

Transportation Problem

Goods are produced at m different supply centers $i = 1, 2, \dots, m$.

The supply produced at supply center i is S_i , $i = 1, 2, \dots, m$.

The demand for the good comes from n different demand centers, d_j $j = 1, 2, \dots, n$.

Cost of shipping one unit from supply center i to demand center j is c_{ij} .

Variables x_{ij} define the number of units shipped from supply center i to demand center j .

Feasibility condition

$$\sum_{j=1}^n d_j \leq \sum_{i=1}^m S_i$$

Math Formulation

$$\sum_{i=1}^m \sum_{j=1}^n c_{ij} \cdot x_{ij} \tag{1}$$

$$\sum_{j=1}^n x_{ij} \leq S_i \quad i = 1, 2, \dots, m \tag{2}$$

$$\sum_{i=1}^m x_{ij} = d_j \quad j = 1, 2, \dots, n \tag{3}$$

$$x_{ij} \geq 0 \quad i = 1, 2, \dots, m, \quad j = 1, 2, \dots, n \tag{4}$$

In this problem you can also assume that variables x_{ij} take on integer values (and non-negative ones), it depends on the good you are dealing with.