ToFu geometric tools
Take into account non-parallel crystal mesh

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1 Problem details

The definition into *ToFu* geometrical tool of Bragg's crystals has been made to take into account geometrical, material and specific Bragg parameters. As we can see on Fig.1, the crystal of curvature radius R has its center C on coordinates (x_c, y_c, z_c) in the Tokamak frame (O, e_x, e_y, x_z).
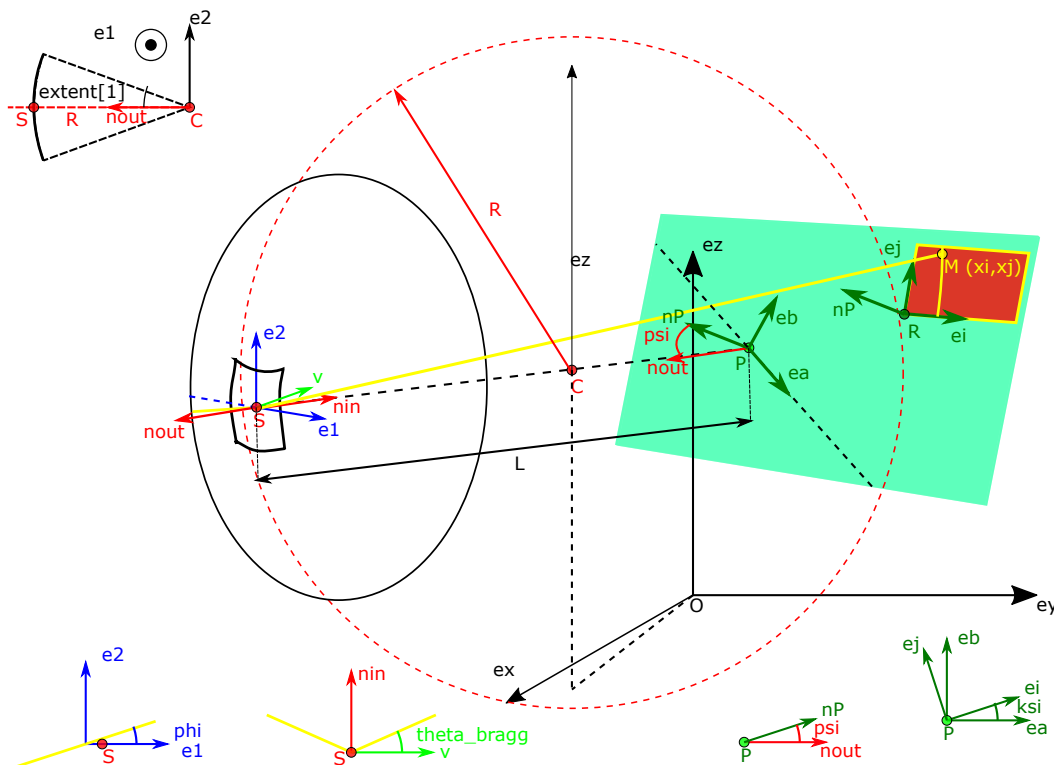

Figure 1: Definition of the generalized geometry

This general description is assumed to be true at any time of the experiment. But there is one major issue that the current definition of the Bragg's crystals doesn't take into account, the non-parallelism of each crystal. As we can see on Fig.2, crystals are industrially made and sold with an index of confidence about the parallelism between the diopter and the crystal mesh. Because every crystal are not perfect, a maximum angle is furnished by the manufacturer, generally in arc-seconds. This defect causes a deviation of the normal vector $\overrightarrow{n_{out}}$ shown in both Fig.1 (colinear to $\overrightarrow{n_{in}}$) and Fig.2 (a deviation $\Delta\alpha$ is drawn).
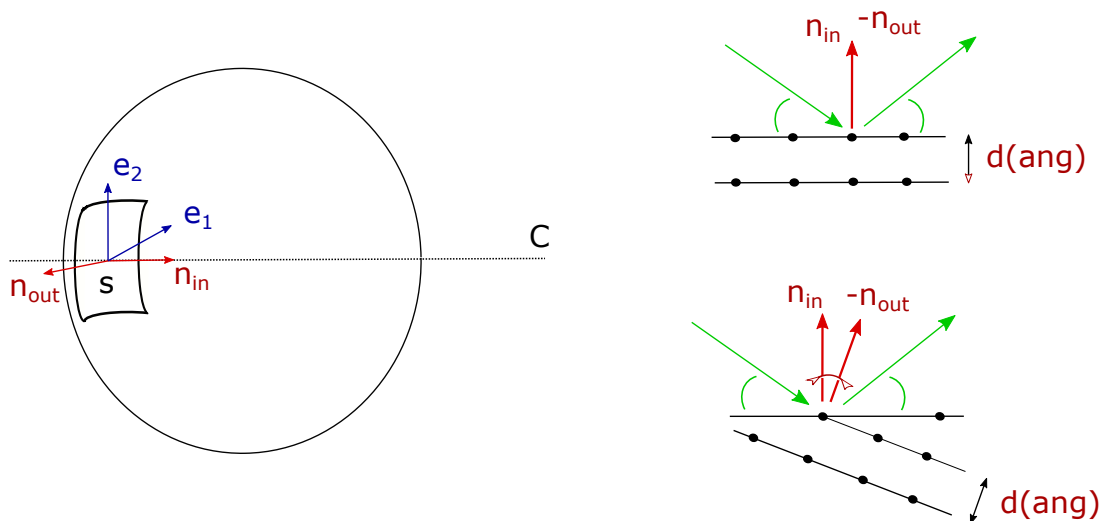

Figure 2: Definition of the non-parallelism between crystal surface and mesh

2 Suggested solution

The main issue due to this property of non-parallelism in each crystal can cause a splitting of the spectral lines. In order to take into account this property, we propose first to define a orthogonal basis in spherical geometry based on the summit S of the crystal, as shown in Fig.3.
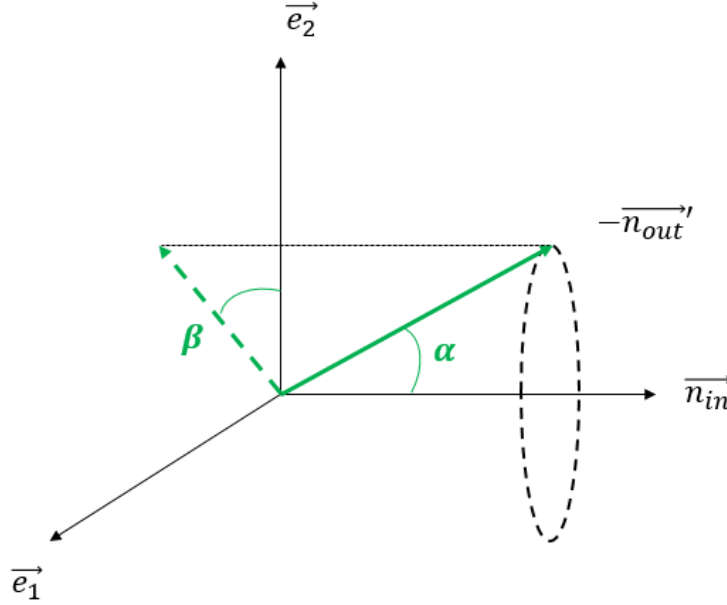

Figure 3: Definition of the the new basis 3D

Thanks to that, we can define easily now the new normal vector to the crystal mesh, which will be useful for few calculations.

$$-\overrightarrow{n_{out}}' = \overrightarrow{n_{in}}' = \frac{1}{cos(\alpha)}.\overrightarrow{n_{in}} + sin(\beta).\overrightarrow{e_1} + cos(\beta).\overrightarrow{e_2} \tag{1}$$

with $\alpha \in [0 \ ; \ \frac{\pi}{2}]$, $\beta \in [0 \ ; \ \pi]$ and $(\overrightarrow{e_1}, \overrightarrow{e_2})$ is the crystal tangent plan on the Rowland sphere.

So in the code, we shall propose the same notation according to Didier's work, (n_{in}, e_1, e_2), in order to prevent some confusion between each set of parameters and to replace the original basis by the new one if the user does not assume perfect parallelism into its crystals.

The point is to let the user decide or not to give any parameter concerning the new basis and in this case the code will, if it's possible mathematically speaking, return all the parameters $(n_{in}, n_{out}, e_1, e_2, \alpha, \beta)$. If he doesn't, then a parallelism configuration will be assumed automatically and a warning notice will be shown in order to notice him about this point. Same thing about the missing of few parameters