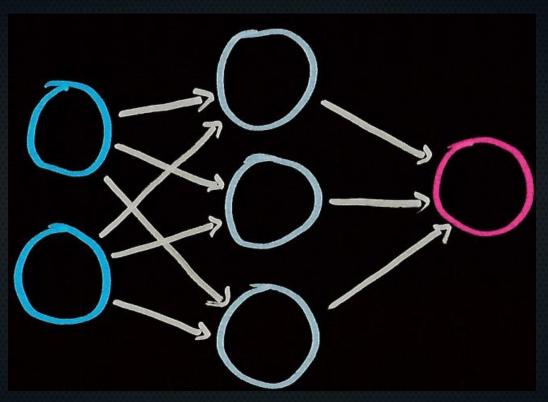
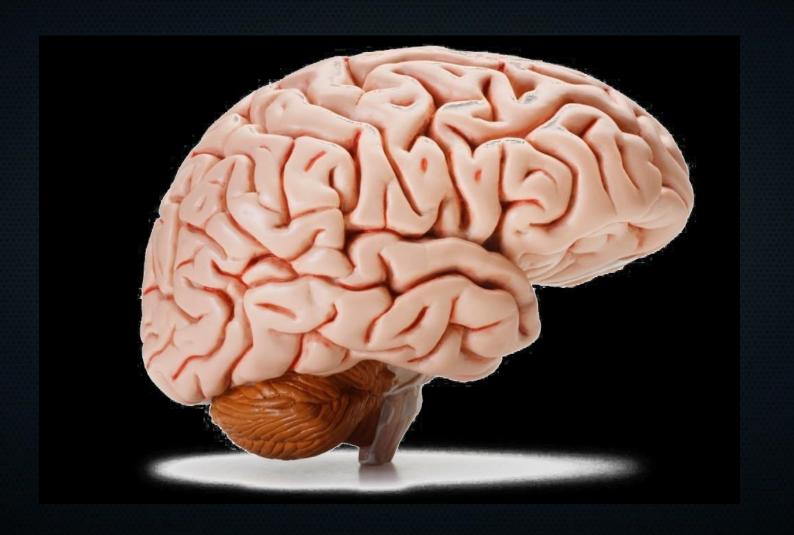
## Switching gears: neural networks

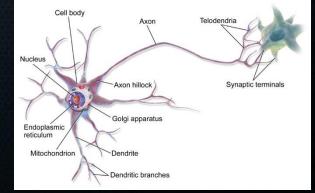


Source: https://thesharperdev.com/build-your-first-neural-network-part-2/



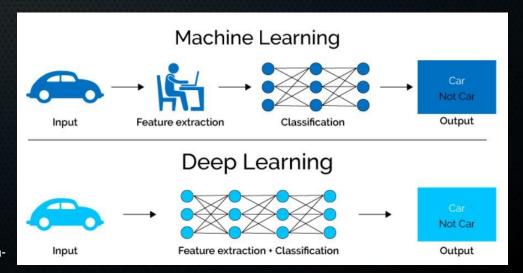
- Best performing algorithms for complex tasks, bar none.
- Known potential of hierarchical organisation of simple units because of biological examples (though neural networks are not good models of actual neurons)
- Observation in frogs and cat visual cortex: there are specific layers of neurons, where earlier layers detect basic shapes

(lines, edges) with later layers incorporating this information into more complex features about what is seen.



Source: https://en.wikipedia.org/wiki/Axon#/media/File:Bla usen\_0657\_MultipolarNeuron.png

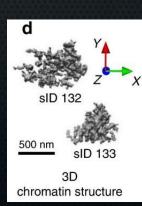
- Until now, we decided on the features to give to our algorithms: think tumour size, biopsy test scores, etc.
- With neural networks and images, the situation changes: we don't arduously describe what is in each image, but rather let the network learn to extract and combine features so that it can classify training examples correctly.

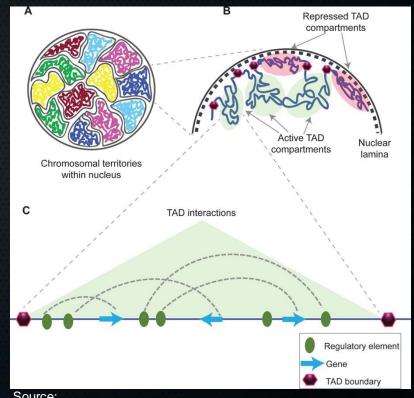


 Caveat for biology: it can be quite difficult to translate biological problems into a framework fit for deep learning.

Example: in images, nearby pixels probably

 hold similar information, i.e. are involved in the same thing. Due to (long-range) 3D-folding of DNA, linearly far DNA can be close together functionally. You need to encode your network or input to accomodate this!

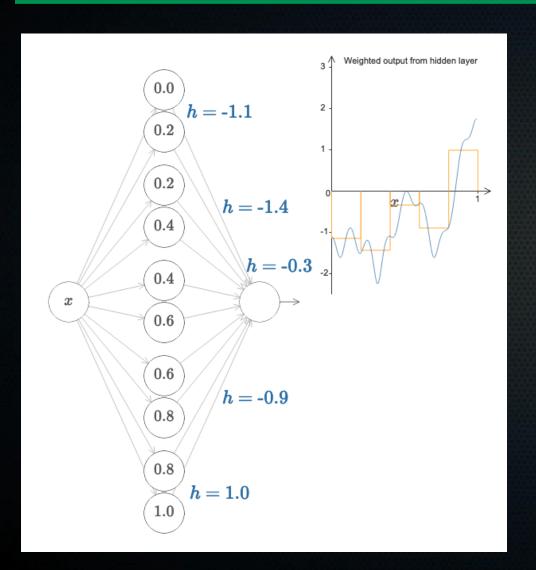


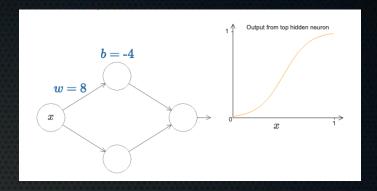


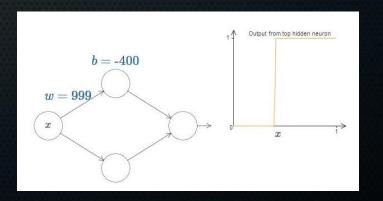
Source: https://en.wikipedia.org/wiki/Topologically\_associating\_domain#/media/File:Structural\_organization\_of\_chromatin.png

 The mythical property of universal approximation. This says that neural networks can approximate any function with arbitrary accuracy, even with only 1 hidden layer (given enough neurons in it).

- The mythical property of universal approximation. This says that neural networks can approximate any function with arbitrary accuracy, even with only 1 hidden layer (given enough neurons in it).
- Of course, that doesn't necessarily mean we would have the data to train such a neural network efficiently. Just that it is provable that for any continuous function a neural network can exist that approximates it as well as you like.

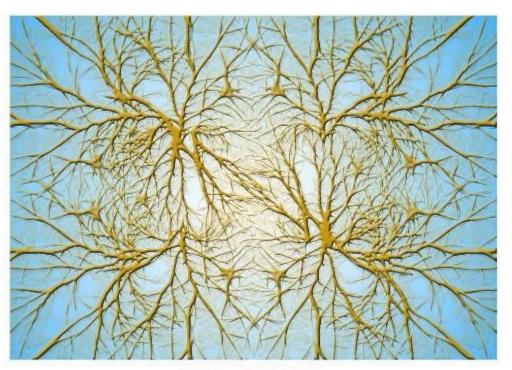




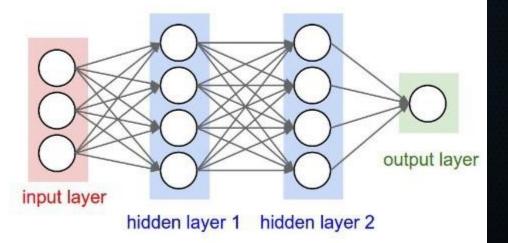


### Like biology? No

#### Biological Neurons: Complex connectivity patterns



Neurons in a neural network: Organized into regular layers for computational efficiency



This image is CC0 Public Domain

### Like biology? No

#### **Biological Neurons:**

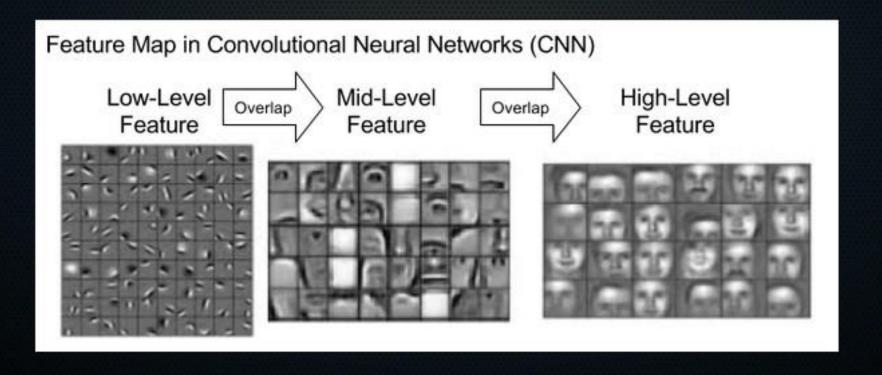
- Many different types
- Dendrites can perform complex non-linear computations
- Synapses are not a single weight but a complex non-linear dynamical system

Source: http://cs231n.stanford.edu/slides/2019/cs231n\_2019\_lecture04.pdf

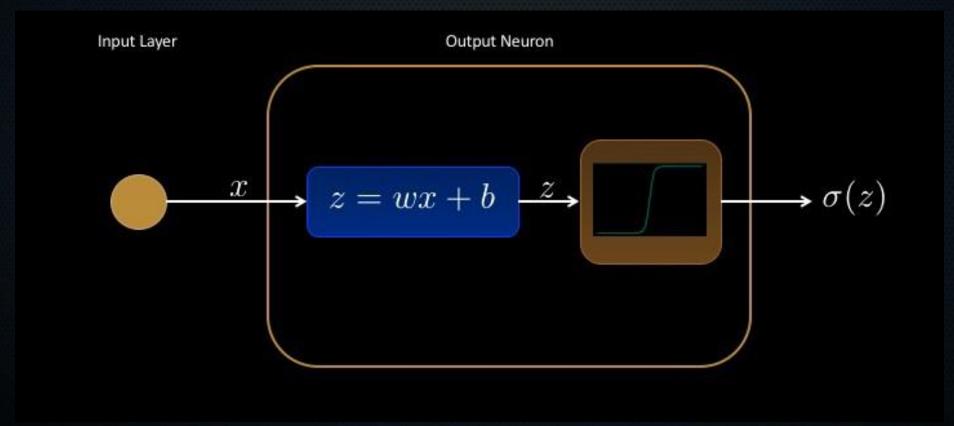
- Human brains ~a cool 86 billion neurons
- A neuron can have 400.000 dendrites
- Real brains vastly outclass their computational analogues

### Like biology? No

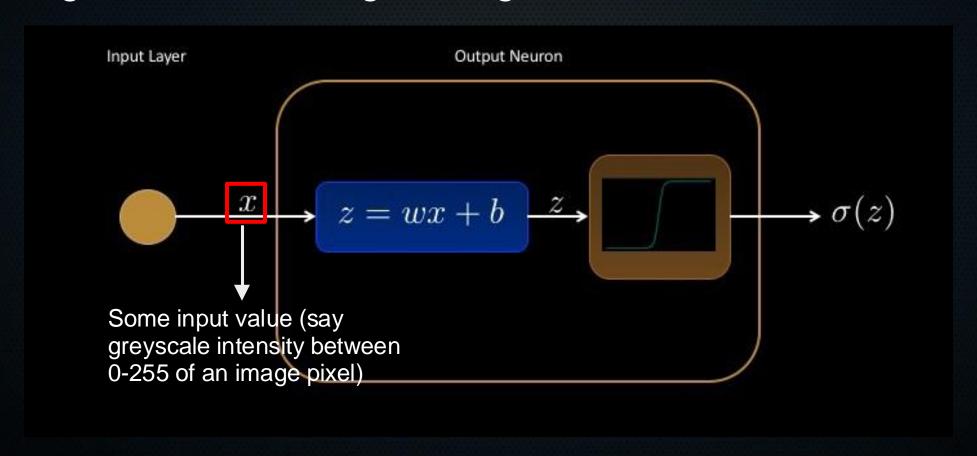
- Still extremely useful
- Parts of how they learn superficially resemble how we learn

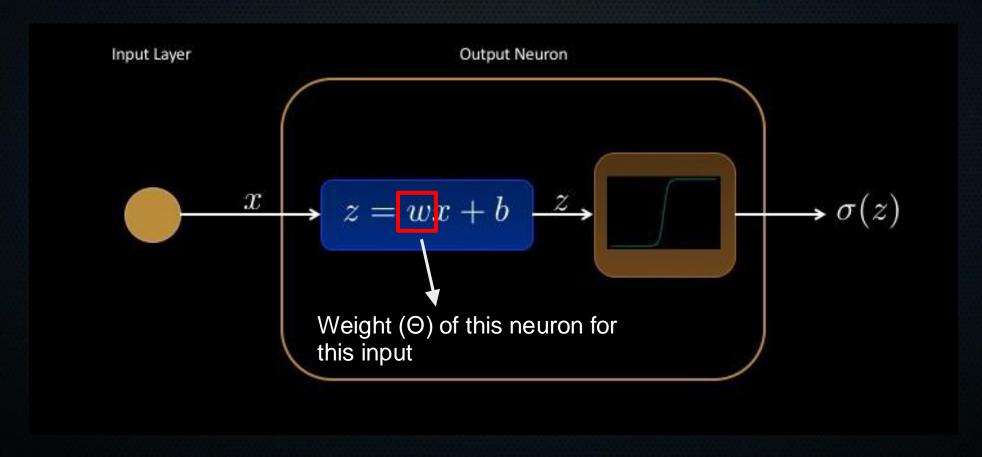


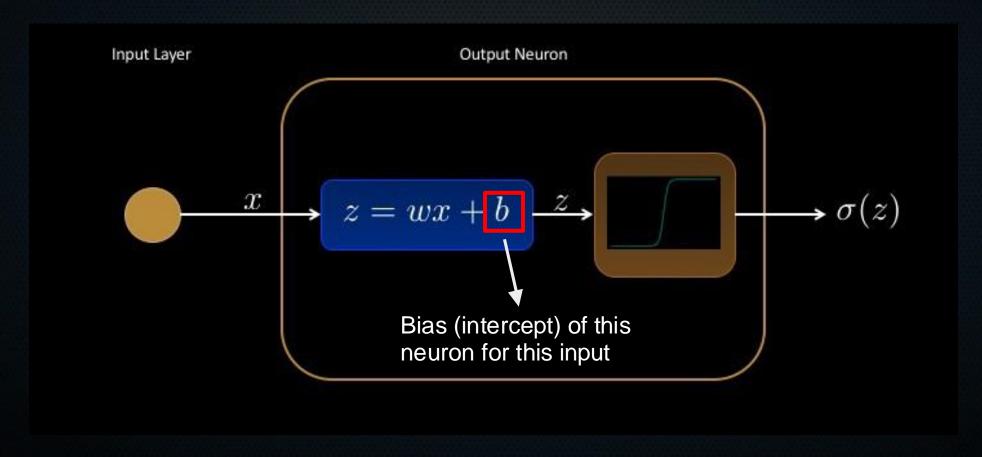
A single neuron is a logistic regressor!\*

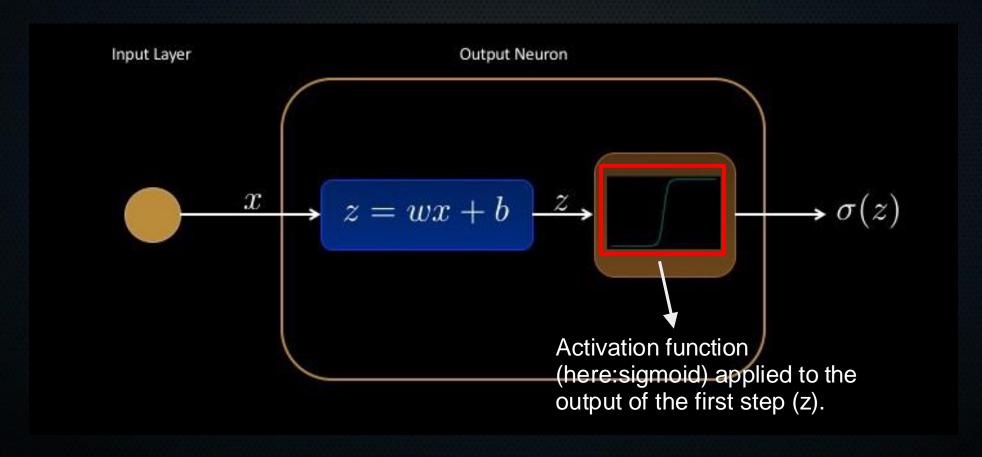


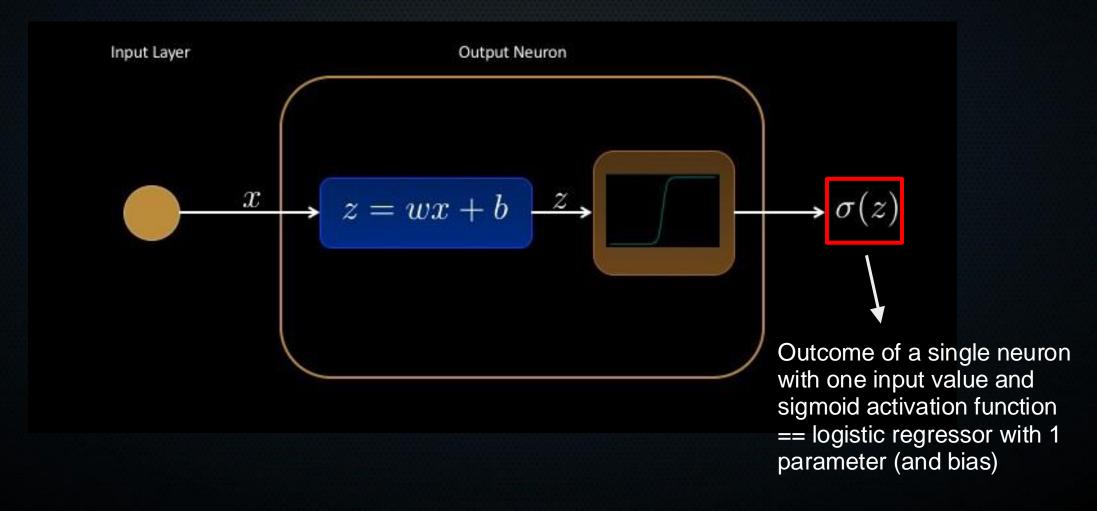
Source: https://thedatafrog.com/en/articles/logistic-regression/

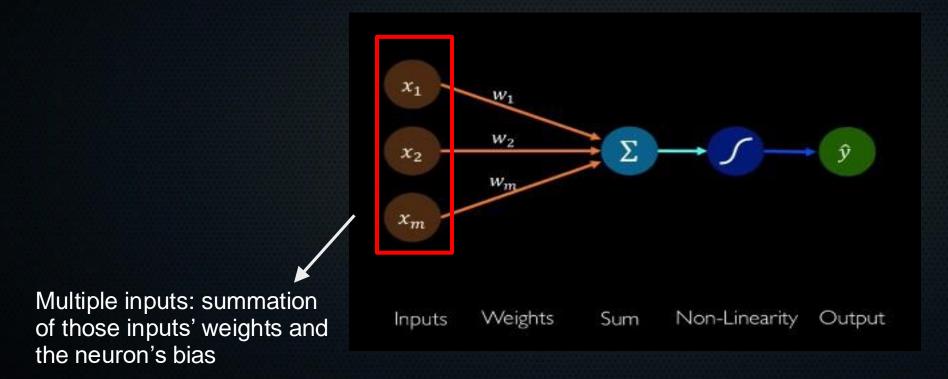


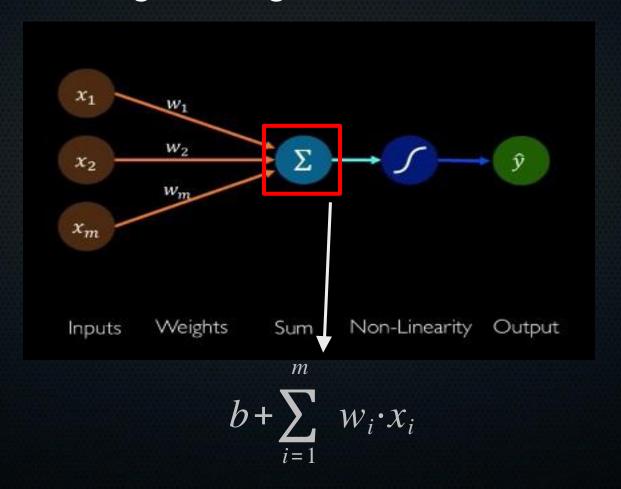


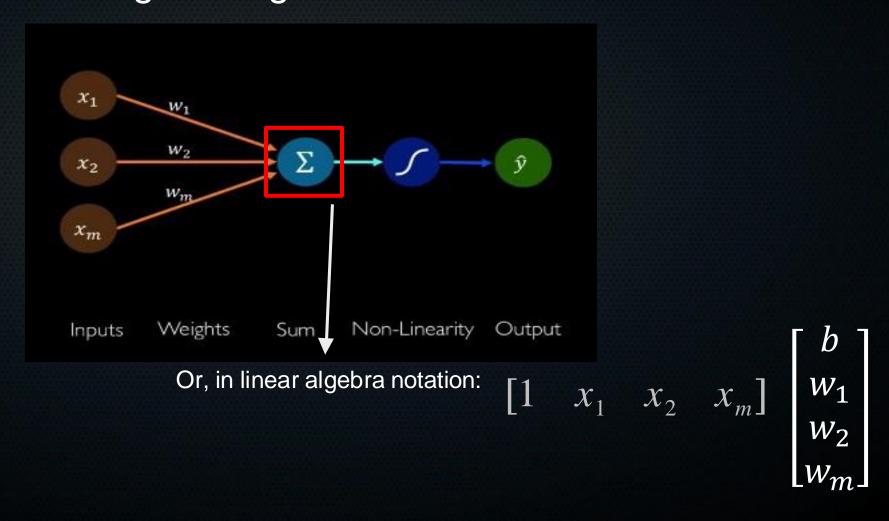


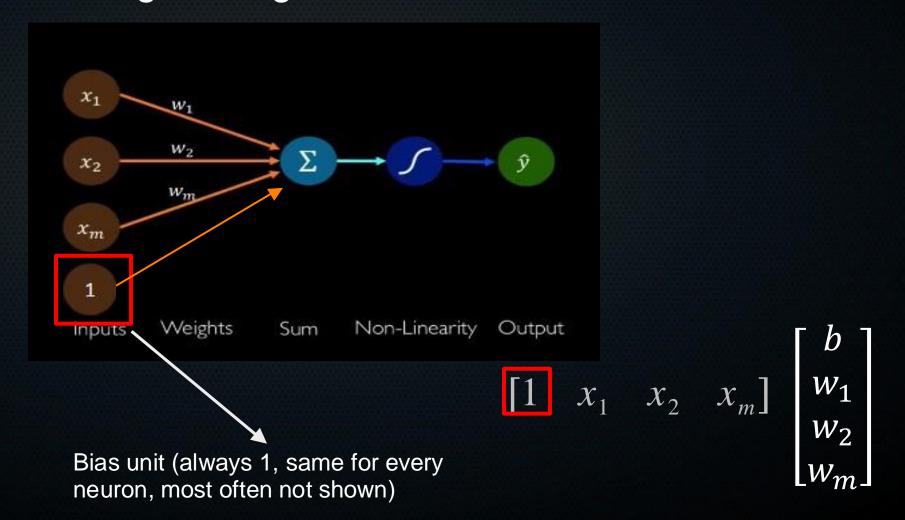


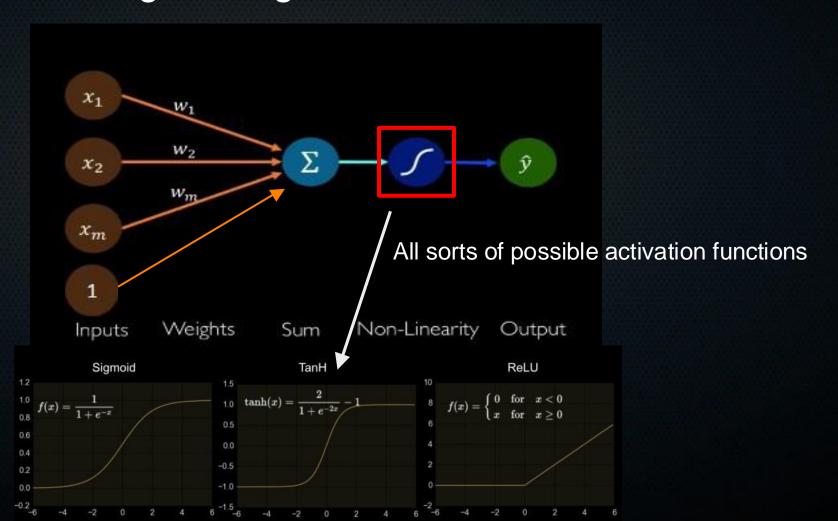






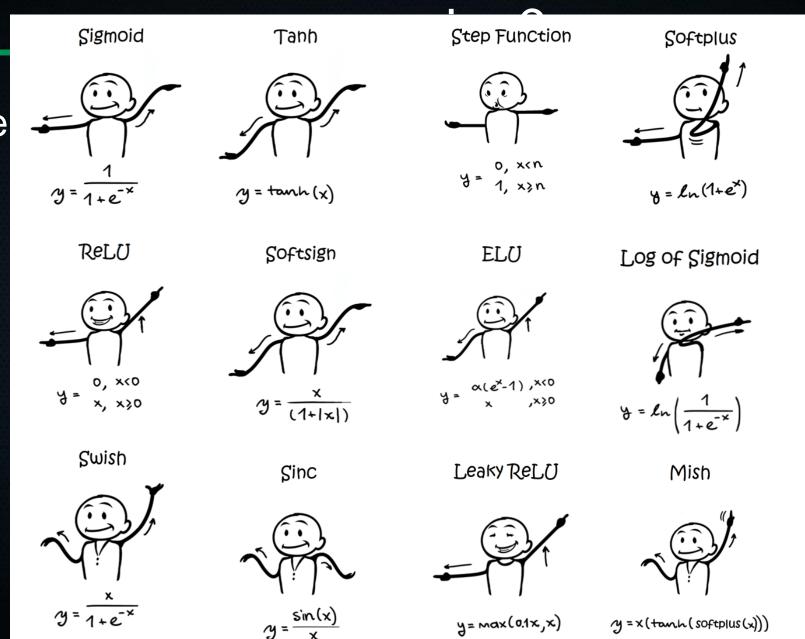






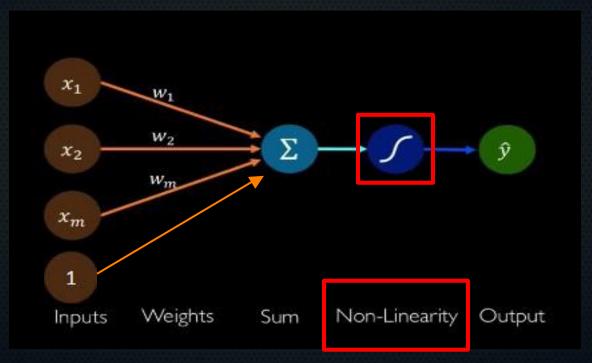
### What do neural nets have to do with logistic

A single



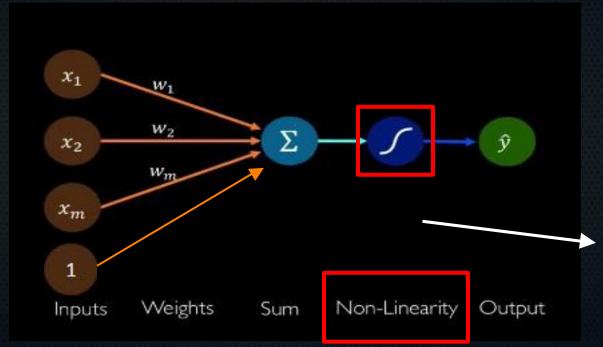
n functions

A single neuron is a logistic regressor!

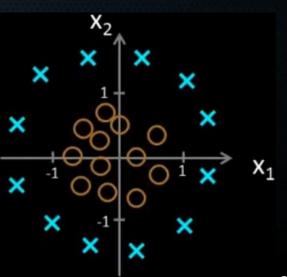


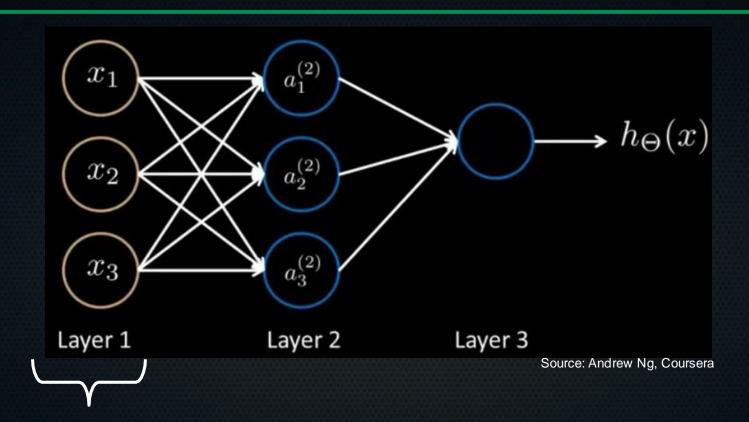
Why non-linearity?

A single neuron is a logistic regressor!

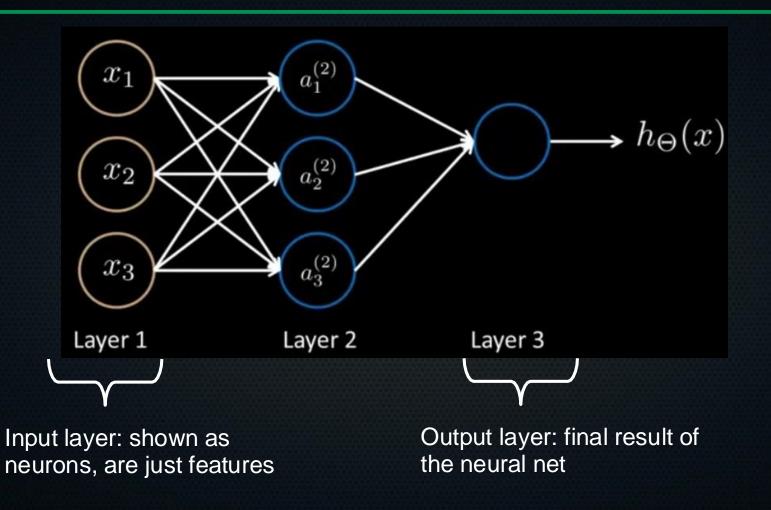


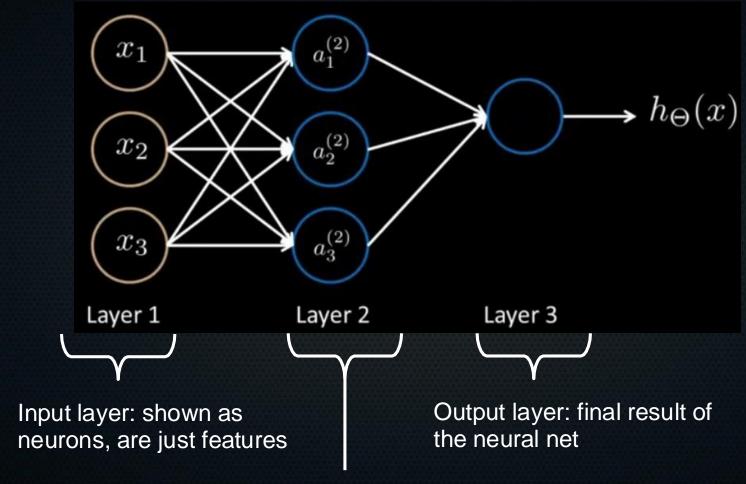
 Why non-linearity? → without them, a NN (no matter how deep) could only approximate linear functions



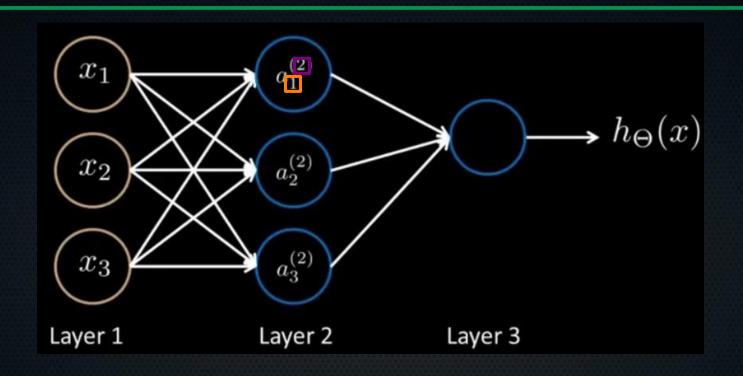


Input layer: shown as neurons, are just features

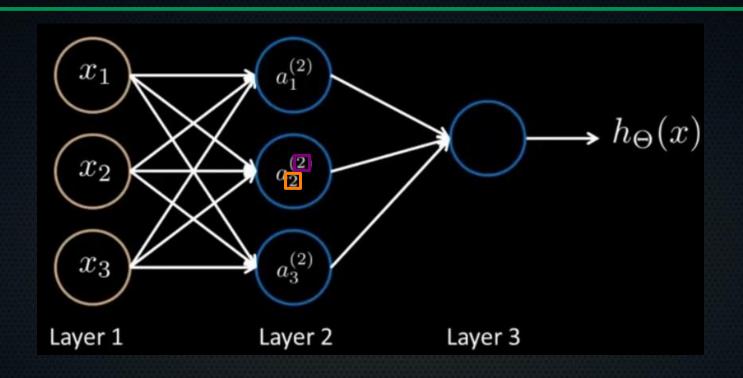




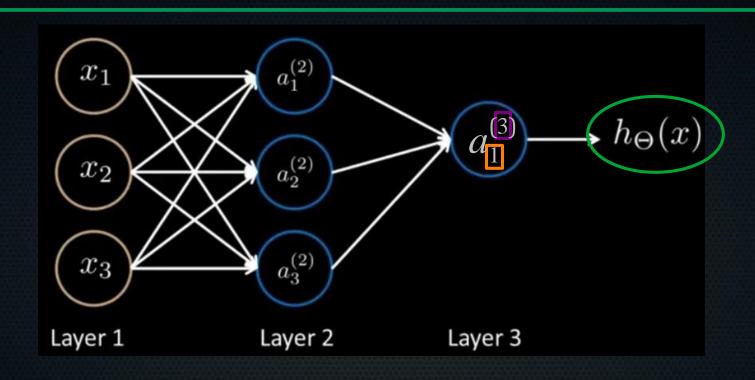
Hidden layer(s): intermediate layers whose outputs are not directly observed (hence hidden). Here: 1 HL. Facebook's DenseNet family of NNs had 121-264 HLs in 2016 (0.8-15.3 million parameters).



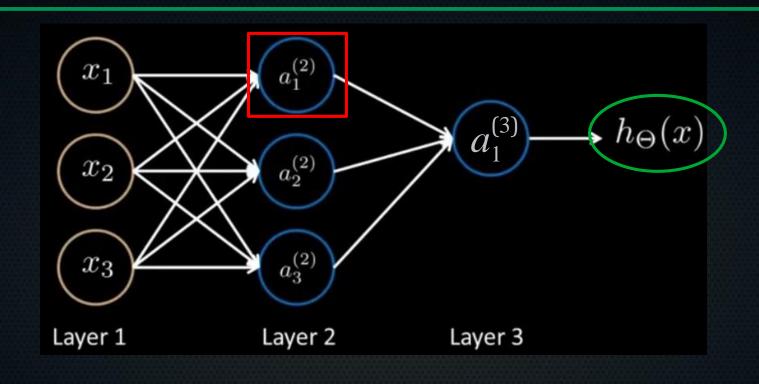
Activation of neuron 1 in the 2<sup>nd</sup> layer of the network.



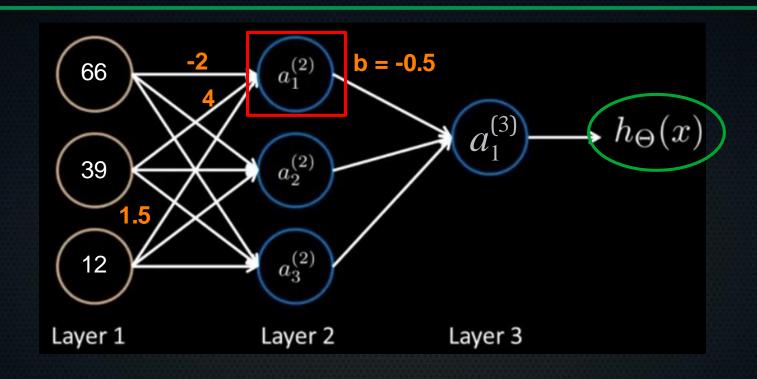
Activation of neuron 2 in the 2<sup>nd</sup> layer of the network.



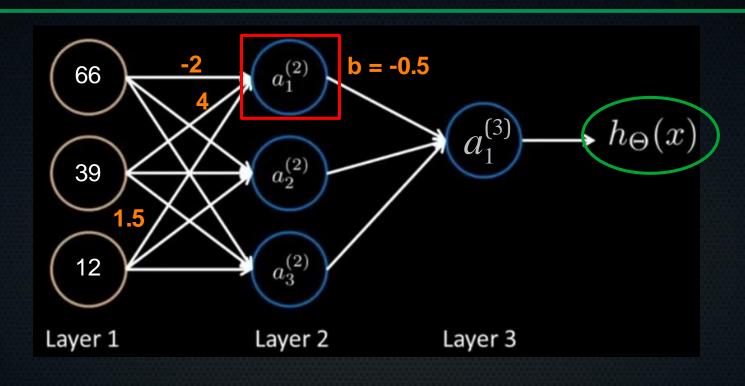
Activation of neuron 1 in the 3rd layer of the network.



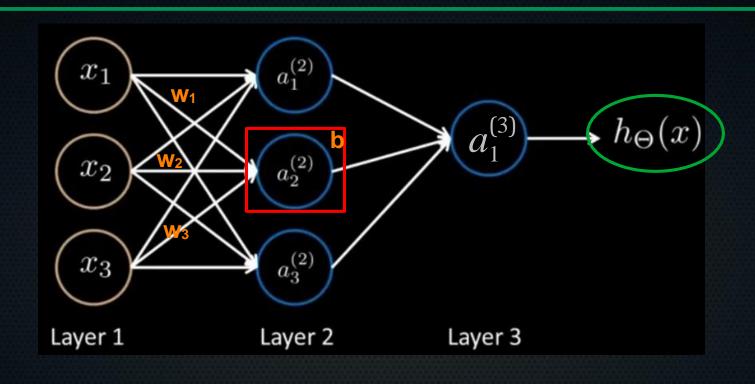
$$\sigma(\begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix})$$



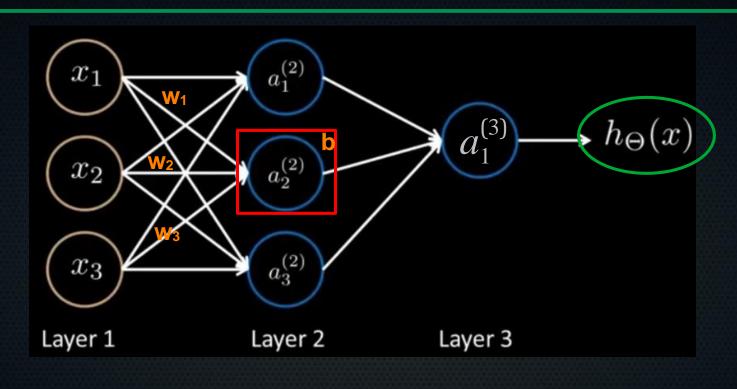
$$\sigma([1 \ x_1 \ x_2 \ x_3] \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix}) \rightarrow \sigma([1 \ 66 \ 39 \ 12] \begin{bmatrix} -0.5 \\ -2 \\ 4 \\ 1.5 \end{bmatrix})$$



$$\sigma([1\ 66\ 39\ 12]\begin{bmatrix} -0.5\\ -2\\ 4\\ 1.5 \end{bmatrix}) \rightarrow \sigma(41.5) \rightarrow 0.999...$$

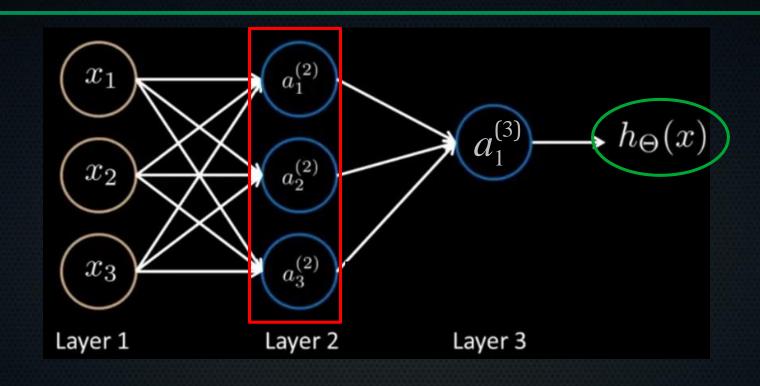


$$\sigma(\begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix})$$



$$\sigma\left(\begin{bmatrix}1 & x_1 & x_2 & x_3\end{bmatrix}\begin{bmatrix}b\\w_1\\w_2\\w_3\end{bmatrix}\right) \longrightarrow \begin{array}{l} \text{Calculate for all units at the same time with a theta matrix } \Theta^{(j)}\\ \text{a theta matrix$$

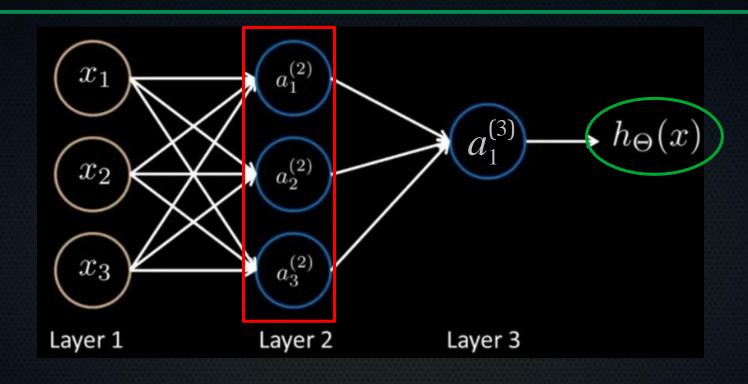
# What is this network calculating?



$$\sigma([1 \quad x_1 \quad x_2 \quad x_3] \begin{bmatrix} b_1 & b_2 & b_3 \\ w_{11} & w_{21} & w_{31} \\ w_{12} & w_{22} & w_{32} \\ w_{13} & w_{23} & w_{33} \end{bmatrix}) \longrightarrow \sigma([1 \quad 2 \quad 3])$$

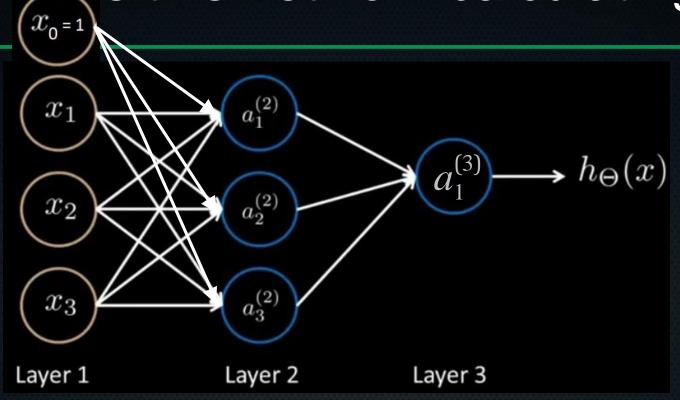
$$[\sigma(1) \quad \sigma(2) \quad \sigma(3)]$$

#### What is this network calculating?



$$\sigma\left(\begin{bmatrix} b_1 & w_{11} & w_{12} & w_{31} \\ b_2 & w_{21} & w_{22} & w_{23} \\ b_3 & w_{31} & w_{32} & w_{33} \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix}\right) \longrightarrow \sigma\left(\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}\right) \longrightarrow \begin{bmatrix} \sigma(1) \\ \sigma(2) \\ \sigma(3) \end{bmatrix}$$

## What is this network calculating?



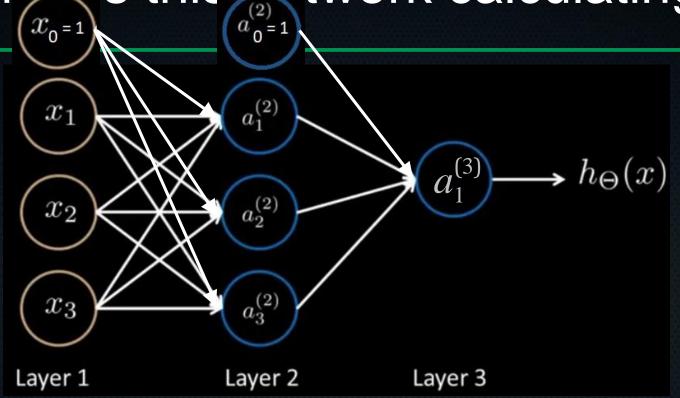
$$a_1^{(2)} = g(\Theta_{10}^{(1)}x_0 + \Theta_{11}^{(1)}x_1 + \Theta_{12}^{(1)}x_2 + \Theta_{13}^{(1)}x_3)$$

$$a_2^{(2)} = g(\Theta_{20}^{(1)}x_0 + \Theta_{21}^{(1)}x_1 + \Theta_{22}^{(1)}x_2 + \Theta_{23}^{(1)}x_3)$$

$$a_3^{(2)} = g(\Theta_{30}^{(1)}x_0 + \Theta_{31}^{(1)}x_1 + \Theta_{32}^{(1)}x_2 + \Theta_{33}^{(1)}x_3)$$

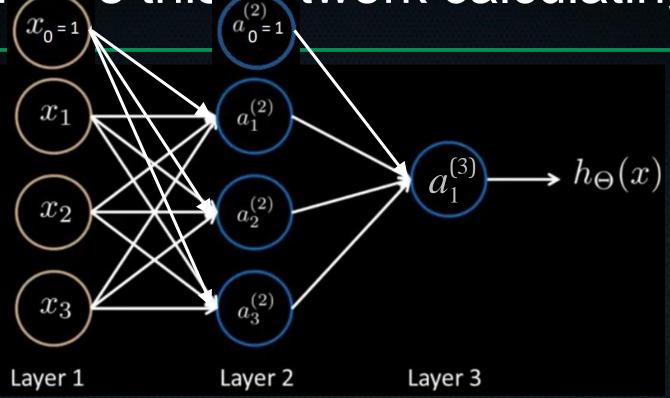
$$\Theta$$
(1) (layer 1 to layer 2)

What is this notwork calculating?  $x_0=1$ 



$$h_{\Theta}(x) = a_1^{(3)} = g(\Theta_{10}^{(2)} a_0^{(2)} + \Theta_{11}^{(2)} a_1^{(2)} + \Theta_{12}^{(2)} a_2^{(2)} + \Theta_{13}^{(2)} a_3^{(2)}) \qquad \begin{bmatrix} b_1 & w_{11} & w_{12} & w_{13} \end{bmatrix}$$

What is this notwork calculating?  $x_0=1$ 



This calculation of the output of the network is called forward propagation

## How do we perform?

- Just like before, there is a cost function.
- But we will talk about that and its implementation tomorrow!

# How do we get parameters?

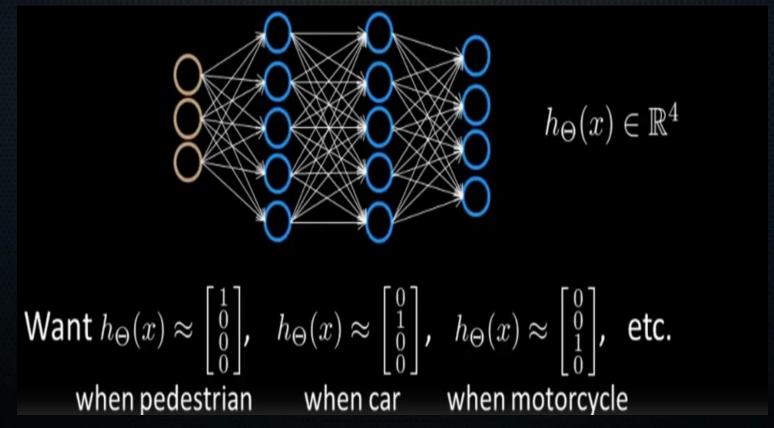
- Just like before, there is a cost function and a way to minimise this. But it's a bit more involved.
- To get parameters, we will use the principle of backpropagation. We'll get to that tomorrow.

#### Recap so far

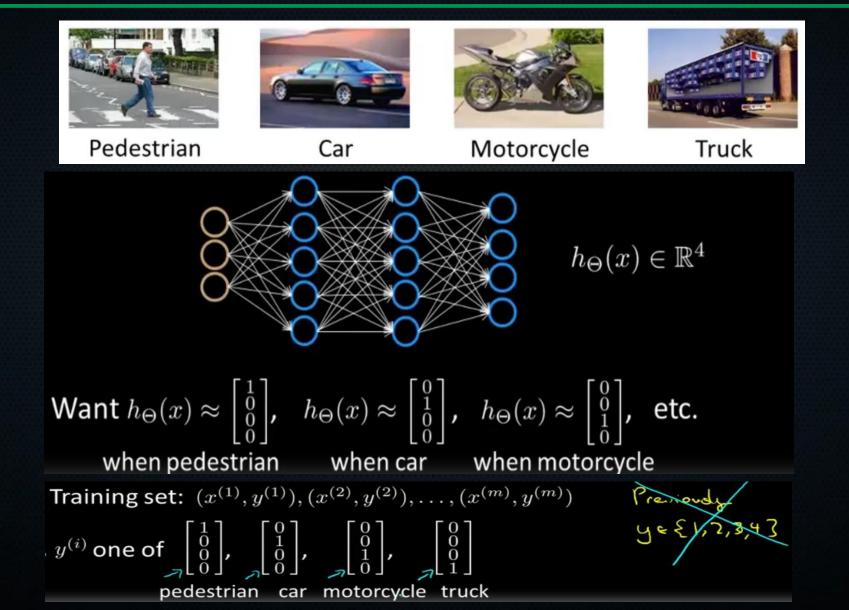
- Neurons in neural networks are not really like biological neurons, except superficially
- Neural networks can be thought of as hiërarchical sets of logistic regressors
- We essentially make earlier layers learn useful features for distinction on their own, and can use these best possible learned features for the classification by the final unit(s)
- Parsing an example through the network and getting the output is called forward propagation
- Universal approximation holds that, in principle, neural networks can learn any continuous function arbitrarily well

#### Multiclass classification in neural nets





#### Multiclass classification in neural nets

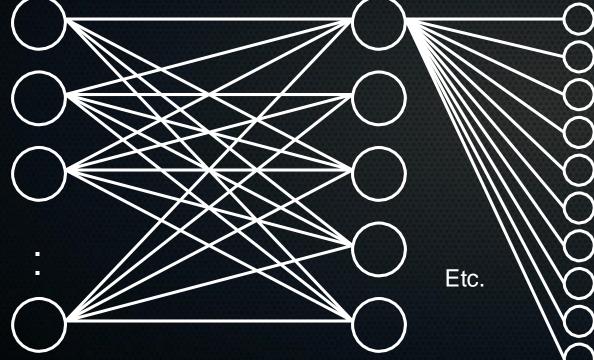


## Question to you

Say we have 10 classes and the following network, how many

parameters in  $\Theta^{(2)}$ ?

 $\Theta^{(j)} = \text{matrix of weights controlling} \\ \text{function mapping from layer } j \text{ to} \\ \text{layer } j+1$ 



 $y^{(10)} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$  Example: 10th training sample is class 3

#### Question to you

Say we have 10 classes and the following network, how many

Etc.

parameters in  $\Theta^{(2)}$ ?

 $\Theta^{(j)} = \mbox{matrix of weights controlling} \label{eq:theta-point} function mapping from layer <math display="inline">j$  to layer j+1

 $y^{(10)} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ 

Example: 10th training sample is class 3

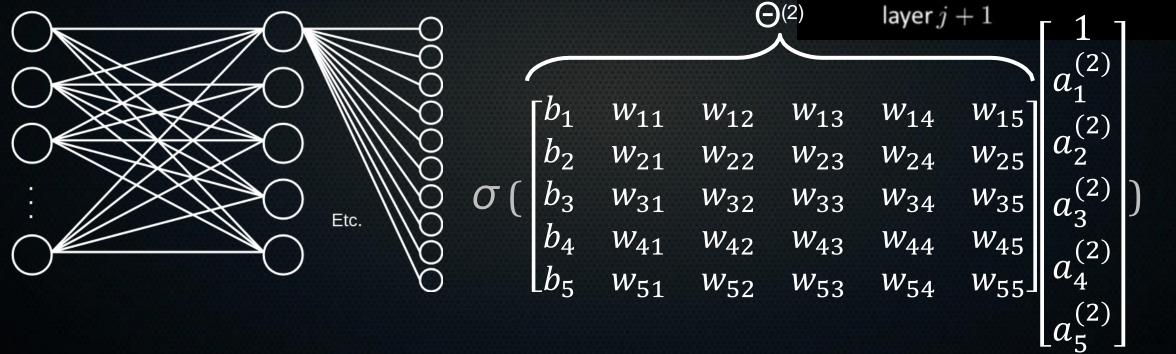
Answer: 60. 5\*10 → weights between units.

+ 10  $\rightarrow$  bias of each unit in output layer  $\lfloor 0 \rfloor$ 

## Question to you

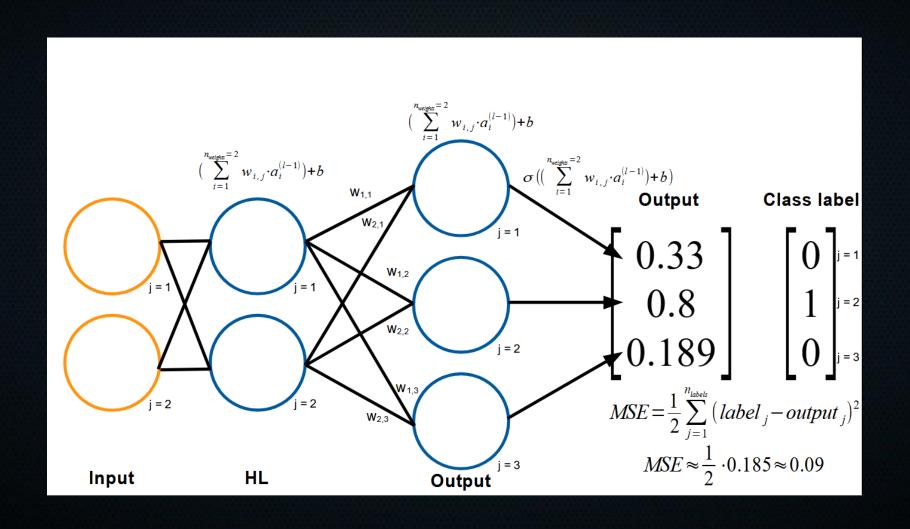
- Say we have 10 classes and the following network, how many parameters in  $\Theta^{(2)}$ ?

function mapping from layer j to



Answer: 60. 5\*10 → weights between units.
 + 10 → bias of each unit in output layer

#### Walk through of linear algebra



#### Please git pull

To pull changes from git while keeping your own modifications:

```
git stash
```

remove any .ipynb\_checkpoints folder in your practical material if git is mad about them (rm --rf .ipynb\_checkpoints). These files are saved states of your notebook, but the .ipynb also has a saved state. It's basically a very simple form of backup, which you don't need.

git pull

git pop stash

Or use github desktop: https://desktop.github.com/download/

## Summary

- We can use individual neurons to calculate simple logic functions
- We can combine the outputs of single neurons to calculate more complex (logic) functions
- For multiclass classification, we simply make class a vector, where we strive for the real class to be 1, and all other classes 0.

# Time for the afternoon practical! \*and continuing where you are

