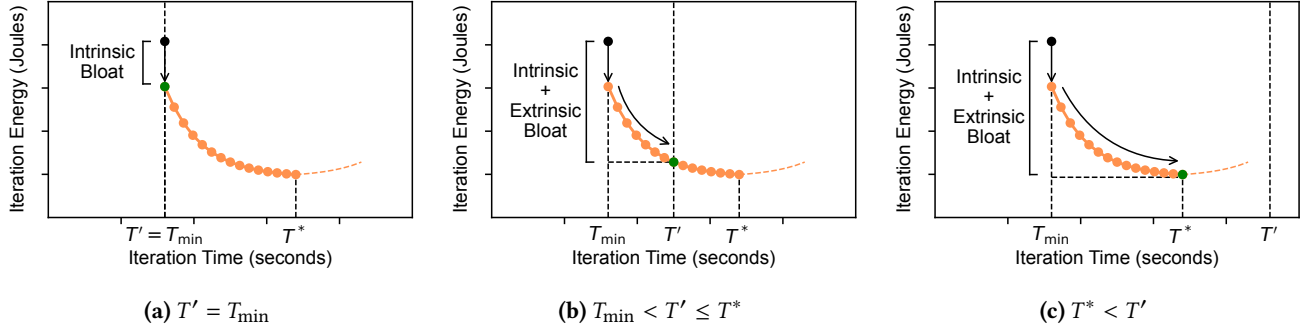
bloat while keeping intrinsic bloat low, one can determine the energy-optimal iteration time for non-straggler pipelines and precisely slow down computations so that non-straggler pipelines attain that iteration time (Figure 2b).

Stragglers arise from numerous sources. Thermal or power throttling in a datacenter can result in 10–50% slowdown [47, 61, 62, 67, 93], and I/O bottlenecks in the storage or network can be longer than GPU computation by up to 4× [54, 83, 89], acting like a persistent straggler pipeline. Recent failure-resilient training frameworks [25, 37, 76] deploy *heterogeneous* pipelines, introducing non-uniform iteration times. With increasing job and infrastructure scale, the probability of encountering stragglers increases [28, 38, 39, 79, 92].

In this work, we focus on stragglers that are known to and anticipated by the training infrastructure, generally because they were created by the infrastructure itself (e.g., power and thermal throttling, non-compute bottlenecks, fault-tolerant planning). Such stragglers also tend to persist beyond typical training iteration times. Therefore, Perseus focuses on planning time and energy consumption across time and allowing quick adaptation, assuming that information about stragglers is available.

### 2.4 Potential Benefits of Reducing Energy Bloat

To gauge potential energy savings, we measure the energy savings achieved by slowing down *every* computation in the pipeline to their minimum-energy frequencies. This will slow down iteration time, but can act as an upper bound for energy savings. For our workloads in Section 6.2, this gives on average 16% and 27% energy reduction on A100 and A40 GPUs, respectively. Section 6.2 shows that Perseus can realize most of the potential savings with negligible slowdown.



**Figure 3.** Three cases showing where the straggler pipeline’s iteration time  $T'$  can be.  $T_{\min}$  and  $T^*$  are the shortest and longest iteration times on the time–energy frontier. The black dot is when all computations run at the maximum speed, which wastes energy. The green dot is the energy-optimal iteration time of the non-straggler pipeline. Solid orange dots make up the frontier, and the orange dotted line shows that iteration energy increases beyond  $T^*$ .

### 3 Perseus Overview

We first present Perseus’s unified optimization framework that aims to remove both types of energy bloat (§3.1), and then walk through the workflow of Perseus (§3.2).

#### 3.1 Unified Optimization Framework

Intuitively, slowing down computations selectively in a training pipeline without affecting its critical path will keep the same iteration time while reducing its energy consumption (§2.2). Furthermore, when stragglers emerge, slowing down computations in a non-straggler pipeline without making it a straggler itself will reduce energy consumption even more (§2.3). We formalize these two intuitions into a unified optimization framework and derive a universal prescription for a non-straggler pipeline’s *energy-optimal* iteration time.

Our goal is to minimize a pipeline’s energy consumption by controlling the execution speed of each computation in the pipeline. In doing so, we can slow down a pipeline’s iteration time up to the straggler’s iteration time  $T'$ :

$$\begin{aligned} \min_F \quad & \text{Energy}(F) \\ \text{s.t.} \quad & \text{Time}(F) \leq T' \end{aligned} \quad (1)$$

where  $F$  is an assignment of GPU frequencies<sup>3</sup> to each forward and backward computation in the pipeline, and  $\text{Time}(F)$  and  $\text{Energy}(F)$  are the iteration time and energy consumption of the pipeline when executed with  $F$ , respectively. Changing  $F$  will lead to different values of  $\text{Time}(F)$  and  $\text{Energy}(F)$ , but we are only interested in  $(\text{Time}(F), \text{Energy}(F))$  points that are on the time–energy tradeoff frontier.

Now, let us assume we have a fully characterized time–energy frontier, bookended by  $T_{\min}$  and  $T^*$  (Section 4 is dedicated to describing how).  $T_{\min}$  is the shortest iteration time on the frontier, which is the same as the iteration time of

running every computation at the maximum speed, and  $T^*$  is the iteration time with minimum energy consumption, which is when each computation runs at the frequency that consumes the least amount of energy for that computation.<sup>4</sup> Figure 3 shows the three possible cases regarding where the straggler’s iteration time  $T'$  can be:

- Figure 3a: When there are no stragglers, we simply select the point on the frontier with iteration time  $T_{\min}$ , which reduces *only intrinsic energy bloat*.
- Figure 3b: When a moderately slow straggler is detected, we *additionally reduce extrinsic energy bloat while keeping intrinsic bloat low* by slowing down all non-straggler pipelines until  $T'$ , using up all the slack time.
- Figure 3c: Finally, the straggler’s iteration time may go beyond the minimum-energy point  $T^*$  on the frontier. In this case, we only slow down non-stragglers until  $T^*$ , because going past  $T^*$  will instead *increase* energy.

The three cases can be merged into one universal prescription for the pipeline’s energy-optimal iteration time:

$$T_{\text{opt}} = \min(T^*, T'). \quad (2)$$

Therefore, when a straggler emerges (i.e.,  $T_{\min} < T'$ ), Perseus can compute  $T_{\text{opt}}$  using Equation 2 and quickly look up the frequency plan  $F_{\text{opt}}$  that leads to iteration time  $T_{\text{opt}}$  using the pre-characterized time–energy frontier.

Finally, we note that, unlike other problem settings that do not consider energy consumption, fully utilizing all the slack time created by the straggler is *not always energy-optimal*; being too fast or too slow can both waste energy.

#### 3.2 Perseus Architecture

**Energy Schedule.** Perseus represents each iteration of the training pipeline as a static directed acyclic graph (DAG), where nodes are forward and backward computations in

<sup>3</sup>The SM frequency of NVIDIA GPUs can be set via NVML [4] in around 10 ms, which is much shorter than typical large model computation latencies. Locking the GPU’s frequency provides deterministic computation latency [4, 27], making it suitable for tightly planning and packing execution over time.

<sup>4</sup>This is typically not the lowest frequency, because computations running with very low frequencies incur more latency increase than power reduction, resulting in *higher* energy consumption.



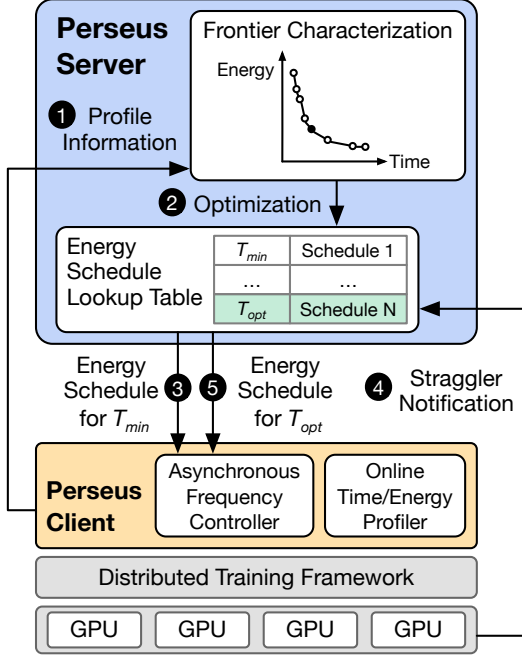


Figure 4. Perseus architecture and workflow.

each stage and edges are dependencies between computations. Each node on the computation DAG is annotated with its planned time and energy consumption, which we call the *energy schedule*. Perseus realizes an energy schedule by executing each computation with a specific GPU frequency.

**System Components.** Perseus’s architecture is shown in Figure 4. Perseus consists of a framework- and accelerator-agnostic server and a framework-integrated and accelerator-specific client. The server is a cluster-wide singleton. For various training jobs, the server pre-characterizes the time-energy frontier of one iteration (§4) and caches energy schedules for fast lookup. The client profiles pipeline computations online during training and realizes energy schedules by setting the GPU’s frequency during runtime (§5).

**Training Lifecycle.** For the Perseus server, a training job is primarily specified by its computation DAG for one training iteration. When the job begins execution, ① the Perseus client invokes its online time-energy profiler (§5) to measure the time and energy of each forward and backward computation on each supported frequency. Profiling is done *in vivo* during the initial tens of training iterations.

Upon receiving profiling results, ② the server begins *asynchronously* characterizing the time-energy frontier (§4) while training continues. When characterization finishes, energy schedules on the frontier are saved in a lookup table indexed by  $T'$ . Then, ③ the energy schedule corresponding to  $T_{\min}$  is deployed to the client. Energy schedules are realized by the client’s asynchronous frequency controller, integrated into the training framework (§5).

During training, ④ the training infrastructure (e.g., data-center rack power/temperature manager) notifies the Perseus server of a straggler and its degree of slowdown. The server then ⑤ quickly reacts to this by looking up the energy schedule corresponding to the anticipated straggler iteration time (the one with iteration time  $T_{\text{opt}}$ ), and deploys it to the client.

## 4 Characterizing the Time-Energy Frontier

In this section, we describe our algorithm to efficiently obtain the time-energy tradeoff frontier for a training pipeline in detail. We first formulate the problem, show that it is NP-hard, and describe a relaxed version (§4.1). Then, we provide an overview of our algorithm (§4.2) and describe the core subroutine in our algorithm (§4.3). Finally, we extend our algorithm to support 3D/hybrid parallelism, constant-time operations, and diverse pipeline schedules (§4.4).

### 4.1 Problem Formulation

**Expression for Energy Consumption.** The energy consumption of a pipeline is not only from computation; it is the sum of three parts: (1) Computation; (2) Blocking on communication between computations; and (3) Blocking on communication until the straggler pipeline finishes:

$$\begin{aligned} & \sum_i e_i(f_i) + P_{\text{blocking}}(N \cdot T - \sum_i t_i(f_i)) + P_{\text{blocking}} \cdot N \cdot (T' - T) \\ &= \underbrace{\sum_i (e_i(f_i) - P_{\text{blocking}} \cdot t_i(f_i))}_{\text{①}} + \underbrace{P_{\text{blocking}} \cdot N \cdot T'}_{\text{②}} \end{aligned} \quad (3)$$

where  $P_{\text{blocking}}$  is the power consumption of the GPU when it is blocking on communication,  $N$  is the number of pipeline stages, and  $t_i(f_i)$  and  $e_i(f_i)$  are the time and energy consumption of computation  $i$  with frequency  $f_i$ , respectively.<sup>5</sup>

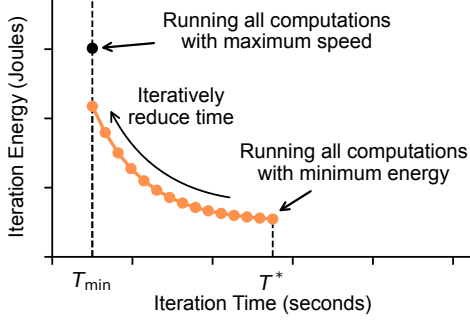
As derived in Section 3.1, given straggler iteration time  $T'$ , we draw a vertical line on the time-energy tradeoff frontier (Time( $F$ ) vs. ①+②) at  $T_{\text{opt}}$  and find  $F_{\text{opt}}$  where the two lines intersect. Equation 3 shows that the time-energy frontier of a pipeline depends on the straggler’s iteration time  $T'$  *only* in the second term ②, which is merely an *upward shift* of the frontier. Therefore, if we characterize the tradeoff frontier of Time( $F$ ) vs. ①, that frontier can be used to find  $T_{\text{opt}}$  and  $F_{\text{opt}}$  for any straggler iteration time  $T'$ . Thus, we define

$$\text{Energy}(F) = \sum_i (e_i(f_i) - P_{\text{blocking}} \cdot t_i(f_i)) \quad (4)$$

and characterize the frontier of Time( $F$ ) vs. Energy( $F$ ).

**Finding the Time-Energy Frontier.** Finding *one point* on the Pareto-optimal tradeoff frontier with iteration time  $T$  is

<sup>5</sup>An assumption here is that  $P_{\text{blocking}}$  is constant, as a GPU blocking on communication is busy-looping inside a NCCL kernel without heavy computation utilization.



**Figure 5.** Starting from the energy schedule that consumes the minimum energy, we iteratively reduce its iteration time to trace up and iteratively discover the tradeoff frontier.

equivalent to solving the following optimization problem:

$$\begin{aligned} \min_F \quad & \text{Energy}(F) \\ \text{s.t.} \quad & \text{Time}(F) \leq T \end{aligned} \quad (5)$$

We call this problem *Pipeline Energy Minimization* (PEM).

**Theorem 4.1.** *Pipeline Energy Minimization is NP-hard.*

*Proof.* Reduction from Knapsack. Details in Appendix C.  $\square$

The complete Pareto-optimal tradeoff frontier can be obtained by solving PEM for all  $T \in [T_{\min}, T^*]$ , which is clearly intractable. Therefore, we seek an appropriate relaxation of the problem that will yield a *nearly* Pareto-optimal frontier.

One of the reasons PEM is NP-hard is because it is a *discrete* optimization problem where the possible choices of computation time and energy are discrete, which is in turn because GPUs only support discrete frequencies (e.g., in 15 MHz steps and nothing in the middle). However, if frequency choices were *continuous*, the problem is exactly and efficiently solvable [70]. This is akin to integer linear programs becoming tractable when relaxed to linear programs.

The transform from the original problem to the relaxed version is done by fitting a *continuous* exponential function ( $a \cdot e^{bt} + c$ ) to Pareto-optimal computation time and energy measurements for each forward and backward computation. We choose the exponential function due to its inherent flexibility and natural fit to data (more details in Appendix D). We show in Section 6.2 that this relaxation produces high-quality approximate solutions that realize most of the opportunity for savings. Solving the relaxed problem returns the time and energy consumption planned for each computation in the pipeline, or the energy schedule. Then, this is transformed back to a feasible solution of the original problem, which is the set of GPU frequencies  $F$ .

## 4.2 Iteratively Discovering the Frontier

Now, we first describe our iterative strategy of characterizing the frontier, and dive deeper into one iteration in Section 4.3.

Although our relaxed problem is no longer NP-hard, solving it for each  $T' \in [T_{\min}, T^*]$  from scratch is inefficient.

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**Input:** DAG  $\mathcal{G}$  of computations  $i \in \mathcal{G}$

Amount of time to reduce in one iteration  $\tau$

Iteration time with all max frequencies  $T_{\min}$

**Output:** Set of optimized schedules  $\mathcal{S}$

---

► Begin with the minimum energy schedule

```

1  $s \leftarrow$  Minimum energy for all computations
2  $\mathcal{S} \leftarrow \{s\}$ 
3 while IterationTime( $\mathcal{G}, s$ ) >  $T_{\min}$  do
   ► Reduce time by  $\tau$  with minimal energy increase (§4.3)
4    $s \leftarrow$  GetNextSchedule( $\mathcal{G}, s, \tau$ )
5    $\mathcal{S} \leftarrow \mathcal{S} \cup \{s\}$ 
6 return  $\mathcal{S}$ 
```

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**Algorithm 1:** Iteratively discovering the frontier.

Instead, what if we can *tweak* an existing schedule already on the frontier to generate its *neighbor* energy schedule on the frontier? Then, we can start from one end of the frontier and trace along to the other end, discovering fine-grained optimized energy schedules.

Figure 5 visualizes our strategy. We start from the right-most point  $T^*$  that consumes the *minimum energy*, which is simply running every computation with the minimum energy.<sup>6</sup> This energy schedule is in fact Pareto-optimal because there are no other schedules that achieve the same energy with faster time. Then, we iteratively reduce iteration time by unit time  $\tau$  (e.g., 1 ms) while increasing total energy *minimally*, which gives us the neighbor energy schedule on the frontier.<sup>7</sup> This is repeated until iteration time reaches  $T_{\min}$ .

We note that tracing down from the energy schedule that consumes the maximum energy (i.e., Figure 5 black dot) would be incorrect. That schedule is far from optimized because, although it will execute with the least amount of time, stage imbalance leaves room for energy reduction (§2.2).

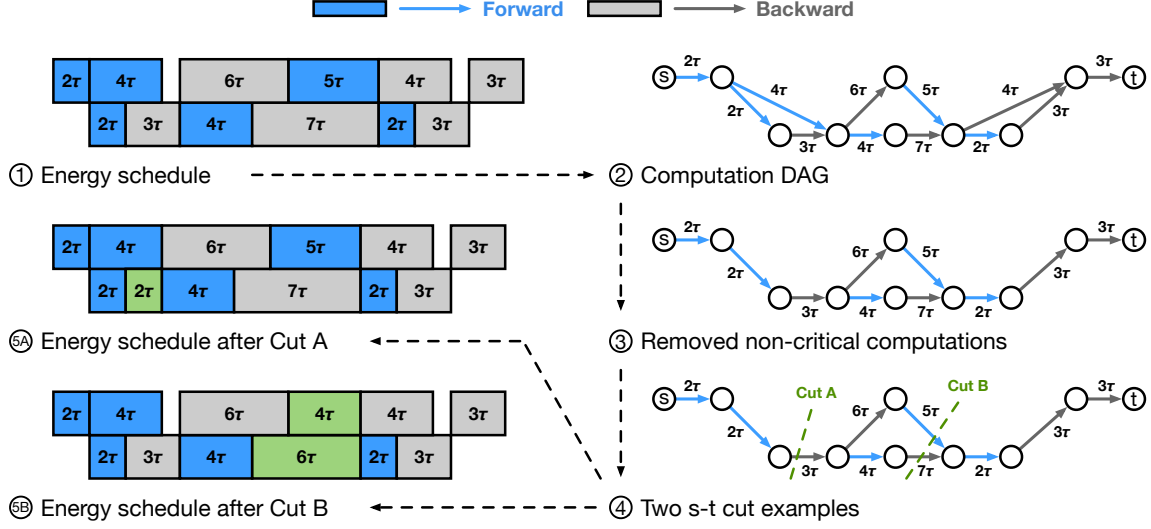
Algorithm 1 provides an overview of our optimization process. First, the energy schedule with the minimum energy consumption is constructed by planning every computation to run with minimum energy (line 1). Starting from there, the iteration time of the schedule is iteratively reduced by unit time  $\tau$  while incurring *minimal energy increase* (line 4; Section 4.3). This is repeated until the total iteration time of the schedule can no longer be reduced, and every energy schedule encountered in the process forms our frontier.

## 4.3 Finding the Neighbor Energy Schedule

In this section, we describe our core subroutine GetNextSchedule (Algorithm 1, line 4). Figure 6 provides visualizations of the process. The entire procedure is given in Algorithm 2.

<sup>6</sup>The minimum energy consumption for each computation type can be queried from the computation time/energy profiling information (§5).

<sup>7</sup> $\tau$  is the unit time parameter that trades off the running time of Perseus’s optimizer and the granularity of energy schedules discovered by Perseus.



**Figure 6.** A simplified example of how to reduce iteration time by unit time  $\tau$ . Given a 1F1B pipeline schedule with 2 stages and 3 microbatches (①), it is first transformed to an equivalent representation of computation DAG (②). Then the Critical DAG (③) is obtained by considering only the computations on the critical path. Our key observation is that any valid s-t cut on the Critical DAG will reduce the iteration time by unit time  $\tau$ . Cut A and Cut B are two examples of valid s-t cuts (④). Either reducing the one computation associated with Cut A (⑤A) or reducing the two computations associated with Cut B (⑤B) reduces the iteration time by  $\tau$ .

**Node- and Edge-Centric Computation DAGs.** Originally, Perseus’s representation of the computation DAG is node-centric, which has forward and backward computations as nodes and their dependencies as edges. As a setup for subsequent steps, we convert this into an edge-centric computation DAG where computations are edges and dependencies are nodes (i.e., all incoming edges must complete before any outgoing edge can begin). This conversion can be done by splitting each node into two and connecting the two with an edge annotated with the computation on the original node.

**Removing Non-Critical Computations.** Our goal is to reduce the execution time of the computation DAG by  $\tau$ , which is equivalent to reducing the length of *all critical paths* by  $\tau$ .<sup>8</sup> Since computations that are not on any critical path (i.e., non-critical computations) do not affect the length of the critical path, we remove them from the computation DAG.

**Finding Computations to Speed Up.** Which computations on the DAG should we speed up in order to reduce the length of all critical paths by  $\tau$ ? The key observation is that *any* s-t cut on the computation DAG represents a way to reduce the execution time of the DAG by  $\tau$ . Specifically, by speeding up the computations on all cut edges by  $\tau$ , the entire computation DAG can be sped up exactly by  $\tau$ .

Figure 6 shows two examples of this. ④ shows two valid s-t cuts: *Cut A* and *Cut B*. ⑤A speeds up the computation edge cut by *Cut A* from  $3\tau$  to  $2\tau$ , and the iteration time of the

energy schedule was reduced by  $\tau$ . Similarly, ⑤B speeds up the computation edges cut by *Cut B* from  $5\tau$  to  $4\tau$  and from  $7\tau$  to  $6\tau$ , and the iteration time of the energy schedule was also reduced by  $\tau$ . Especially, in the second case, iteration time was only reduced because computations on two parallel critical paths were sped up *together*.

**Solving with Minimum Cut.** We have seen that any s-t cut represents a way to speed up the entire DAG by  $\tau$ . But speeding up computations increases energy. Then, a natural question is, which cut brings the smallest energy increase?

We can precisely map the *flow capacity* of an s-t cut to the amount of *energy increase* from speeding up cut edges. That is, by finding the amount of energy increase each computation will incur with the slope of its exponential function (§4.1) and defining it to be the edge’s flow capacity, we can reduce our problem to minimum cut, which we can solve with maximum flow. After finding the minimum cut, we modify the durations of the computations involved in the cut, obtaining the neighbor energy schedule. Appendix E provides details with mathematical expressions for flow capacities.

**Converting Back to GPU Frequencies.** Finally, we convert the energy schedule into GPU frequencies that can be realized by the Perseus client. For each computation, we convert its planned execution time  $t$  to the slowest GPU frequency that will execute *faster* than  $t$ . This is because when computations are tightly packed by our algorithm, while slightly speeding up a computation is acceptable, slowing down *any computation* on the critical path will directly slow down the entire DAG, increasing intrinsic energy bloat.

<sup>8</sup>Let’s say there are two critical paths that run in parallel. They must be of equal length to both be critical paths. Here, if only one were shortened, the other will remain the sole critical path and the DAG will not execute faster.

API	Description
<code>profiler.begin(type)</code>	Begin time and energy profiling for computation type.
<code>profiler.end(type)</code>	Record time and energy profiling results for computation type.
<code>controller.set_speed(type)</code>	Set the hardware’s execution speed as planned for computation type.
<code>server.set_straggler(id, delay, degree)</code>	Notify that a straggler is anticipated after delay seconds. A straggler returning to normal can be communicated by setting degree to 1.

**Table 2.** The minimal set of Perseus client and server APIs that require implementation. One client process manages each accelerator. The type parameter should be either "forward" or "backward". On GPUs, the "speed" control knob is the SM frequency. `set_straggler` is invoked by the infrastructure with the `id` of an accelerator to notify the server via HTTP/RPC.

<b>Input:</b> DAG $\mathcal{G}$ of computations $i \in \mathcal{G}$ Current energy schedule $s$ Amount of iteration time to reduce $\tau$ <b>Output:</b> Neighbor schedule with reduced time $s'$	
<hr/> <p>► Construct edge-centric computation DAG (②)</p> 1 $\mathcal{G} \leftarrow$ Split nodes into two and connect with edge <p>► Find and remove non-critical computations (③)</p> 2 Annotate earliest & latest start times for $\forall i \in \mathcal{G}$ 3 <b>for</b> $i \in \mathcal{G}$ <b>do</b> 4 <b>if</b> $i$ has different earliest and latest start <b>then</b> 5         Remove $i$ from $\mathcal{G}$ <p>► Find set of computations to modify (④)</p> 6 $S, T \leftarrow \text{FindMinCut}(\mathcal{G}, s)$ <p>► Modify computation durations (⑤)</p> 7 Modify duration of $\forall i$ in $S - T$ cut by $\tau$ <p>► Assign frequencies from planned computation times</p> 8 $s' \leftarrow \min f_i$ that runs no slower than planned 9 <b>return</b> $s'$	

**Algorithm 2:** GetNextSchedule: Reducing the execution time of the DAG by  $\tau$  with minimal energy increase.

**Time Complexity Analysis.** Our optimization algorithm has polynomial runtime. Let  $N$  and  $M$  denote the number of stages and microbatches, respectively. Then, the computation DAG will have  $O(NM)$  number of nodes and edges, and maximum flow with Edmonds-Karp runs in  $O(N^3M^3)$ . While for general DAGs the total number of steps is known to be exponential to the size of the DAG [71], we prove that for DAGs that represent pipeline computations, the number of steps is  $O(N + M)$ , yielding a final polynomial time complexity of  $O((N + M)N^3M^3)$ . See Appendix F for proof.

In reality, commonly used number of stages ( $N$ ) is 4 to 8 (at most tens) to reduce pipeline bubble ratio [18, 57]. Number of microbatches ( $M$ ) is typically around  $4N$  [34, 72], but recently with high data parallel degree, far fewer have been reported even for high-performance settings [18]. As such, algorithm runtime is practically negligible (§6.5), especially given that large model training easily takes weeks or months [63].

#### 4.4 Generalizations

In this section, we present generalizations to our optimization algorithm useful for planning large model training.

**3D/Hybrid Parallelism.** Operator parallelism techniques (e.g., data, tensor, or sequence parallelism) split operations in *equal sizes*, resulting in each GPU running the same computation. This allows Perseus to profile only one GPU per stage, decide the energy schedule for that GPU, and replicate it to all other GPUs in the same stage. We show that Perseus works well for 3D parallelism in Section 6.4.

**Constant-Time Operations.** There are operations in the training pipeline that may take non-trivial latency, other than computation and blocking on communication. For instance, loading and copying input data into VRAM or communication over slower links can take considerable latency. However, the time and energy consumption of these operations are not affected by the GPU’s frequency. Perseus can take constant-time operations into account during planning by viewing them as a node with only one frequency choice.

**Other Pipeline Schedules.** There are various schedules for pipeline parallel training, including GPipe [34], 1F1B [56], interleaved 1F1B [69], and early recomputation 1F1B [45]. As long as the computations on the schedule can be expressed as a DAG, Perseus can optimize its energy consumption without modification. As long as there is stage imbalance, any pipeline schedule will have intrinsic energy bloat.

## 5 Implementation

The Perseus server and client are implemented in Python. Perseus can optimize any training infrastructure, framework, and accelerator as long as the APIs in Table 2 can be implemented, and the accelerator supports multiple execution speeds that trade off computation time and energy.

As a reference, we have integrated the Perseus client with Merak [45], which marries high-performance tensor parallelism of Megatron-LM [3] and the generic pipeline execution engine of DeepSpeed [1]. While training engine implementations differ widely, many have separate code blocks for forward and backward, allowing them to be wrapped with the profiler APIs. We provide an example of what looks



like to integrate the client with a training engine in Appendix G. Activation recomputation [13] is enabled to allow large batch sizes to fit in GPUs.

**Profiler.** Accurate profiling is important to our optimization algorithm; inaccurate latency profiles (especially underestimations) may slow down the end-to-end latency of the DAG, whereas inaccurate energy profiles can lead the algorithm to incorrectly select computations to speed up.

Fortunately, the latency of a fixed set of GPU computations, especially with the GPU’s frequency locked, is known to be very stable [4, 27]. Furthermore, to ensure that profiling results are representative of real training, the Perseus client profiles the time and energy of each forward and backward computation at the beginning of the training job *in vivo*. Each supported GPU frequency is profiled one by one from the highest to the lowest for about five iterations (more if one iteration has less microbatches). After a certain frequency, lower frequencies result in both more time *and* energy consumed, making them strictly suboptimal compared to higher frequencies. Profiling is terminated at that point.

Finally, we profile  $P_{\text{blocking}}$  using two GPUs. One GPU blocks on P2P communication and the other sleeps, and we measure the power consumption of the blocking GPU. It is sufficient to profile  $P_{\text{blocking}}$  *once per GPU model*.

**Asynchronous Frequency Controller.** The client-side controller spawns a separate process that asynchronously sets the GPU’s frequency through NVML [4] without blocking the main training process. Training frameworks can call `set_speed` at the beginning of forward or backward to set the GPU’s frequency as planned by the server.

## 6 Evaluation

We evaluate Perseus on five workloads and compare it against EnvPipe and Zeus. Our key findings are the following:

- Perseus can effectively reduce intrinsic and extrinsic energy bloat. Training on real GPUs shows up to 28.5% energy savings using Perseus (§6.2).
- In emulated large-scale training scenarios, Perseus significantly outperforms the baselines by consistently providing up to 30% energy savings (§6.3).
- Energy bloat reduction is possible because Perseus can enumerate efficient energy schedules on the time–energy frontier (§6.4).
- Perseus reduces energy bloat with low overhead (§6.5).

### 6.1 Experimental Setup

**Testbed.** We run our evaluation workloads in a GPU cluster, where each node is equipped with an AMD EPYC 7513 CPU, 512 GB DRAM, and four NVIDIA A40-48G GPUs. For A100 results, we use a node provided by Chameleon Cloud [41], equipped with two Intel Xeon Platinum 8380 CPUs, 512 GB DRAM, and four NVIDIA A100-80G PCIe GPUs.

**Workloads and experiment parameters.** We evaluate Perseus with various workloads spanning from GPT-3 [8], Bloom [82], BERT [19], T5 [66], to Wide-ResNet [87]. We use model variants with 1.3B to 6.7B parameters to run the models in our testbed, and scale them up to 176B parameters in large-scale emulation. We chose the microbatch size and number of microbatches that yield the highest throughput given the global batch size. We use the minimum imbalance stage partitioning method described in Section 2.2 for all workloads. Appendix B lists complete model configurations, parameters, and stage partitioning details.

**Metrics.** We report GPU energy reduction and slowdown of a training iteration (%) relative to using all maximum GPU frequencies. In most cases slowdown is close to zero, in which case energy and average power reductions coincide. Reducing only extrinsic bloat is not possible, because Perseus reduces extrinsic bloat *while keeping* intrinsic bloat low as it slows down non-straggler pipelines. Therefore, we report (1) intrinsic bloat reduction *without* stragglers and (2) intrinsic + extrinsic bloat reduction *with* stragglers.

**Baselines.** We mainly compare with two prior works:

- **EnvPipe** [15] reduces only intrinsic energy bloat while trying to minimize slowdown. We compare Perseus’s energy bloat reduction with EnvPipe (§6.2, §6.3).
- **Zeus** [86] characterizes the time–energy tradeoff of single GPU training. We compare Perseus’s time–energy frontier against that of Zeus (§6.4).

### 6.2 Reducing Energy Bloat

We start with overall energy bloat reduction—intrinsic bloat without stragglers (§6.2.1) and intrinsic + extrinsic bloat with stragglers (§6.2.2)—achieved by Perseus and EnvPipe. All numbers were obtained by running on testbed GPUs. All solutions use the same amount of GPU hardware resources.

#### 6.2.1 Intrinsic Bloat Reduction Without Stragglers.

Table 3 compares the energy savings achieved by Perseus’s minimum iteration time energy schedule (leftmost point of the time–energy frontier) and that by EnvPipe.

We make two observations regarding Perseus. First, models show varying amounts of energy savings because (1) their stage imbalances vary (Table 1), and (2) their forward and backward are composed of different computations, which affects time/energy sensitivity when changing the frequency. For instance, unlike other models, Wide-ResNet 1.5B on A100 after minimum imbalance stage partitioning has nearly perfect stage balance, resulting in low intrinsic energy bloat. However, as will be seen in Section 6.2.2, such models tend to achieve greater extrinsic bloat savings because most of their computations run at a high frequency, and slowing them down due to stragglers leads to higher energy reduction.

Second, A40 demonstrates more energy savings compared to A100. This is because the dynamic clock frequency range

Model	Energy Savings (%)		Slowdown (%)	
	Perseus	EnvPipe	Perseus	EnvPipe
GPT-3 1.3B	13.2	8.8	0.1	0.1
BERT 1.3B	12.9	8.0	0.5	0.0
T5 3B	10.6	7.4	1.3	3.4
Bloom 3B	11.7	8.9	0.2	0.2
Wide-ResNet 1.5B	3.2	3.7	2.3	4.1

(a) Four stage pipeline parallelism on A100 GPUs

Model	Energy Savings (%)		Slowdown (%)	
	Perseus	EnvPipe	Perseus	EnvPipe
GPT-3 2.7B	21.1	21.7	0.2	5.6
BERT 1.3B	15.7	16.5	0.0	9.7
T5 3B	28.5	19.3	0.0	0.0
Bloom 3B	22.4	19.9	0.0	0.0
Wide-ResNet 1.5B	20.4	16.5	0.2	0.5

(b) Eight stage pipeline parallelism on A40 GPUs

**Table 3.** [Experiment] Intrinsic energy bloat (without stragglers) reduction and iteration time slowdown.

of A100 (210–1410 MHz) is smaller than that of A40 (210–1740 MHz). Thus, tuning down the GPU’s frequency yields a relatively smaller change in computation time and energy compared to those at the maximum frequency. However, we expect the more recent GPUs to have better percentage savings due to higher maximum frequency (e.g., 1980 MHz for H100 SXM [58]) and better absolute savings due to high TDP (e.g., 1,200 W for each GPU on GB200 [50]).

EnvPipe in general provides lower energy savings, primarily due to its assumption that the final stage of a pipeline is always the heaviest. This is only correct with a probability of  $1/N$ , where  $N$  is the number of pipeline stages. Additionally, it sometimes considerably degrades iteration time because it is not aware of *single-choice operations* inside the pipeline (§4.4) and can slow down some computations too much.

**6.2.2 Intrinsic + Extrinsic Bloat Reduction With Stragglers.** When stragglers create extrinsic energy bloat, the amount of energy savings depends on how much energy reduction the time–energy frontier yields for longer iteration times. Table 4 shows the amount of energy savings of a non-straggler pipeline given varying straggler slowdowns. For a given slowdown factor ( $T'/T$ ), a non-straggler pipeline’s iteration time is set to be  $T_{\text{opt}} = \min(T^*, T')$  (§3.1), and energy reduction comes from (1) slowing down the pipeline itself and (2) reducing the time (and energy) blocking on communication, waiting for the straggler.

The percentage of savings initially increases with the straggler’s iteration time, but then gradually decreases as it slows down beyond  $T^*$ . This is expected. The absolute amount of energy reduction in Joules is the largest when the straggler’s iteration time is  $T^*$  and constant afterward, because Perseus does not slow down non-straggler pipelines beyond

Model # Params	Method	Energy Savings (%) given $T'/T$					
		1.05	1.1	1.2	1.3	1.4	1.5
GPT-3 1.3B	Perseus	14.7	15.9	15.5	15.0	14.6	14.3
	EnvPipe	8.7	8.5	8.3	8.1	7.9	7.7
Bloom 3B	Perseus	13.6	15.6	15.2	14.7	14.3	14.0
	EnvPipe	8.8	8.7	8.4	8.2	8.0	7.8
BERT 1.3B	Perseus	14.9	16.9	16.4	15.9	15.5	15.0
	EnvPipe	7.9	7.8	7.5	7.3	7.1	6.9
T5 3B	Perseus	15.3	18.0	17.9	17.4	16.9	16.5
	EnvPipe	8.4	8.2	8.0	7.8	7.6	7.4
Wide-ResNet 1.5B	Perseus	9.4	12.7	12.6	12.3	12.0	11.6
	EnvPipe	4.9	4.8	4.7	4.5	4.4	4.3

(a) Four stage pipeline parallelism on A100 GPUs

Model # Params	Method	Energy Savings (%) given $T'/T$					
		1.05	1.1	1.2	1.3	1.4	1.5
GPT-3 2.7B	Perseus	24.5	26.0	25.9	25.2	24.6	24.0
	EnvPipe	22.9	22.6	22.0	21.4	20.9	20.4
Bloom 3B	Perseus	25.5	26.4	25.9	25.2	24.6	24.0
	EnvPipe	19.6	19.3	18.8	18.3	17.8	17.4
BERT 1.3B	Perseus	20.0	22.6	24.1	23.4	22.8	22.2
	EnvPipe	19.2	18.9	18.3	17.8	17.4	16.9
T5 3B	Perseus	27.9	27.3	26.2	25.2	24.3	23.4
	EnvPipe	18.4	18.0	17.3	16.6	16.0	15.4
Wide-ResNet 1.5B	Perseus	24.3	26.2	26.3	25.7	25.0	24.4
	EnvPipe	16.4	16.2	15.8	15.4	15.0	14.6

(b) Eight stage pipeline parallelism on A40 GPUs

**Table 4.** [Experiment] Energy savings given varying straggler slowdown ( $T'/T$ ). Perseus can reduce extrinsic bloat while keeping intrinsic bloat low, whereas EnvPipe cannot.

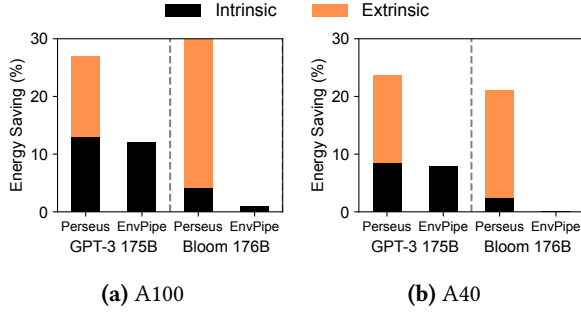
$T^*$  (§3.1). Thus, as the straggler slows down beyond  $T^*$ , additional time and energy is consumed while waiting for the straggler, lowering the *percentage* of energy savings.

Finally, the point of maximum energy savings is different for each model. This is because each model has a different  $T^*$  value, which is determined by how much each stage’s computation slows down on the minimum-energy frequency.

**6.2.3 How Much Potential Saving Was Realized?** The largest possible savings under our problem setting occurs when running every computation at their minimum-energy frequencies (i.e., the  $T^*$  point on the time–energy frontier). For intrinsic bloat without stragglers, Perseus realizes on average 74% and 89% of the potential savings on A100 and A40, respectively, with negligible slowdown. This is possible because there are much more non-critical computations in the DAG that can be slowed down than critical ones. With stragglers, Perseus fully realizes potential savings when the straggler’s slowdown degrees are on average 1.1 and 1.15 on A100 and A40 respectively, which is not unrealistic considering slowdowns reported in literature (§2.3).

# GPUs	# Pipelines	# Microbatches Per Pipeline	Global Batch Size
1024	16	96	1536
2048	32	48	
4096	64	24	
8192	128	12	

**Table 5.** Strong scaling parameters for large-scale emulation. A pipeline has tensor parallel degree 8 and 8 pipeline stages.



**Figure 7.** [Emulation] Energy savings breakdown with straggler slowdown 1.2 and 1,024 GPUs.

### 6.3 Large-Scale Emulation

Because we do not have access to a GPU cluster required to run huge models like GPT-3 175B, we use *emulation* grounded on fine-grained profiling for large-scale evaluation. In general, trends in our emulation result match those obtained from real training in Section 6.2.

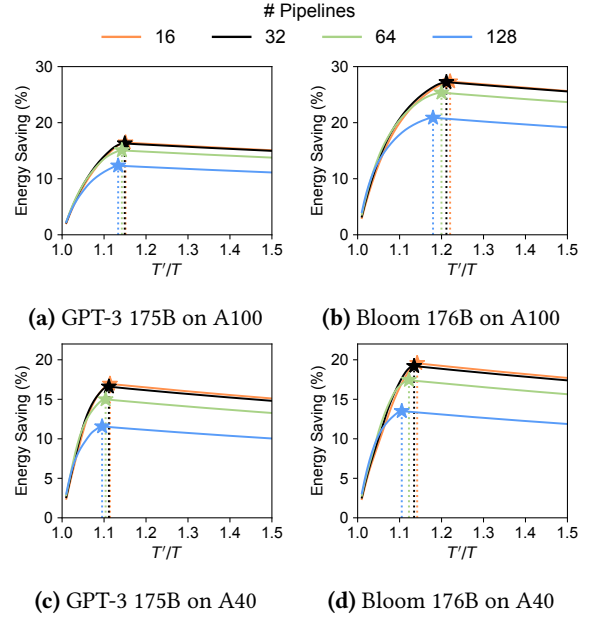
**Emulation Methodology.** We profile the time and energy consumption of each layer (e.g., Transformer decoder) in GPT-3 175B and Bloom 176B and run our optimization algorithm to obtain the time–energy frontier. We perform *strong scaling* when varying the number of GPUs (Table 5) in order to keep the global batch size constant [26, 42]. We used A100 SXM GPUs for emulation, which we believe are more representative of large-scale training infrastructure.

**Emulator Fidelity.** We compare the percentage of energy savings vs. running all maximum frequencies given by our emulator and real experiments for our A100 workloads and find that the emulator *always underestimates* energy savings. Specifically, savings on the leftmost and rightmost point of the frontier are underestimated by 18.6% and 21.7% on average, respectively. We believe this is due to our simplifying assumption that  $P_{\text{blocking}}$  is constant regardless of the GPU’s frequency. This means the savings given by the emulator can be considered a lower bound for actual savings.

**Result Summary.** Figure 7 breaks down the amount of energy bloat reduction for GPT-3 175B and Bloom 176B when slowdown degree is 1.2 on 1,024 GPUs. EnvPipe can only reduce intrinsic bloat as it does not provide a time–energy frontier; even for intrinsic bloat, it is suboptimal. In contrast, Perseus reduces energy consumption by up to 30% by reducing both intrinsic and extrinsic energy bloat.

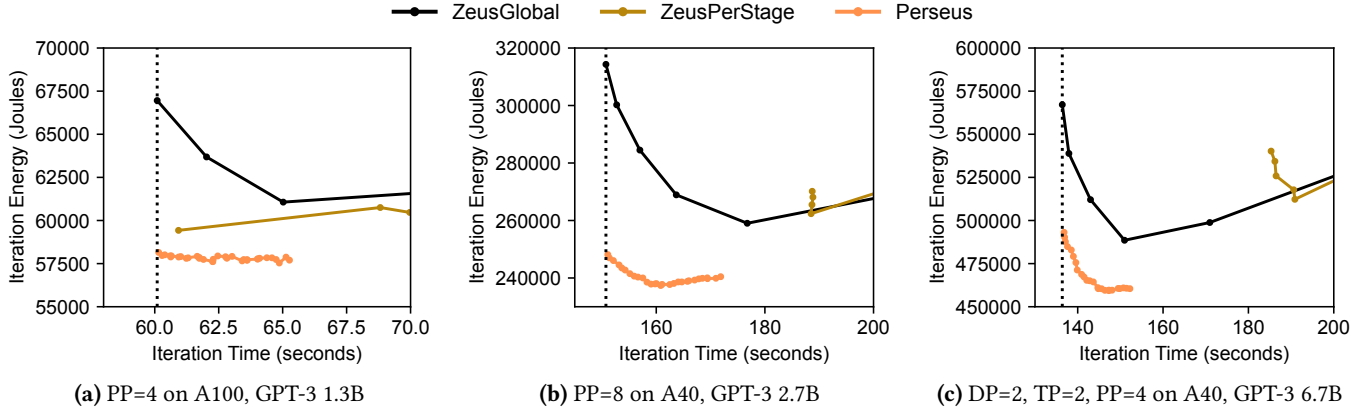
Model	GPU Type	Energy Savings (%) Given # Microbatches			
		12	24	48	96
GPT-3 175B	A100	15.20	14.19	13.62	13.32
	A40	11.81	10.22	9.34	8.88
Bloom 176B	A100	10.47	7.06	5.23	4.28
	A40	6.97	4.49	3.12	2.41

**Table 6.** [Emulation] Perseus’s intrinsic energy bloat reduction without stragglers for GPT-3 175B and Bloom 176B. Number of microbatches is varied following Table 5.



**Figure 8.** [Emulation] Perseus’s intrinsic + extrinsic energy bloat reduction with varying straggler slowdown ( $T'/T$ ). Number of pipelines is varied following Table 5. ★ denotes  $T^*/T$  for each pipeline. Please note the different Y-axes.

**Intrinsic Bloat Reduction Without Stragglers.** Table 6 shows Perseus’s intrinsic energy bloat reduction without stragglers for GPT-3 175B and Bloom 176B. The number of microbatches is varied based on Table 5. For all models, as more microbatches are added to the pipeline, the amount of intrinsic bloat decreases. This is fundamentally due to the ratio of microbatches in the 1F1B’s warm-up and flush phase (beginning and end) versus the steady state phase (middle). Most microbatches in the warm-up and flush phases can slow down until their minimum energy frequency, yielding large energy savings. However, microbatches in the pipeline’s steady state cannot slow down to their full potential when the amount of stage imbalance is not large, thereby yielding modest savings. When the number of microbatches in the pipeline increases, only the number of steady state microbatches increases, and energy reduction converges to the average energy savings of steady state microbatches.



**Figure 9.** [Experiment] Iteration time–energy frontiers for GPT-3, achieved by Perseus and the two baselines derived from Zeus [86]. Perseus Pareto-dominates all other approaches. The dotted vertical line is the iteration time of running all GPUs at their maximum power limit, which is the default mode of operation. Please note the different X- and Y-axes.

### Intrinsic + Extrinsic Bloat Reduction With Stragglers.

We introduce stragglers of varying slowdowns in large-scale emulation. Figure 8 reports the amount of intrinsic + extrinsic energy bloat reduction achieved by Perseus. The trend where energy saving increases until  $T' < T^*$  and wanes afterward is consistent with Section 6.2.2.

An interesting observation here is that there is a trade-off between scale and energy savings: *configurations with more pipelines have less percentage of energy savings or less amount of energy savings per pipeline*. It may seem intuitive to assume that more pipelines bring more energy savings, as there is only one straggler pipeline and all the other pipelines can reduce their energy consumption. However, this holds only in weak scaling scenarios, where the per-pipeline batch size is held constant (i.e., increasing the global batch size proportionally with the number of pipelines). Instead, in the more realistic strong scaling configuration (i.e., the global batch size is constant and per-pipeline batch size is decreased as more pipelines deployed), each pipeline’s number of microbatches changes. With fewer microbatches, the ratio of pipeline bubble (time that GPUs are idle) at the beginning and end of each pipeline iteration increases [57]. These bubbles cannot be perfectly eliminated by intrinsic energy bloat reduction, resulting in a smaller energy savings percentages. However, as the absolute number of GPUs increases, even a small savings percentage is expected to yield *huge absolute energy savings*.

### 6.4 Iteration Time–Energy Frontier Comparison

The energy bloat reductions in Sections 6.2 and 6.3 were made possible by the time–energy frontier obtained using Perseus’s optimization algorithm (§4). Here, we further examine the frontier with different parallelization configurations and models and compare against Zeus [86]. Since Zeus only produces the training time–energy frontier for *single-GPU* training jobs, we implemented two Zeus-based baselines for large model training scenarios:

- **ZeusGlobal:** Scans one global power limit for all stages.
- **ZeusPerStage:** Finds a set of per-stage power limits that balances forward computation time.

Figure 9 shows the frontiers of all solutions for different sizes of GPT-3 under three parallelization configurations: (a) four stage pipeline parallelism on A100; (b) eight stage pipeline parallelism on A40; and (c) 3D parallelism (data parallelism 2, tensor parallelism 2, pipeline parallelism 4) on A40. All results were obtained from running on testbed GPUs. Appendix H has frontiers for other models.

Perseus Pareto-dominates both baselines derived from Zeus. ZeusGlobal is unaware of pipeline stage imbalances and slows down every stage, and therefore is unable to intrinsic energy bloat. ZeusPerStage can balance the forward computation time of each stage, but is unaware of the *critical path* of the DAG, slowing down critical computations. In contrast, Perseus can precisely slow down non-critical computations, effectively reducing energy bloat.

### 6.5 Overhead of Perseus

**Profiling.** At the beginning of training, the client-side profiler (§5) profiles forward and backward computations in each stage. For our A100 workloads, the initial profiling phase increased end-to-end training time by 13 minutes on average, which is negligible overhead for large model training.

**Algorithm Runtime.** The average runtime of the optimization algorithm (§4) across our A100 workloads was 6.5 minutes, with the longest being Bloom 3B (15.7 minutes). For our largest-scale emulation workload (GPT-3 175B on A100 with 8,192 GPUs), the algorithm took 87 seconds, which is short because it is sufficient to optimize just one data parallel pipeline (§4.4). While runtime will increase with larger DAGs for larger models, we believe the overhead is justified because training time is likely to also increase with the scale of the training job. Looking up the optimal energy schedule given the straggler’s iteration time  $T'$  is instantaneous.



## 7 Related Work

**Large Model Training.** Many recent works focus on enabling and accelerating large model training using 3D parallelism. GPipe [34] and PipeDream [55] first introduced pipeline parallelism. 3D parallelism, especially popularized for Transformer-based models by Megatron-LM [57, 69], is considered to be the go-to solution for modern large model training due to strong open-source projects [1, 3, 6] and relatively low implementation complexity. Extending this, Alpa [90], GSPMD [88], and nnScaler [48] provide automatic parallelization for general DNNs. However, energy consumption is not an optimization metric for any of the major large model training frameworks.

Several works utilize computation idle times within large model training pipelines to insert additional useful work [33, 59, 76]. In contrast, Perseus’s approach is to slow down preceding computations to fill the idle time and reduce power and energy consumption. The rationale is twofold. First, the amount of idle time—especially in the steady state of the pipeline—is typically short. Inserting extra work may slow down the entire pipeline or require pipeline re-partitioning to make it feasible. Second, GPUs, especially those in the earlier stage of the pipeline, are likely already constrained by memory capacity, leaving little headroom for extra computation. We note that even with extra computation inserted, some idle time is likely to remain, leaving room for Perseus to provide energy savings.

**Deep Learning and Energy Consumption.** A line of work measures or estimates the large amount of energy consumption and carbon emission of deep learning workloads [20, 44, 49, 63, 73]. In terms of optimization, some works determine the GPU’s execution speed for a single fixed sequence of GPU computations [16, 36, 43, 78, 85, 91], falling short when the time–energy frontier of a complex large model computation DAG needs to be characterized. Zeus [86] is a recent work that observes the tradeoff between GPU computation time and energy consumption, but still focuses on single-GPU training. EnvPipe [15], on the other hand, aims to find a point solution that reduces the energy consumption of large model training with minimum slowdown. However, EnvPipe’s heuristic assumes that the last pipeline stage is always the bottleneck, leading to suboptimal savings. In terms of optimizing a single training job, Perseus is a superset of both Zeus and EnvPipe, achieved by viewing large model training as a computation DAG and introducing a principled optimization algorithm.

**Big Data and Energy Consumption.** There are existing works that change the frequency of CPUs to improve the energy efficiency of big data workloads, including those that only execute computation-intensive phases (e.g., map and reduce) with the maximum frequency [35, 80], those that

choose the lowest frequency that can meet a given deadline [10, 51], or those that choose frequencies that balance the completion time of parallel tasks (yet simply minimizing idle time for smaller tasks within one stage) [46]. Perseus provides a principled approach to setting the job’s end-to-end completion time (§3.1) and task execution speed (§4), and can be directly applied to big data workloads by generating a DAG of CPU computations and optimizing the CPU’s frequencies.

## 8 Conclusion

We presented Perseus, a software-based energy optimization system for large model training. Perseus builds on the observation that there are computation imbalances at different levels in large model training that cause *intrinsic and extrinsic energy bloat*, and simultaneously reduces both with a principled graph cut-based algorithm. As a result, Perseus advances the state-of-the-art of DNN training energy optimization by delivering energy savings with negligible slowdown, thereby also reducing average power draw and enhancing the sustainability of large model training.

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