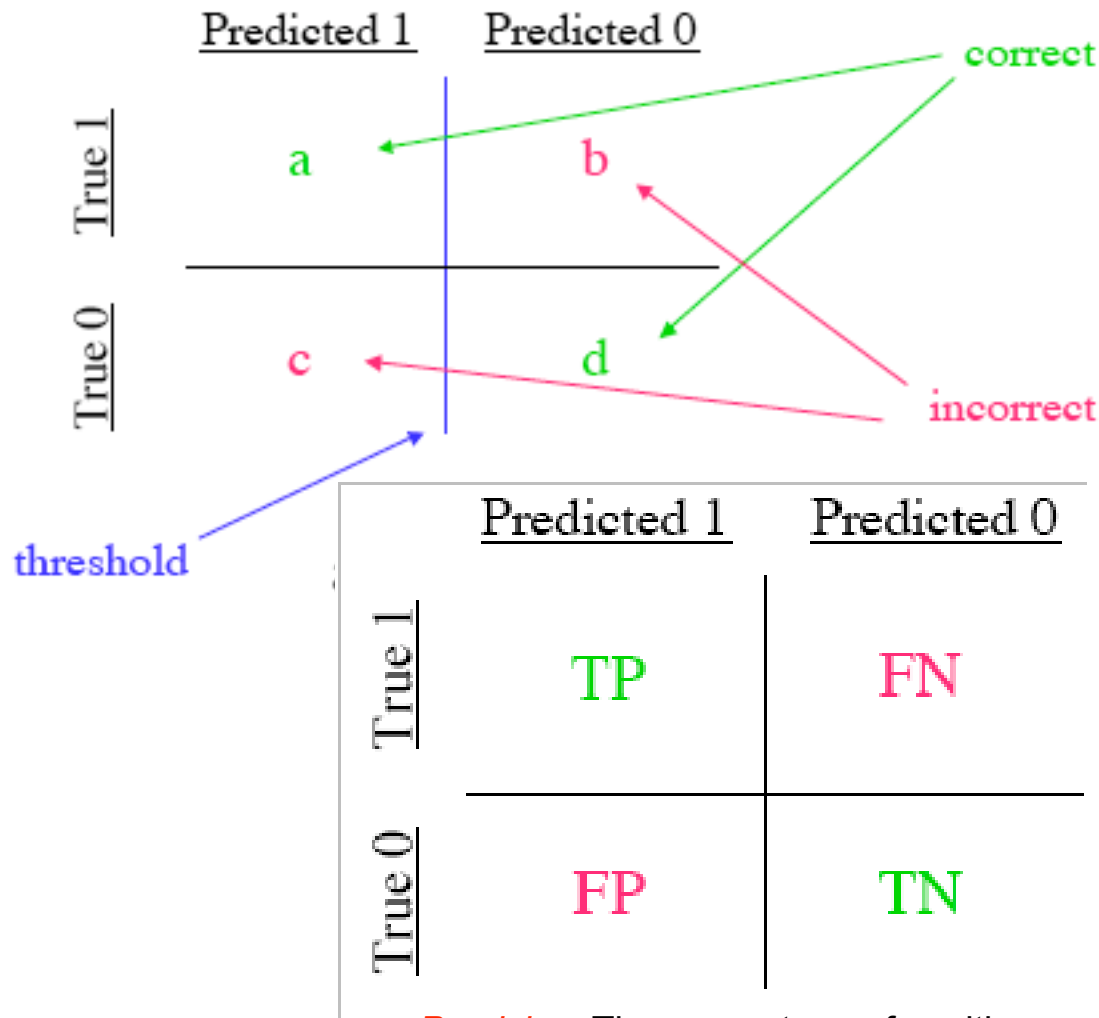


Performance Evaluation



$$\begin{aligned}
 \text{Precision} &= a/(a+c) \\
 \text{Recall} &= a/(a+b) \\
 \text{Sensitivity} &= \text{Recall} \\
 \text{Specificity} &= d/(d+c) \\
 \text{Accuracy} &= (a+d)/(a+b+c+d)
 \end{aligned}$$

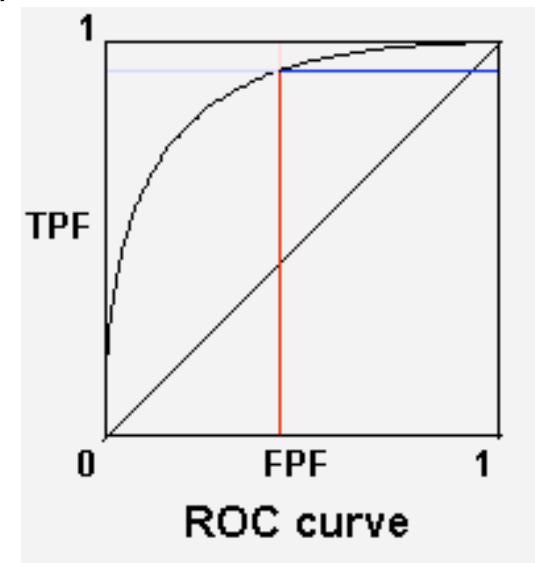
$$\begin{aligned}
 \text{TPR} &= a/(a+b) \\
 \text{FNR} &= b/(a+b) \\
 \text{FPR} &= c/(c+d) \\
 \text{TNR} &= d/(c+d) \\
 \text{TPR} + \text{FNR} &= 1 \\
 \text{FPR} + \text{TNR} &= 1
 \end{aligned}$$

Precision: The percentage of positive predictions that are correct.

Recall: The percentage of positive labeled instances that were predicted as positive.

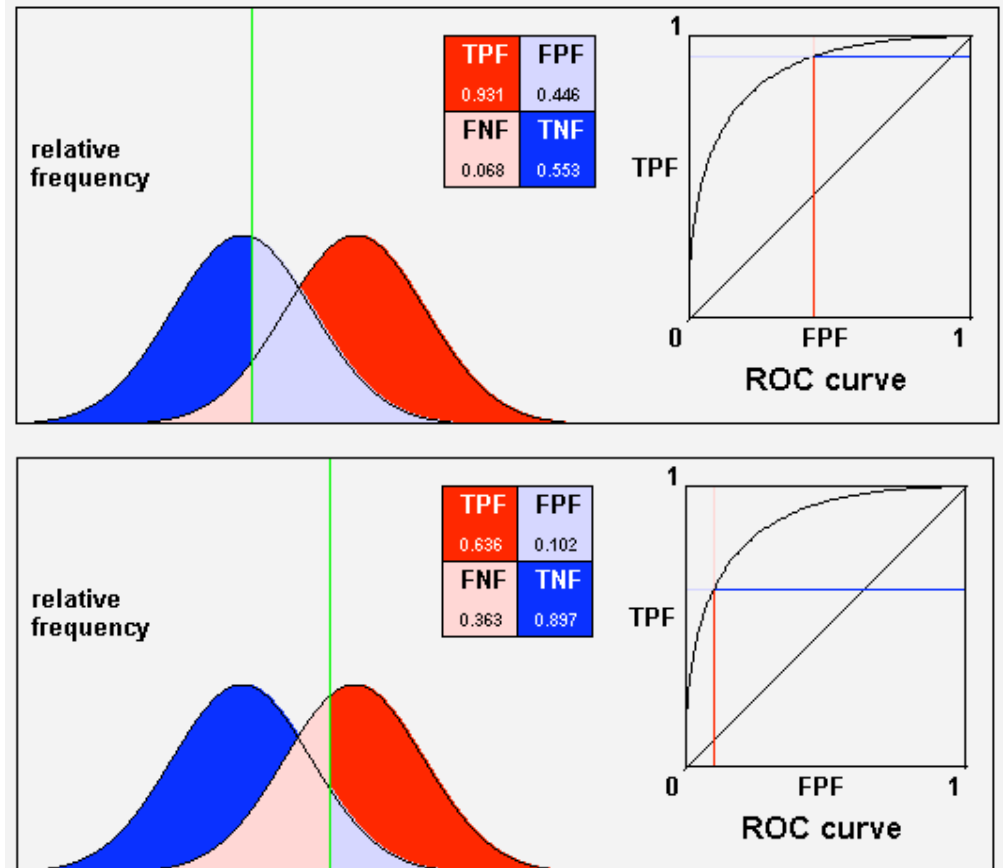
Performance Evaluation

- ROCs (Receiver Operating Characteristic Curves)
 - They are commonly used for decision-making
 - They summarize the performance of the classifier
 - Using them, it is easy to visualize and analyze the output of the classifier
 - They facilitates the comparison of the performance of different methods
 - True Positives Rate (TPR):
 - Fraction of *positives* (faces), classified as *positives*.
 - True Negative Rate (TNR):
 - Fraction of *negatives* (non-faces), classified as *negatives*.
 - False Positives Rate (FPR):
 - Fraction of *positives*, classified as *negatives*.
 - False Negative Rate (FNR):
 - Fraction of *negatives*, classified as *positives*.
- $TPR + FNR = 1$
 $TNR + FPR = 1$



Performance Evaluation

- ROCs
 - A ROC represents the accuracy of the classifier for differentiating the two classes.
 - They define how much overlapped are the outputs for the two classes (the classifier output distribution for the two classes).
 - When different threshold levels are applied to the classifier output, different operation points are obtained.
 - The larger the TPR, the larger the FPR.

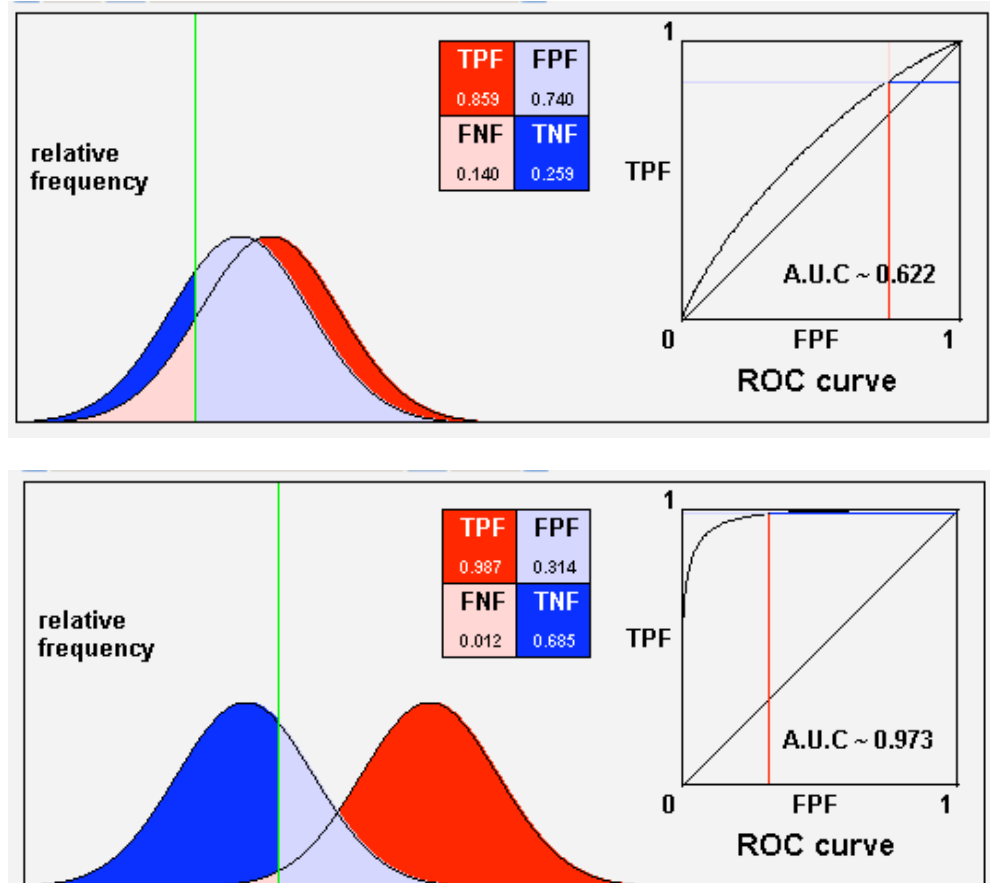


In the example the output of the classifiers each of the class follows a Gaussian distribution for

Images from: <http://www.anaesthetist.com/mnm/stats/roc/>

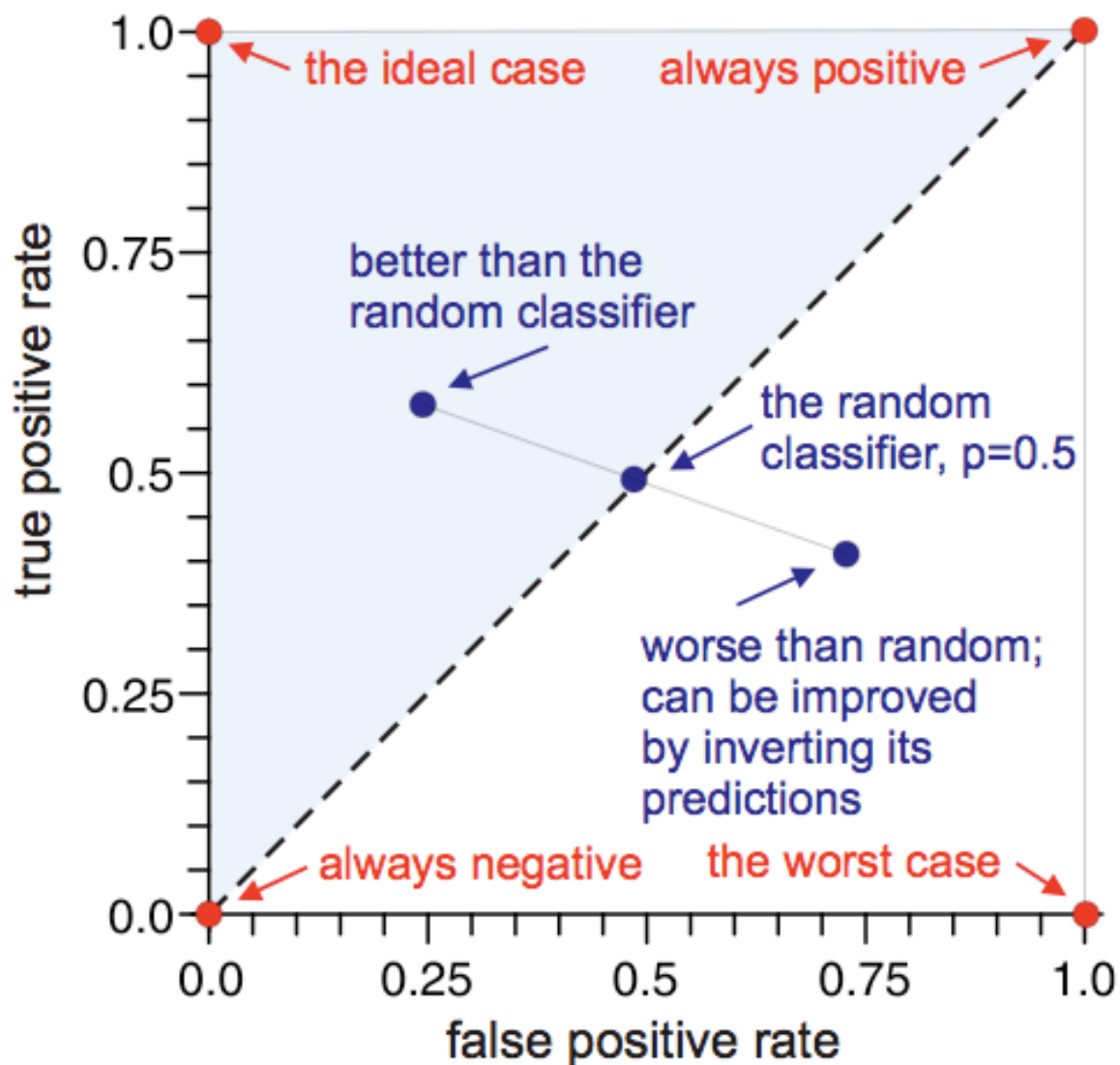
Performance Evaluation

- ROCs
 - The AUC (Area Under the Curve) is used as performance measure in some cases.
 - In detection problems is usual the use of the number of false positives, instead of the FPR.

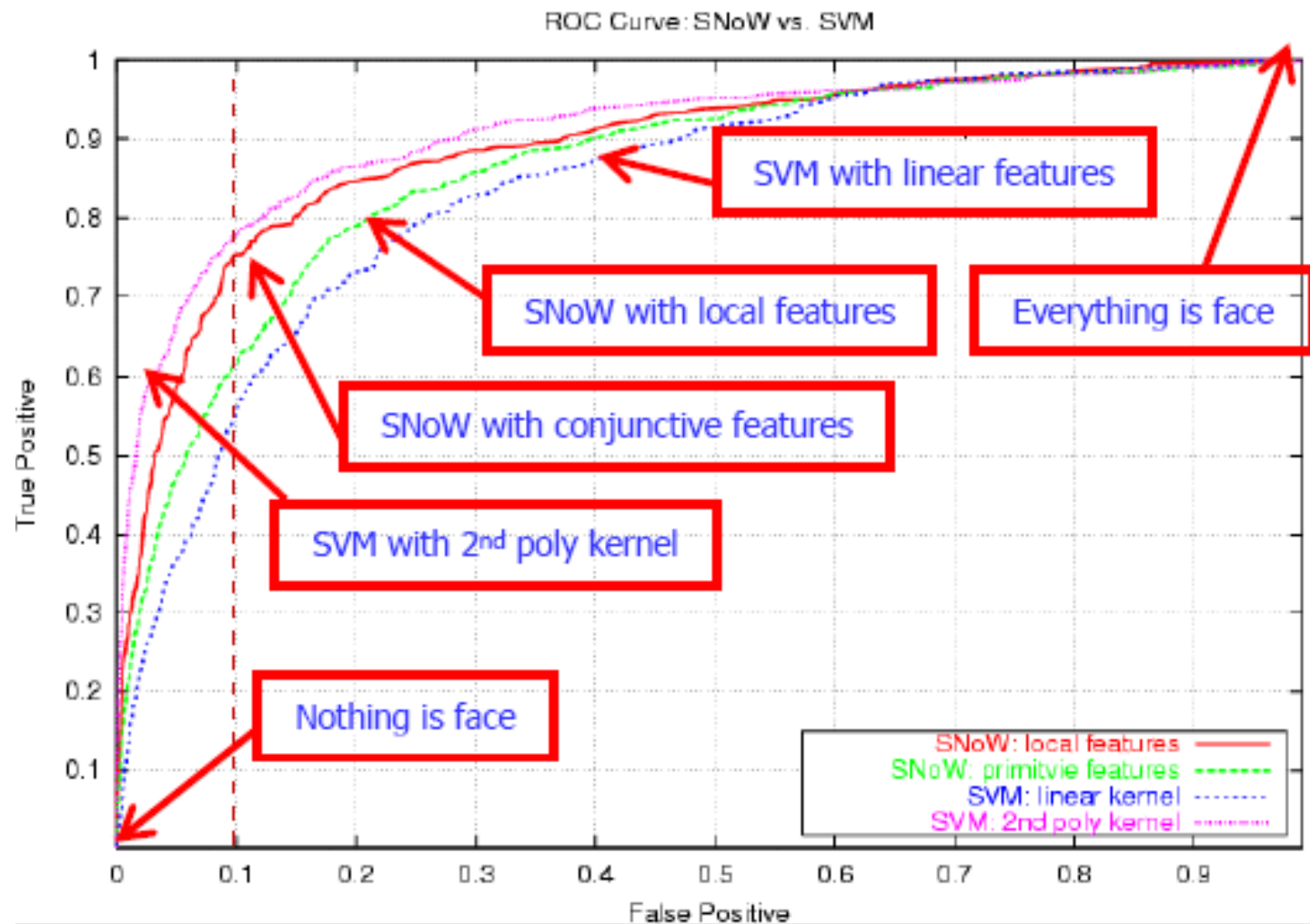


Images from: <http://www.anaesthetist.com/mnm/stats/roc/>

Properties of the ROC space

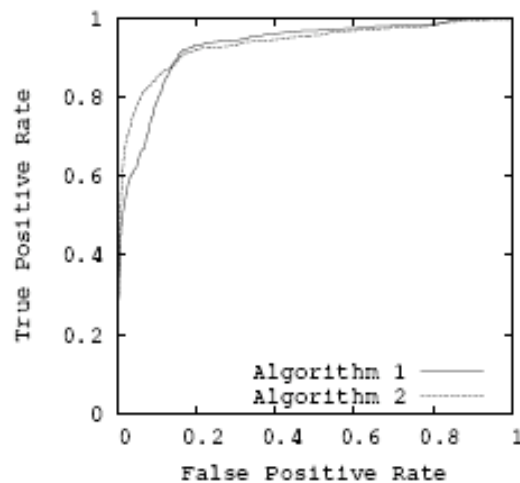


Result comparison example

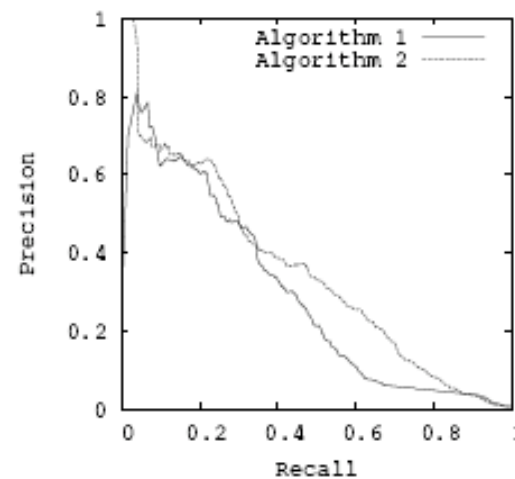


Precision-Recall Curve

- ROC curves can present an overly optimistic view of an algorithm's performance if there is a large skew in the class distribution.
- In this case Precision-Recall curves give a more informative view
- Looking at PR curves can expose differences between algorithms that are not apparent in ROC space.
- For any dataset, the ROC and PR curves for a given algorithm contain the same points.



(a) Comparison in ROC space



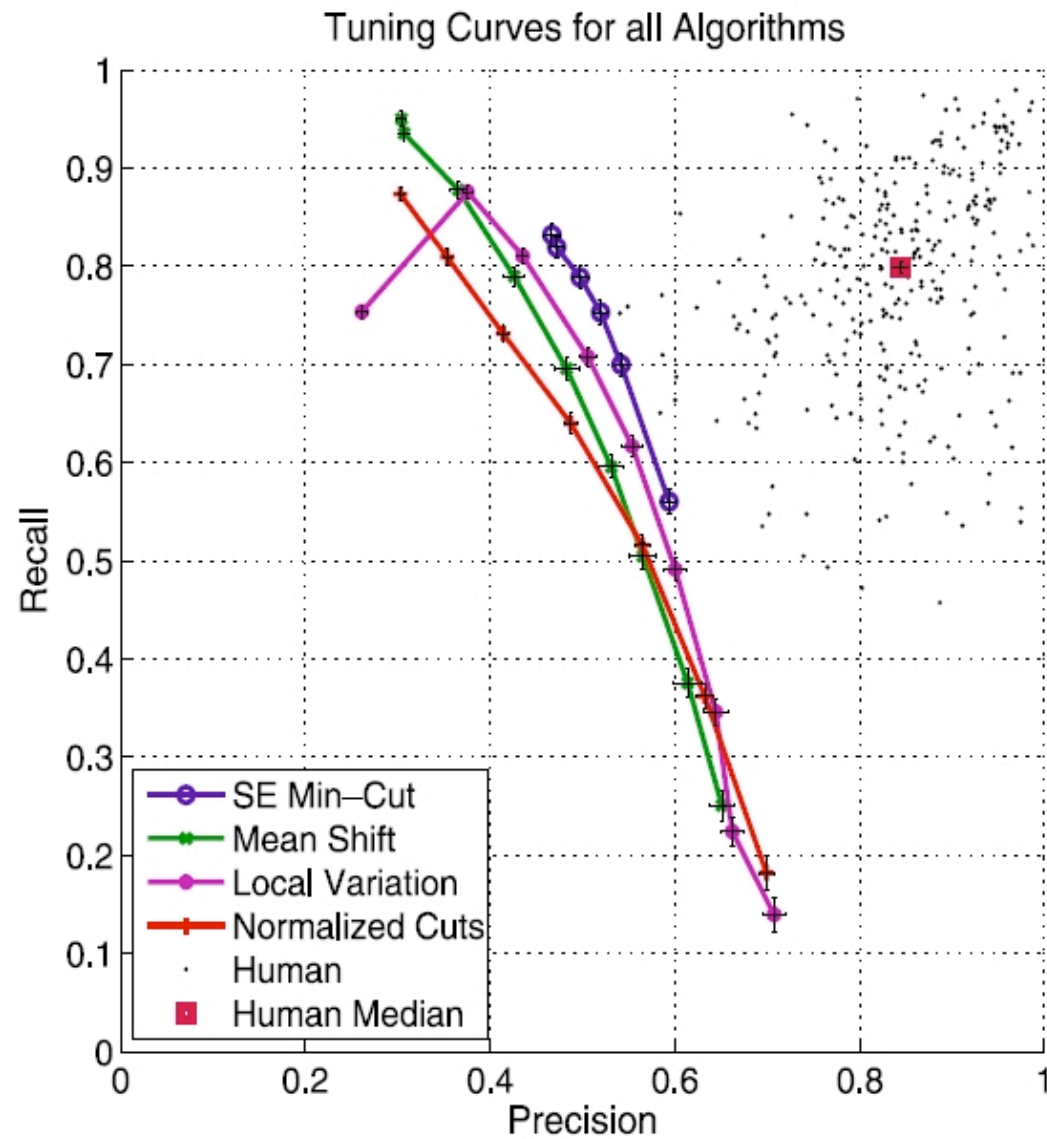
(b) Comparison in PR space

Skewness: A measure of the extent to which a probability distribution of a real-valued random variable "leans" to one side of the mean

Precision: The percentage of positive predictions that are correct.

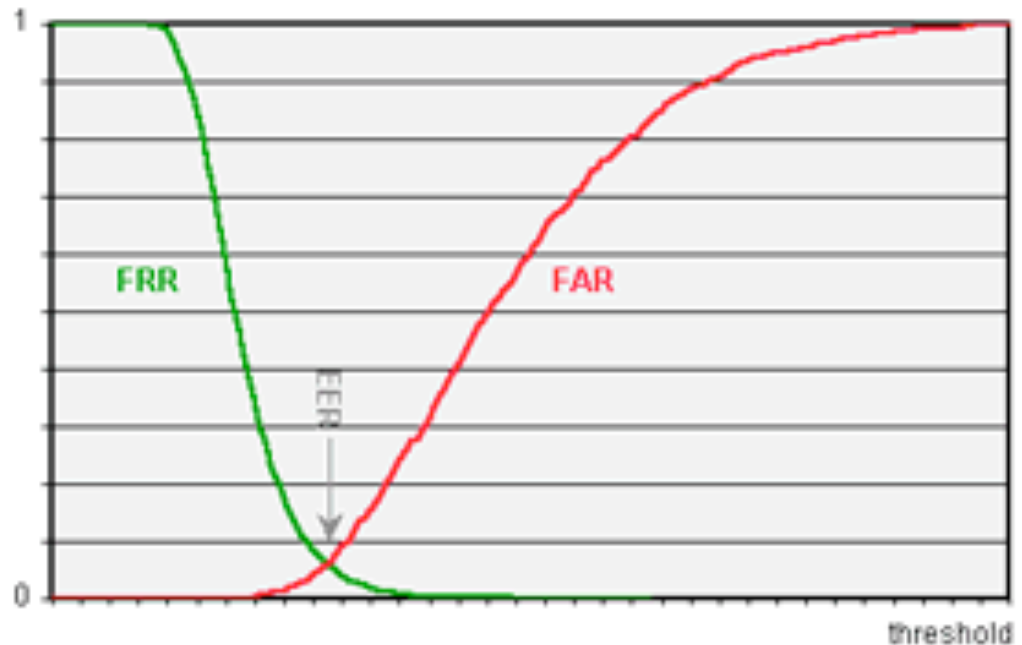
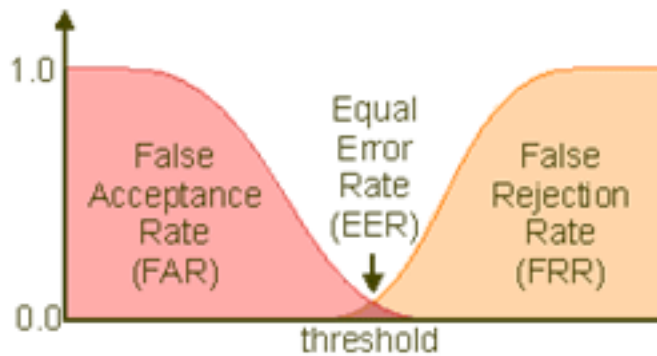
Recall: The percentage of positive labeled instances that were predicted as positive.

PR Curve Example



FAR-FRR Curve

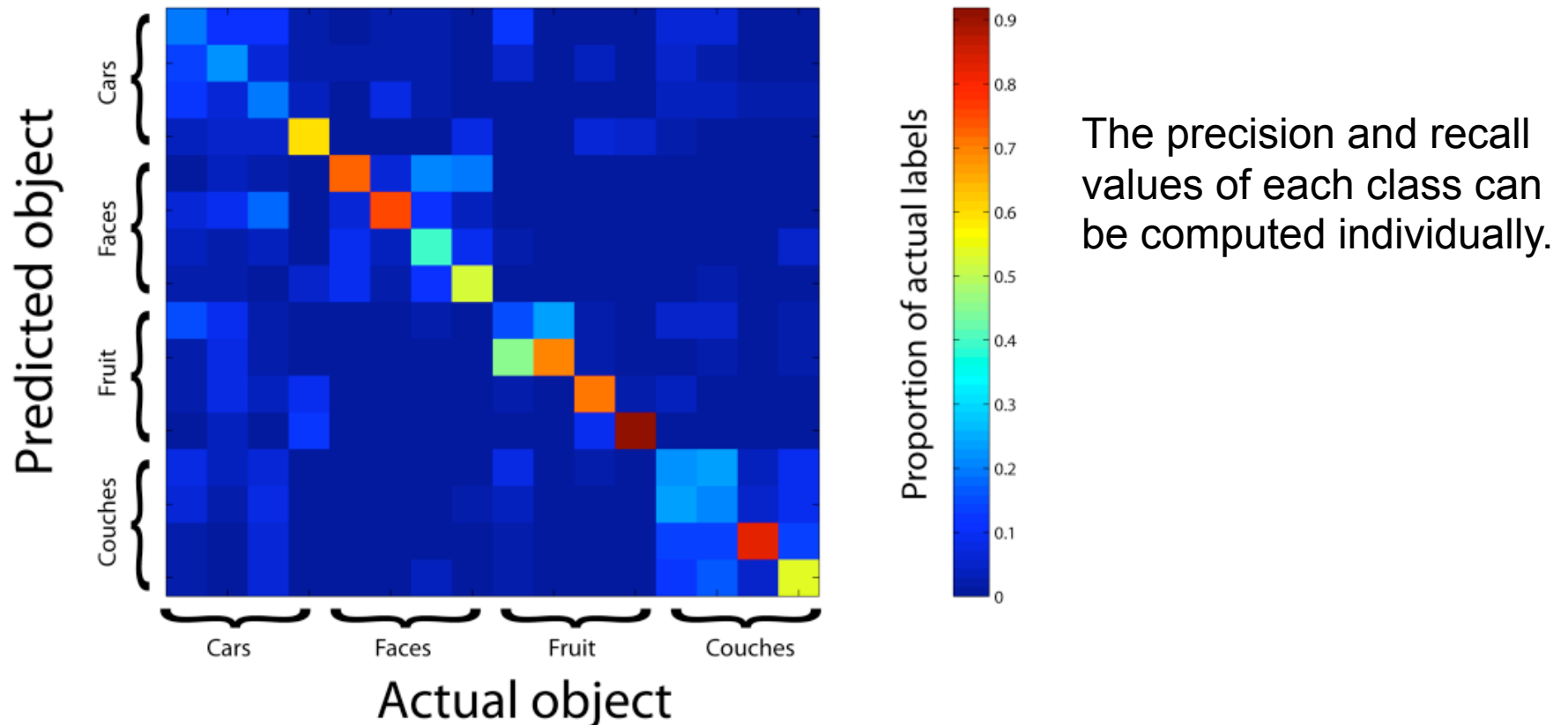
Used in biometric contexts.



$FRR = FNR$
 $FAR = FPR$

Confusion Matrix

A confusion matrix contains information about actual and predicted classifications done by a classification system.. Each column of the matrix represents the instances in a predicted class, while each row represents the instances in an actual class.



Feature Selection/Extraction

1. Measurements and different from features (e.g. pixels versus area).
2. Measurement/Feature Filtering
 - Noise filtering
 - Normalization
 - Cleaning (outliers elimination, inconsistent data, duplicate data, missing values)
 - Data discretization
3. Feature/Attribute Selection
 - Selection based on attribute characteristics, e.g. variability or correlation
 - Selection using a classifier
 - Elimination versus aggregation Strategies
4. Dimensionality Reduction
 - Features/attributes can be correlated and therefore reduced using algorithms such as PCA