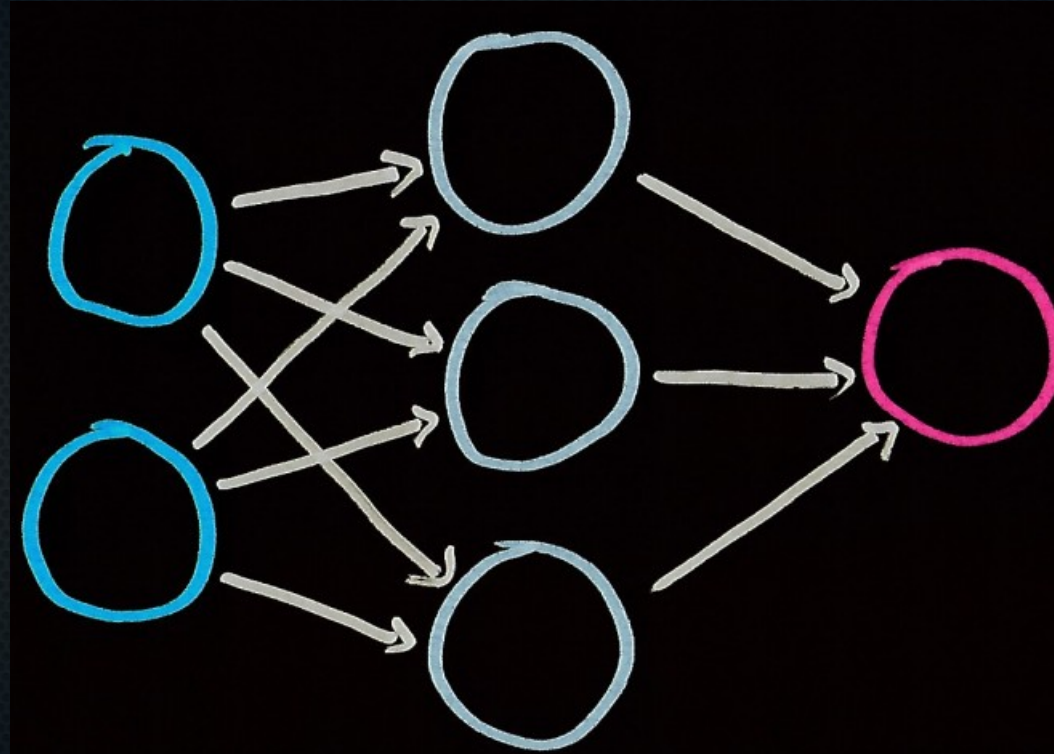


# Switching gears: neural networks

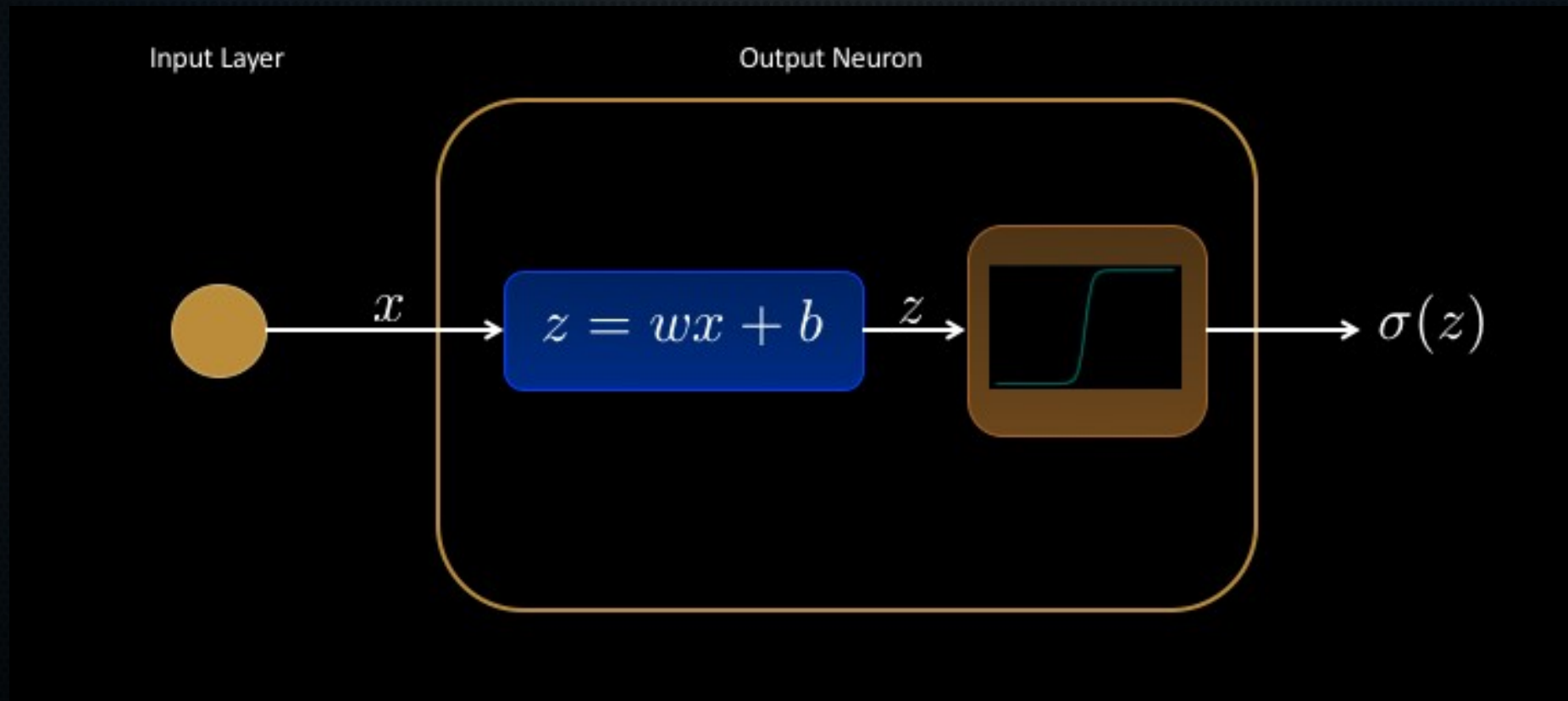
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Source: <https://thesharperdev.com/build-your-first-neural-network-part-2/>

# What do neural nets have to do with logistic regression?

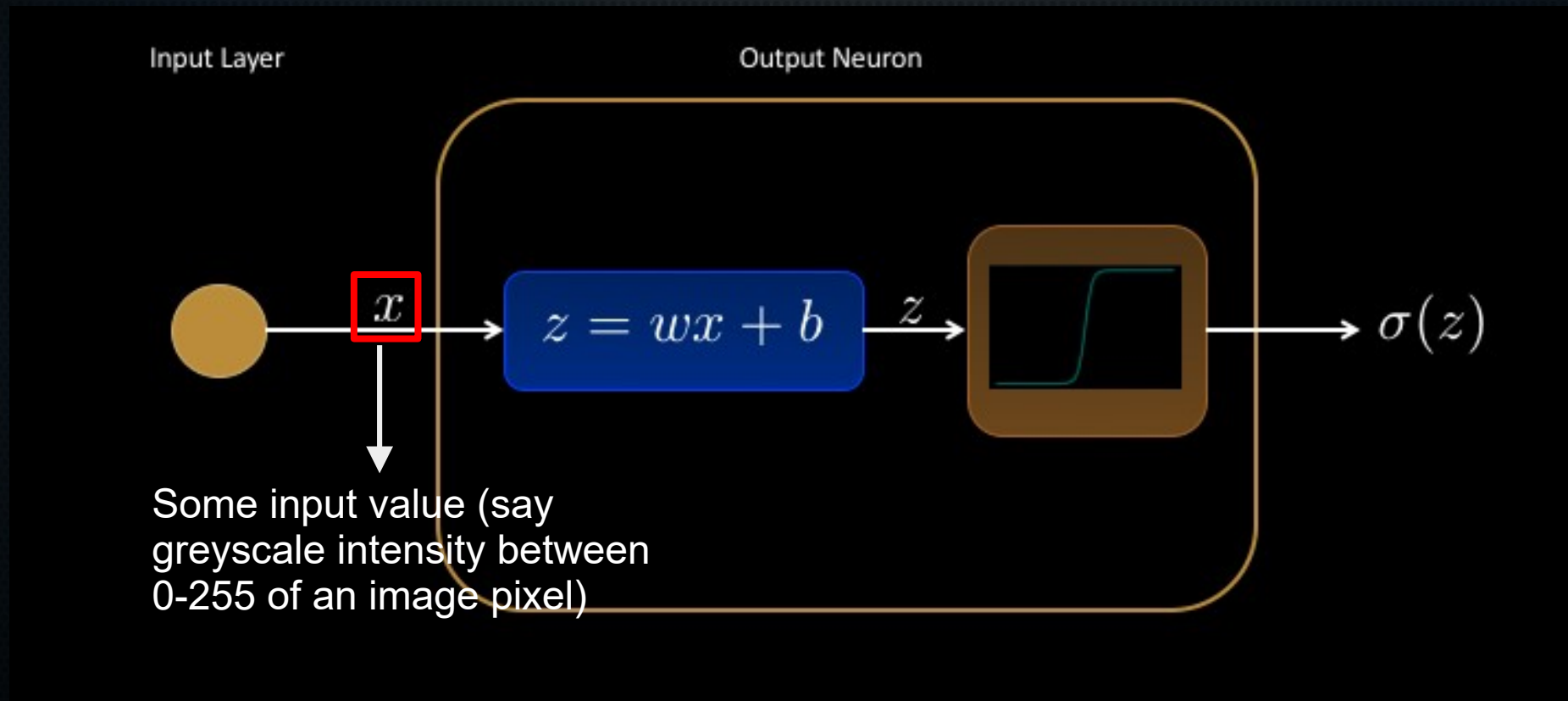
- A single neuron is a logistic regressor!\*



Source: <https://thedatafrog.com/en/articles/logistic-regression/>

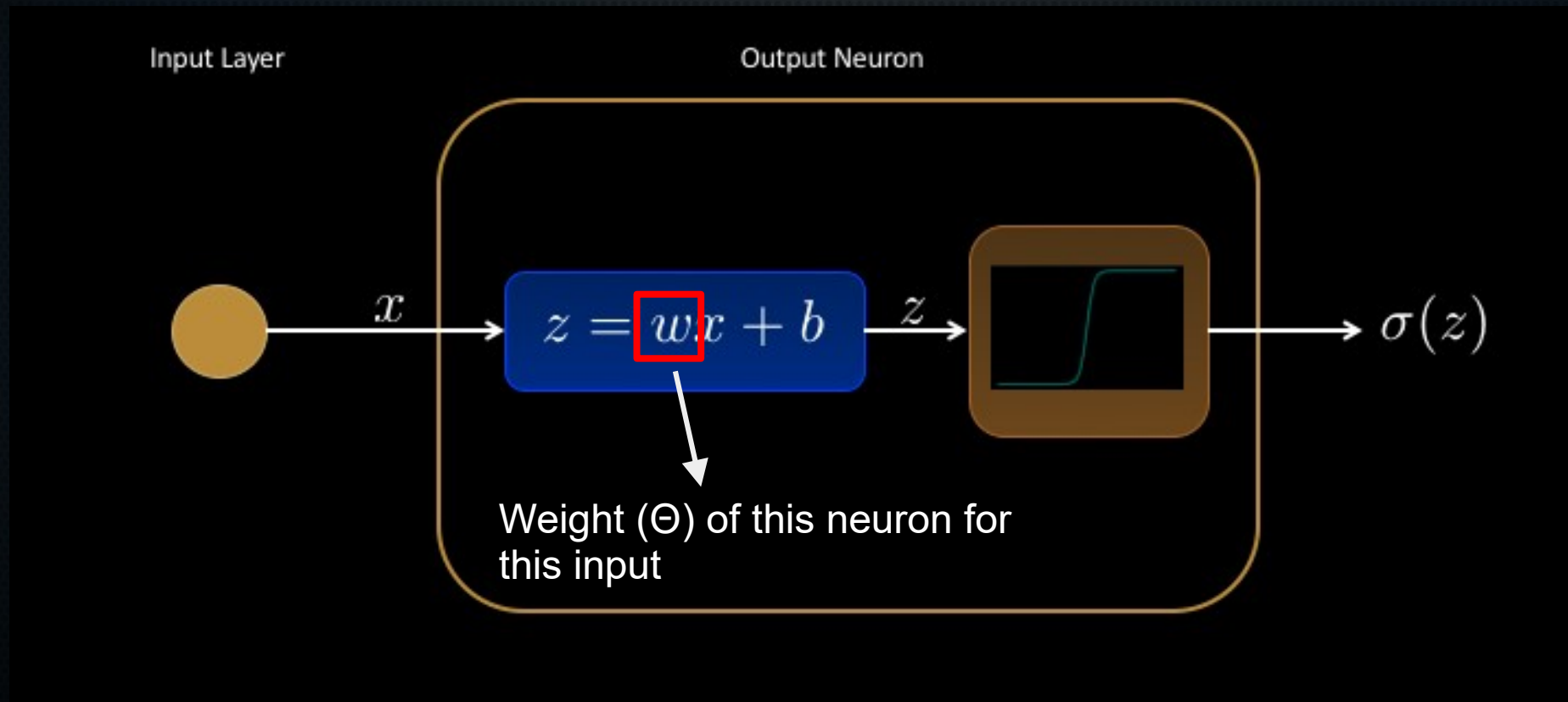
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# What do neural nets have to do with logistic regression?

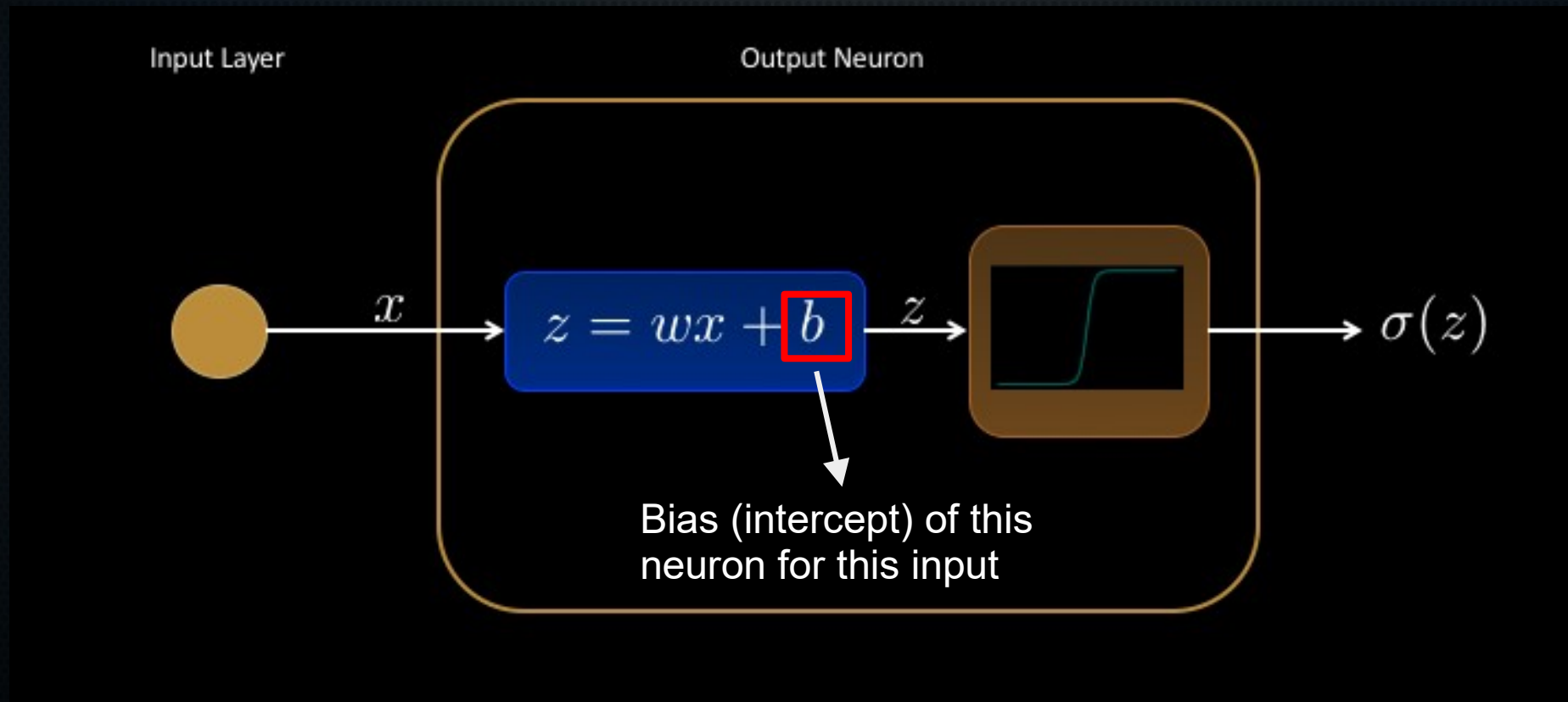
- A single neuron is a logistic regressor!





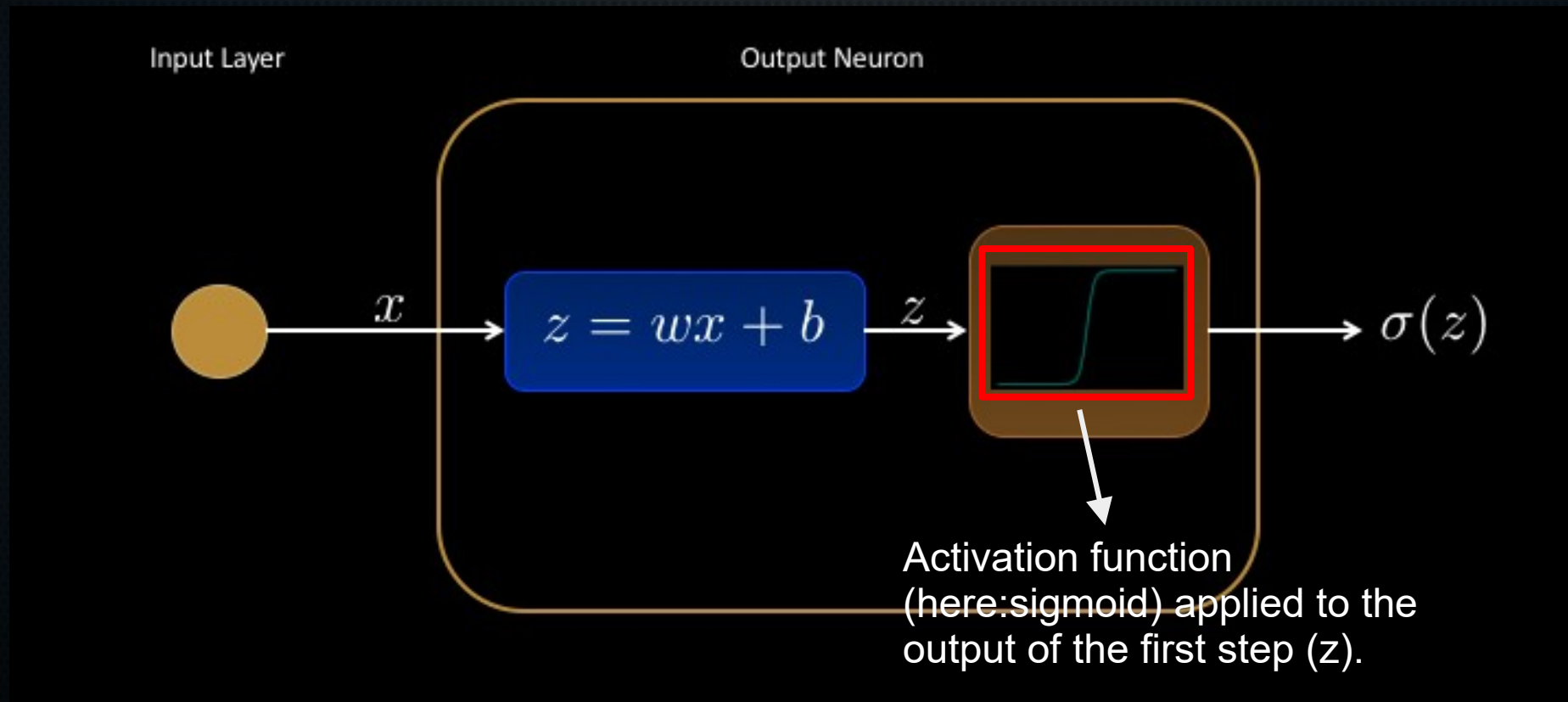
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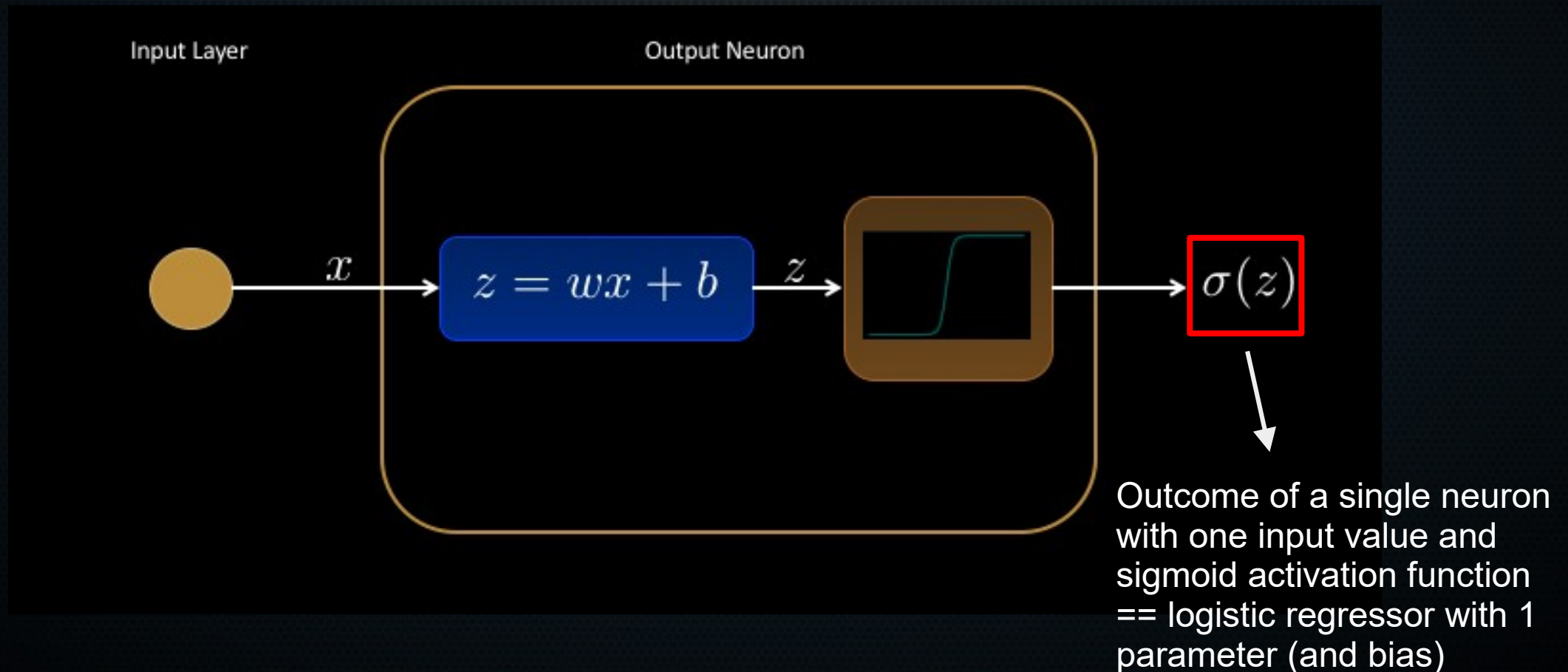
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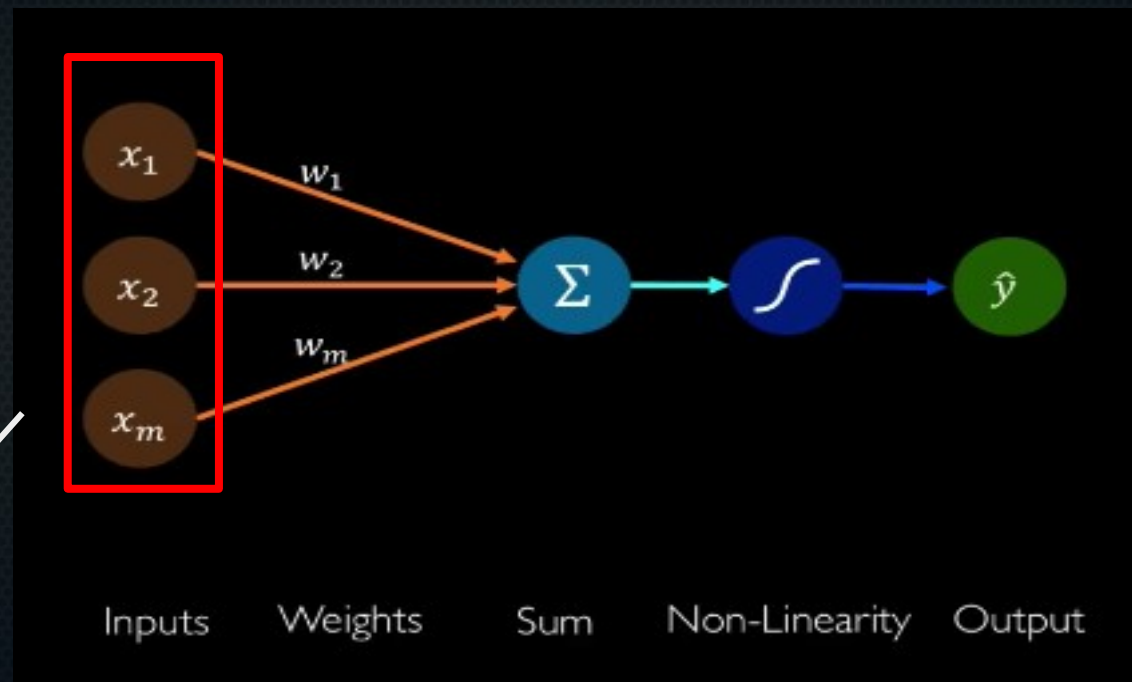
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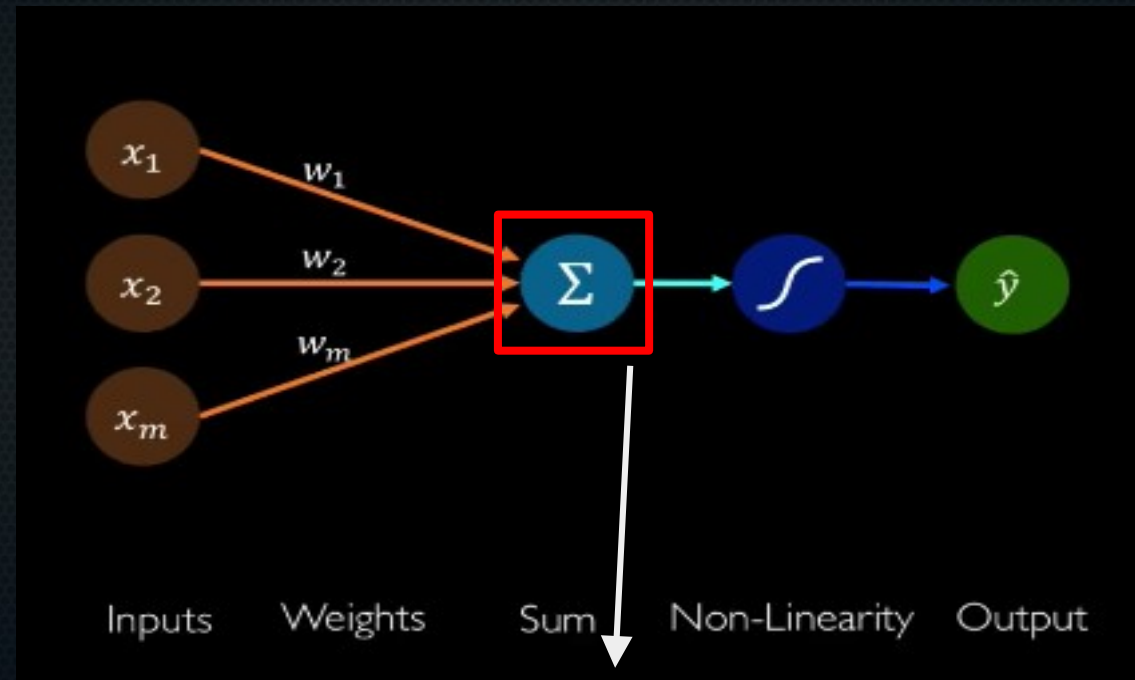


Multiple inputs: summation of those inputs' weights and the neuron's bias



# What do neural nets have to do with logistic regression?

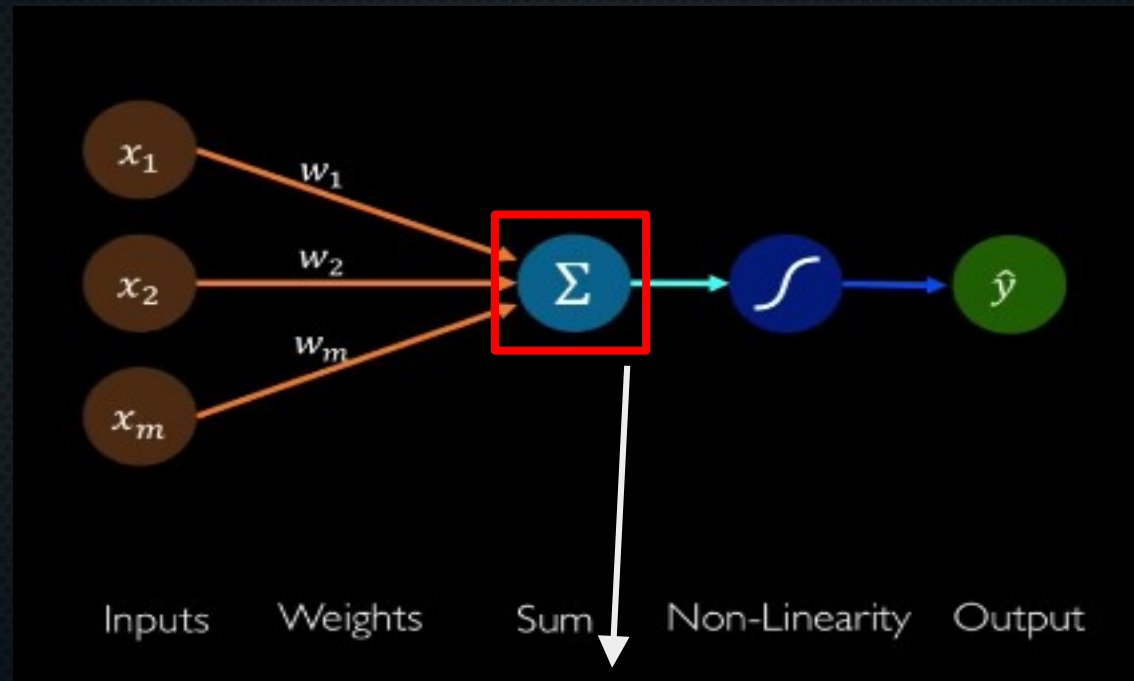
- A single neuron is a logistic regressor!



$$b + \sum_{i=1}^m w_i \cdot x_i$$

# What do neural nets have to do with logistic regression?

- A single neuron is a logistic regressor!

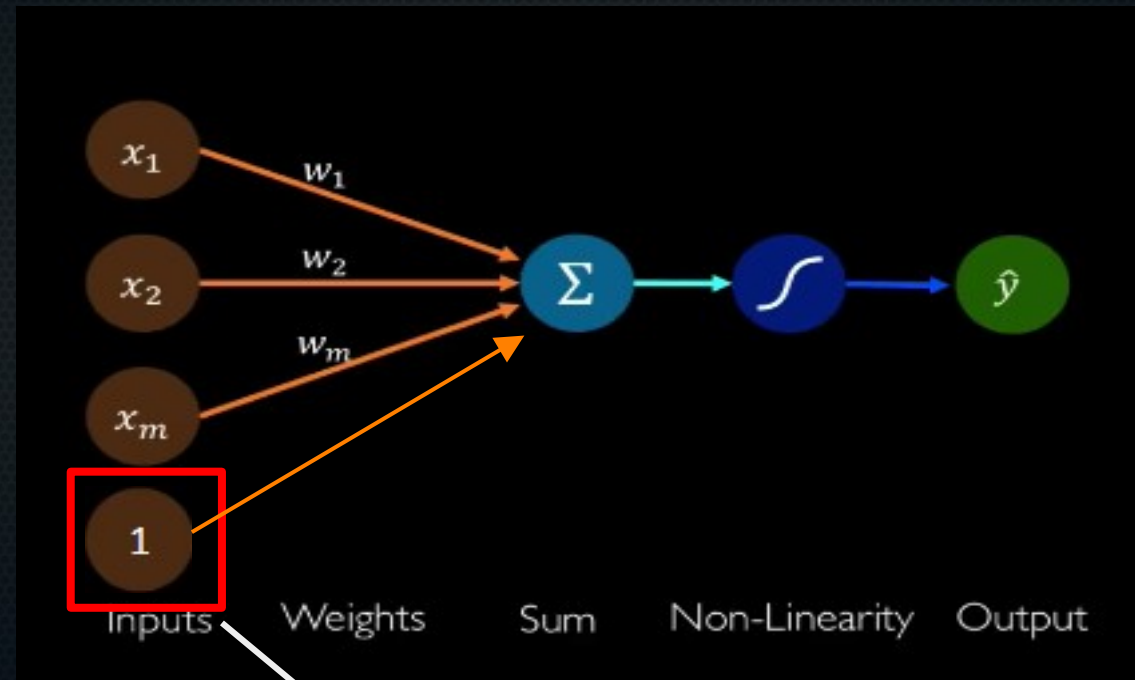


Or, in linear algebra notation:

$$\begin{bmatrix} 1 & x_1 & x_2 & x_m \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_m \end{bmatrix}$$

# What do neural nets have to do with logistic regression?

- A single neuron is a logistic regressor!



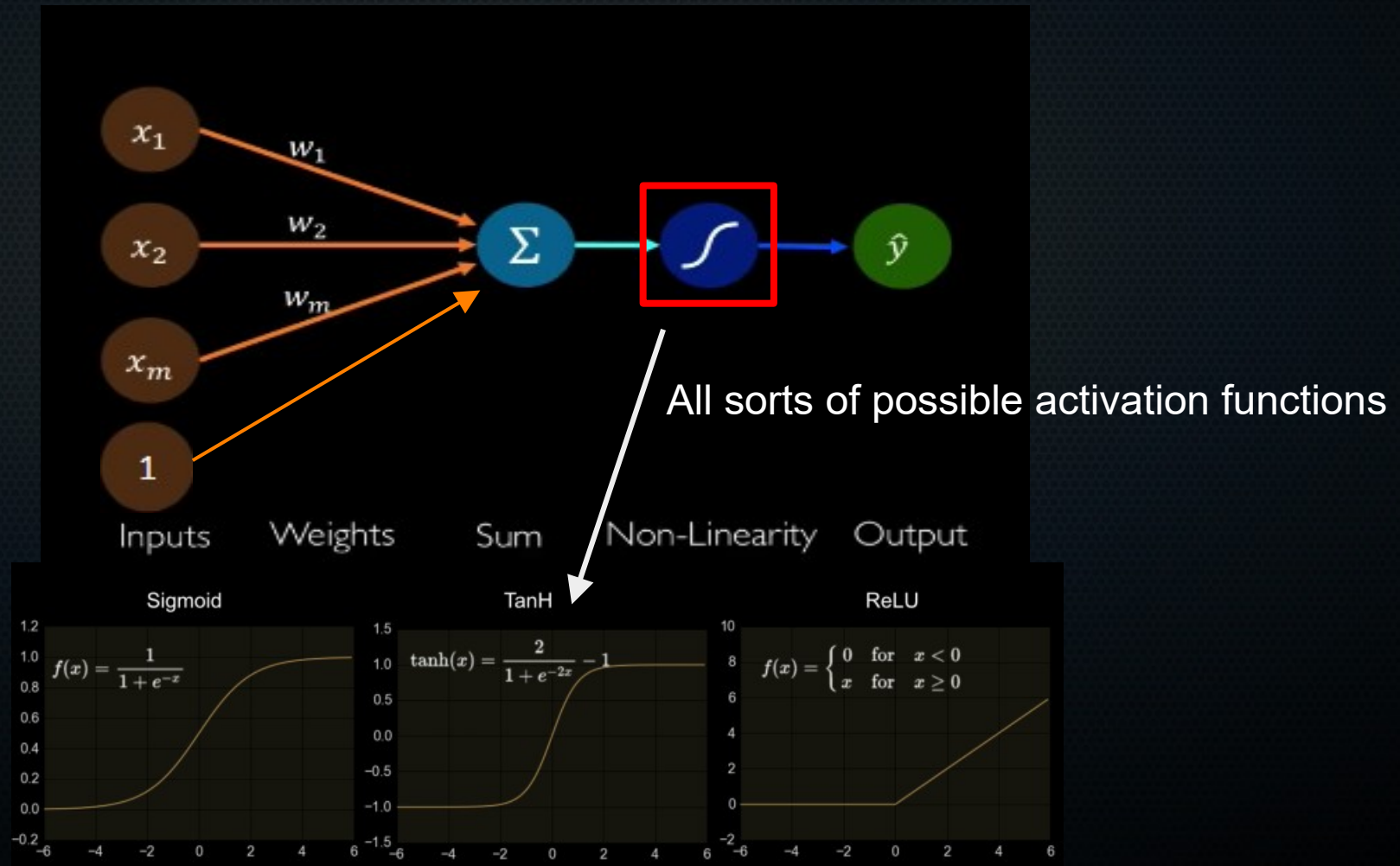
Bias unit (always 1, same for every neuron, most often not shown)

$$\begin{bmatrix} 1 & x_1 & x_2 & x_m \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_m \end{bmatrix}$$



# What do neural nets have to do with logistic regression?

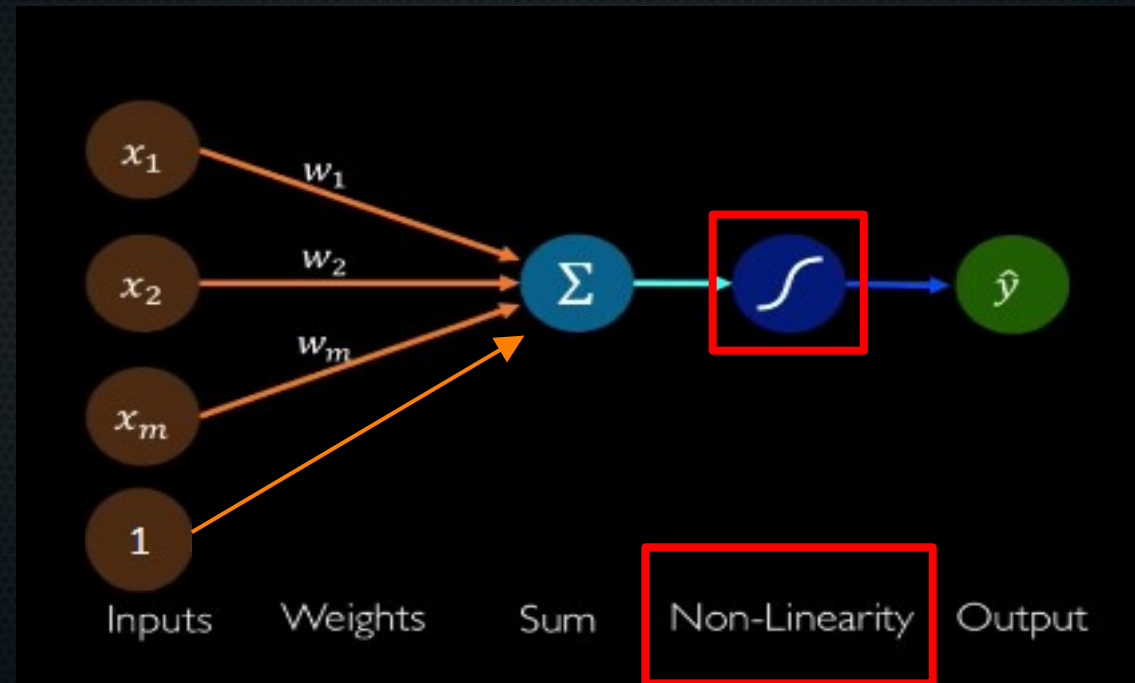
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# What do neural nets have to do with logistic regression?

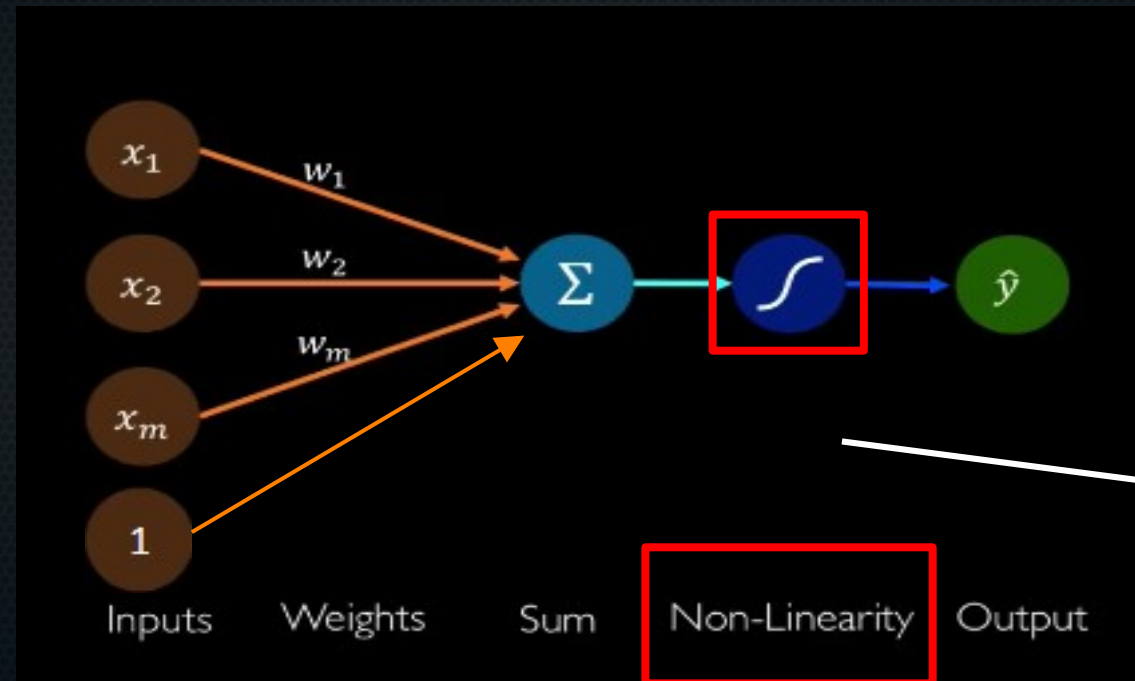
- A single neuron is a logistic regressor!



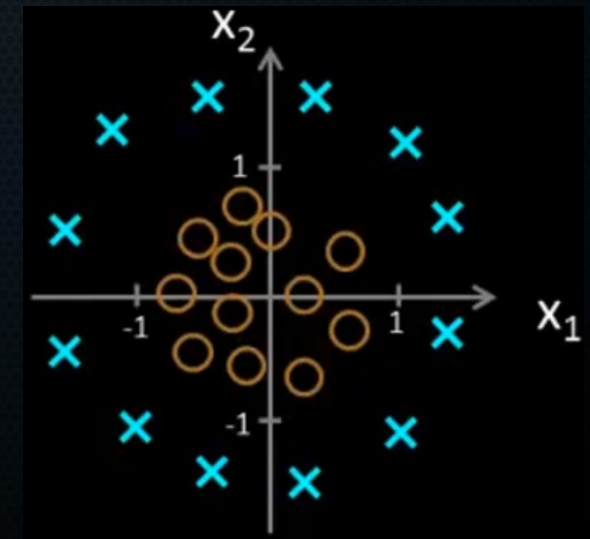
- Why non-linearity?

# What do neural nets have to do with logistic regression?

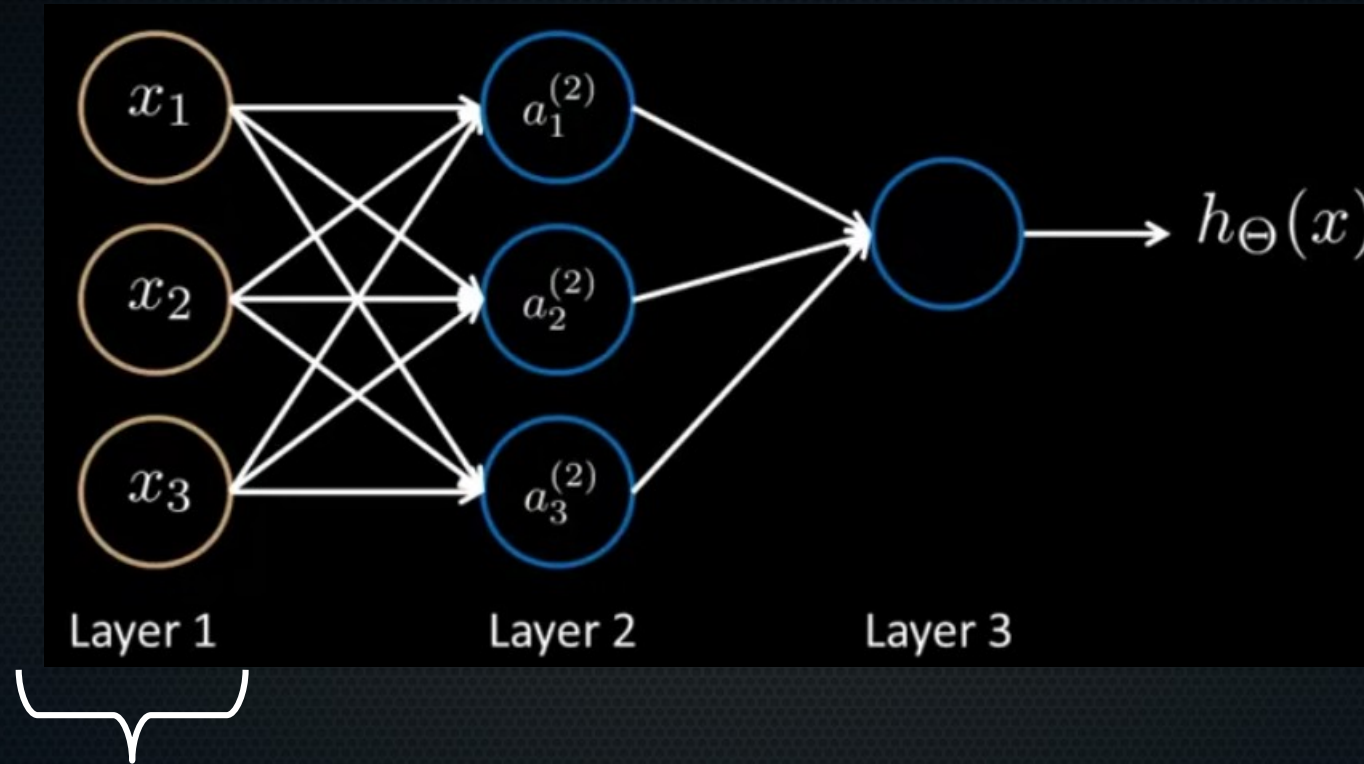
- A single neuron is a logistic regressor!



- Why non-linearity?  $\rightarrow$  without them, a NN (no matter how deep) could only approximate linear functions



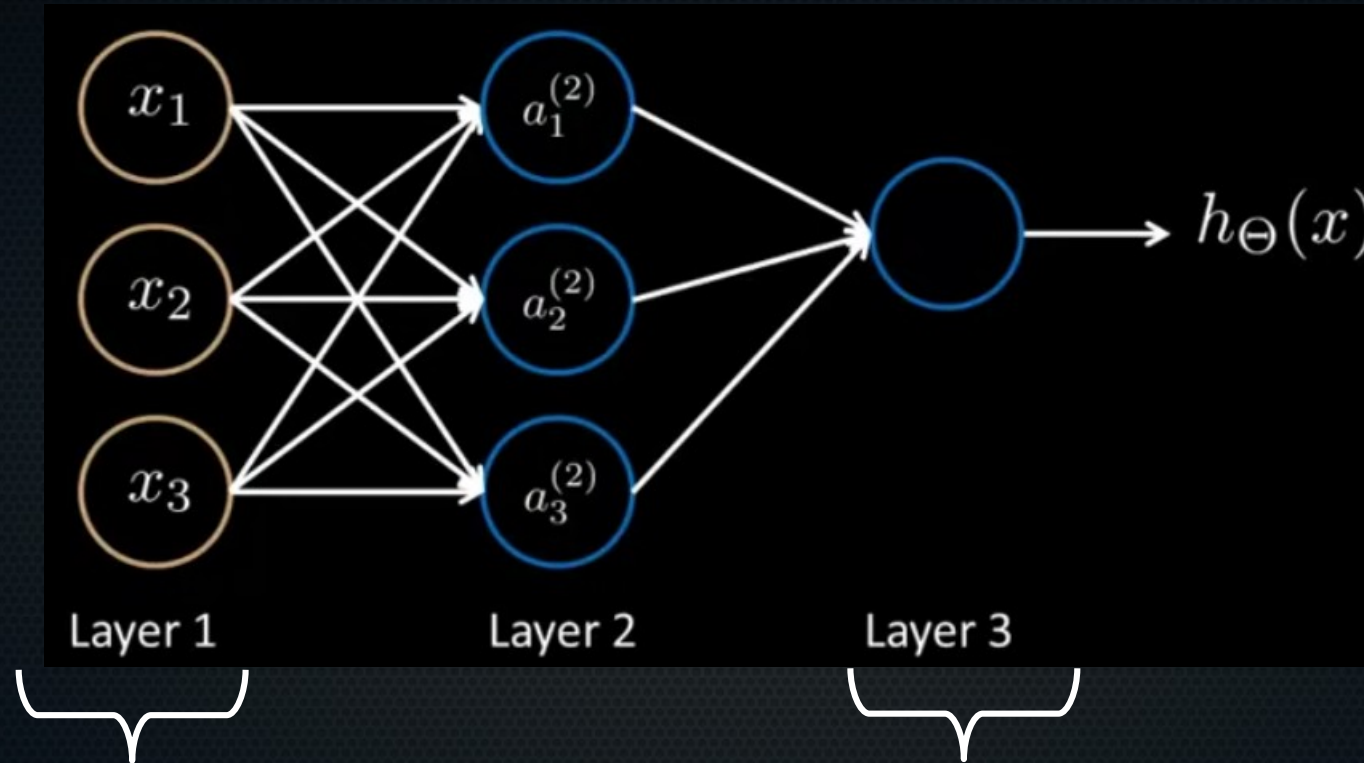
# Workings of a simple neural network



Input layer: shown as neurons, are just features



# Workings of a simple neural network

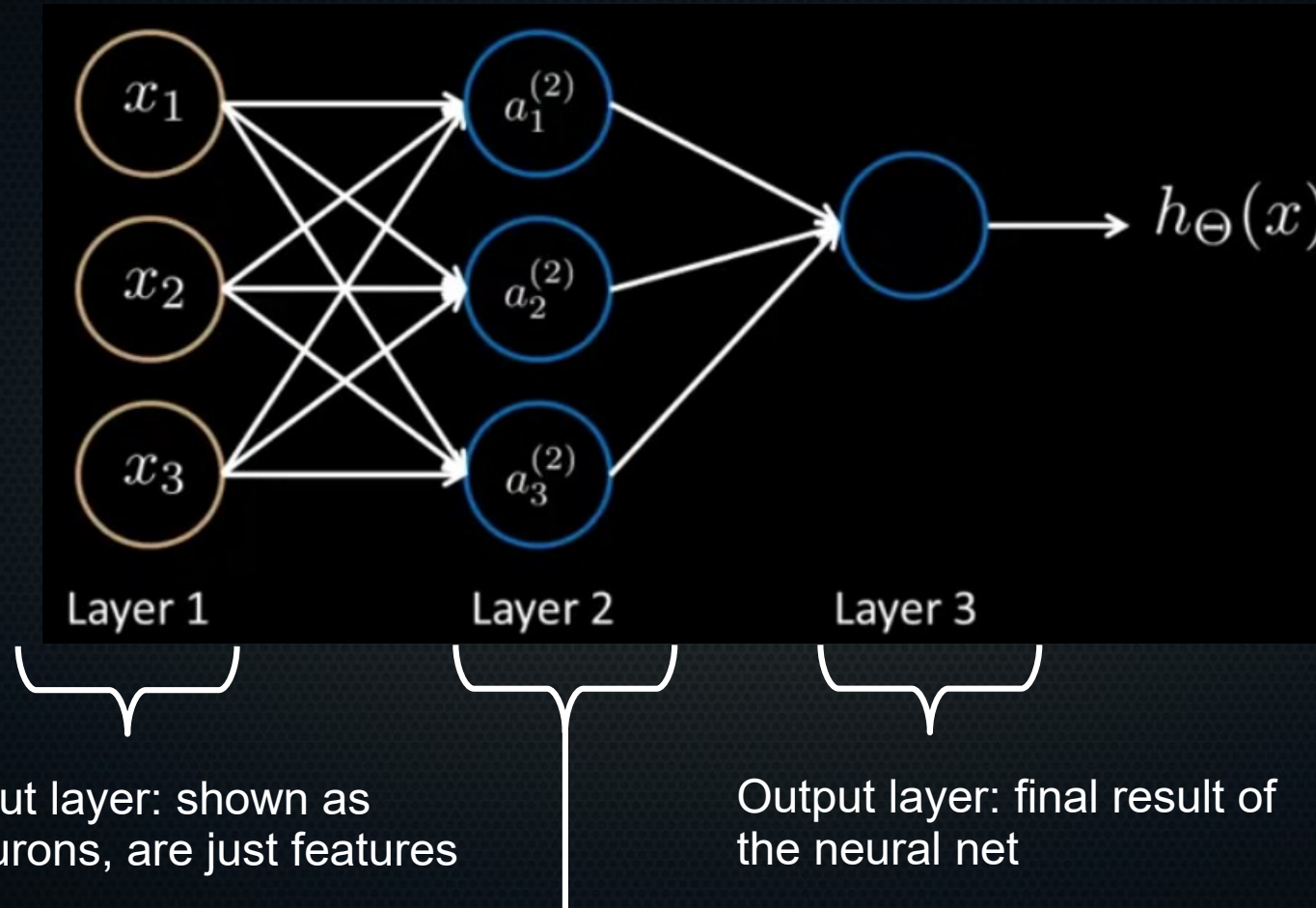


Input layer: shown as neurons, are just features

Output layer: final result of the neural net

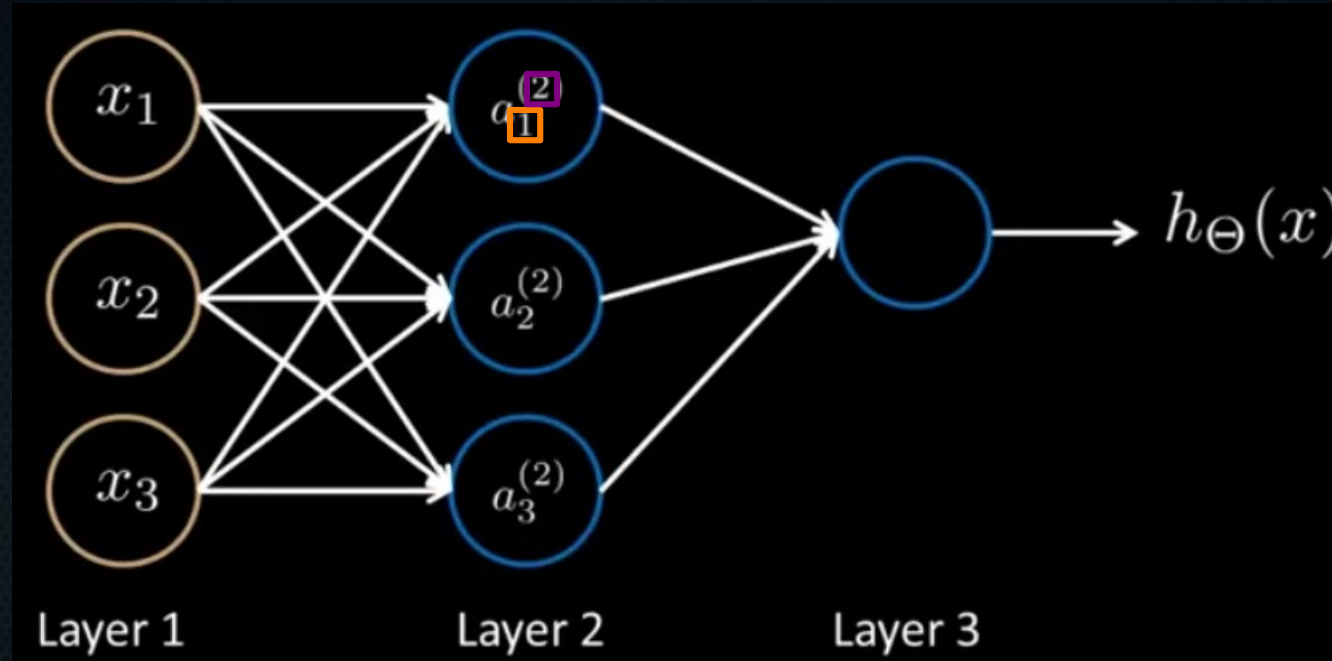


# Workings of a simple neural network



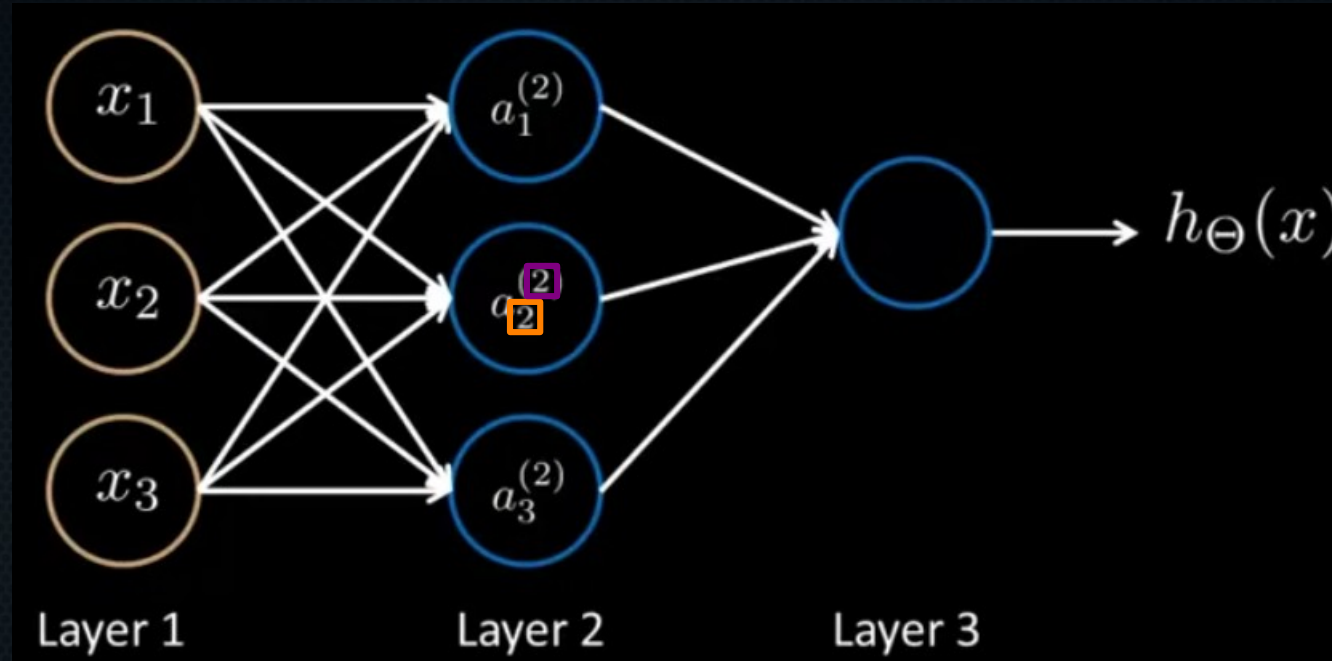
Hidden layer(s): intermediate layers whose outputs are not directly observed (hence hidden). Here: 1 HL. Facebook's DenseNet family of NNs had 121-264 HLs in 2016 (0.8-15.3 million parameters).

# Workings of a simple neural network



Activation of neuron 1 in the 2<sup>nd</sup> layer of the network.

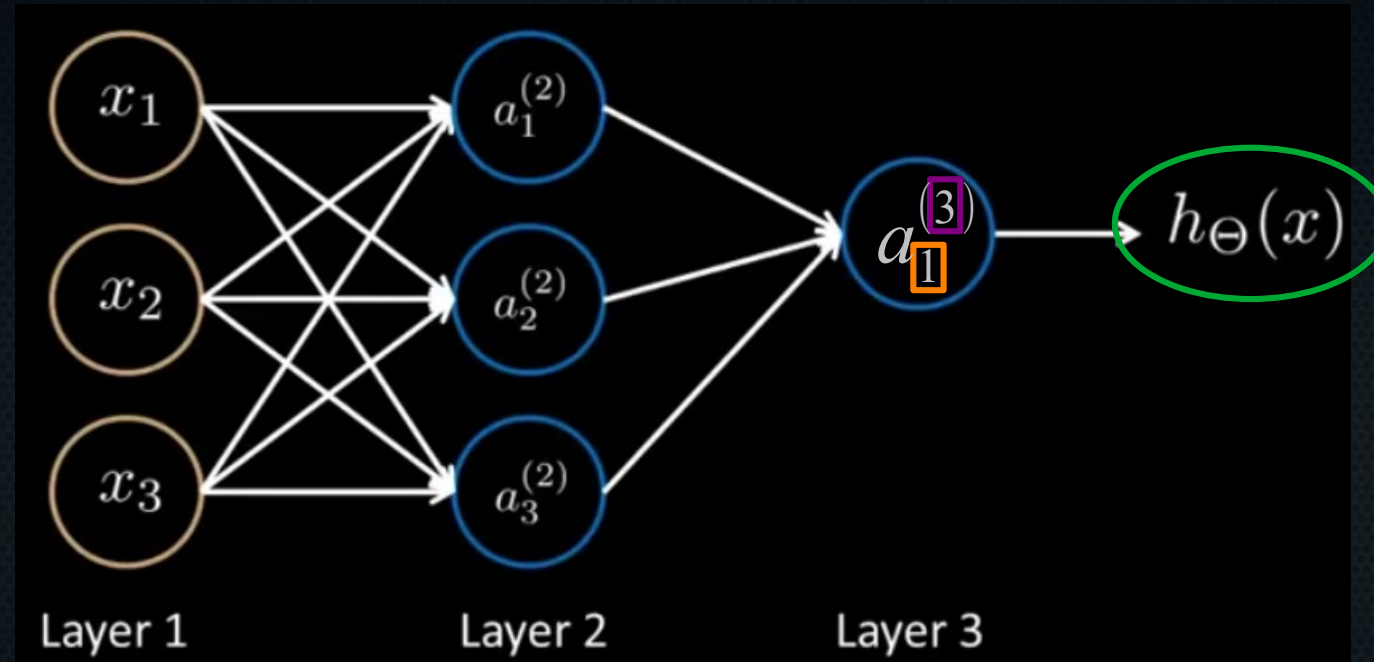
# Workings of a simple neural network



Activation of neuron 2 in the 2<sup>nd</sup> layer of the network.



# Workings of a simple neural network

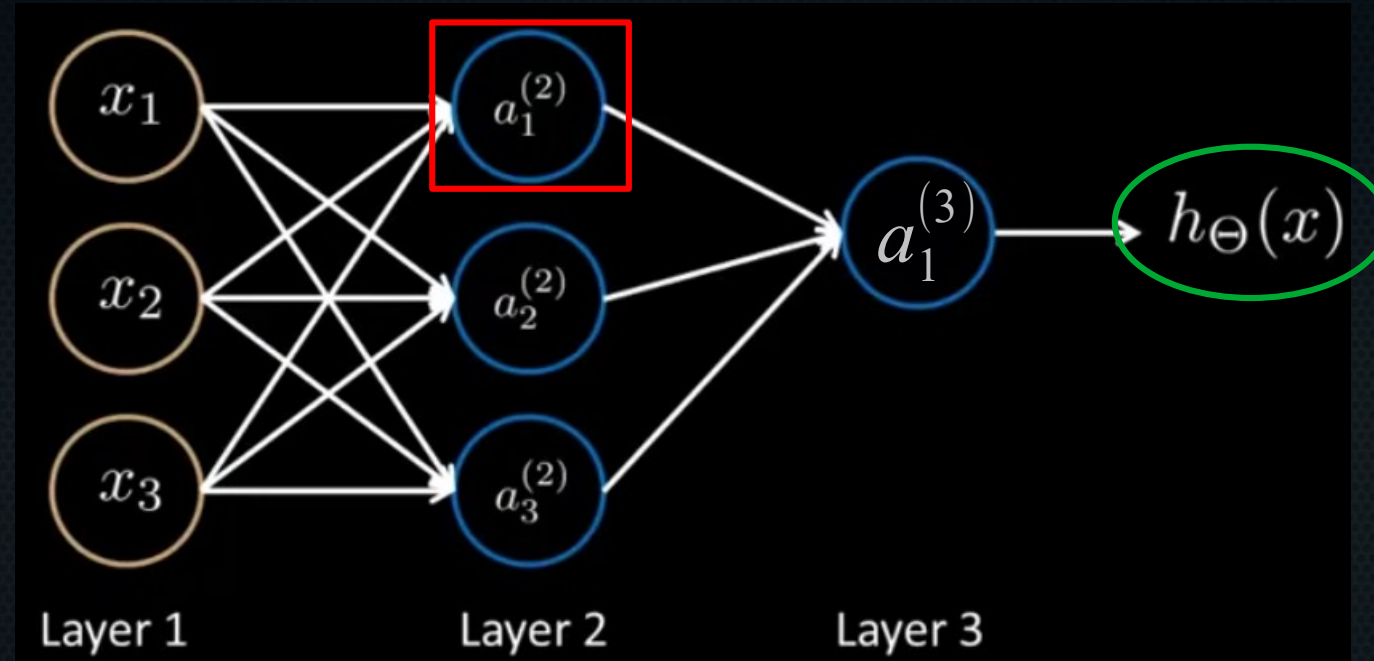


<https://www.louisbouchard.ai/densenet-explained/>

Activation of neuron 1 in the 3<sup>rd</sup> layer of the network.

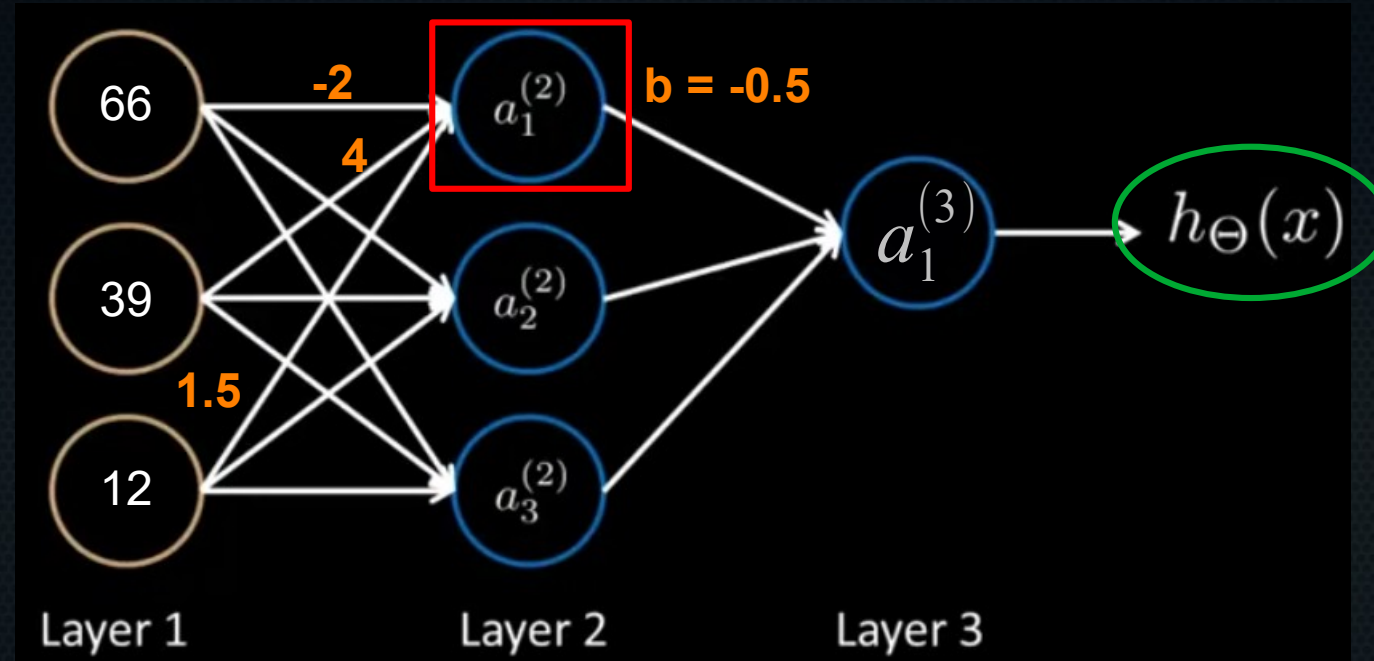


# What is this network calculating?



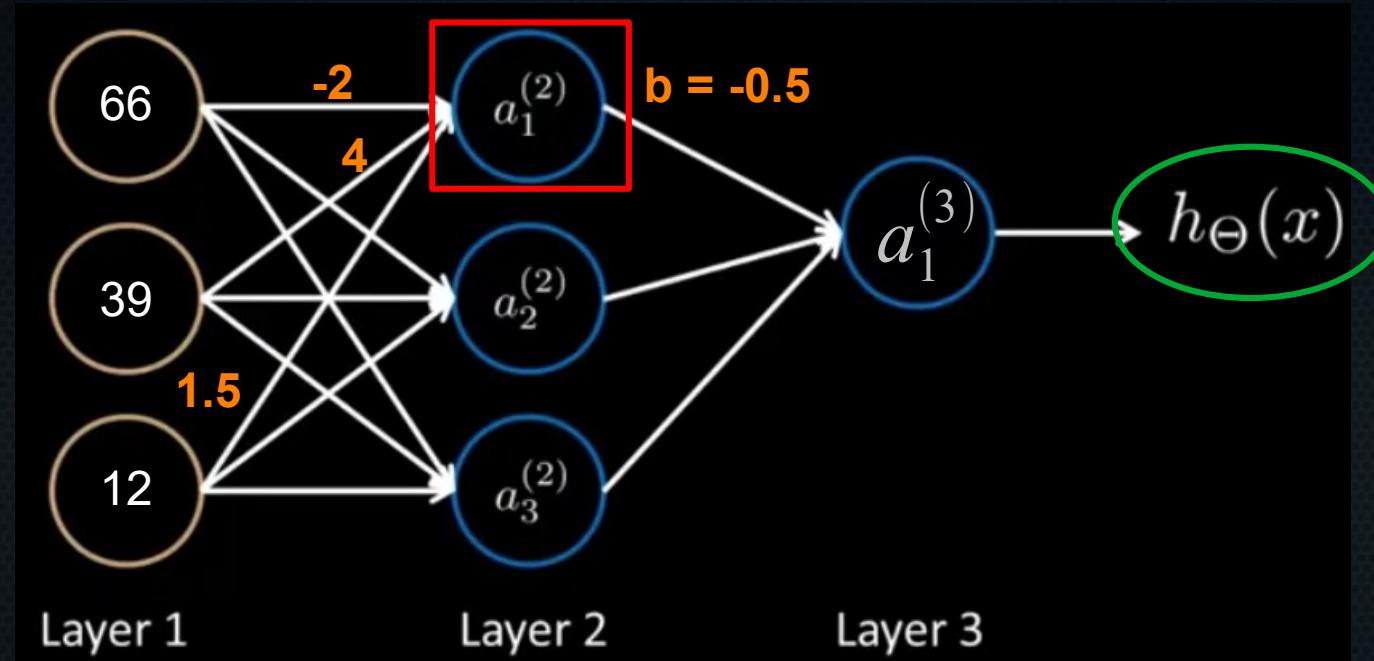
$$\sigma \left( \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} \right)$$

# What is this network calculating?



$$\sigma \left( \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} \right) \rightarrow \sigma \left( \begin{bmatrix} 1 & 66 & 39 & 12 \end{bmatrix} \begin{bmatrix} -0.5 \\ -2 \\ 4 \\ 1.5 \end{bmatrix} \right)$$

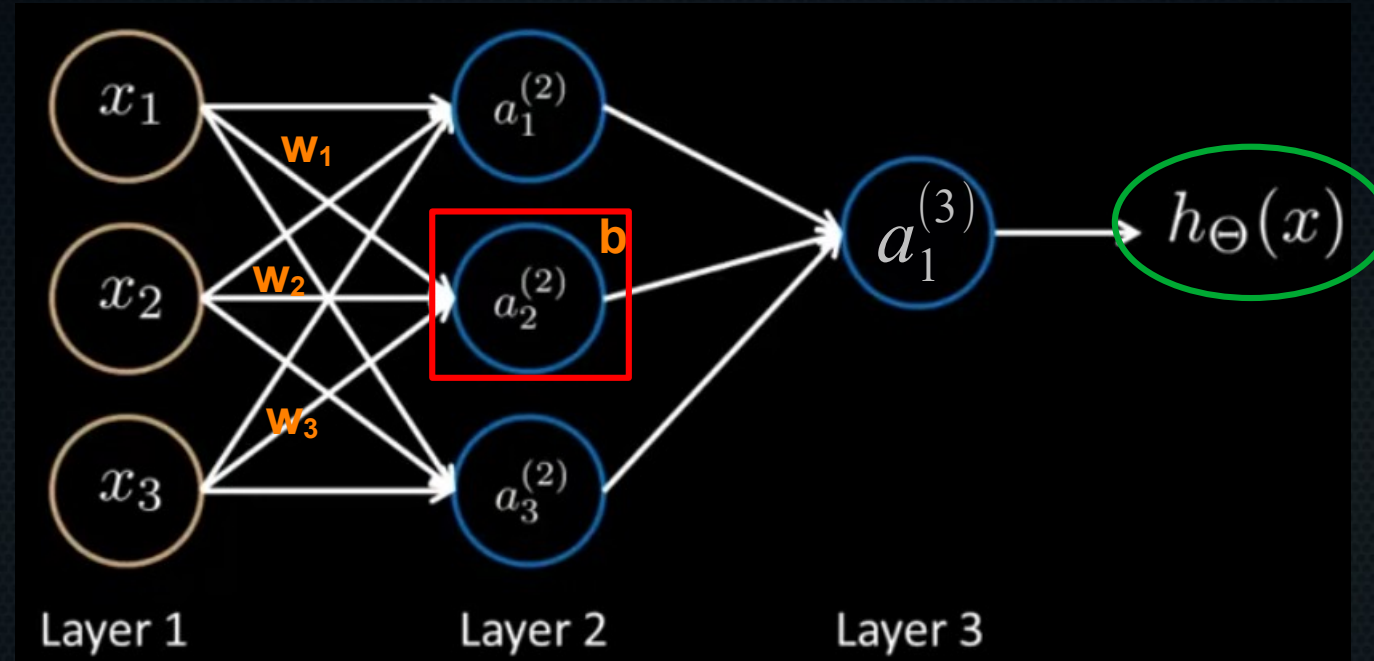
# What is this network calculating?



$$\sigma\left([1 \quad 66 \quad 39 \quad 12] \begin{bmatrix} -0.5 \\ -2 \\ 4 \\ 1.5 \end{bmatrix}\right) \rightarrow \sigma(41.5) \rightarrow 0.999 \dots$$



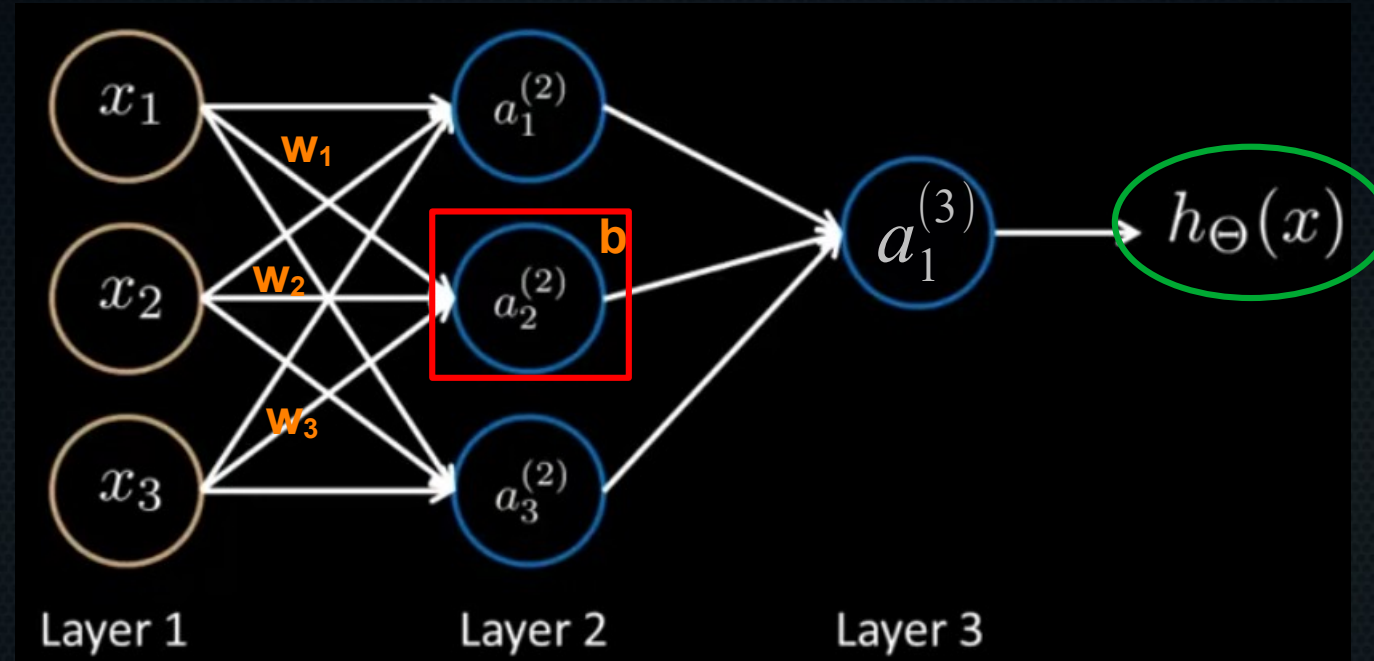
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$$\sigma \left( \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} \right)$$

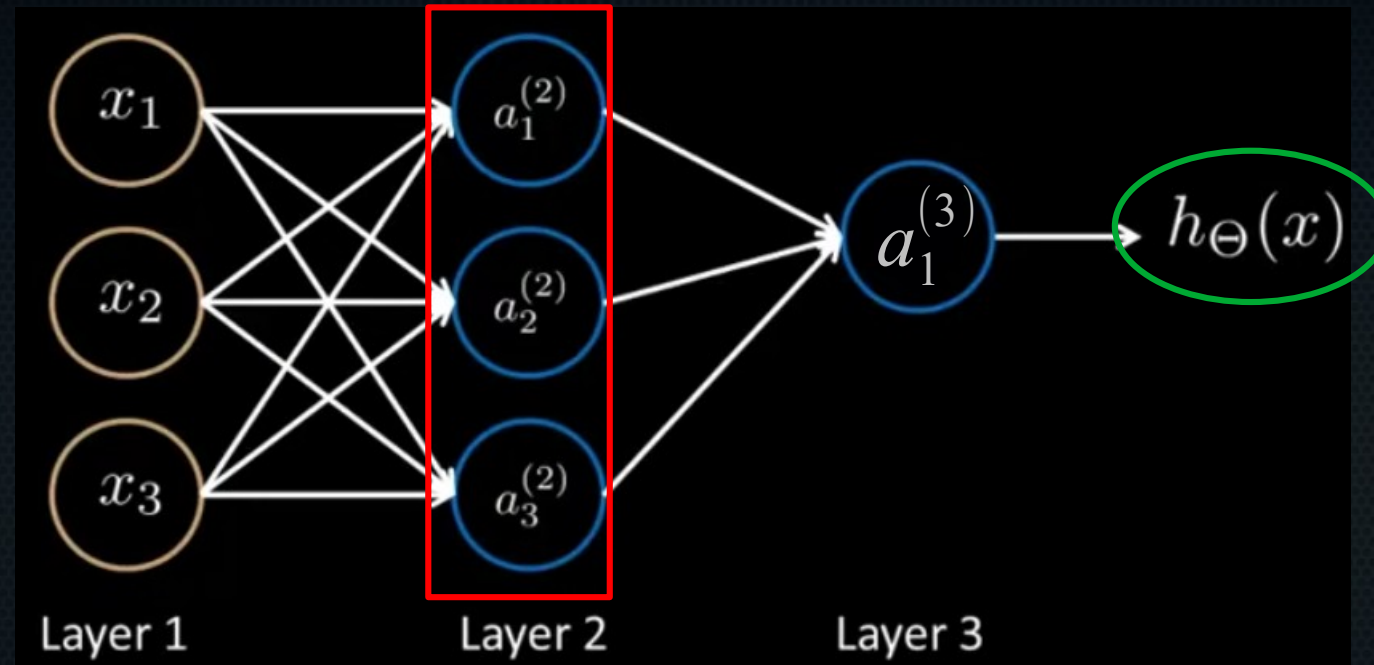


# What is this network calculating?



$$\sigma \left( \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b \\ w_1 \\ w_2 \\ w_3 \end{bmatrix} \right) \rightarrow \text{Calculate for all units at the same time with a theta matrix } \Theta^{(j)}$$

# What is this network calculating?

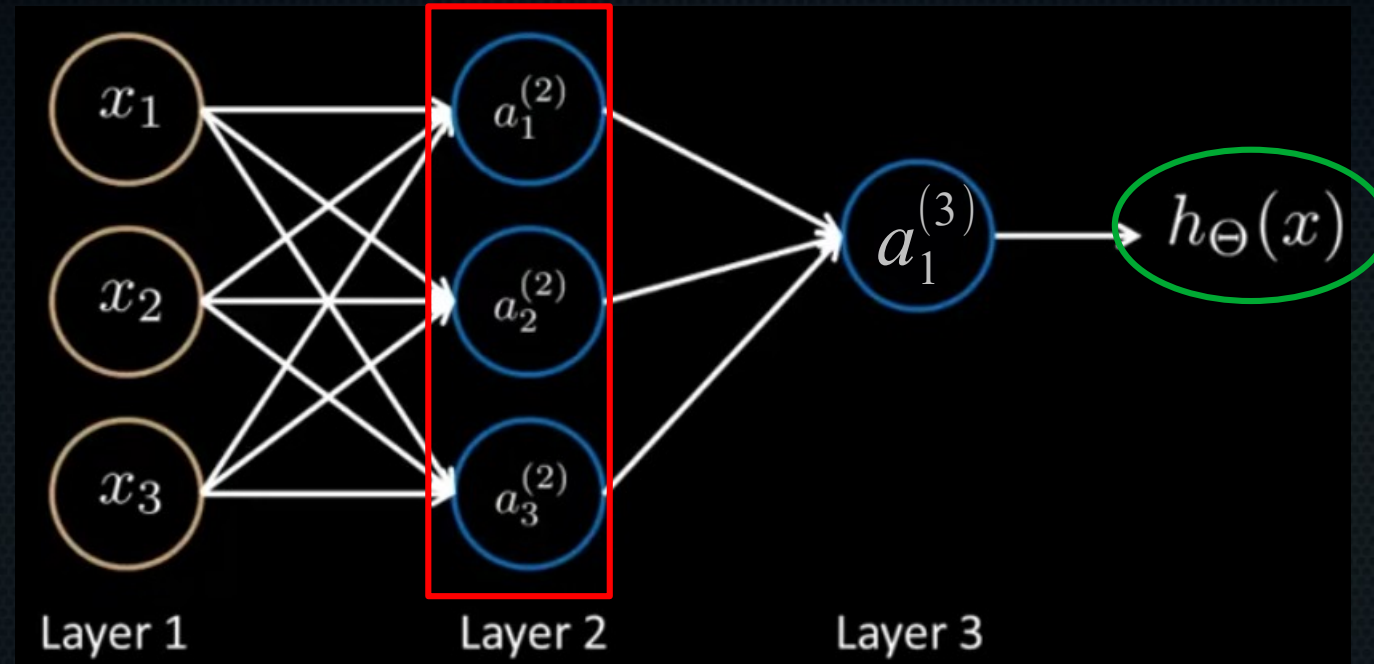


$$\sigma \left( \begin{bmatrix} 1 & x_1 & x_2 & x_3 \end{bmatrix} \begin{bmatrix} b_1 & b_2 & b_3 \\ w_{11} & w_{21} & w_{31} \\ w_{12} & w_{22} & w_{32} \\ w_{13} & w_{23} & w_{33} \end{bmatrix} \right) \rightarrow \sigma \left( \begin{bmatrix} 1 & 2 & 3 \end{bmatrix} \right)$$

$\downarrow$

$$\boxed{[\sigma(1) \quad \sigma(2) \quad \sigma(3)]}$$

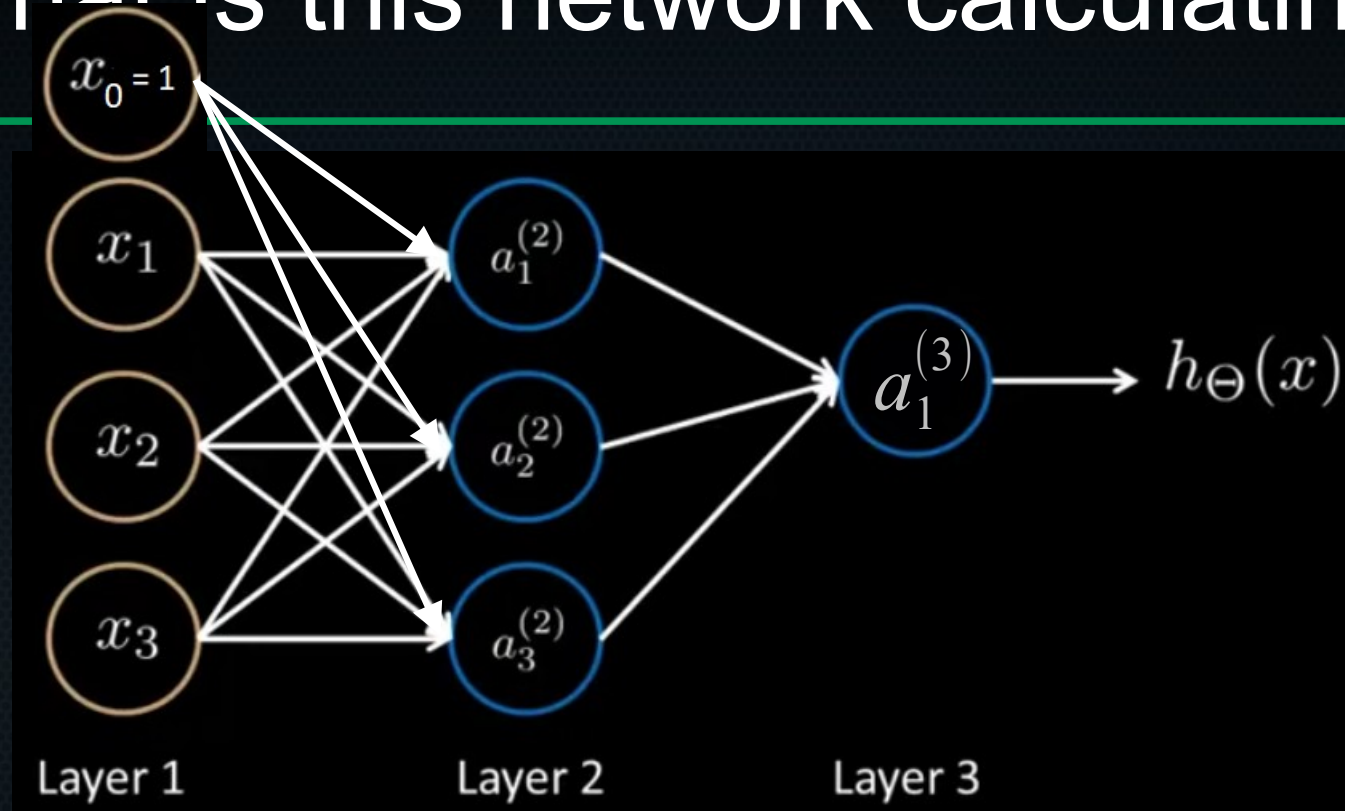
# What is this network calculating?



$$\sigma \left( \begin{bmatrix} b_1 & w_{11} & w_{12} & w_{13} \\ b_2 & w_{21} & w_{22} & w_{23} \\ b_3 & w_{31} & w_{32} & w_{33} \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix} \right) \rightarrow \sigma \left( \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} \right) \rightarrow \begin{bmatrix} \sigma(1) \\ \sigma(2) \\ \sigma(3) \end{bmatrix}$$



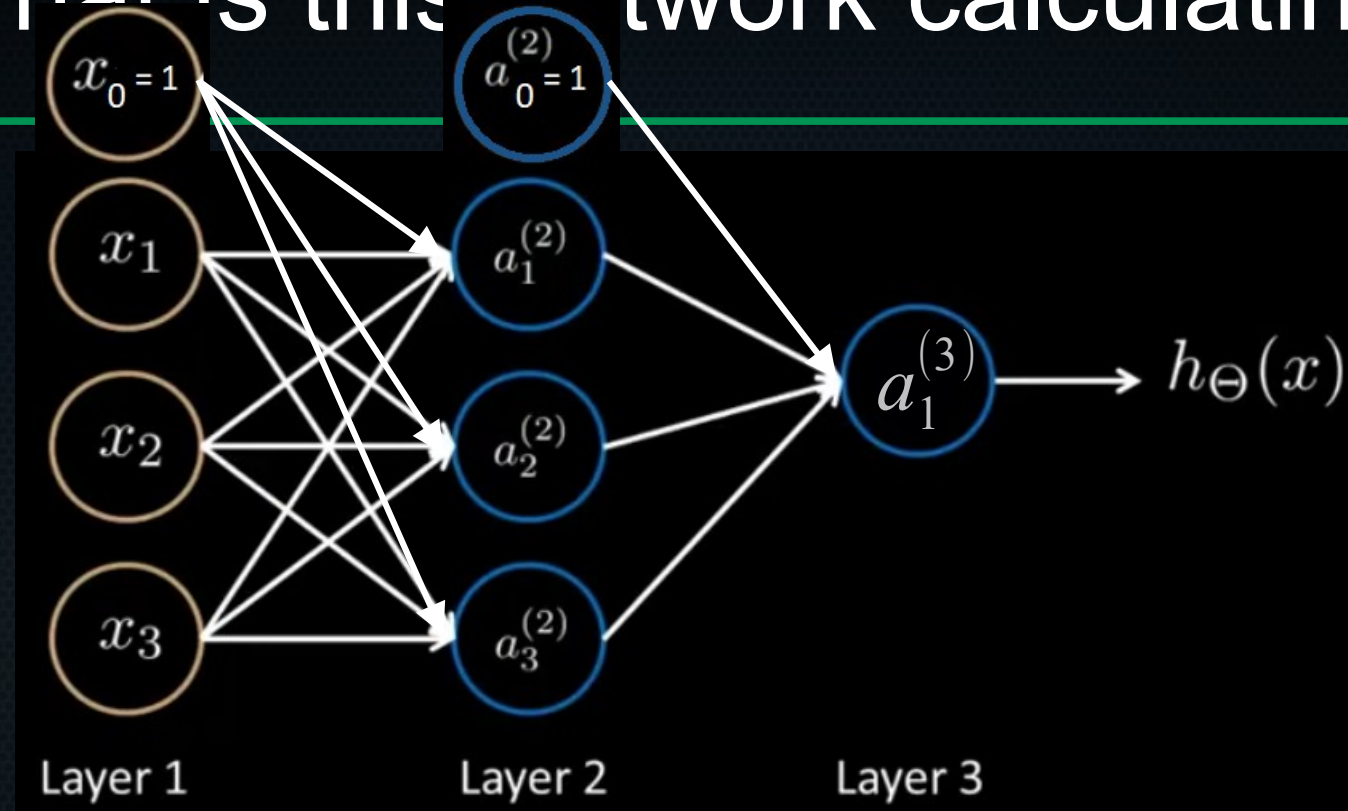
# What is this network calculating?



$$\begin{aligned}a_1^{(2)} &= g(\Theta_{10}^{(1)} x_0 + \Theta_{11}^{(1)} x_1 + \Theta_{12}^{(1)} x_2 + \Theta_{13}^{(1)} x_3) \\a_2^{(2)} &= g(\Theta_{20}^{(1)} x_0 + \Theta_{21}^{(1)} x_1 + \Theta_{22}^{(1)} x_2 + \Theta_{23}^{(1)} x_3) \\a_3^{(2)} &= g(\Theta_{30}^{(1)} x_0 + \Theta_{31}^{(1)} x_1 + \Theta_{32}^{(1)} x_2 + \Theta_{33}^{(1)} x_3)\end{aligned}$$

$$\Theta^{(1)}_{\text{(layer 1 to layer 2)}} = \begin{bmatrix} b_1 & w_{11} & w_{12} & w_{13} \\ b_2 & w_{21} & w_{22} & w_{23} \\ b_3 & w_{31} & w_{32} & w_{33} \end{bmatrix}$$

# What is this network calculating?



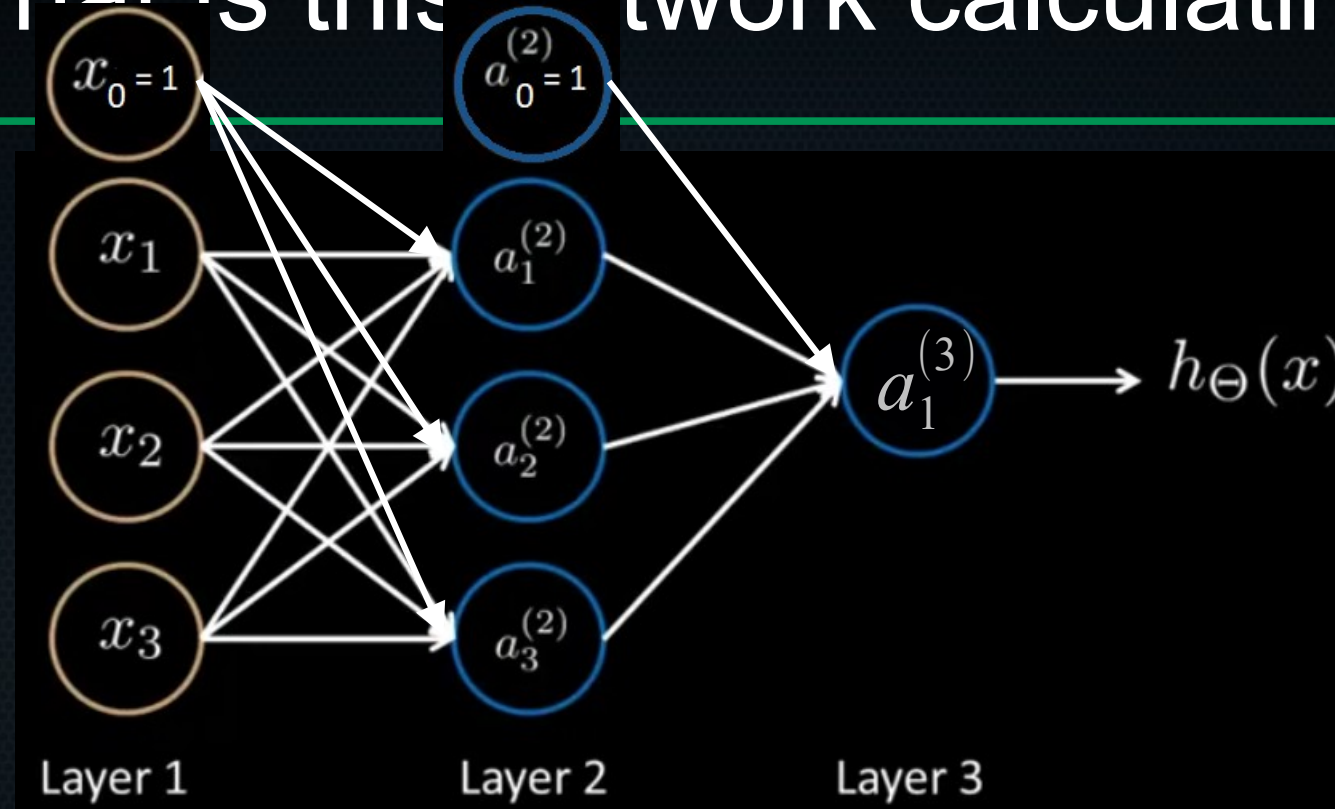
$$h_{\Theta}(x) = a_1^{(3)} = g(\Theta_{10}^{(2)} a_0^{(2)} + \Theta_{11}^{(2)} a_1^{(2)} + \Theta_{12}^{(2)} a_2^{(2)} + \Theta_{13}^{(2)} a_3^{(2)})$$

$\Theta^{(2)}$  (layer 2 to layer 3)

$$\begin{bmatrix} b_1 & w_{11} & w_{12} & w_{13} \end{bmatrix}$$



# What is this network calculating?



- This calculation of the output of the network is called forward propagation



# How do we perform?

---

- Just like before, there is a cost function.
- But we will talk about that and its implementation tomorrow!

# How do we get parameters?

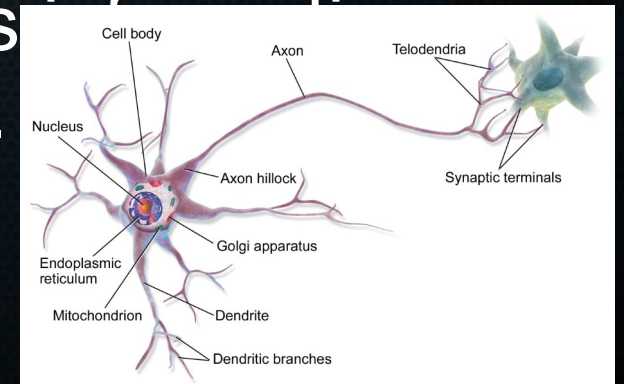
---

- Just like before, there is a cost function and a way to minimise this. But it's a bit more involved.
- To get parameters, we will use the principle of backpropagation. We'll get to that tomorrow.
- First, we need to discuss *why* we want to use neural networks at all!



# Why neural networks?

- Best performing algorithms for complex tasks, bar none.
- Known potential of hierarchical organisation of simple units because of biological examples (though neural networks are not good models of actual neurons)
- Observation in frogs and cat visual cortex: there are specific layers of neurons, where earlier layers detect basic shapes (lines, edges) with later layers incorporating this information into more complex features about what is seen.

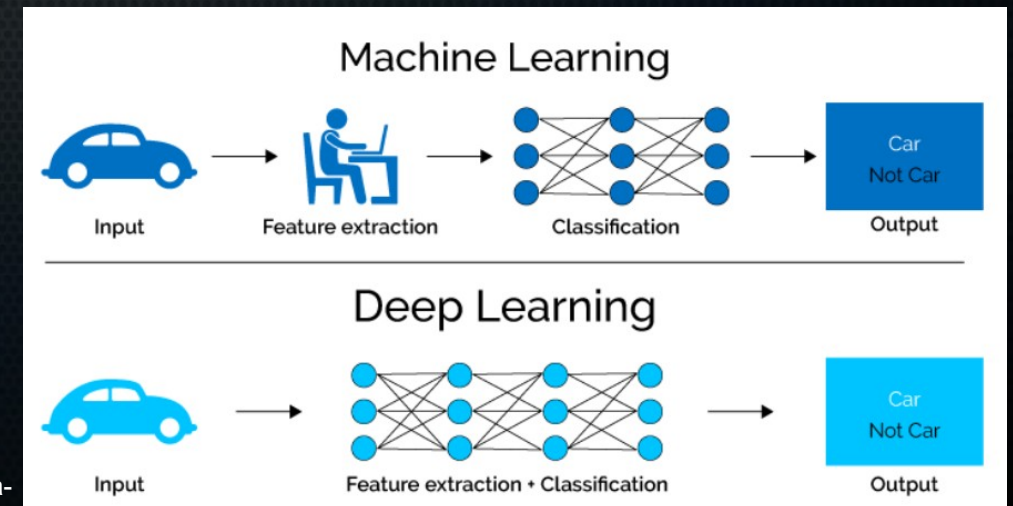


Source:  
[https://en.wikipedia.org/wiki/Axon#/media/File:Blusen\\_0657\\_MultipolarNeuron.png](https://en.wikipedia.org/wiki/Axon#/media/File:Blusen_0657_MultipolarNeuron.png)



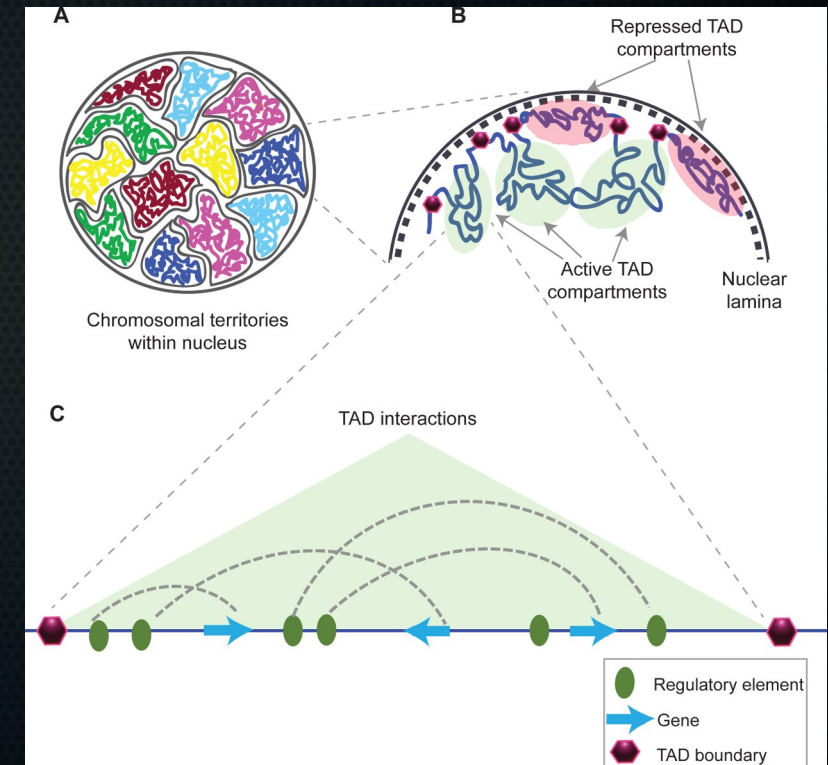
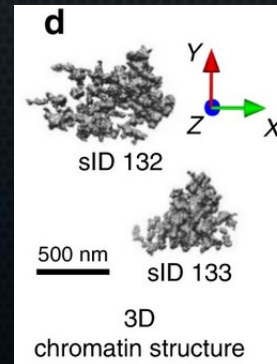
# Why neural networks?

- Until now, we decided on the features to give to our algorithms: think tumour size, biopsy test scores, etc.
- With neural networks and images, the situation changes: we don't arduously describe what is in each image, but rather let the network learn to extract and combine features so *that* it can classify training examples correctly.



# Why neural networks?

- Caveat for biology: it can be quite difficult to translate biological problems into a framework fit for deep learning, for reasons that will become clear later.
- Example: in images, nearby pixels probably hold similar information, i.e. are involved in the same thing. Due to (long-range) 3D-folding of DNA, linearly far DNA can be close together functionally. You need to encode network or input to accomodate this!



Source:  
[https://en.wikipedia.org/wiki/Topologically\\_associating\\_domain#/media/File:Structural\\_organization\\_of\\_chromatin.png](https://en.wikipedia.org/wiki/Topologically_associating_domain#/media/File:Structural_organization_of_chromatin.png)



# Why neural networks?

---

- The mythical property of *universal approximation*. This says that neural networks can approximate any function with arbitrary accuracy, even with only 1 hidden layer (given enough neurons in it).



# Why neural networks?

---

- The mythical property of *universal approximation*. This says that neural networks can approximate any function with arbitrary accuracy, even with only 1 hidden layer (given enough neurons in it).
- How can that be? You will find out in-depth in the next practical.
- Of course, that doesn't necessarily mean we would have the data to *train* such a neural network efficiently. Just that it is provable that for *any continuous function* a neural network can exist that approximates it as well as you like.

# Recap so far

---

- Neural networks can be thought of as hierarchical sets of logistic regressors
- We essentially make earlier layers learn useful features for distinction on their own, and can use these best possible learned features for the classification by the final unit(s)
- Parsing an example through the network and getting the output is called forward propagation
- *Universal approximation* holds that, in principle, neural networks can learn any continuous function arbitrarily well.



# Making simple functions ourselves

---

- Networks with a single hidden layer can approximate any function. Let's get some more intuition by building our own logic circuit.



# Making simple functions ourselves

- Networks with a single hidden layer can approximate any function. Let's get some more intuition by building our own logic circuit.
- Boolean operators:

| <i>NOT</i> |           | <i>AND</i> |          |           | <i>OR</i> |          |            | <i>XOR</i> |          |            |
|------------|-----------|------------|----------|-----------|-----------|----------|------------|------------|----------|------------|
| <i>x</i>   | <i>x'</i> | <i>x</i>   | <i>y</i> | <i>xy</i> | <i>x</i>  | <i>y</i> | <i>x+y</i> | <i>x</i>   | <i>y</i> | <i>x⊕y</i> |
| 0          | 1         | 0          | 0        | 0         | 0         | 0        | 0          | 0          | 0        | 0          |
| 1          | 0         | 0          | 1        | 0         | 0         | 1        | 1          | 0          | 1        | 1          |
|            |           | 1          | 0        | 0         | 1         | 0        | 1          | 1          | 0        | 1          |
|            |           | 1          | 1        | 1         | 1         | 1        | 1          | 1          | 1        | 0          |

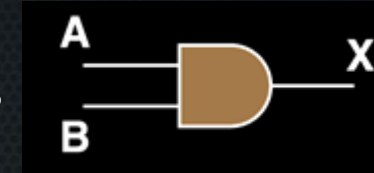
Source: <https://introcs.cs.princeton.edu/java/71boolean/>

# Making simple functions ourselves

- Networks with a single hidden layer can approximate any function. Let's get some more intuition by building our own logic circuit.

- Boolean operators:

Only if two incoming connections are on, the output is on



Source: <https://www.electronicstutorial.net/digital-logic-gates/and-gate/>

| NOT |    | AND |   |    | OR |   |     | XOR |   |              |
|-----|----|-----|---|----|----|---|-----|-----|---|--------------|
| x   | x' | x   | y | xy | x  | y | x+y | x   | y | $x \oplus y$ |
| 0   | 1  | 0   | 0 | 0  | 0  | 0 | 0   | 0   | 0 | 0            |
| 1   | 0  | 0   | 1 | 0  | 0  | 1 | 1   | 0   | 1 | 1            |
|     |    | 1   | 0 | 0  | 1  | 0 | 1   | 1   | 0 | 1            |
|     |    | 1   | 1 | 1  | 1  | 1 | 1   | 1   | 1 | 0            |

Source: <https://introcs.cs.princeton.edu/java/71boolean/>

# Making simple functions ourselves

- Networks with a single hidden layer can approximate any function. Let's get some more intuition by building our own logic circuit.

- Boolean operators:

Only if either incoming connection is on, the output is on



Source: <https://projectiot123.com/2019/05/26/introduction-to-xor-gate/>

**XOR**

| NOT |      | AND |     |      | OR  |     |       | XOR |     |              |
|-----|------|-----|-----|------|-----|-----|-------|-----|-----|--------------|
| $x$ | $x'$ | $x$ | $y$ | $xy$ | $x$ | $y$ | $x+y$ | $x$ | $y$ | $x \oplus y$ |
| 0   | 1    | 0   | 0   | 0    | 0   | 0   | 0     | 0   | 0   | 0            |
| 1   | 0    | 0   | 1   | 0    | 0   | 1   | 1     | 0   | 1   | 1            |
|     |      | 1   | 0   | 0    | 1   | 0   | 1     | 1   | 0   | 1            |
|     |      | 1   | 1   | 1    | 1   | 1   | 1     | 1   | 1   | 0            |

Source: <https://introcs.cs.princeton.edu/java/71boolean/>



# Making simple functions ourselves

- Networks with a single hidden layer can approximate any function. Let's get some more intuition by building our own logic circuit.

- Boolean operators:

Combine: XNOR



Source:  
[https://www.tutorialspoint.com/computer\\_logical\\_organization/logic\\_gates.htm](https://www.tutorialspoint.com/computer_logical_organization/logic_gates.htm)

**NOT**

| $x$ | $x'$ |
|-----|------|
| 0   | 1    |
| 1   | 0    |

**XNOR**

| Inputs |   | Output      |
|--------|---|-------------|
| A      | B | $A \odot B$ |
| 0      | 0 | 1           |
| 0      | 1 | 0           |
| 1      | 0 | 0           |
| 1      | 1 | 1           |

**XOR**

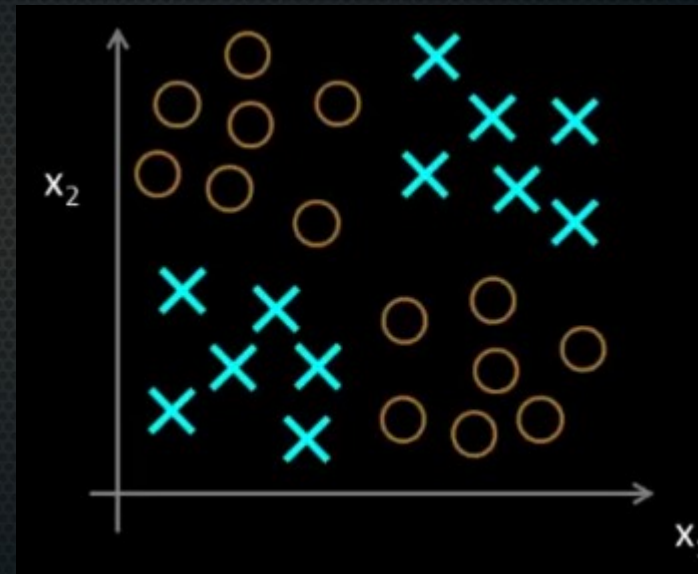
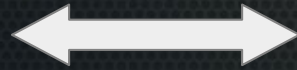
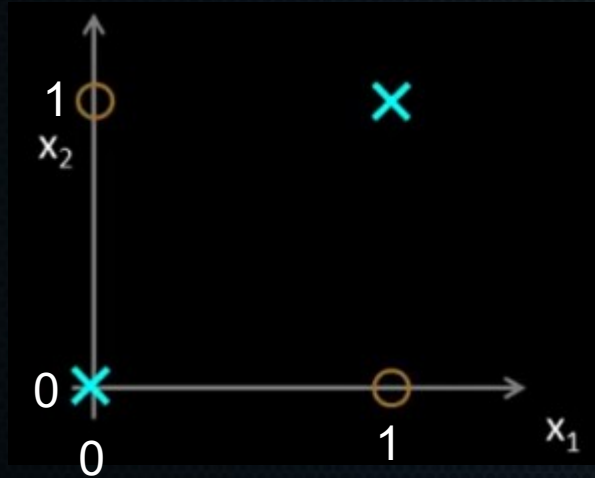
| $x$ | $y$ | $x \oplus y$ |
|-----|-----|--------------|
| 0   | 0   | 0            |
| 0   | 1   | 1            |
| 1   | 0   | 1            |
| 1   | 1   | 0            |

Source: <https://introcs.cs.princeton.edu/java/71boolean/>

See for more info: [https://www.tutorialspoint.com/computer\\_logical\\_organization/logic\\_gates.htm](https://www.tutorialspoint.com/computer_logical_organization/logic_gates.htm)

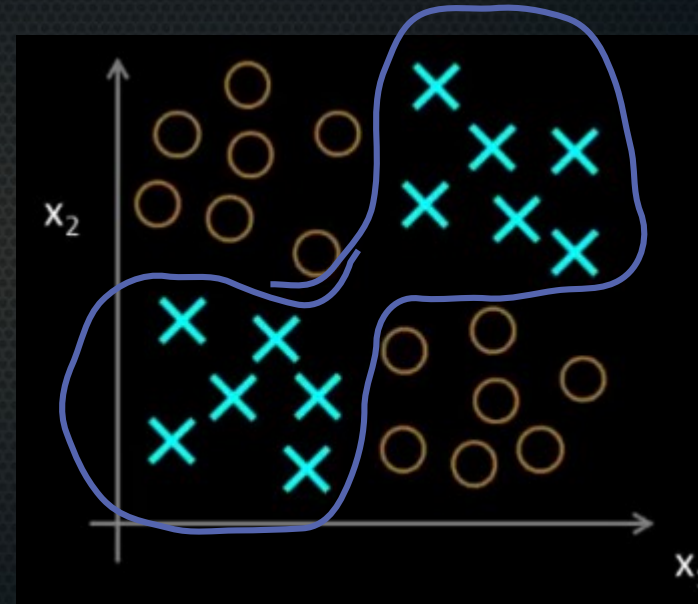
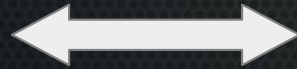
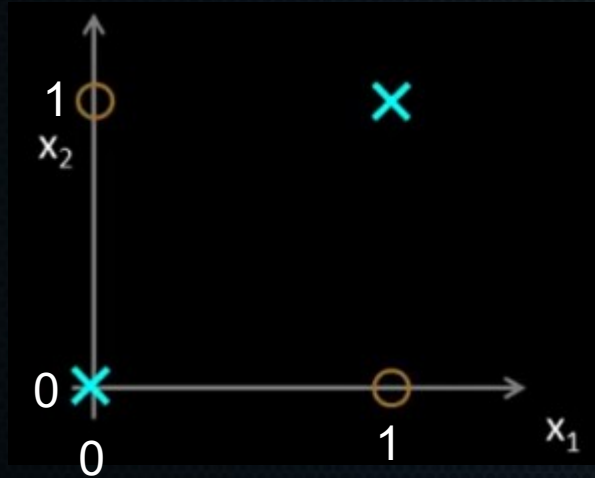
# Making simple functions ourselves

- Motivating example:



# Making simple functions ourselves

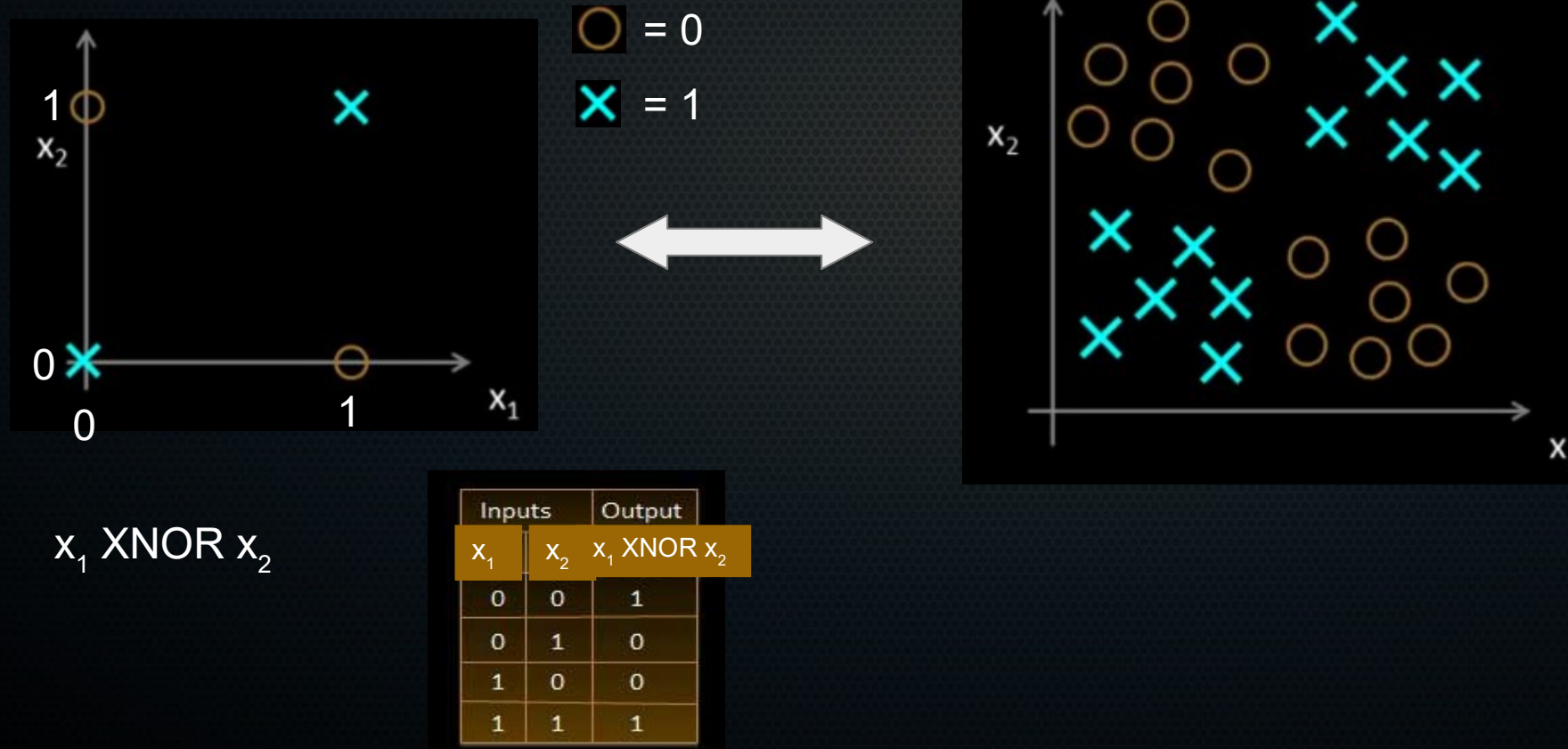
- Motivating example:





# Making simple functions ourselves

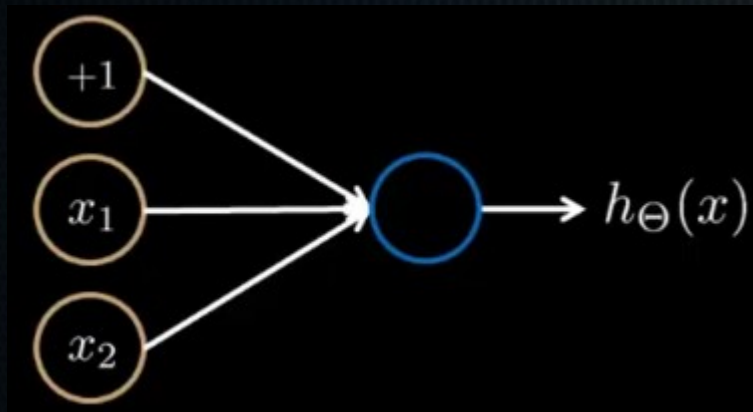
- Motivating example:



# Making simple functions ourselves

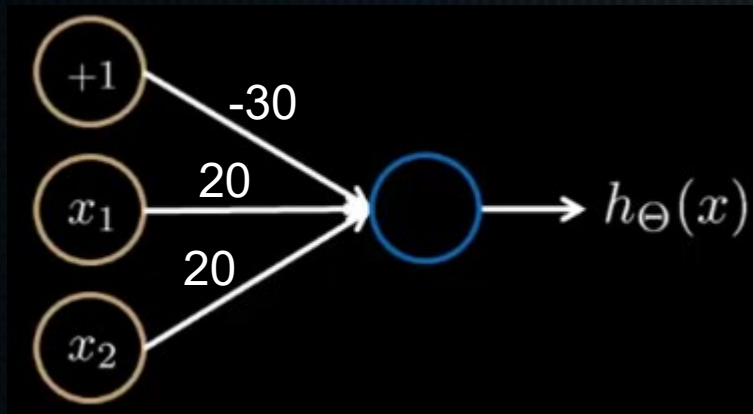
---

- AND function  $\rightarrow x_1$  and  $x_2$  can be either 0 or 1



# Making simple functions ourselves

- AND function  $\rightarrow x_1$  and  $x_2$  can be either 0 or 1



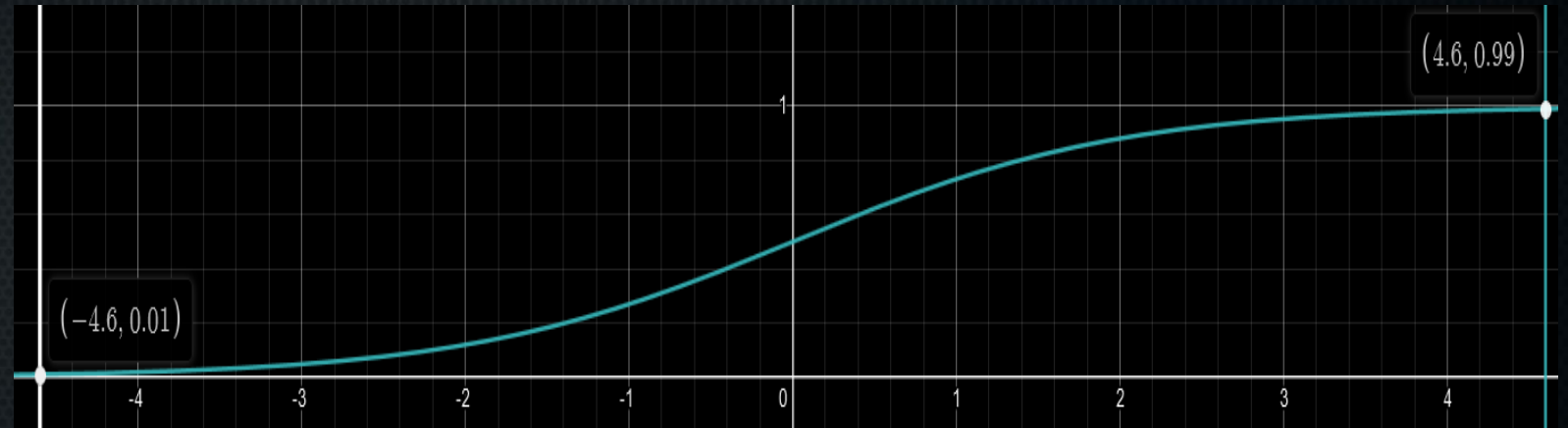
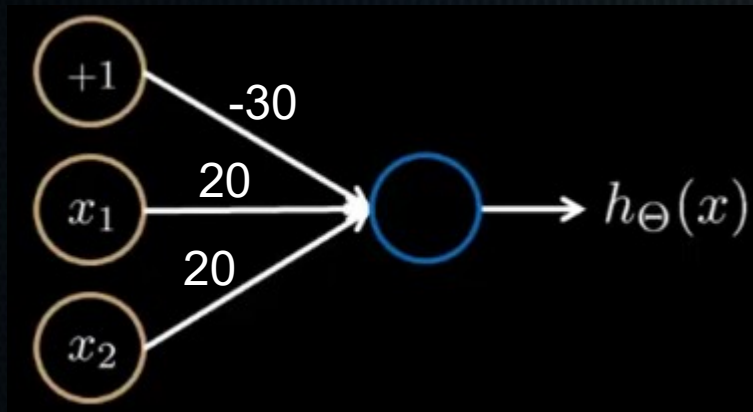
$$h_{\theta}(x) = \text{sigmoid}(-30 + 20 \cdot x_1 + 20 \cdot x_2)$$

$$h_{\theta}(x) = \sigma \left( \begin{bmatrix} -30 & 20 & 20 \end{bmatrix} \begin{bmatrix} 1 \\ x_1 \\ x_2 \end{bmatrix} \right)$$



# Making simple functions ourselves

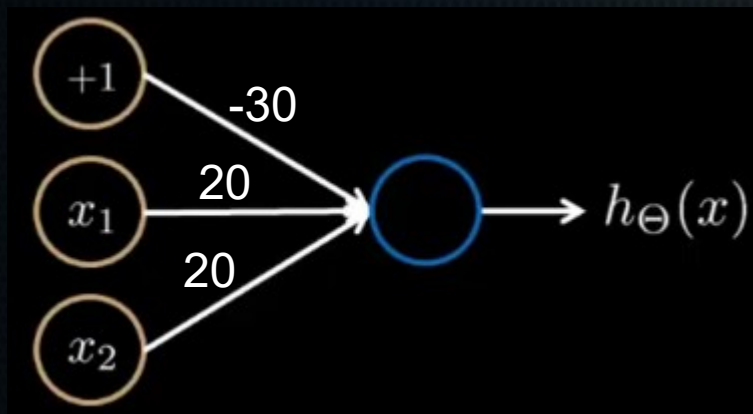
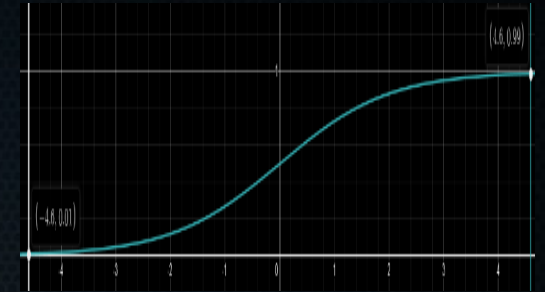
- AND function  $\rightarrow x_1$  and  $x_2$  can be either 0 or 1



$$h_{\theta}(x) = \text{sigmoid}(-30 + 20 \cdot x_1 + 20 \cdot x_2)$$

# Making simple functions ourselves: AND

- AND function  $\rightarrow x_1$  and  $x_2$  can be either 0 or 1

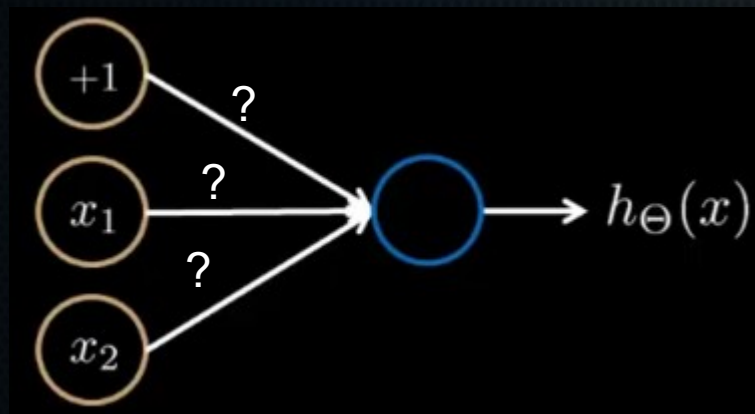
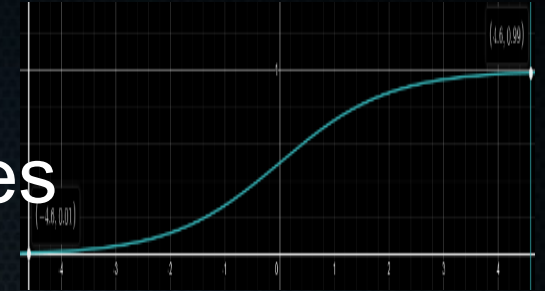


$$h_{\theta}(x) = \text{sigmoid}(-30 + 20 \cdot x_1 + 20 \cdot x_2)$$

| $x_1$ | $x_2$ | $h_{\theta}(x)$    |
|-------|-------|--------------------|
| 0     | 0     | $g(-30) \approx 0$ |
| 0     | 1     | $g(-10) \approx 0$ |
| 1     | 0     | $g(-10) \approx 0$ |
| 1     | 1     | $g(10) \approx 1$  |

# Making simple functions ourselves: OR

- Over to you: make an OR function → try it yourself and discuss with neighbours for 2 minutes



OR

| x | y | x+y |
|---|---|-----|
| 0 | 0 | 0   |
| 0 | 1 | 1   |
| 1 | 0 | 1   |
| 1 | 1 | 1   |

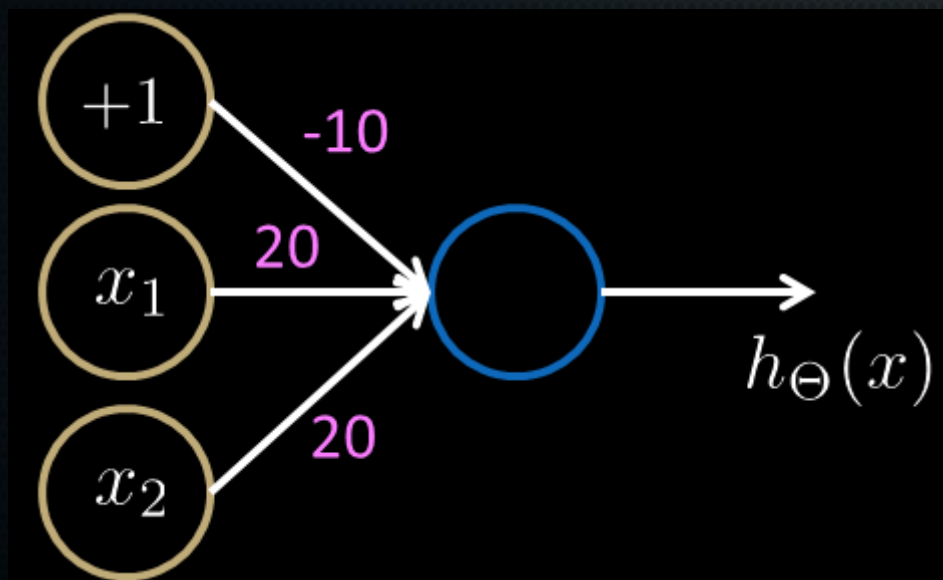
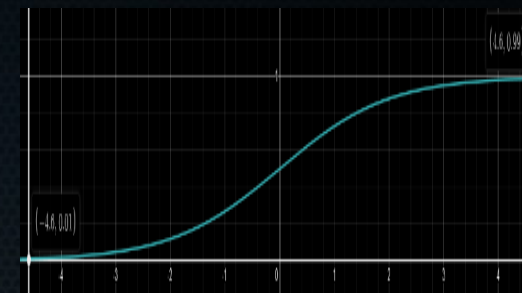
**Zorg dat ik op de slide kan schrijven!**

$h_{\theta}(x) = \text{sigmoid}(\text{?} + \text{?} \cdot x_1 + \text{?} \cdot x_2)$  **Om hier truth table van studenten te maken**



# Making simple functions ourselves: OR

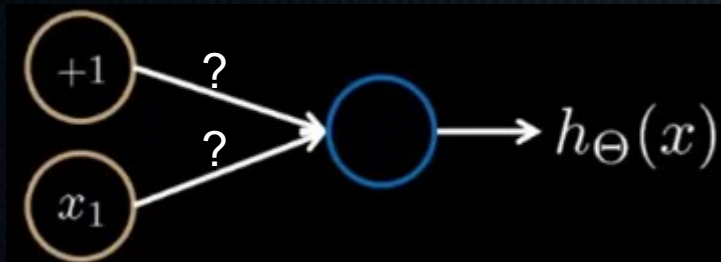
- Answer



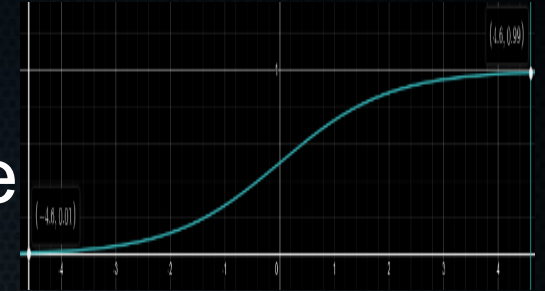
| $x_1$ | $x_2$ | $h_{\Theta}(x)$              |
|-------|-------|------------------------------|
| 0     | 0     | $g(-10) \approx 0$           |
| 0     | 1     | $g(-10+20) \approx 1$        |
| 1     | 0     | $g(-10+20) \approx 1$        |
| 1     | 1     | $g(-10 + 20 + 20) \approx 1$ |

# Making simple functions ourselves: NOT

- Over to you: make a NOT function → try it yourself and discuss with neighbours for 2 minute



| NOT |      |
|-----|------|
| $x$ | $x'$ |
| 0   | 1    |
| 1   | 0    |



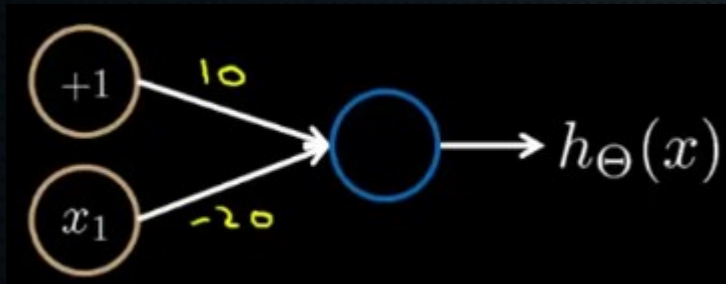
**Zorg dat ik op de slide kan schrijven!**

$$h_{\theta}(x) = \text{sigmoid}(\text{?} + \text{?} \cdot x_1)$$

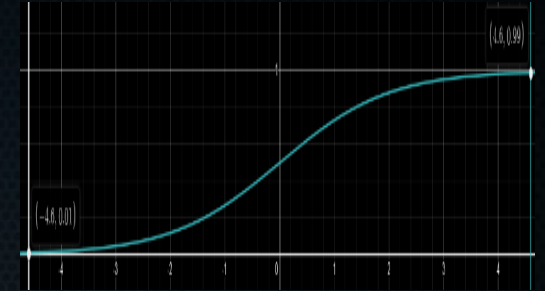
**Om hier truth table van studenten te maken**

# Making simple functions ourselves: NOT

- Answer



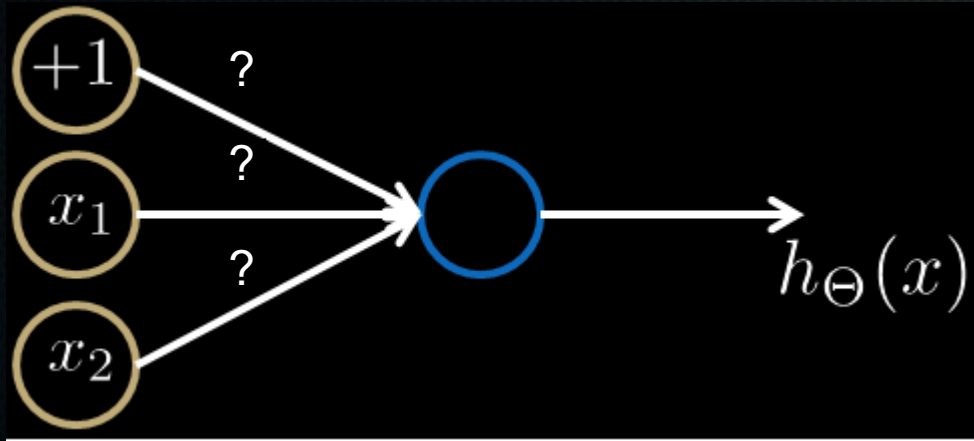
Just put a large negative weight in front of whatever you want to negate (enough to overcome the bias)





# Making simple functions ourselves: (NOT $x_1$ ) AND (NOT $x_2$ )

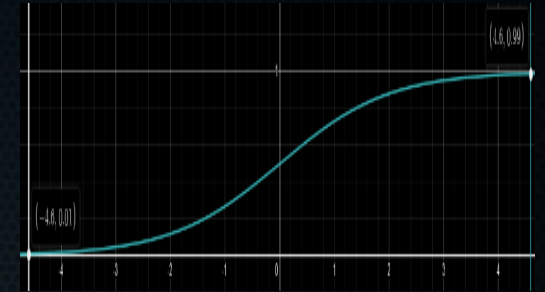
- Make NOT  $x_1$  AND NOT  $x_2 \rightarrow$  try it yourself and discuss with neighbours for 2 minutes



$$h_{\theta}(x) = \text{sigmoid} (? + ? \cdot x_1 + ? \cdot x_2)$$

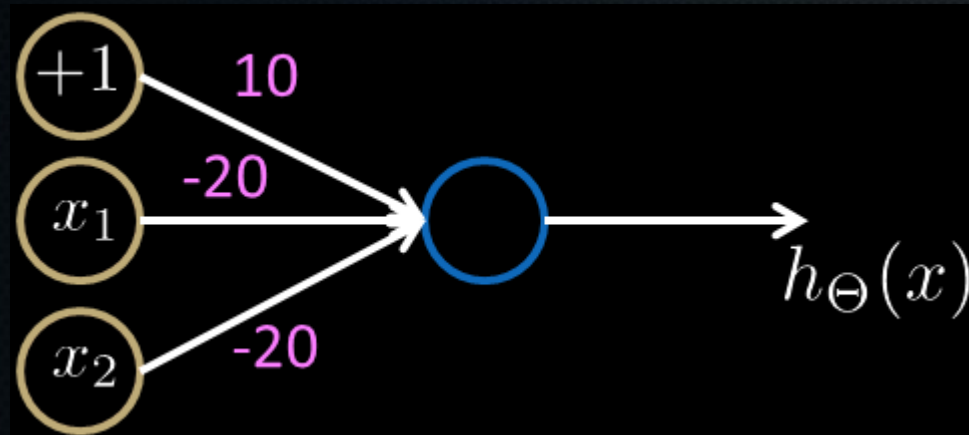
**Zorg dat ik op de slide kan schrijven!**

**Om hier truth table van studenten te maken**



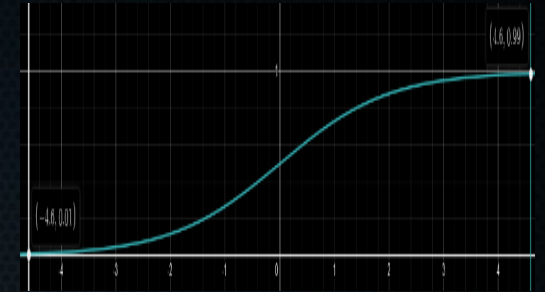
# Making simple functions ourselves: (NOT $x_1$ ) AND (NOT $x_2$ )

- Answer

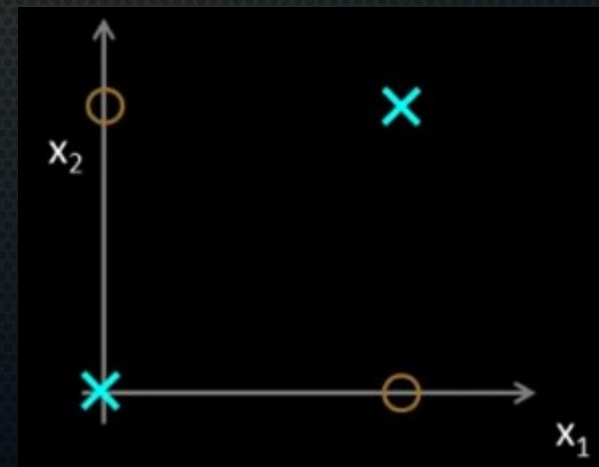
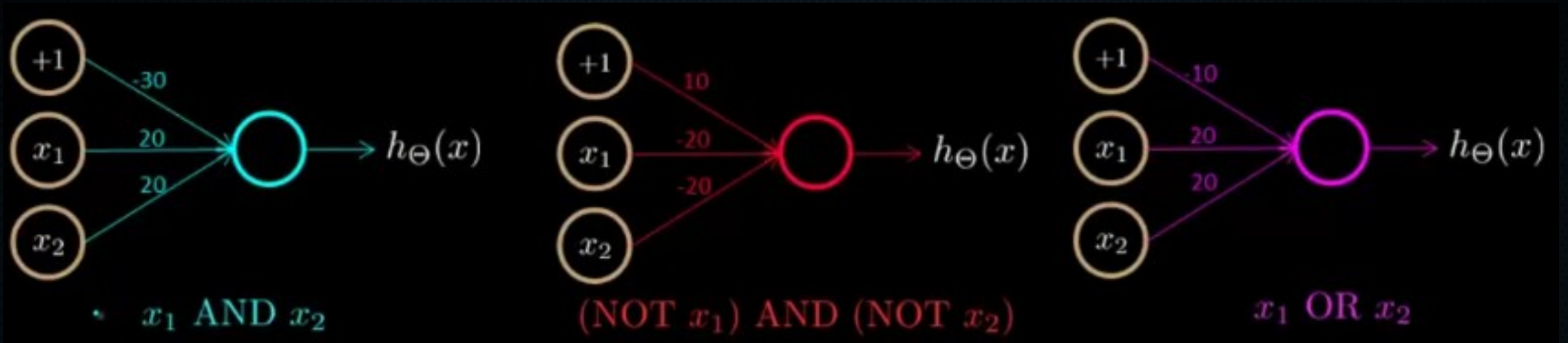


Just put a large negative weight in front of whatever you want to negate (enough to overcome the bias)

Only positive when  $x_1 = x_2 = 0$



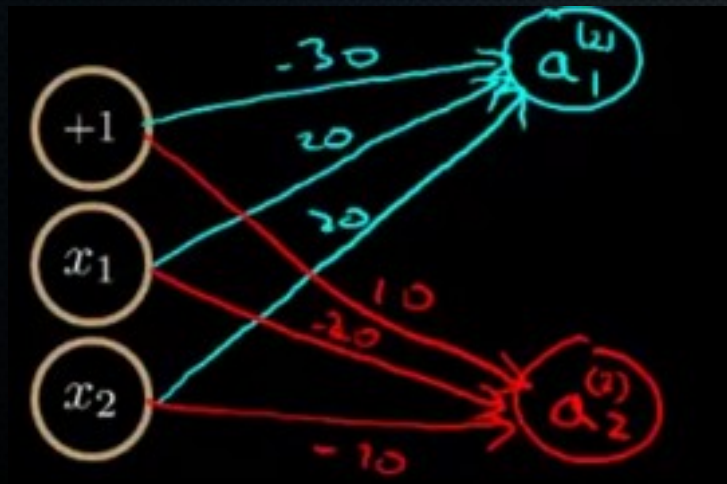
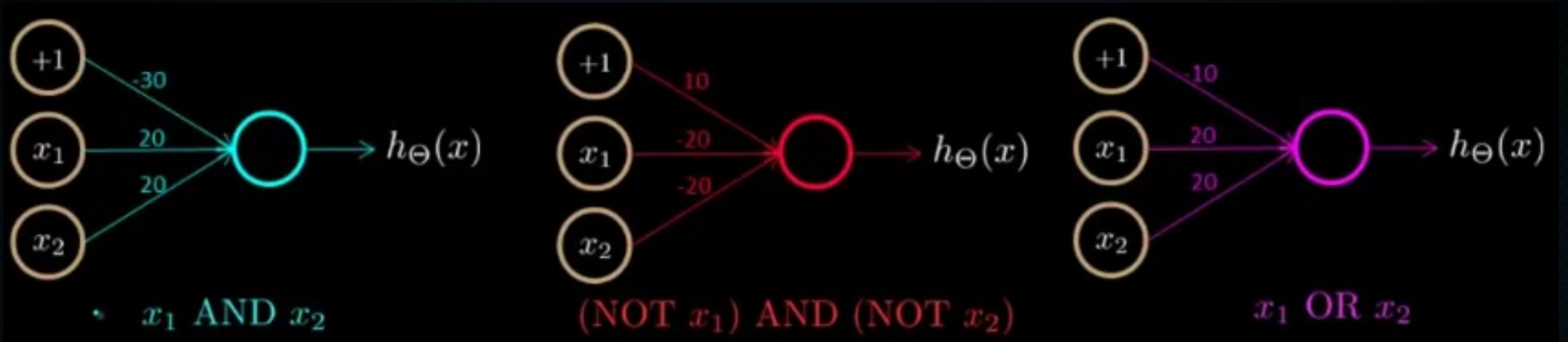
# Finally: $x_1$ XNOR $x_2$



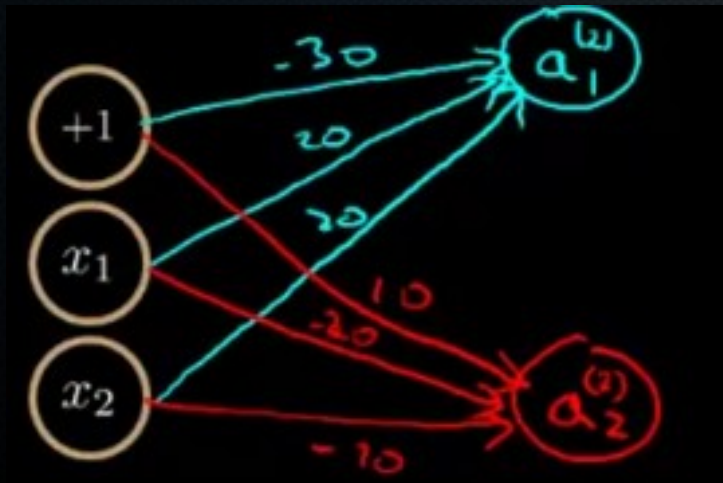
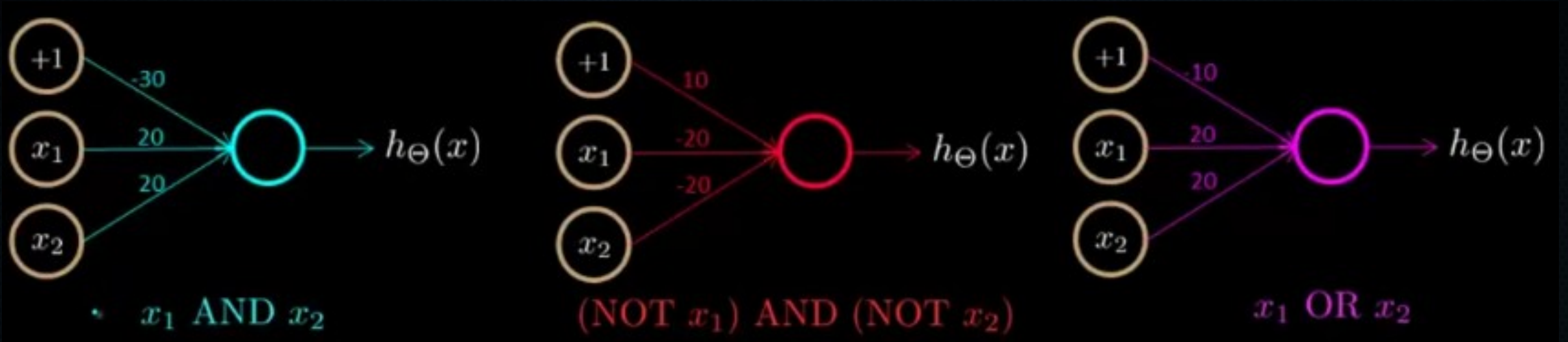
○ = 0  
x = 1



# Finally: $x_1$ XNOR $x_2$



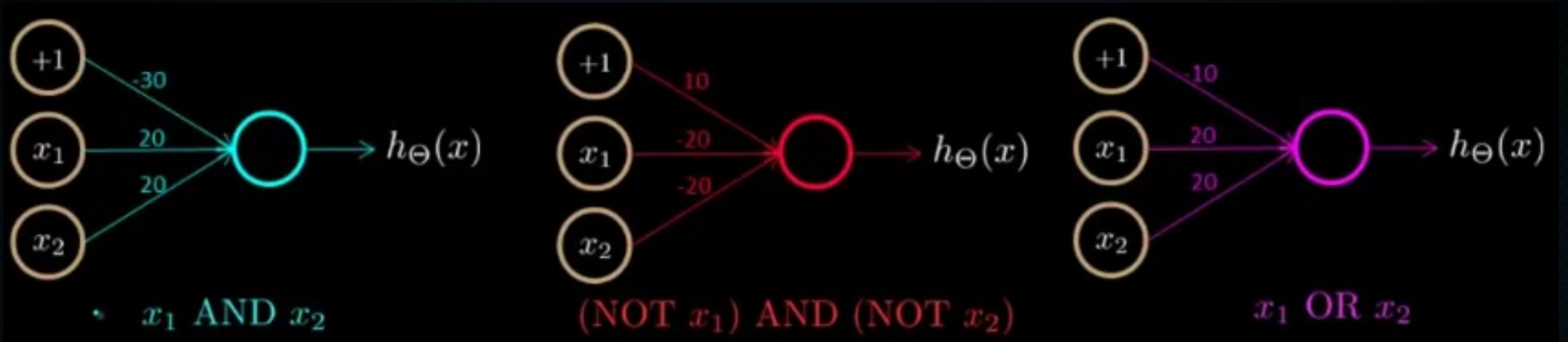
# Finally: $x_1$ XNOR $x_2$



| $x_1$ | $x_2$ | $a_1^{(2)}$ | $a_2^{(2)}$ |
|-------|-------|-------------|-------------|
| 0     | 0     | 0           | 1           |
| 0     | 1     | 0           | 0           |
| 1     | 0     | 0           | 0           |
| 1     | 1     | 1           | 0           |



# Finally: $x_1$ XNOR $x_2$



| $x_1$ | $x_2$ | $a_1^{(2)}$ | $a_2^{(2)}$ | $h_{\Theta}(x)$ |
|-------|-------|-------------|-------------|-----------------|
| 0     | 0     | 0           | 1           | 1               |
| 0     | 1     | 0           | 0           | 0               |
| 1     | 0     | 0           | 0           | 0               |
| 1     | 1     | 1           | 0           | 1               |

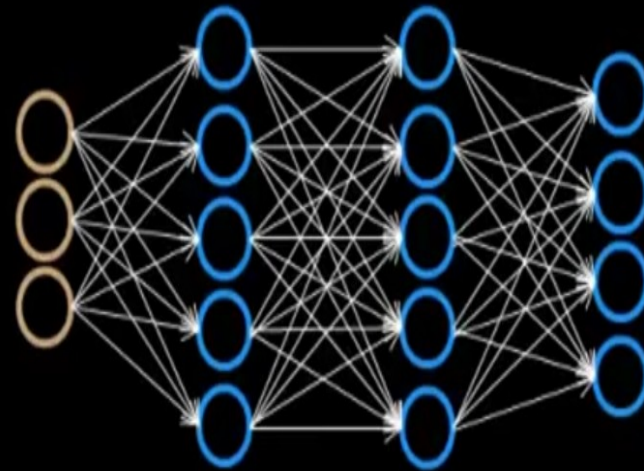


# Computing complex functions

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- This is an illustration of how neural networks work: earlier layers can compute simple functions like AND and OR. By combining those outputs, you can compute more complex functions.

# Multiclass classification in neural nets

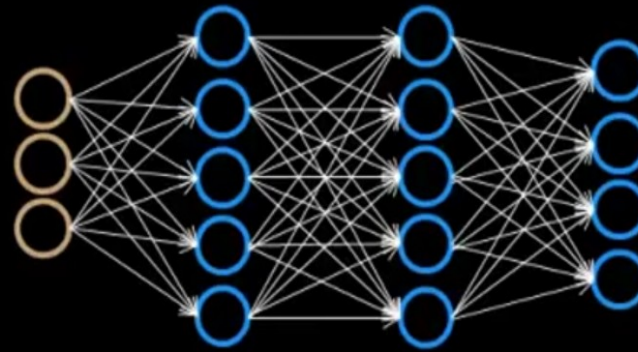


$$h_{\Theta}(x) \in \mathbb{R}^4$$

Want  $h_{\Theta}(x) \approx \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ,  $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$ ,  $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$ , etc.  
when pedestrian      when car      when motorcycle



# Multiclass classification in neural nets



$$h_{\Theta}(x) \in \mathbb{R}^4$$

Want  $h_{\Theta}(x) \approx \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ,  $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$ ,  $h_{\Theta}(x) \approx \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$ , etc.  
when pedestrian      when car      when motorcycle

Training set:  $(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), \dots, (x^{(m)}, y^{(m)})$

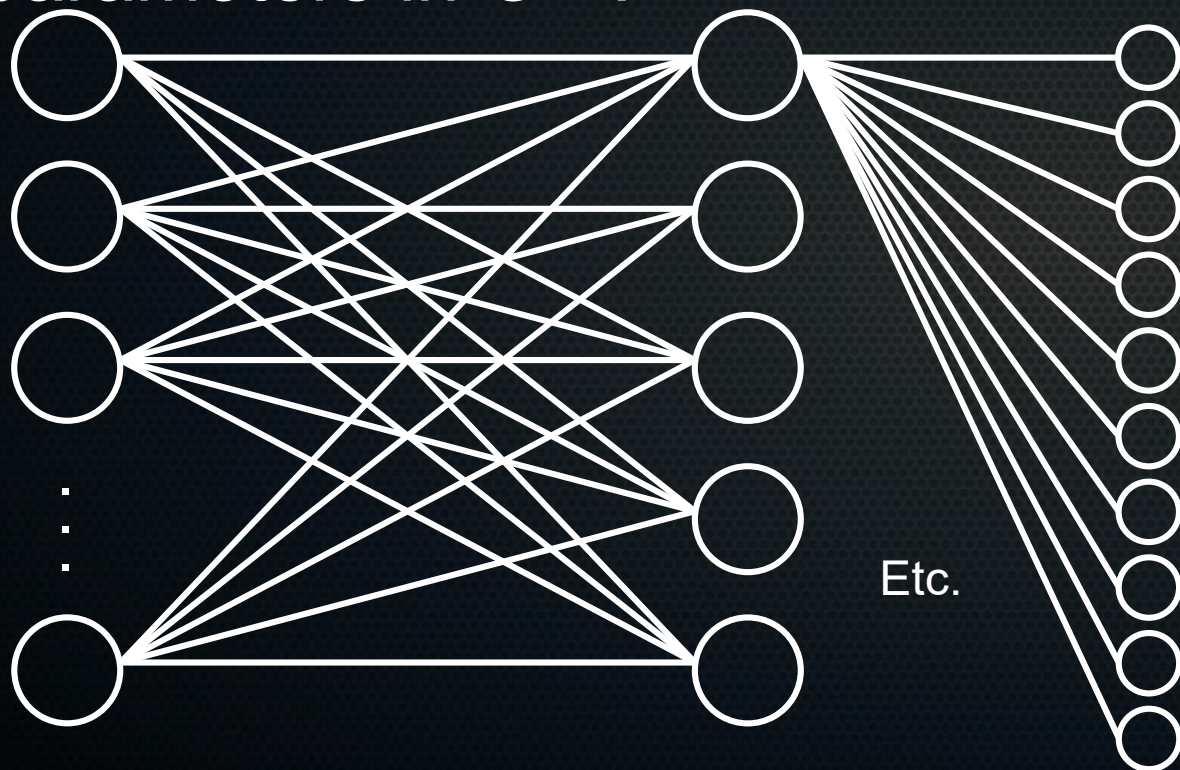
$y^{(i)}$  one of  $\begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}$ ,  $\begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix}$ ,  $\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix}$ ,  $\begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix}$   
pedestrian      car      motorcycle      truck

~~Previously~~  
 ~~$y \in \{1, 2, 3, 4\}$~~



# Question to you

- Say we have 10 classes and the following network, how many parameters in  $\Theta^{(2)}$ ?



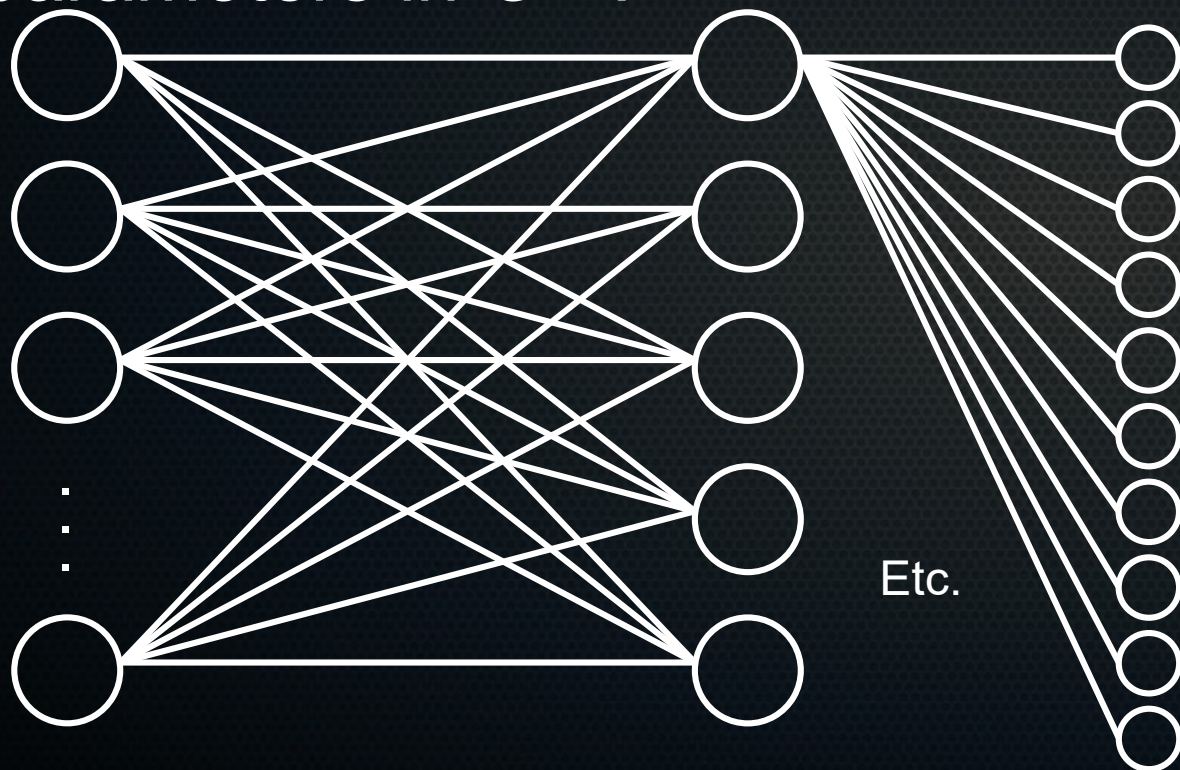
$\Theta^{(j)}$  = matrix of weights controlling function mapping from layer  $j$  to layer  $j + 1$

$$y^{(10)} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Example:  
10th training  
sample is class 3

# Question to you

- Say we have 10 classes and the following network, how many parameters in  $\Theta^{(2)}$ ?



$\Theta^{(j)}$  = matrix of weights controlling function mapping from layer  $j$  to layer  $j + 1$

$$y^{(10)} = \begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

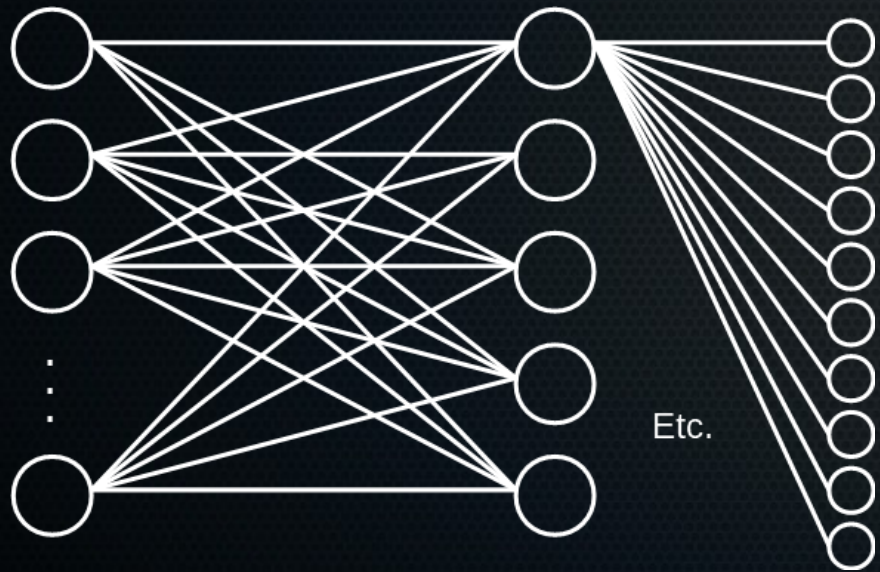
Example:  
10th training  
sample is class 3

- Answer: 60.  $5 \times 10 \rightarrow$  weights between units.  
+ 10  $\rightarrow$  bias of each unit in output layer



# Question to you

- Say we have 10 classes and the following network, how many parameters in  $\Theta^{(2)}$ ?



$$\sigma \left( \overbrace{\begin{bmatrix} b_1 & w_{11} & w_{12} & w_{13} & w_{14} & w_{15} \\ b_2 & w_{21} & w_{22} & w_{23} & w_{24} & w_{25} \\ b_3 & w_{31} & w_{32} & w_{33} & w_{34} & w_{35} \\ b_4 & w_{41} & w_{42} & w_{43} & w_{44} & w_{45} \\ b_5 & w_{51} & w_{52} & w_{53} & w_{54} & w_{55} \end{bmatrix}}^{\Theta^{(2)}} \begin{bmatrix} 1 \\ a_1^{(2)} \\ a_2^{(2)} \\ a_3^{(2)} \\ a_4^{(2)} \\ a_5^{(2)} \end{bmatrix} \right)$$

$\Theta^{(j)}$  = matrix of weights controlling function mapping from layer  $j$  to layer  $j + 1$

- Answer: 60.  $5 \times 10 \rightarrow$  weights between units.  
+ 10  $\rightarrow$  bias of each unit in output layer



# Summary

---

- We can use individual neurons to calculate simple logic functions
- We can combine the outputs of single neurons to calculate more complex (logic) functions
- For multiclass classification, we simply make class a vector, where we strive for the real class to be  $\sim 1$ , and all other classes 0.

# Afternoon practical 1

- Laat de studenten kijken naar/lezen:

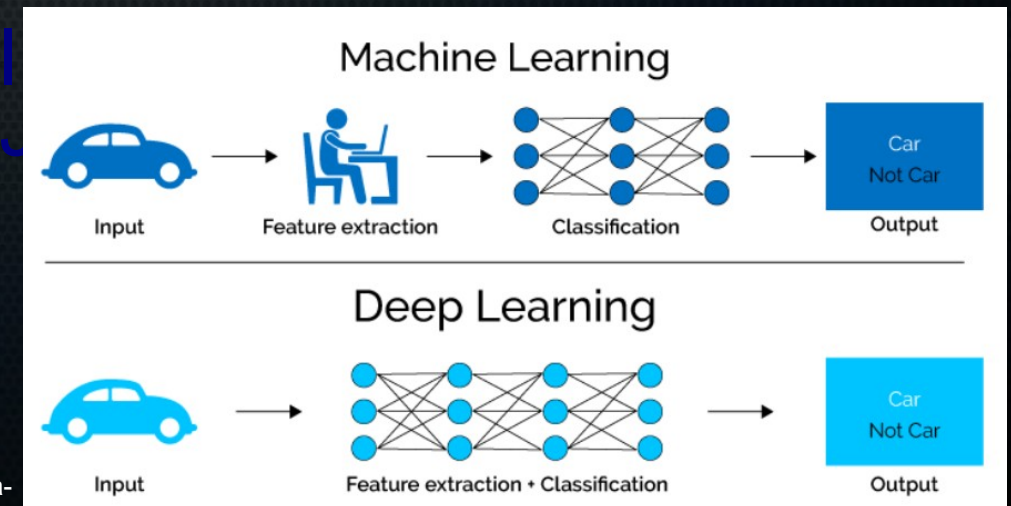
<https://www.youtube.com/watch?v=Ijqkc7OLenI> en

<http://neuralnetworksanddeeplearning.com/chap4.html>

en :

[https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1\\_67000Dx\\_ZCJB-3pi&index=1](https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1_67000Dx_ZCJB-3pi&index=1)

<https://www.youtube.com/watch?v=Ijqkc7OLenI>  
[https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1\\_67000Dx\\_ZCJB-3pi&index=1](https://www.youtube.com/watch?v=aircAruvnKk&list=PLZHQObOWTQDNU6R1_67000Dx_ZCJB-3pi&index=1)





# Afternoon practical 2

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- Multiclass logistic regression: geef bio dataset met, zeg, 6 kankerclasses en wat features.
  - laat splitsen in test en trainset
  - train 6 binaire classifiers (laat ook zelf data transformeren daartoe) met gradient descent
  - plot resultaat van elke classifier op train en testset gedurende training. (liefst in 6 aparte plotjes met decision boundary erop geprojecteerd)
- (optioneel) → laat zelfde kort doen op MNIST data
- Neural network:
  - start met vrijelijk 15 minuten klooien met <https://playground.tensorflow.org/#activation=sigmoid&batchSize=10&dataset=circle&regDataset=reg-plane&learningRate=0.03&regularizationRate=0&noise=0&networkShape=4,2,2&seed=0.12635&showTestData=false&discretize=false&percTrainData=50&x=true&y=true&xTimesY=false&xSquared=false&ySquared=false&cosX=false&sinX=false&cosY=false&sinY=false&collectStats=false&problem=classification&initZero=false&hideText=false>
  - geef netwerkarchitectuur + pretrained weights voor MNIST, laat:
    - MNIST-data visualiseren
    - zelf netwerkuitkomst bouwen middels correcte vermenigvuldigingen en toevoegen bias units
    - Afrondend: youtubefilmpje over GAN (<https://www.youtube.com/watch?v=p5U4NgVGAwg>) of jazzmuziek maken: <https://www.youtube.com/watch?v=nA3YOFUCn4U> of iets lezen over GANs als cool extra ding: <https://medium.com/sigmoid/a-brief-introduction-to-gans-and-how-to-code-them-2620ee465c30>
  - Beste misschien: laat ze clip 1 en 2 kijken van 3blue1brown neural net (~halfuur)