

# Vehicle Routing Problem (VRP)

A seller needs to send trucks with goods to customers.

Let be the following constraints:

- Demand of each customer must be satisfied by one truck;
- Truck capacity must not be exceeded for any truck;
- Total distance should be minimized (*Objective function*);

## Parameters

- $n$  = amount of points (1 - depot, 2,  $\dots$ ,  $n$  - customers)
- $d_{ij}$  = distance from node  $i$  to node  $j$
- $D_i$  = demand of customer  $i$
- $C$  = capacity of each truck

## Variables

- $x_{ij} = \begin{cases} 1 & \text{if a truck goes from node } i \text{ to node } j; \\ 0 & \text{otherwise.} \end{cases}$
- $f_{ij}$  = number of units in a truck going from node  $i$  to node  $j$ .

$$\begin{aligned} \min \quad & \sum_{i=1}^n \sum_{j=1}^n d_{ij} \cdot x_{ij} \\ \text{s.t.} \quad & \end{aligned} \tag{1}$$

$$\sum_{j=1}^n x_{ij} = 1 \quad \forall i = 2, \dots, n \tag{2}$$

$$\sum_{j=1}^n x_{ji} = 1 \quad \forall i = 2, \dots, n \tag{3}$$

$$\sum_{j=1}^n f_{ji} - \sum_{j=1}^n f_{ij} = D_i \quad \forall i = 2, \dots, n \tag{4}$$

$$0 \leq f_{ij} \leq C \cdot x_{ij} \quad \forall i, j = 1, \dots, n \tag{5}$$

$$x_{ij} \in \{0, 1\} \quad \forall i, j = 1, \dots, n \tag{6}$$