



# Lagrangian

$$T = \frac{1}{2} m_1 (l_1 \dot{\theta}_1)^2 + \frac{1}{2} m_2 (l_1 \dot{\theta}_1 + l_2 \dot{\theta}_2)^2 + \frac{1}{2} m_2 l_2^2 \dot{\theta}_2^2$$

$$V = -gm_1 \frac{l_1}{2} \cos \theta_1 - gm_2 \left( \frac{l_1}{2} \cos \theta_1 + \frac{l_2}{2} \cos \theta_2 \right)$$

$$L = T - V$$

$$\left( \frac{1}{2} m_1 l_1^2 + \frac{1}{2} m_2 l_1^2 + m_2 l_1 l_2 \right) \ddot{\theta}_1 + \left( \frac{1}{2} m_2 l_2^2 \right) \ddot{\theta}_2 + \left( \frac{1}{2} m_2 l_1 l_2 \right) \ddot{\theta}_1 = -\left( \frac{1}{2} m_1 l_1 \sin \theta_1 + \frac{1}{2} m_2 l_1 \sin \theta_1 + \frac{1}{2} m_2 l_2 \sin \theta_2 \right) g$$

$$\ddot{\theta}_1 = - \frac{3(gl_1 m_1 \sin \theta_1 + 2gl_1 m_2 \sin \theta_1 - gl_2 m_2 \sin \theta_2)}{2l_2 m_1 - 3l_1 l_2 m_2 + 6l_2 m_2}$$

$$\ddot{\theta}_2 = - \frac{3(-3gl_2 m_1 \sin \theta_1 - 6gl_2 m_2 \sin \theta_1 + 2gl_2 m_1 \sin \theta_2 + 6gl_2 m_2 \sin \theta_2)}{2l_2 (2l_2 m_1 - 3l_1 l_2 m_2 + 6l_2 m_2)}$$