

Game-theoretic scheduling in integrated energy system considering energy flexibility from consumers

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MENUE

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Introduction

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Consumer Modelling and IES Modelling

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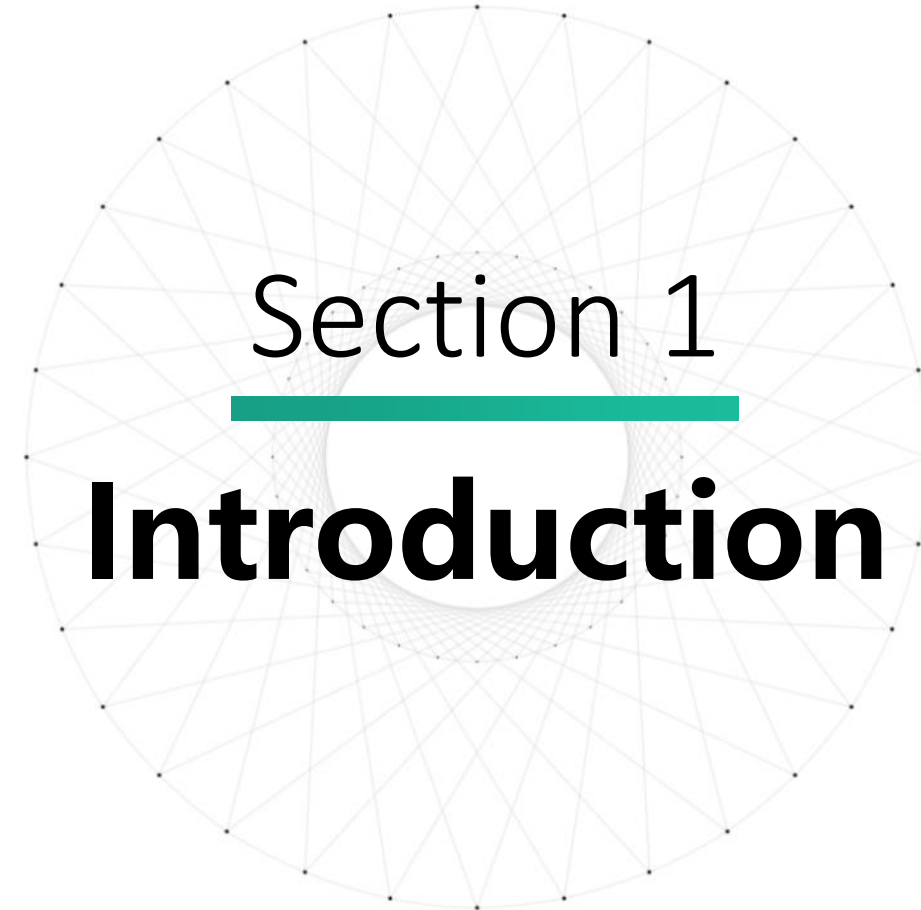
Game-theoretic Scheduling Model

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Case Study

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Conclusion



Section 1

Introduction

1.1 Overview

Community Energy
Management

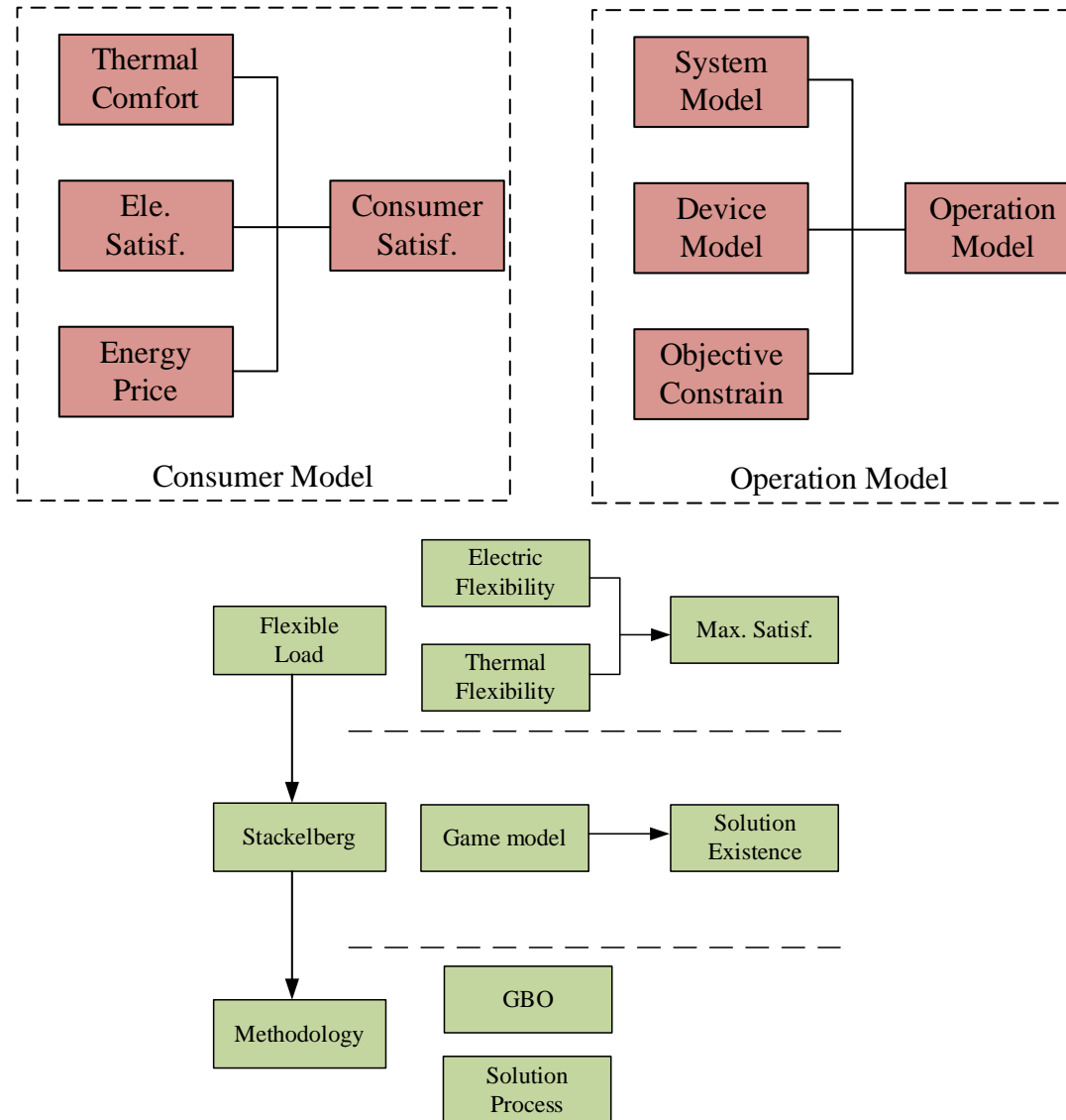
Consumer
Comfort

IES
Operator

Energy Operation
& Flexible Dispatch

Supply & Tariff

Game-theoretic



1.2 Background & Inspiration

- Increasing Energy Demand
- Carbon Reduction Request
- Renewable Energy Penetration
- Integrated Energy Community

- Energy Management
- Demand Response
- Consumer Comfort

- Prosumer Operator
- Economic Revenue
- Energy Supply Tariff

- Game-theoretic Structure
- Flexible Load Scheduling

1.3 Contribution

**Consumer satisfaction
formulation based on comfort
and tariff**

**Consumer flexible load
scheduling model considering
comfort and satisfaction**

**Mechanism designing for
distributing the mitigated cost**

**Comfort modelling formulation
based on
Activity, metabolism,
temperature**

**Demand response to optimize
the energy operation**

**System operator –lower cost
Consumer –lower tariff with
good comfort**



Section2

Consumer Modelling and IES Modelling

2.1 Satisfaction Model and Consumer Model

PMV

$$PMV = (0.303e^{-0.036M} + 0.028) \cdot [(M - W) - E_s - E_b - C_b - H]$$

$$E_s = -3.05 \cdot 10^{-3} \cdot [5773 - 6.99 \cdot (M - W) - p_a]$$

$$E_b = 1.7 \cdot 10^{-5} M \cdot (5876 - p_a)$$

$$C_b = 0.0014 \cdot M(34 - t_a)$$

$$H = 3.96 \cdot 10^{-8} \cdot f_{cl} \cdot [(t_{cl} + 273)^4 - (t_r + 273)^4] - f_{cl} h_c (t_{cl} - t_a)$$

Exist PMV-
temperature

$$PMV_{i,t} = a_1 \cdot T_{i,t}^{in} + b_1, t \in [T^c, T^d]$$

Thermal Comfort(PTS)

$$T_{i,t+1}^{in} = T_{i,t}^{in} - \frac{\Delta T}{C \cdot R} \cdot [T_{i,t}^{in} - T_{i,t}^{out} - \frac{1.75}{Q_{\max}} u_{i,Q}(t) \cdot R \cdot Q_{i,t} + \frac{1.75}{H_{\max}} u_{i,H}(t) \cdot R \cdot H_{i,t}]$$

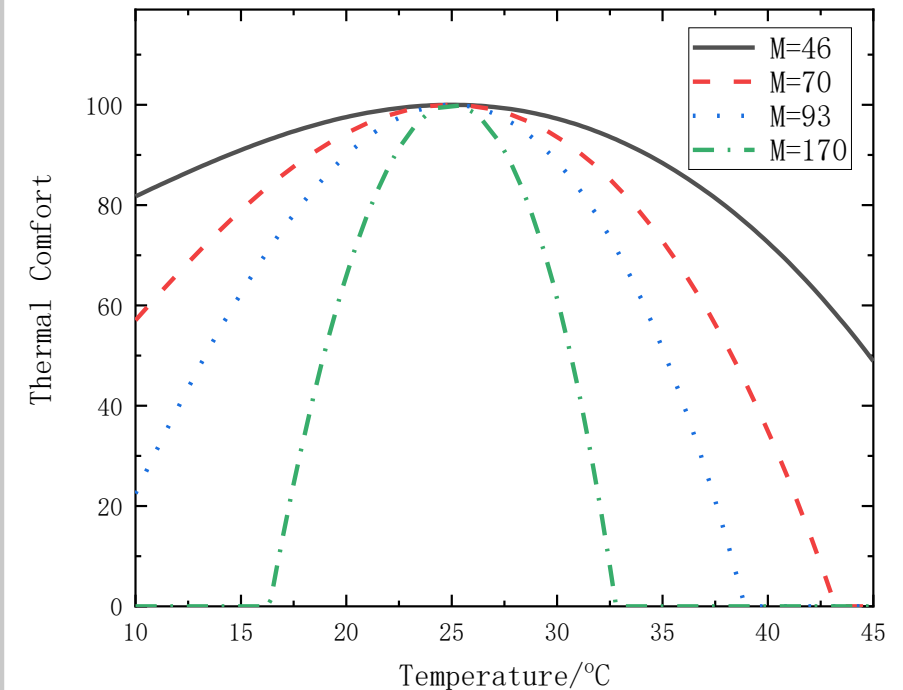
$$PPD(PMV_{i,t})_{i,t} = 100 - 95 \times \exp[-(0.003353 \times PMV_{i,t}^4 + 0.2179 \times PMV_{i,t}^2)]$$

$$PTS_{i,t} = 1 - PPD_{i,t} / 100$$

Formulate
PTS-
temperature

Activity	$M(W/m^2)$
Sleeping	46
Sedentary	70
Shopping	93
Work	170
Walk	200

Different comfort
under different
temperature and
metabolism M



2.1 Satisfaction Model and Consumer Model

Piecewise
linearization

PMV-PTS

$$b_1 \leq b_2 \leq \dots \leq b_n \leq b_{n+1}$$

$$b_1 = PMV_{\min}, b_k = PMV_{\min} + k \cdot \frac{PMV_{\max} - PMV_{\min}}{n}, b_{n+1} = PMV_{\max}, k = 2, \dots, n$$

$$PMV_{i,t} = \sum_{k=1}^{n+1} b_k \cdot \gamma_{i,t,k}$$

$$PTS_{i,t}^{linear} = \sum_{k=1}^{n+1} [PTS(b_k)_{i,t} \cdot \gamma_{i,t,k}]$$

$$s.t. \begin{cases} \gamma_{i,t,1} \leq \kappa_{i,t,1}, \gamma_{i,t,n+1} \leq \kappa_{i,t,n+1}, \gamma_{i,t,k} \leq \sum_{j=k-1}^k \kappa_{i,t,j}, k = 2 \dots n \\ \sum_{k=1}^n \gamma_{i,t,k} = 1 \\ \sum_{k=1}^n \kappa_{i,t,k} = 1 \end{cases}$$

Consumer
Objective

Ele. satisfaction
 $PES_{i,t} = P_{i,t}^E / E_{i,t}$



Thermal Comfort

Satisfaction per cost

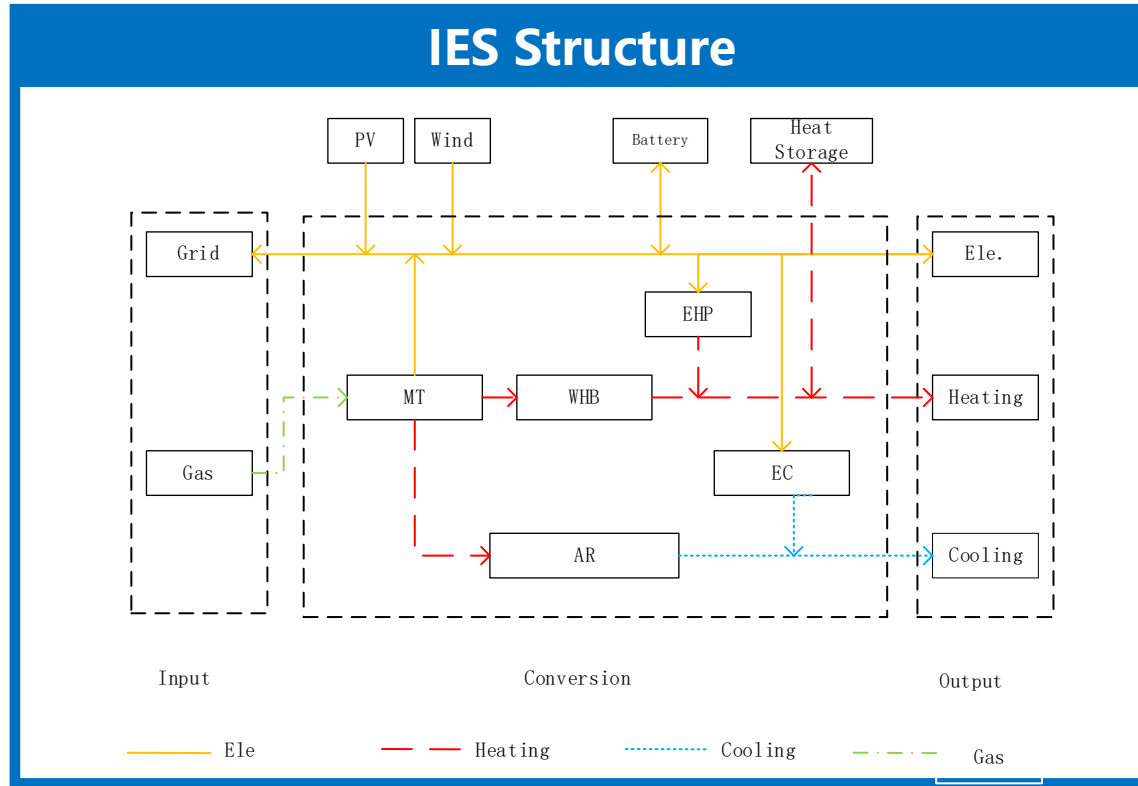


Ele. cost



Thermal Cost

2.2 IES Operation Model



Heat Pump

Cooling

$$Q_{i,s,t}^{EC} = P_{i,s,t}^{EC} \cdot COP_{i,s,t}^{EC}$$

Heating

$$H_{i,s,t}^{EHP} = P_{i,s,t}^{EHP} \cdot COP_{i,s,t}^{EHP}$$

Storage

Battery

$$E_{i,s,t}^{ba} = E_{i,s,t_0}^{ba} + \eta_{i,s,t}^{ba_in} E_{i,s,t}^{ba_in} - \eta_{i,s,t}^{ba_out} E_{i,s,t}^{ba_out}$$

Heat Storage

$$H_{i,s,t}^{hs} = H_{i,s,t_0}^{hs} + \eta_{i,s,t}^{hs_in} E_{i,s,t}^{hs_in} - \eta_{i,s,t}^{hs_out} E_{i,s,t}^{hs_out}$$

CCHP

Micro Turbine

$$P_{i,s,t}^{MT} = \frac{\eta_{i,s,t}^{MT} C_{i,s,t}^{MT}}{R_{gas}} \cdot LH$$

Absorption Refrigeration

$$Q_{i,s,t}^{AR} = \frac{P_{i,s,t}^{MT}(t)}{\eta_{i,s,t}^{MT}} \cdot \xi_{i,s,t}^{AR} (1 - \eta_{i,s,t}^{MT} - \eta_l) \cdot COP_{i,s,t}^{AR}$$

Waste Heat Boiler

$$H_{i,s,t}^{WHB} = \frac{P_{i,s,t}^{MT}(t)}{\eta_{i,s,t}^{MT}} \cdot \xi_{i,s,t}^{WHB} (1 - \eta_{i,s,t}^{MT} - \eta_l) \cdot COP_{i,s,t}^{WHB}$$

DER

PV

$$P_{i,s,t}^{pv} = A_{i,s,t}^{pv} \times \eta_{s,t}^{pv} \times SRI_{s,t}$$

Wind turbine

$$P_{i,s,t}^{wt} = \begin{cases} 0 & v_{i,s,t} < v_{ci} \\ k_1 v_{i,s,t} + k_2 & v_{ci} < v_{i,s,t} < v_r \\ P_r & v_{i,s,t} > v_r \end{cases}$$

2.2 IES Operation Model

Objective

revenue

$$\max F = \sum_t [RE_t - C_t^{fd} - C_t^{wh}]$$

Consumer Cost

$$RE_t = CE_{jm,t} + CT_{jm,t} + CE_{gy,t} + CT_{gy,t} + CE_{sy,t} + CT_{sy,t}$$

Operation Cost

$$C_t^{fd} = C_{i,s,t}^{MT} + P_{i,s,t}^{gr} \cdot G_t^{gr}$$

$$C_t^{wh} = \sum \theta_{i,s,t}^{\varphi} \cdot P_{i,s,t}^{\varphi}, \varphi = MT, AR, WHB, EHP, wt, pv, ba, hs$$

Constraints

Energy Balance

$$\sum_i P_{i,t}^E = \sum_i P_{i,s,t}^{MT} - \sum_i P_{i,s,t}^{EHP} - \sum_i P_{i,s,t}^{EC} + \sum_i P_{i,s,t}^{wt} + \sum_i P_{i,s,t}^{pv} +$$

$$\sum_i E_{i,s,t}^{ba_out} - \sum_i E_{i,s,t}^{ba_in} + \sum_i P_{i,s,t}^{gr}$$

$$\sum_i H_{i,t} = \sum_i H_{i,s,t}^{WHB} + \sum_i H_{i,s,t}^{EHP} + \sum_i E_{i,s,t}^{hs_out} - \sum_i E_{i,s,t}^{hs_in}$$

$$\sum_i Q_{i,t} = \sum_i Q_{i,s,t}^{AR} + \sum_i Q_{i,s,t}^{EC}$$

Device Constraints

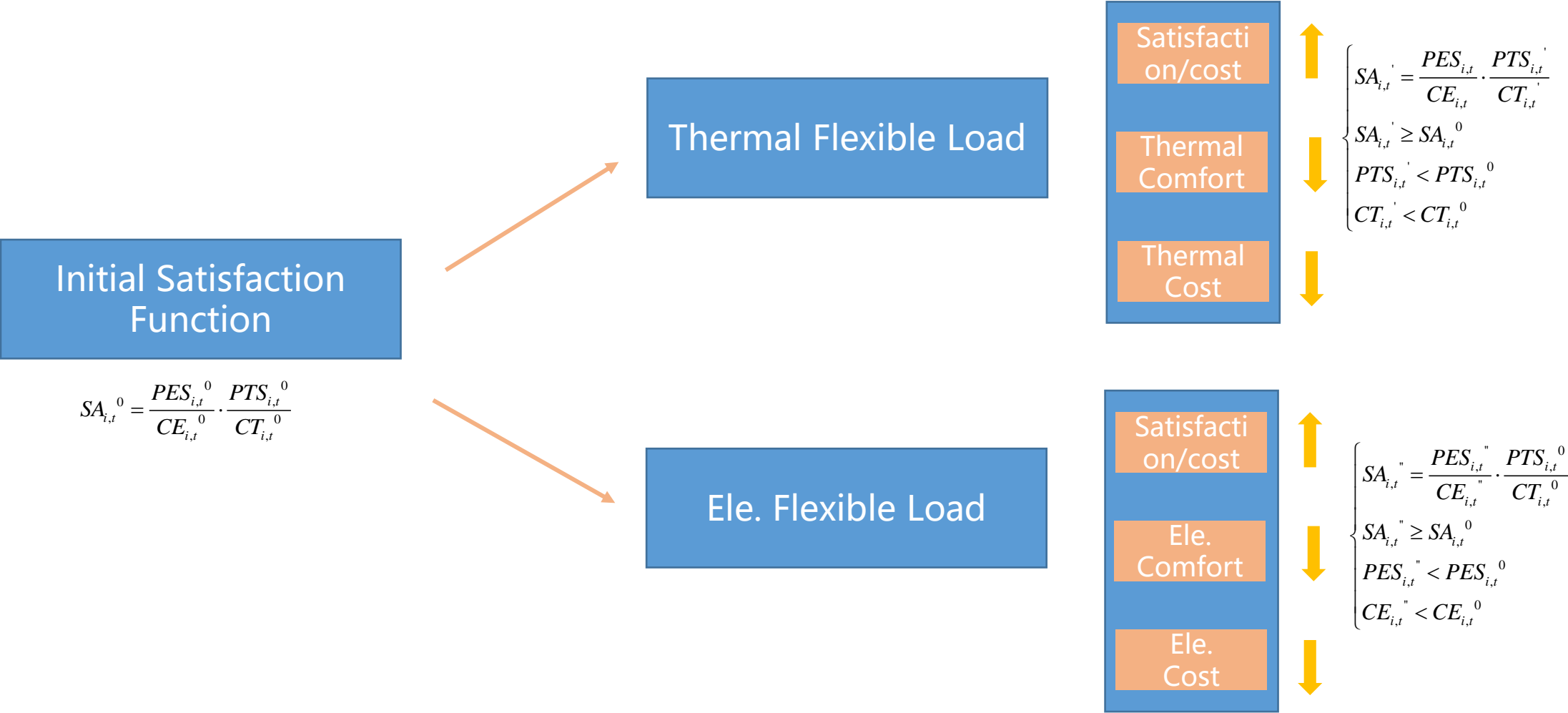
$$P_{\min}^{\varphi} \leq P_{i,s,t}^{\varphi} \leq P_{\max}^{\varphi}, \varphi = MT, AR, WHB, EHP, wt, pv, ba, hs$$



Section3

Game-theoretic Scheduling Model

3.1 Flexible Load



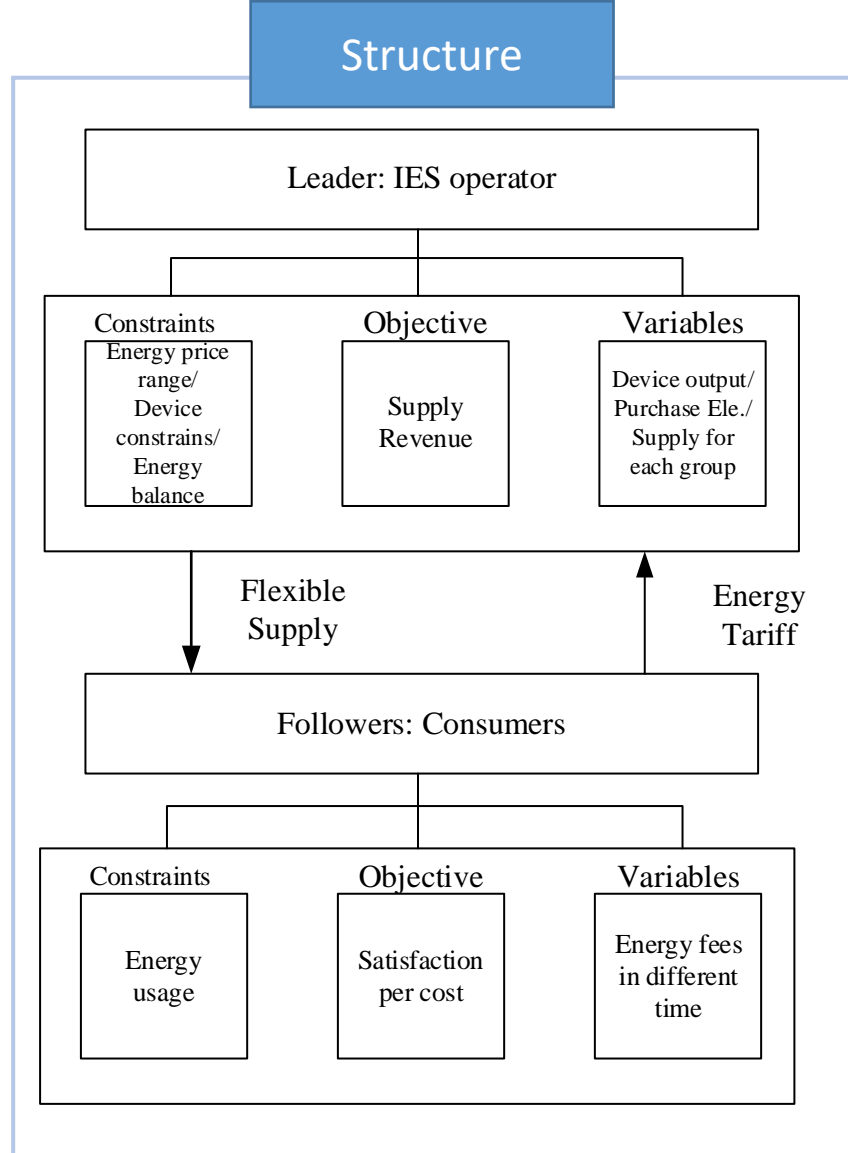
3.2 Game Model

Stackelberg

$$\begin{cases} \min F(x, \bar{y}) \\ s.t. \ G(x, \bar{y}) \leq 0 \\ H(x, \bar{y}) = 0 \\ \bar{y} \in S(x) \end{cases} \quad \text{leader}$$

$$\begin{cases} \bar{y}^i = \arg \min f_i(x, y^i, y^{-i}) \\ s.t. \ g_i(x, y^i) \leq 0 \\ h_i(x, y^i) = 0 \end{cases} \quad \text{follower: } \forall i$$

Structure



Equilibrium

$$G = \left\{ \begin{aligned} &\{IER \cup users\}; \\ &\{\rho_{IER}\}; \{C_{users}\}; \\ &F; SA_{users} \end{aligned} \right\}$$

$$users = \{user_jm \cup user_gy \cup user_sy\}$$

$$SA_{users} = \{SA_{jm}, SA_{sy}, SA_{gy}\}$$

$$\begin{cases} F(\rho_{IES}^*, C_{users}^*) \geq F(\rho_{IES}, C_{users}) \\ SA_{users}(\rho_{IES}^*, C_{users}^*) \geq SA_{users}(\rho_{IES}, C_{users}) \end{cases}$$

3.3 Algorithm and Process

GBO

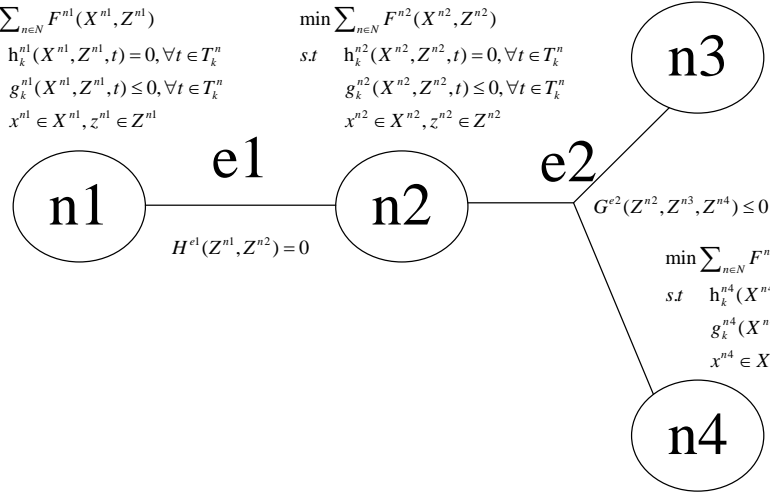
$$\begin{aligned} \min \sum_{n \in N} F^n(X^n, Z^n) \\ \text{s.t. } h_k^n(X^n, Z^n, t) = 0, \forall t \in T_k^n \\ g_k^n(X^n, Z^n, t) \leq 0, \forall t \in T_k^n \\ H^e(Z^e) = 0, \forall e \in \mathcal{E} \\ G^e(Z^e) \leq 0, \forall e \in \mathcal{E} \\ x^n \in X^n, z^n \in Z^n, \forall n \in N \end{aligned}$$

$$\begin{aligned} \min \sum_{n \in N} F^{n1}(X^{n1}, Z^{n1}) \\ \text{s.t. } h_k^{n1}(X^{n1}, Z^{n1}, t) = 0, \forall t \in T_k^{n1} \\ g_k^{n1}(X^{n1}, Z^{n1}, t) \leq 0, \forall t \in T_k^{n1} \\ x^{n1} \in X^{n1}, z^{n1} \in Z^{n1} \end{aligned}$$

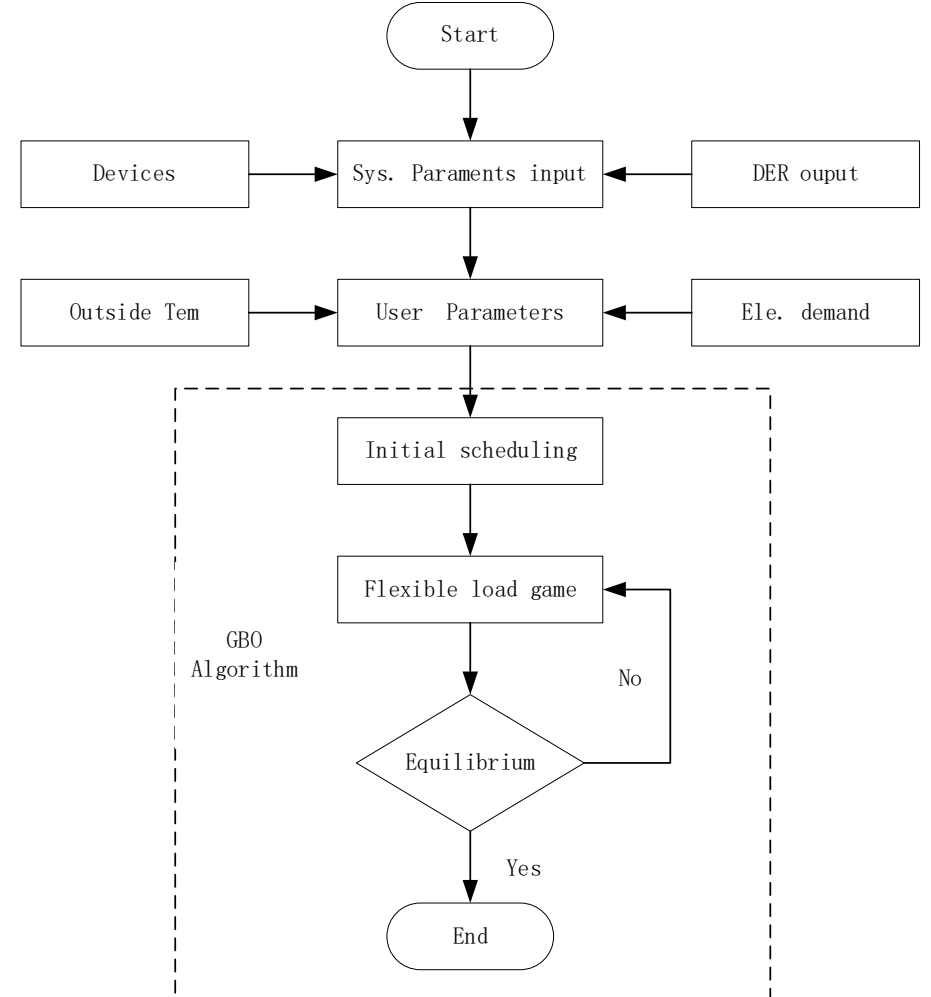
$$\begin{aligned} \min \sum_{n \in N} F^{n2}(X^{n2}, Z^{n2}) \\ \text{s.t. } h_k^{n2}(X^{n2}, Z^{n2}, t) = 0, \forall t \in T_k^{n2} \\ g_k^{n2}(X^{n2}, Z^{n2}, t) \leq 0, \forall t \in T_k^{n2} \\ x^{n2} \in X^{n2}, z^{n2} \in Z^{n2} \end{aligned}$$

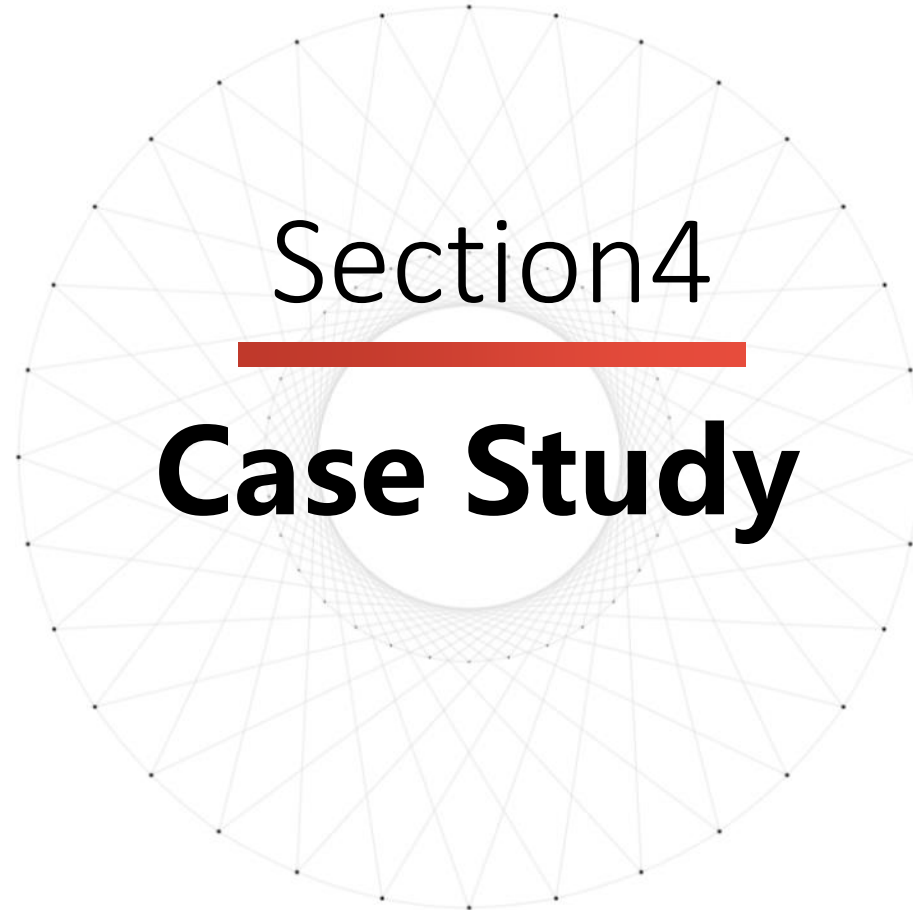
$$\begin{aligned} \min \sum_{n \in N} F^{n3}(X^{n3}, Z^{n3}) \\ \text{s.t. } h_k^{n3}(X^{n3}, Z^{n3}, t) = 0, \forall t \in T_k^{n3} \\ g_k^{n3}(X^{n3}, Z^{n3}, t) \leq 0, \forall t \in T_k^{n3} \\ x^{n3} \in X^{n3}, z^{n3} \in Z^{n3} \end{aligned}$$

$$\begin{aligned} \min \sum_{n \in N} F^{n4}(X^{n4}, Z^{n4}) \\ \text{s.t. } h_k^{n4}(X^{n4}, Z^{n4}, t) = 0, \forall t \in T_k^{n4} \\ g_k^{n4}(X^{n4}, Z^{n4}, t) \leq 0, \forall t \in T_k^{n4} \\ x^{n4} \in X^{n4}, z^{n4} \in Z^{n4} \end{aligned}$$



Process



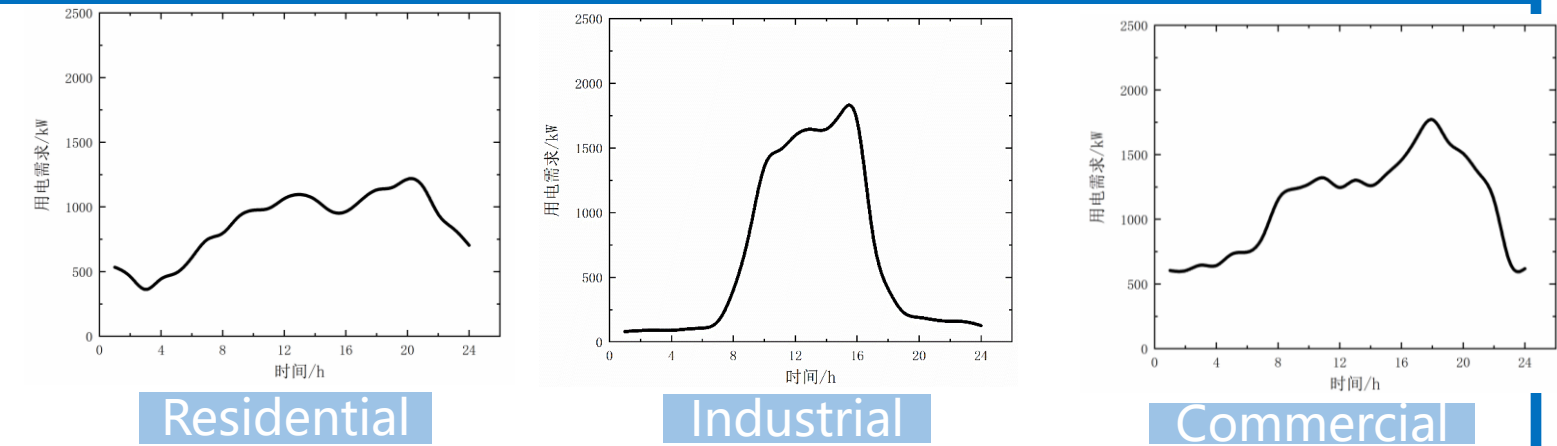


Section4

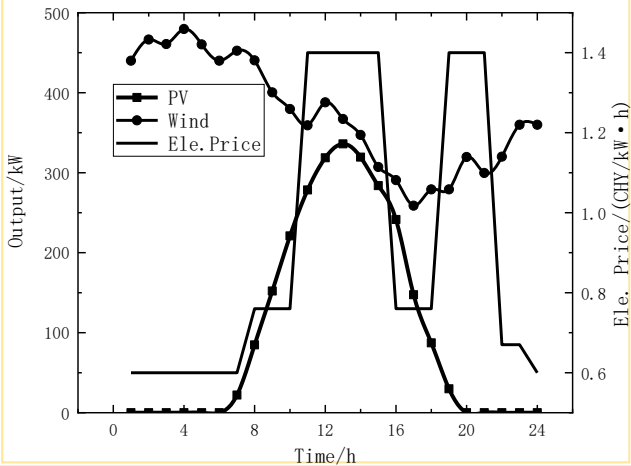
Case Study

4.1 System Parameters

Electricity Demand



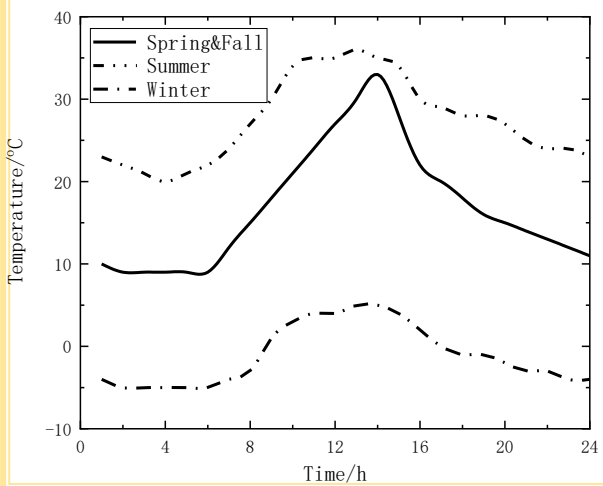
PV&WT&Ele. Price



Device Parameters

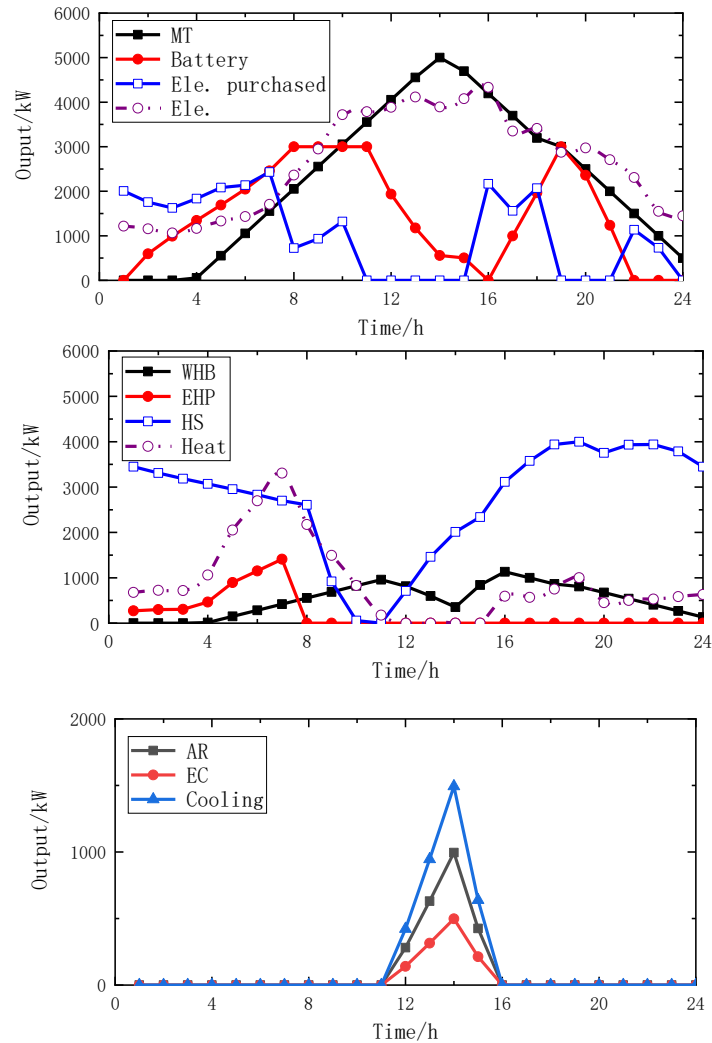
Device	capacity (kW)	maintenance (CHY/kW)	Efficiency
MT	5000	0.03	0.73
EHP	1500	0.02	2
AR	2000	0.015	2.5
EC	2000	0.015	2.5
WHB	1000	0.02	1.5
Battery	3000	0.01	0.95
HS	4000	0.005	0.98

Temperature in seasons

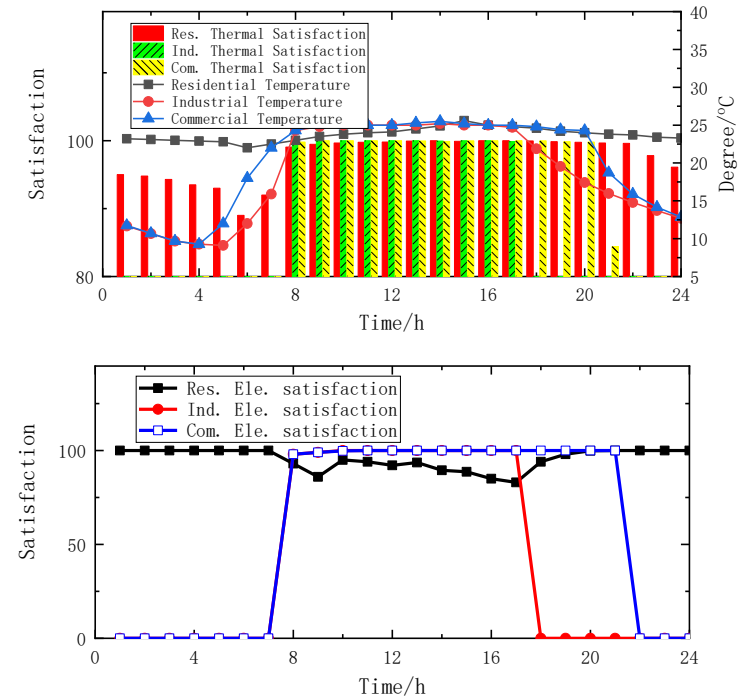


4.2 Results and Analysis

Scheduling Result in Spring&Fall



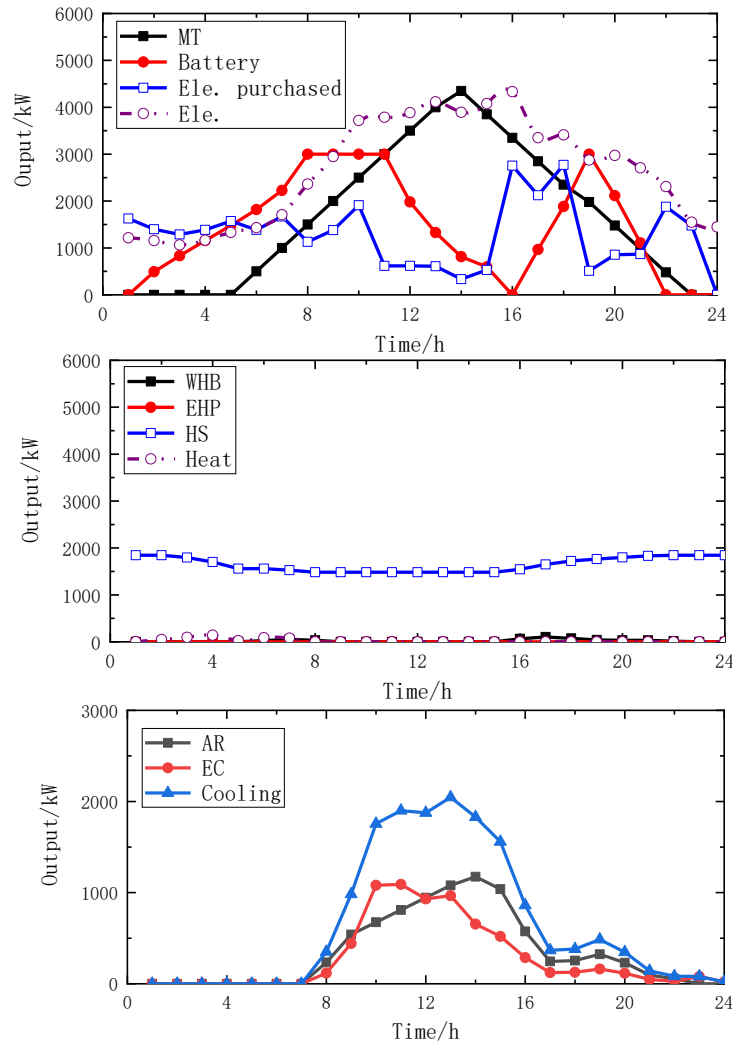
Consumer satisfaction & indoor Tem.



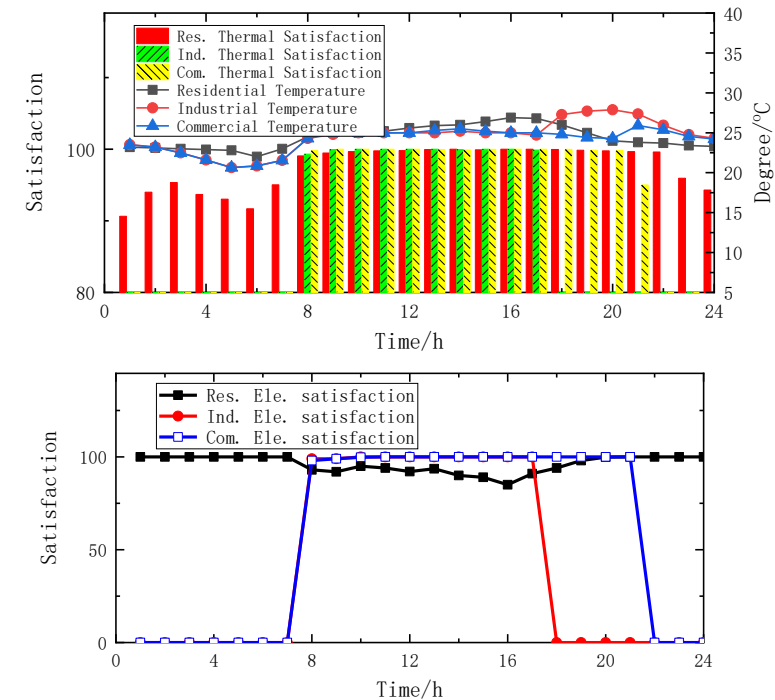
- ◆ MT 5000kW during the peak
- ◆ HS absorb day, release night
- ◆ AR main cooling

4.2 Results and Analysis

Scheduling Result in Summer



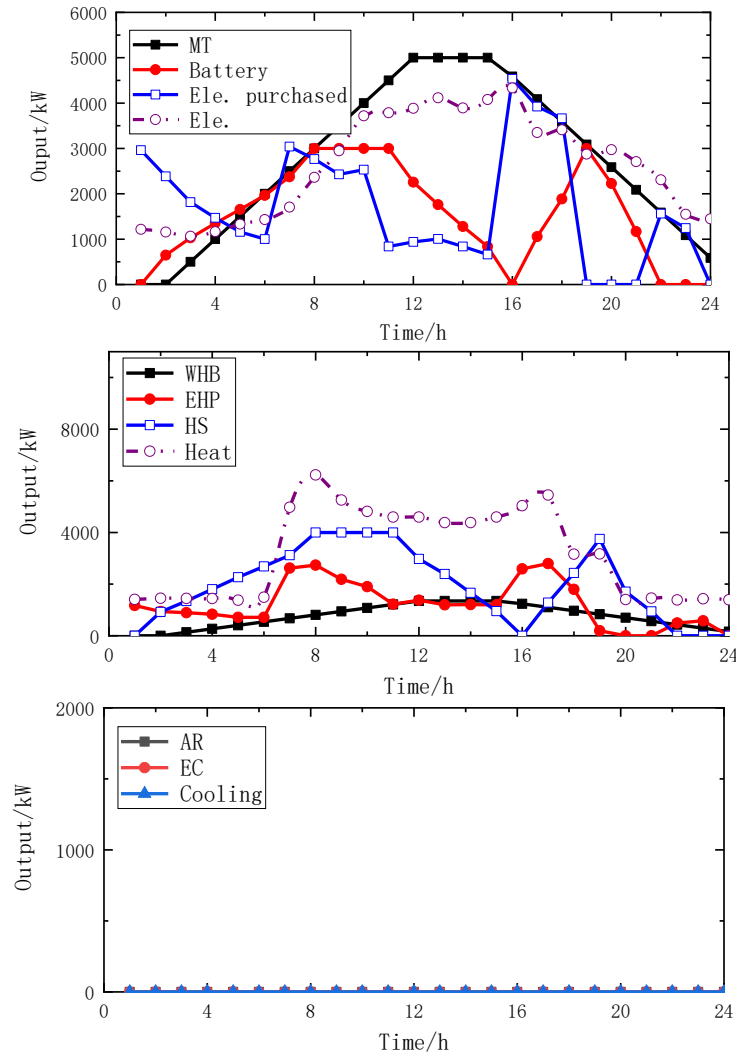
Consumer satisfaction & indoor Tem.



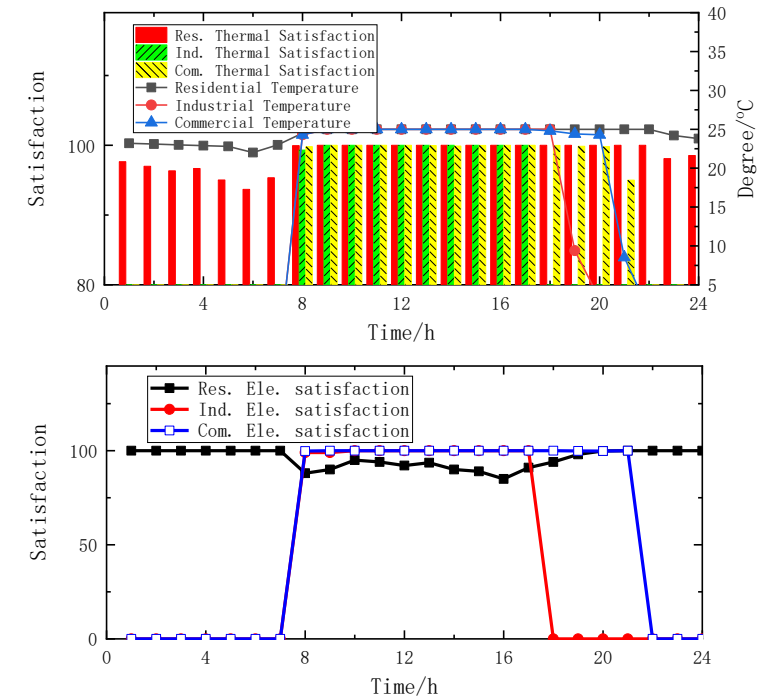
- ◆ MT 4000kW during the peak
- ◆ WHB, HS no work
- ◆ EC, AR for cooling

4.2 Results and Analysis

Scheduling Result in Winter



Consumer satisfaction & indoor Tem.



- ◆ MT afternoon 5000kW
- ◆ Large Heating 8-9am & sunset
- ◆ EHP main in peak time

4.2 Results and Analysis

Economic Result with Flexible Load

	Spr.&Fall	Summer	Winter
IES Operation(CHY)	51433.08	51034.08	72051.99
Res. Cooling (CHY)	380.01	1747.22	0.00
Ind. Cooling (CHY)	879.32	3509.04	0.00
Com. Cooling (CHY)	624.24	2992.68	0.00
Res. Heating (CHY)	3321.51	166.83	10758.28
Ind. Heating(CHY)	2332.34	0.00	8996.12
Com. Heating(CHY)	2776.61	0.00	9777.35
Res. Ele. (CHY)	11993.33	11993.33	11993.33
Ind. Ele. (CHY)	11564.08	11564.08	11564.08
Com. Ele. (CHY)	19509.41	19509.41	19509.41
Cooling Fees (CHY)	1883.57	8248.92	0.00
Heating Fees(CHY)	8430.45	166.83	29848.17
Ele. Fees(CHY)	43066.83	43066.83	43066.83
All Fees(CHY)	53380.86	51482.59	72915.01
Net Revenue(CHY)	1947.77	448.51	863.02

Operation Reduction

Spr.&Fall 15.97%
Summer 11.42%
Winter 20.65%

Consumer Cost Reduction

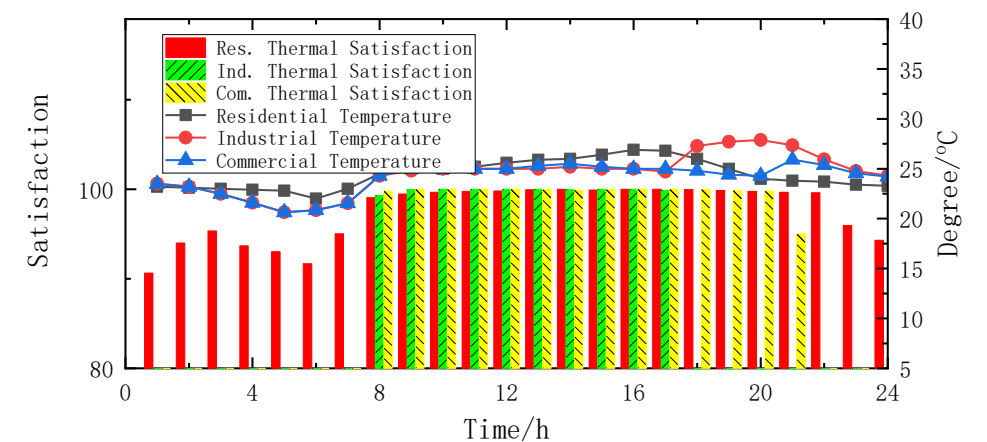
Spr.&Fall 13.32%
Summer 8.25%
Winter 20.21%

Result without Flexible Load

	Spr.&Fall	Summer	Winter
IES Operation(CHY)	61205.38	57618.96	90812.91
Res. Cooling (CHY)	470.49	2163.2	0.00
Ind. Cooling (CHY)	879.32	3509.04	0.00
Com. Cooling (CHY)	636.48	3051.36	0.00
Res. Heating (CHY)	5504.24	276.46	18352.36
Ind. Heating(CHY)	3145.95	0.00	12423.21
Com. Heating(CHY)	3834.35	0.00	13502.06
Res. Ele. (CHY)	15508.62	15508.62	15508.62
Ind. Ele. (CHY)	11564.09	11564.09	11564.09
Com. Ele. (CHY)	20043.92	20043.92	20043.92
Cooling Fees (CHY)	1986.29	8723.60	0.00
Heating Fees(CHY)	12484.51	276.46	44277.64
Ele. Fees(CHY)	47116.63	47116.63	47116.63
All Fees(CHY)	61587.44	56116.71	91394.27
Net Revenue(CHY)	382.06	-1502.26	581.36

4.3 Sensitivity Analysis

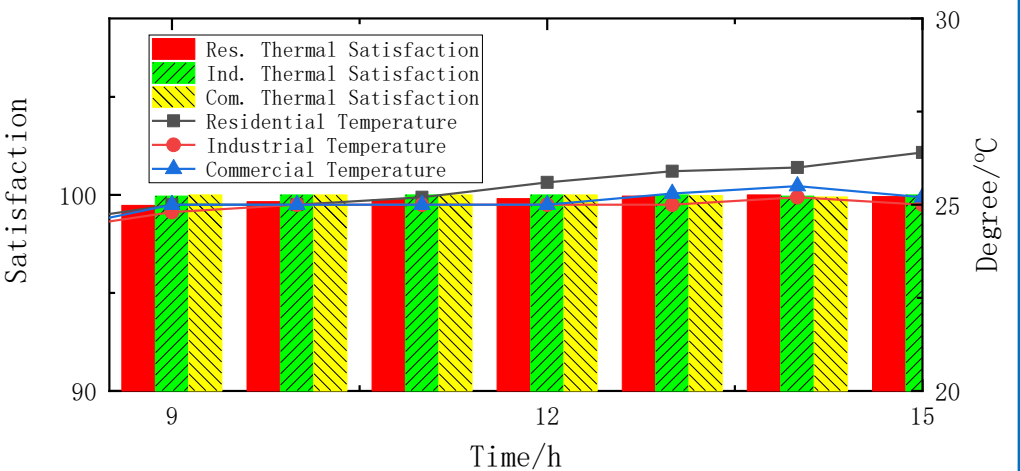
Thermal comfort & Temperature in Sum.



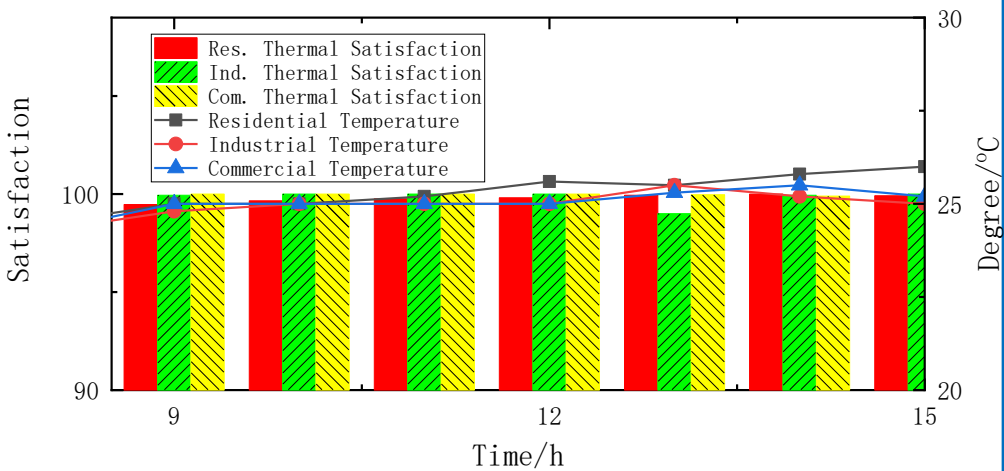
Metabolic
M

Summer
Industrial
Noon break

Without
Noon
Break



With
Noon
Break



A decorative circular geometric pattern composed of many small dots connected by thin lines, forming a complex web-like structure. The pattern is centered on the page and serves as a background for the text.

Section5

Conclusion

5.1 Conclusion

■ **Formulate the consumer satisfaction function to describe the perceived satisfaction of customers**

■ **Personal condition affect the energy flexibility of consumer**

■ **Revenue distributed based on consumer urgency and condition**

5.2 Future Work

■ Refine consumer behavior pattern and satisfaction model

■ Long-term operation optimization & Optimal planning

■ Future participation in the power market

Thank you