

Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

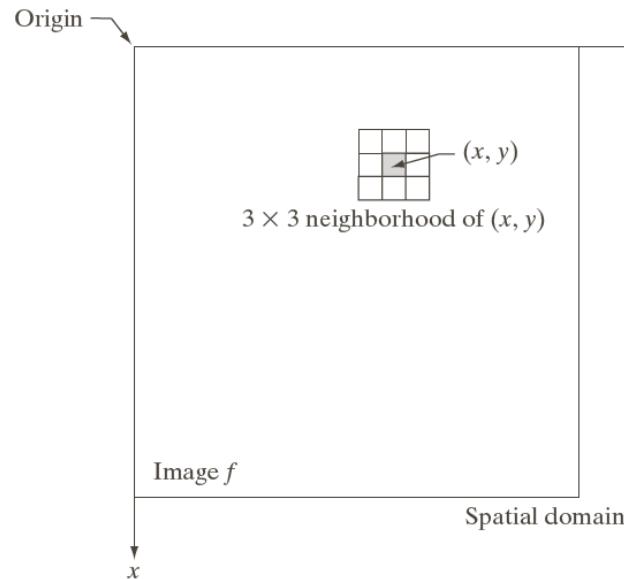
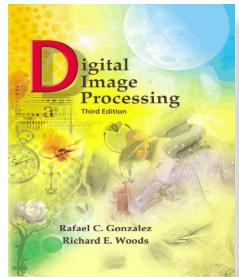


FIGURE 3.1
A 3×3 neighborhood about a point (x, y) in an image in the spatial domain. The neighborhood is moved from pixel to pixel in the image to generate an output image.



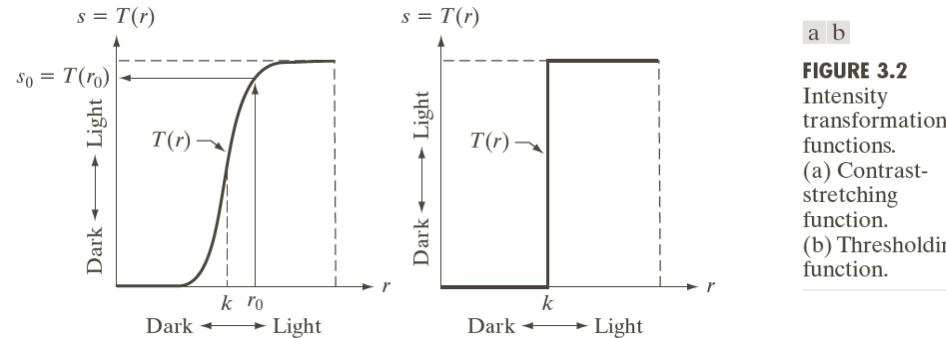
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

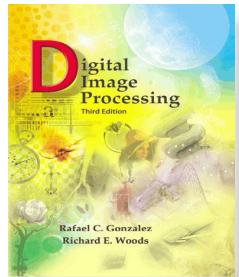
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.2
Intensity
transformation
functions.
(a) Contrast-
stretching
function.
(b) Thresholding
function.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

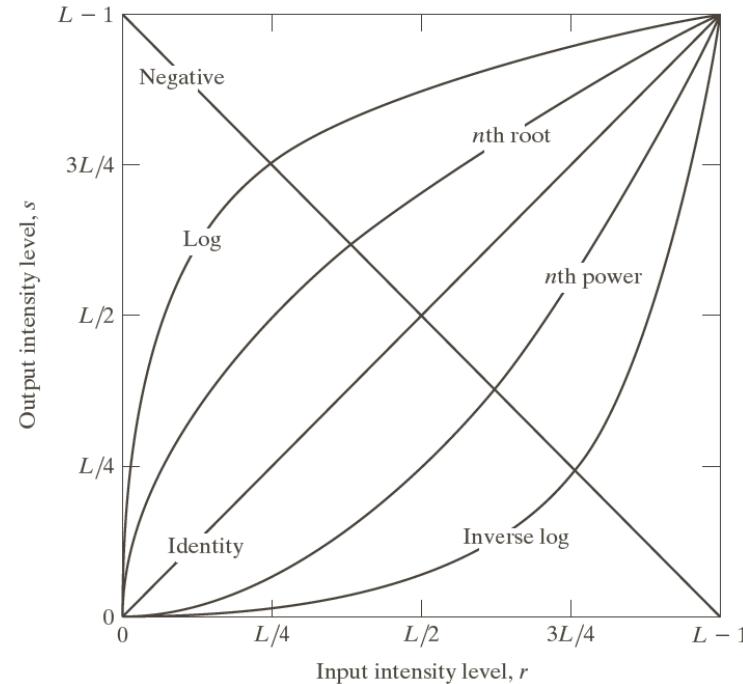
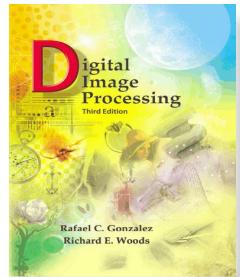


FIGURE 3.3 Some basic intensity transformation functions. All curves were scaled to fit in the range shown.



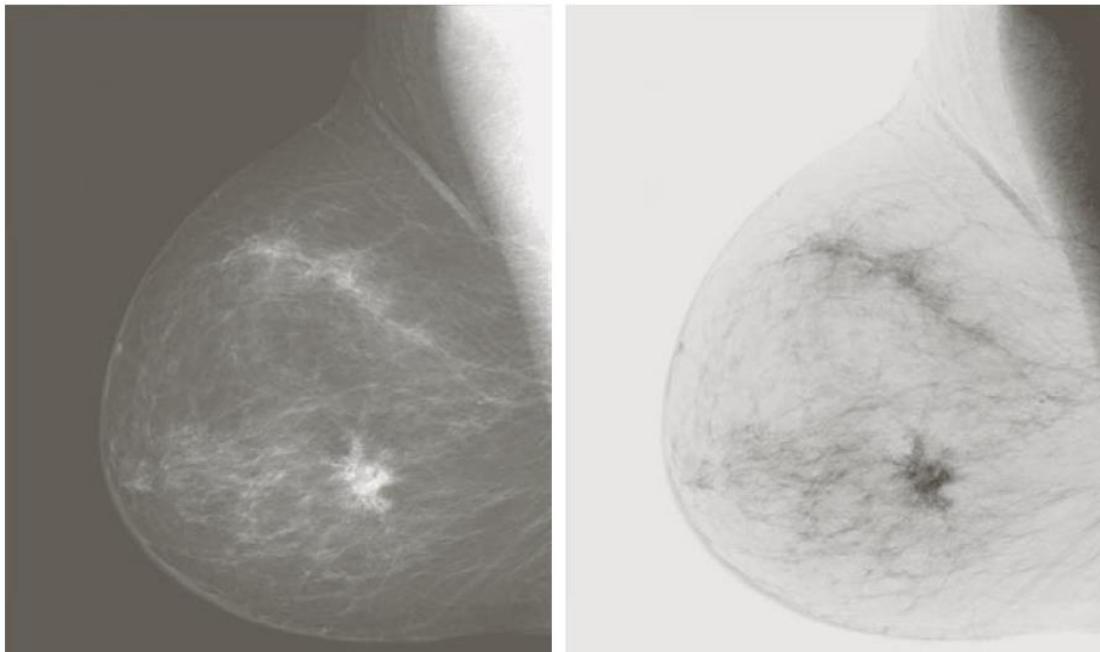
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

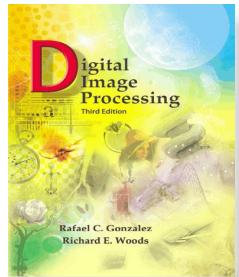
Intensity Transformations & Spatial Filtering



a b

FIGURE 3.4

(a) Original digital mammogram.
(b) Negative image obtained using the negative transformation in Eq. (3.2-1).
(Courtesy of G.E. Medical Systems.)



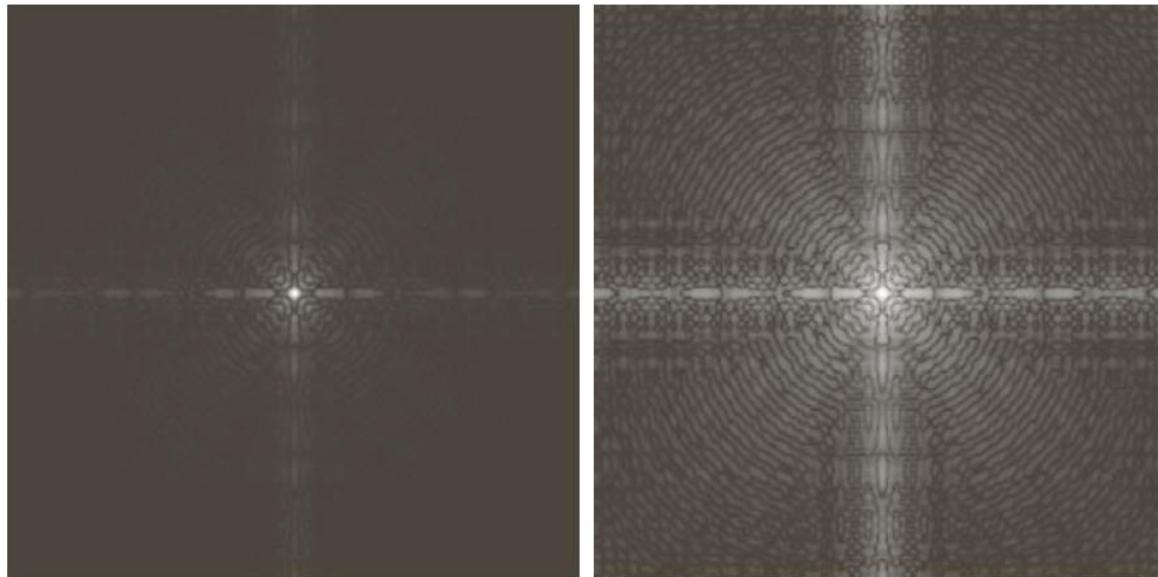
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

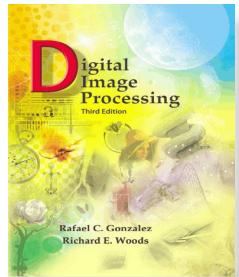
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.5
(a) Fourier spectrum.
(b) Result of applying the log transformation in Eq. (3.2-2) with $c = 1$.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

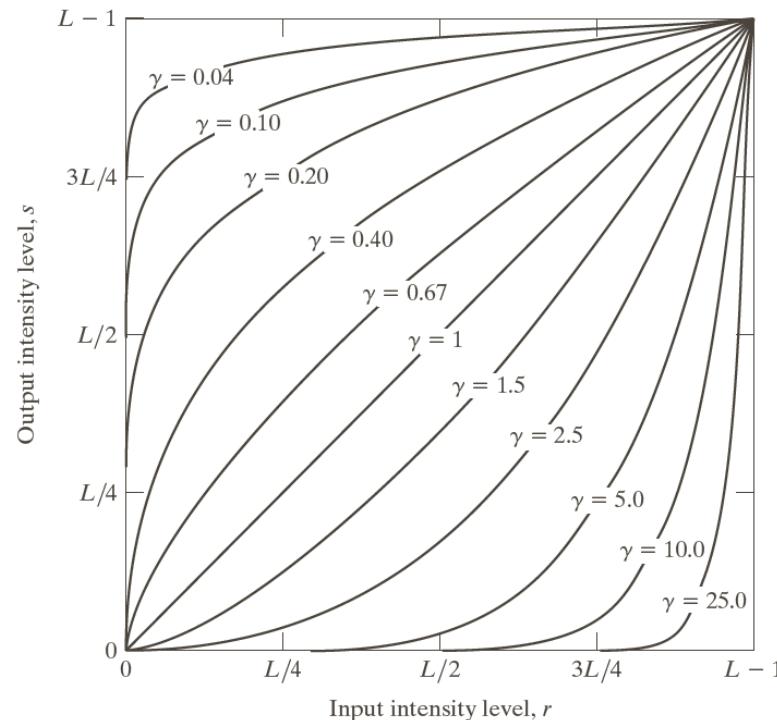
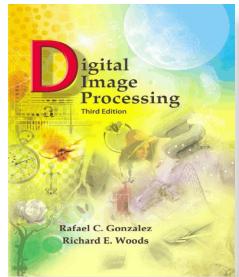


FIGURE 3.6 Plots of the equation $s = cr^\gamma$ for various values of γ ($c = 1$ in all cases). All curves were scaled to fit in the range shown.

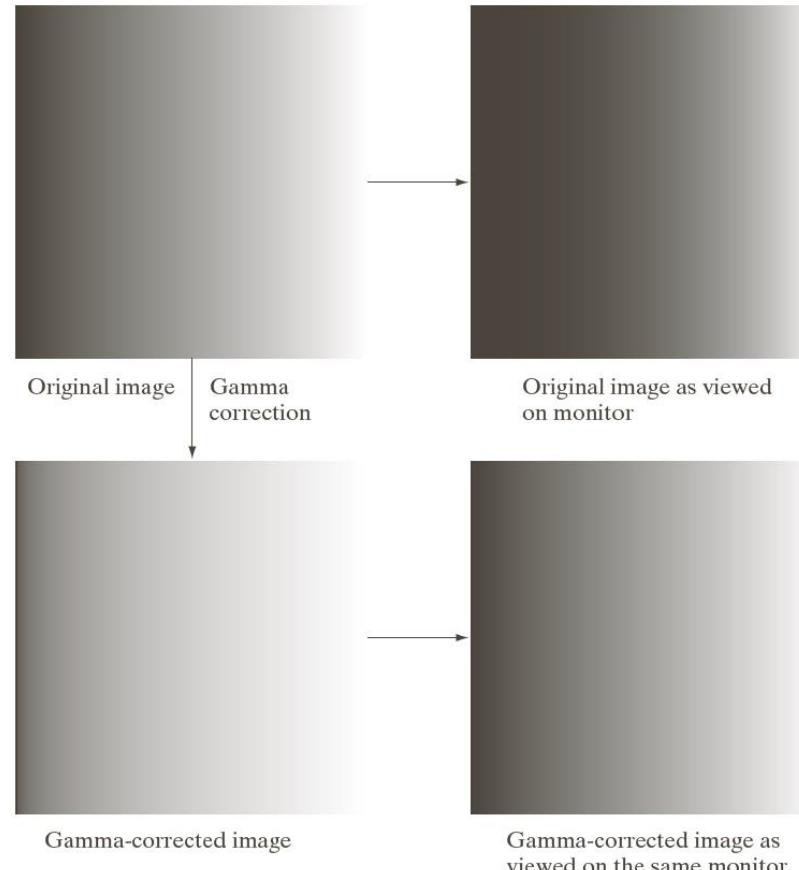


Digital Image Processing, 3rd ed.

Gonzalez & Woods

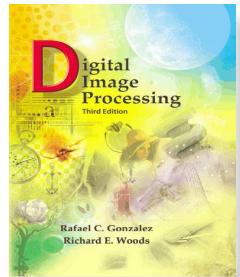
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a	b
c	d

FIGURE 3.7
(a) Intensity ramp image. (b) Image as viewed on a simulated monitor with a gamma of 2.5. (c) Gamma-corrected image. (d) Corrected image as viewed on the same monitor. Compare (d) and (a).



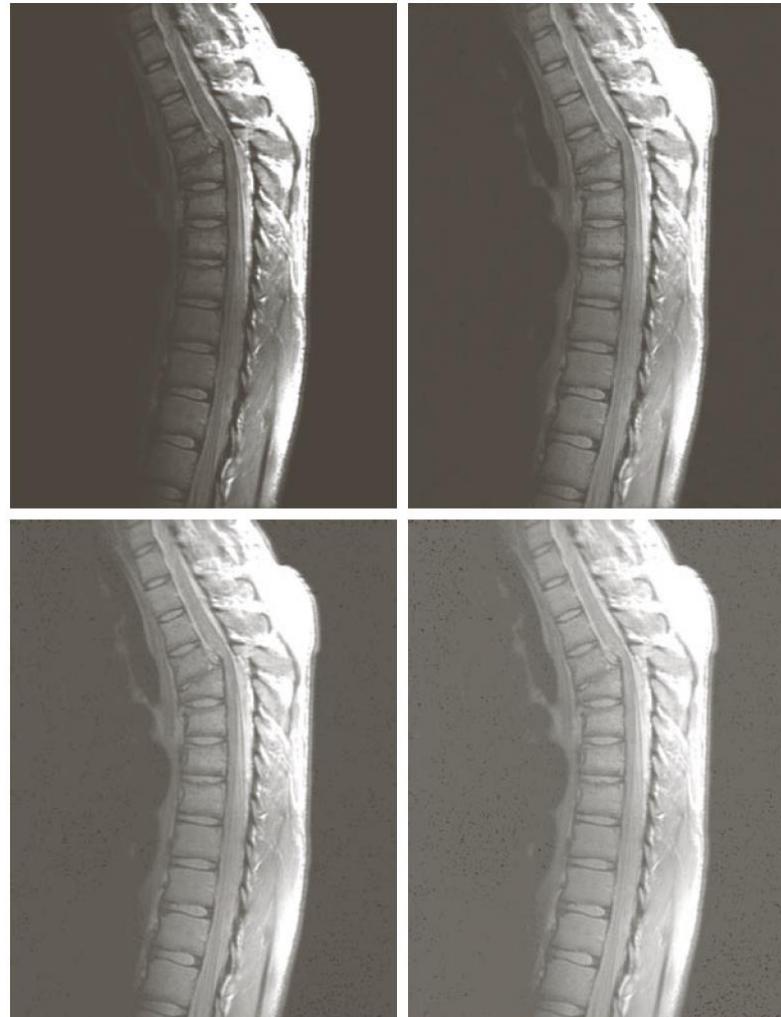
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

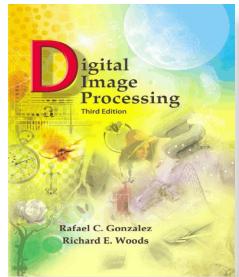
Chapter 3

Intensity Transformations & Spatial Filtering



a b
c d

FIGURE 3.8
(a) Magnetic resonance image (MRI) of a fractured human spine.
(b)–(d) Results of applying the transformation in Eq. (3.2-3) with $c = 1$ and $\gamma = 0.6, 0.4,$ and $0.3,$ respectively.
(Original image courtesy of Dr. David R. Pickens, Department of Radiology and Radiological Sciences, Vanderbilt University Medical Center.)



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

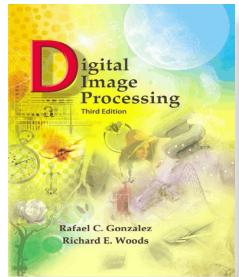
Chapter 3

Intensity Transformations & Spatial Filtering



a
b
c
d

FIGURE 3.9
(a) Aerial image.
(b)–(d) Results of
applying the
transformation in
Eq. (3.2-3) with
 $c = 1$ and
 $\gamma = 3.0, 4.0,$ and
 $5.0,$ respectively.
(Original image
for this example
courtesy of
NASA.)



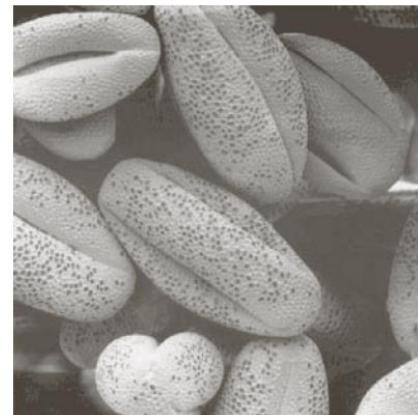
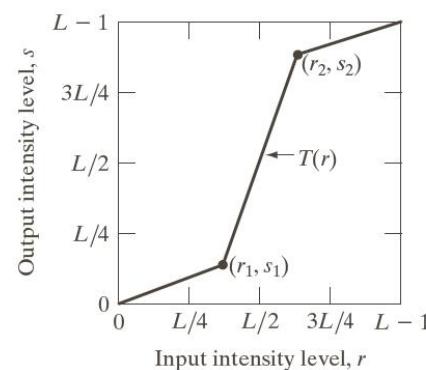
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

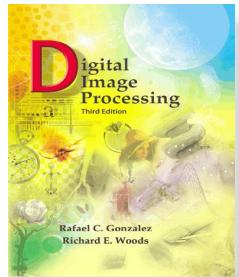
Chapter 3

Intensity Transformations & Spatial Filtering



a b
c d

FIGURE 3.10
Contrast stretching.
(a) Form of transformation function. (b) A low-contrast image. (c) Result of contrast stretching. (d) Result of thresholding. (Original image courtesy of Dr. Roger Heady, Research School of Biological Sciences, Australian National University, Canberra, Australia.)



Digital Image Processing, 3rd ed.

Gonzalez & Woods

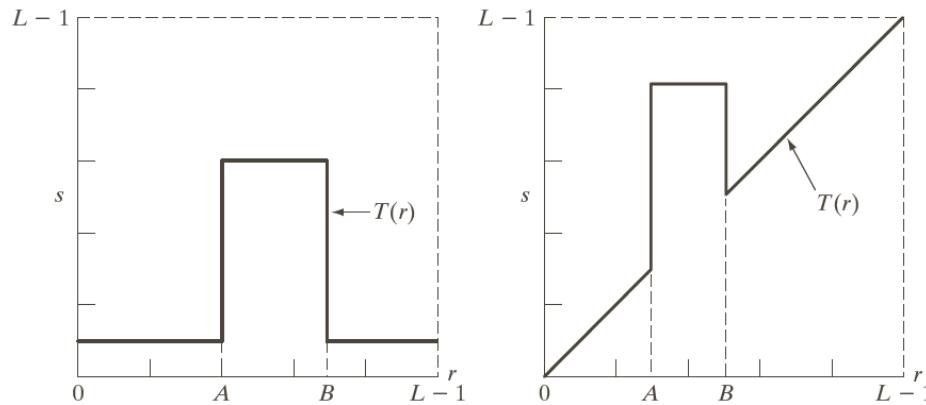
www.ImageProcessingPlace.com

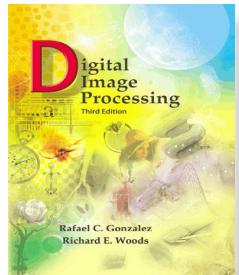
Chapter 3

Intensity Transformations & Spatial Filtering

a b

FIGURE 3.11 (a) This transformation highlights intensity range $[A, B]$ and reduces all other intensities to a lower level. (b) This transformation highlights range $[A, B]$ and preserves all other intensity levels.





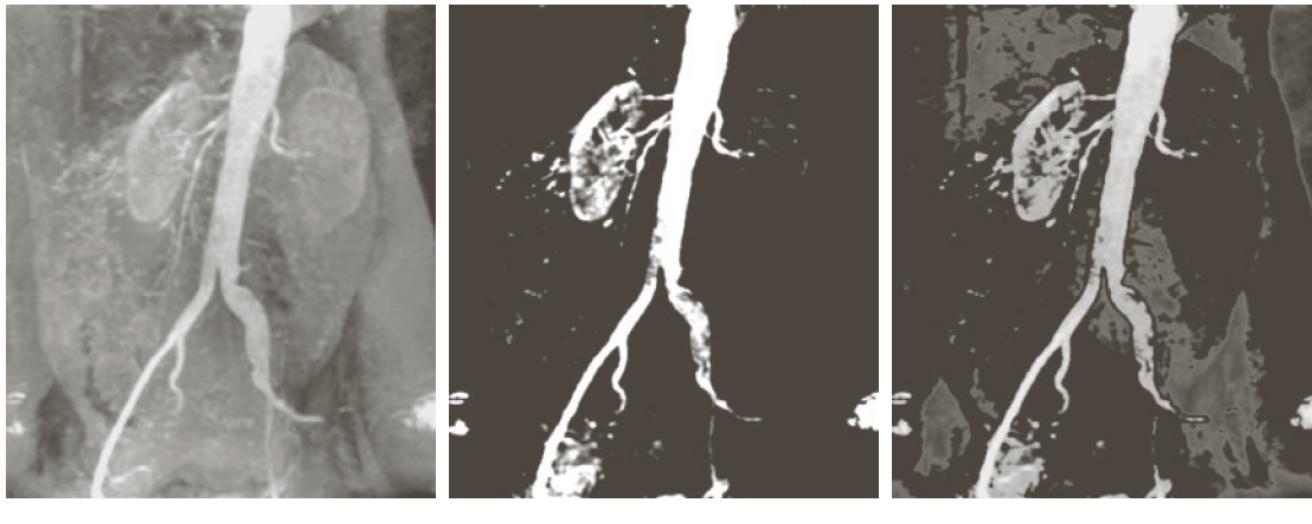
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

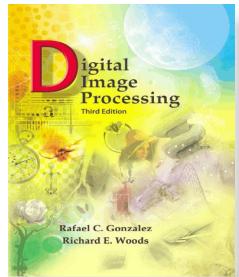
Chapter 3

Intensity Transformations & Spatial Filtering



a | b | c

FIGURE 3.12 (a) Aortic angiogram. (b) Result of using a slicing transformation of the type illustrated in Fig. 3.11(a), with the range of intensities of interest selected in the upper end of the gray scale. (c) Result of using the transformation in Fig. 3.11(b), with the selected area set to black, so that grays in the area of the blood vessels and kidneys were preserved. (Original image courtesy of Dr. Thomas R. Gest, University of Michigan Medical School.)



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

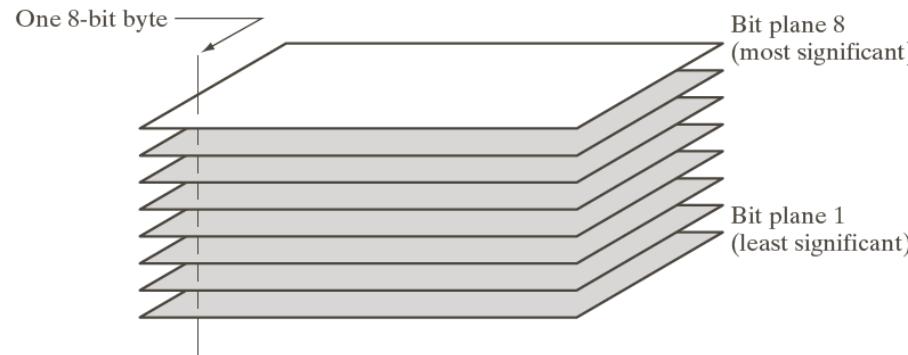
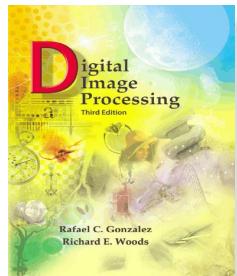


FIGURE 3.13
Bit-plane
representation of
an 8-bit image.

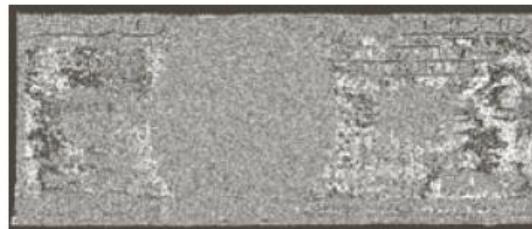
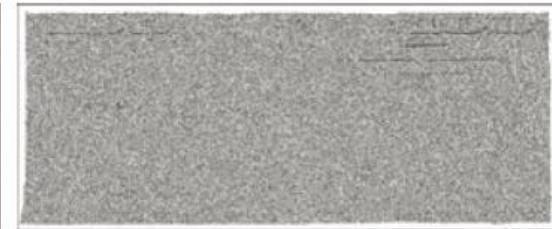


Digital Image Processing, 3rd ed.

Gonzalez & Woods

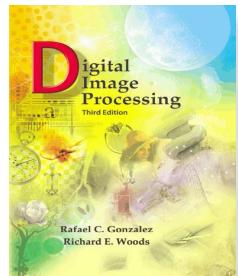
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a b c
d e f
g h i

FIGURE 3.14 (a) An 8-bit gray-scale image of size 500×1192 pixels. (b) through (i) Bit planes 1 through 8, with bit plane 1 corresponding to the least significant bit. Each bit plane is a binary image.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering



a

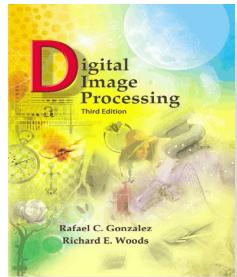


b



c

FIGURE 3.15 Images reconstructed using (a) bit planes 8 and 7; (b) bit planes 8, 7, and 6; and (c) bit planes 8, 7, 6, and 5. Compare (c) with Fig. 3.14(a).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering

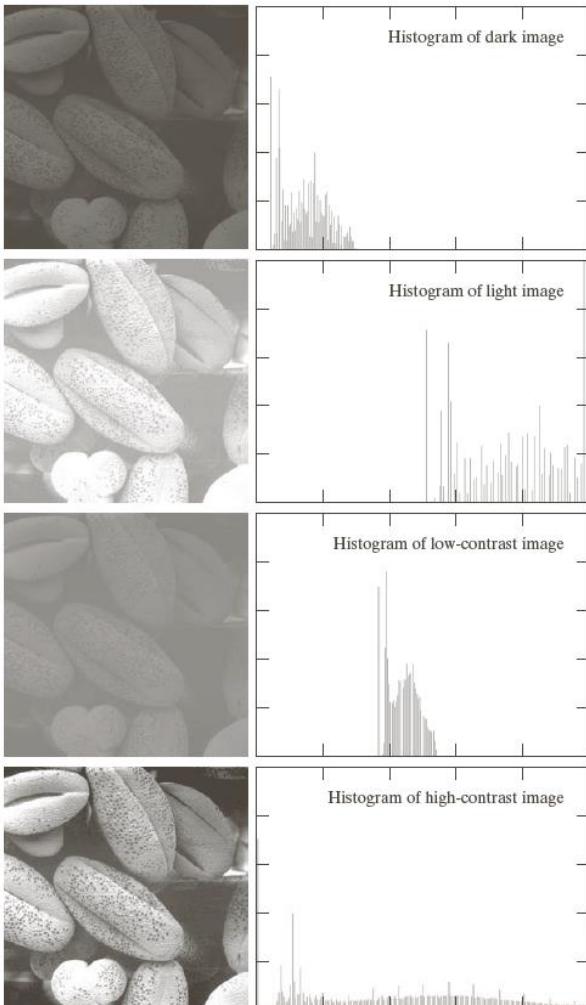
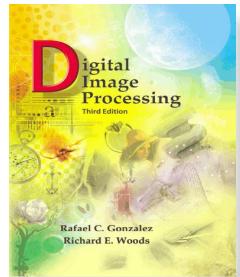


FIGURE 3.16 Four basic image types: dark, light, low contrast, high contrast, and their corresponding histograms.



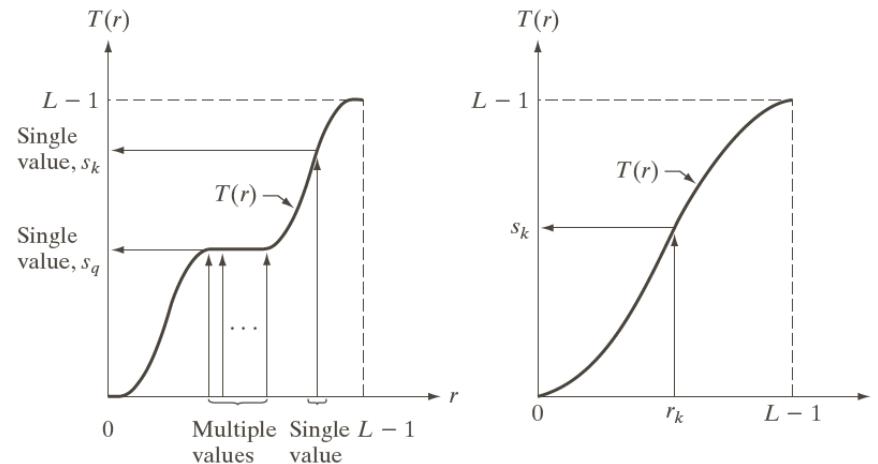
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

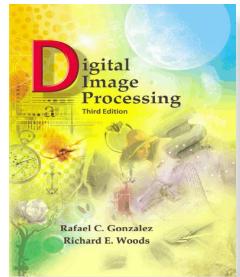


a b

FIGURE 3.17

(a) Monotonically increasing function, showing how multiple values can map to a single value.

(b) Strictly monotonically increasing function. This is a one-to-one mapping, both ways.



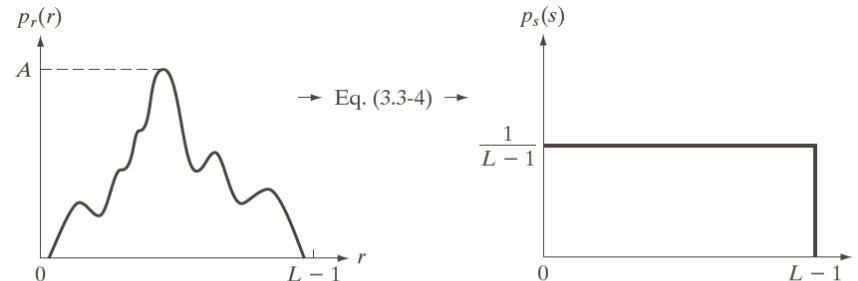
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

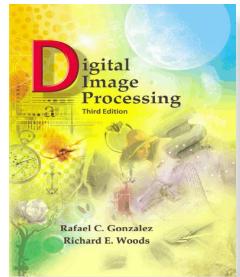
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.18 (a) An arbitrary PDF. (b) Result of applying the transformation in Eq. (3.3-4) to all intensity levels, r . The resulting intensities, s , have a uniform PDF, independently of the form of the PDF of the r 's.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

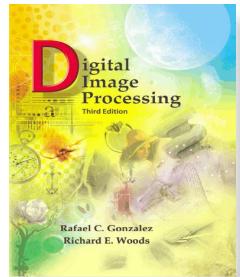
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

r_k	n_k	$p_r(r_k) = n_k/MN$
$r_0 = 0$	790	0.19
$r_1 = 1$	1023	0.25
$r_2 = 2$	850	0.21
$r_3 = 3$	656	0.16
$r_4 = 4$	329	0.08
$r_5 = 5$	245	0.06
$r_6 = 6$	122	0.03
$r_7 = 7$	81	0.02

TABLE 3.1
Intensity distribution and histogram values for a 3-bit, 64×64 digital image.



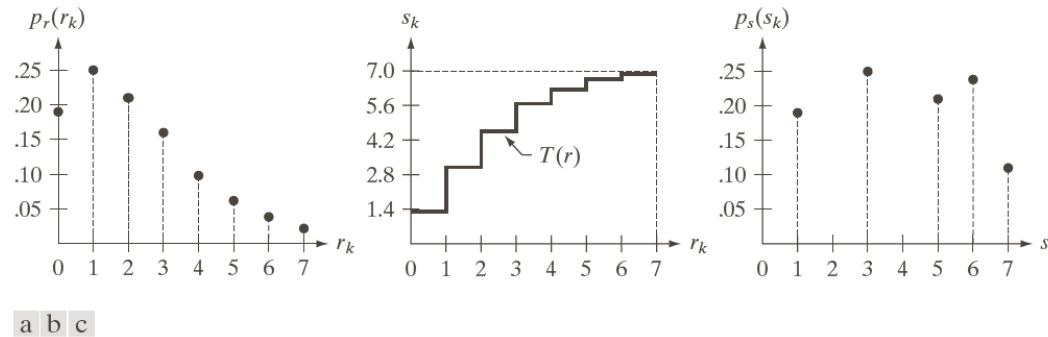
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

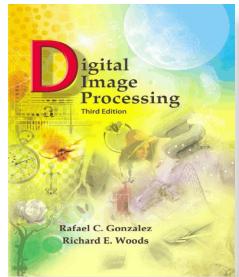
Chapter 3

Intensity Transformations & Spatial Filtering



a b c

FIGURE 3.19 Illustration of histogram equalization of a 3-bit (8 intensity levels) image. (a) Original histogram. (b) Transformation function. (c) Equalized histogram.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering

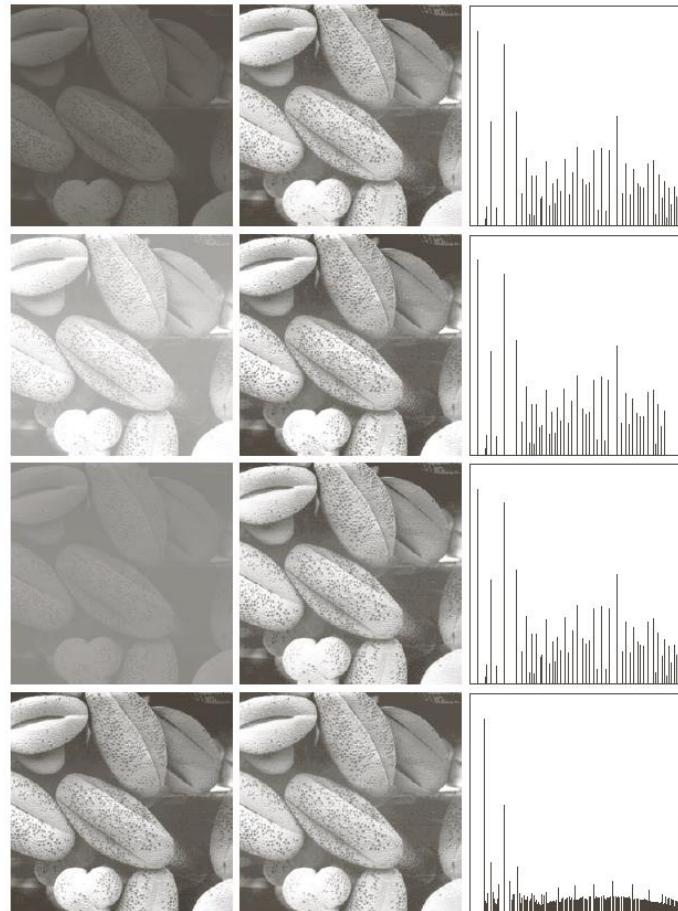
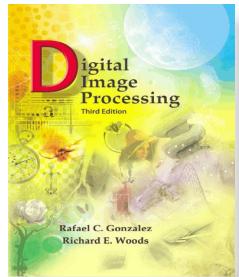


FIGURE 3.20 Left column: images from Fig. 3.16. Center column: corresponding histogram-equalized images. Right column: histograms of the images in the center column.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

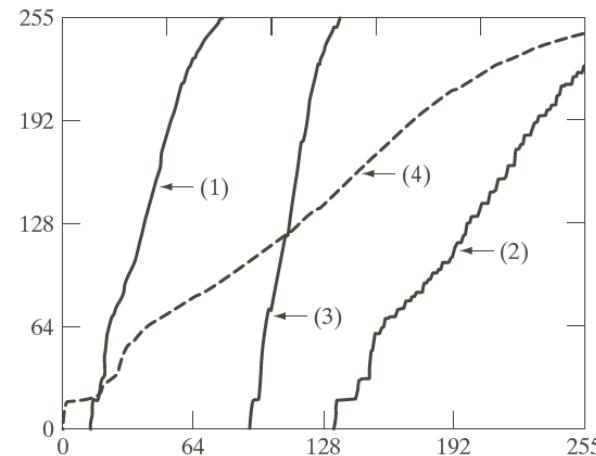
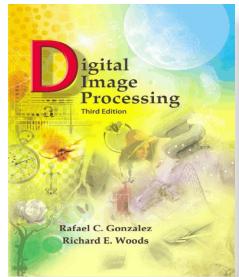


FIGURE 3.21
Transformation functions for histogram equalization. Transformations (1) through (4) were obtained from the histograms of the images (from top to bottom) in the left column of Fig. 3.20 using Eq. (3.3-8).



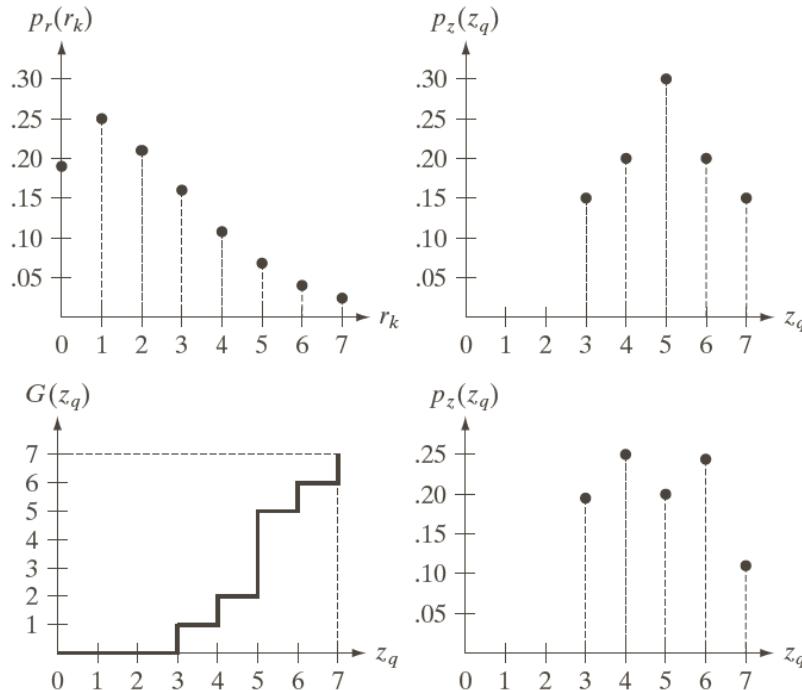
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

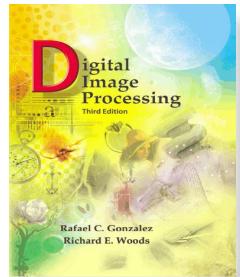
Intensity Transformations & Spatial Filtering



a
b
c
d

FIGURE 3.22

- (a) Histogram of a 3-bit image. (b) Specified histogram. (c) Transformation function obtained from the specified histogram. (d) Result of performing histogram specification. Compare (b) and (d).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

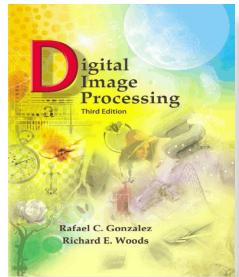
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

z_q	Specified $p_z(z_q)$	Actual $p_z(z_k)$
$z_0 = 0$	0.00	0.00
$z_1 = 1$	0.00	0.00
$z_2 = 2$	0.00	0.00
$z_3 = 3$	0.15	0.19
$z_4 = 4$	0.20	0.25
$z_5 = 5$	0.30	0.21
$z_6 = 6$	0.20	0.24
$z_7 = 7$	0.15	0.11

TABLE 3.2
Specified and
actual histograms
(the values in the
third column are
from the
computations
performed in the
body of Example
3.8).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

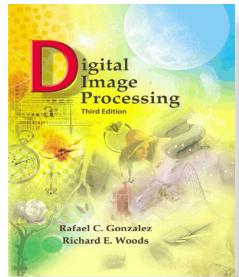
Chapter 3

Intensity Transformations & Spatial Filtering

z_q	$G(z_q)$
$z_0 = 0$	0
$z_1 = 1$	0
$z_2 = 2$	0
$z_3 = 3$	1
$z_4 = 4$	2
$z_5 = 5$	5
$z_6 = 6$	6
$z_7 = 7$	7

TABLE 3.3

All possible values of the transformation function G scaled, rounded, and ordered with respect to z .



Digital Image Processing, 3rd ed.

Gonzalez & Woods

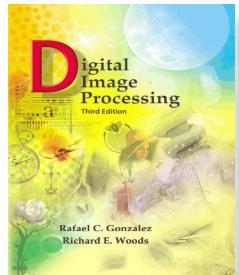
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

s_k	→	z_q
1	→	3
3	→	4
5	→	5
6	→	6
7	→	7

TABLE 3.4
Mappings of all
the values of s_k
into corresponding
values of z_q .



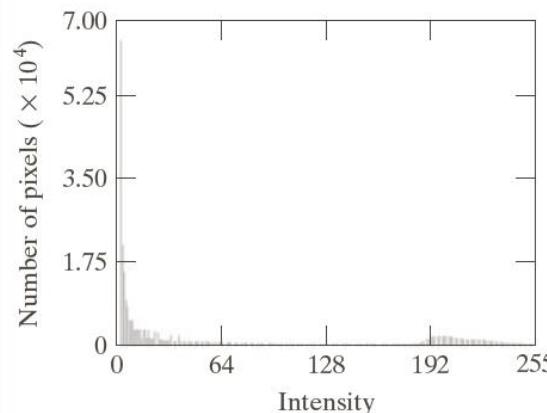
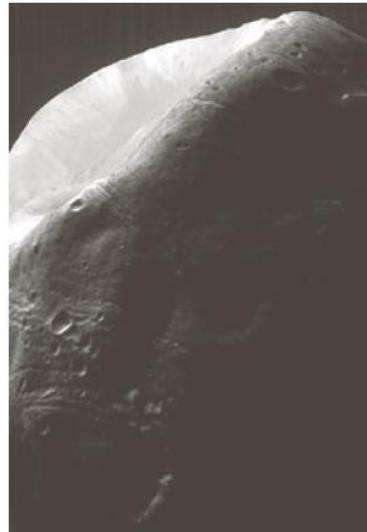
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

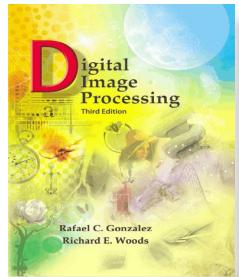
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.23
(a) Image of the
Mars moon
Phobos taken by
NASA's *Mars
Global Surveyor*.
(b) Histogram.
(Original image
courtesy of
NASA.)



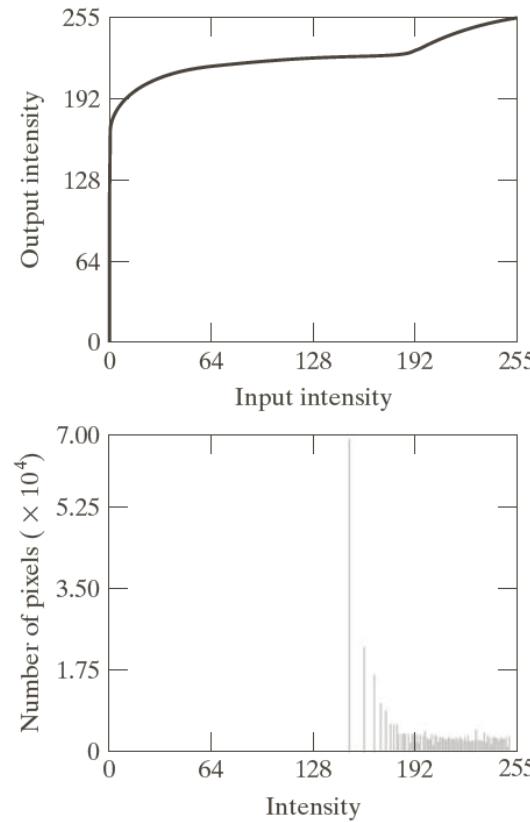
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

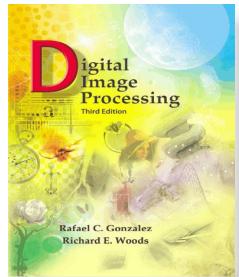
Intensity Transformations & Spatial Filtering



a b
c

FIGURE 3.24
(a) Transformation function for histogram equalization.
(b) Histogram-equalized image (note the washed-out appearance).
(c) Histogram of (b).





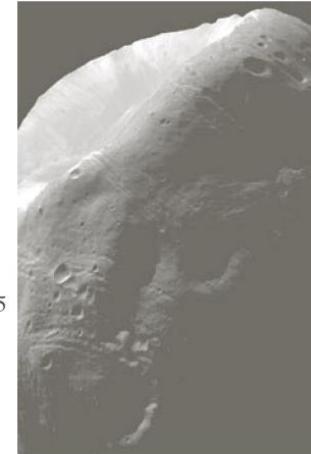
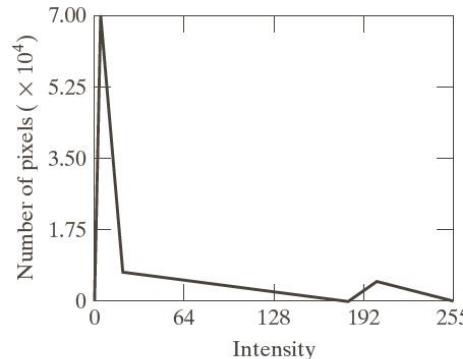
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

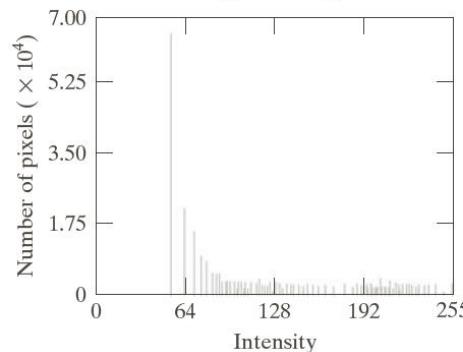
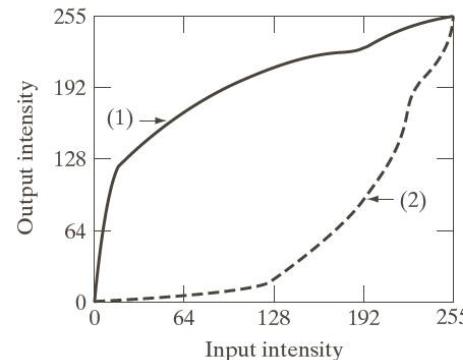
Intensity Transformations & Spatial Filtering

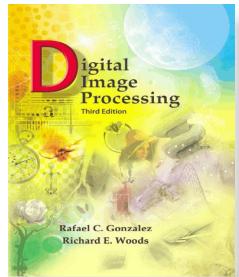


a
b
c
d

FIGURE 3.25

- (a) Specified histogram.
- (b) Transformations.
- (c) Enhanced image using mappings from curve (2).
- (d) Histogram of (c).





Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

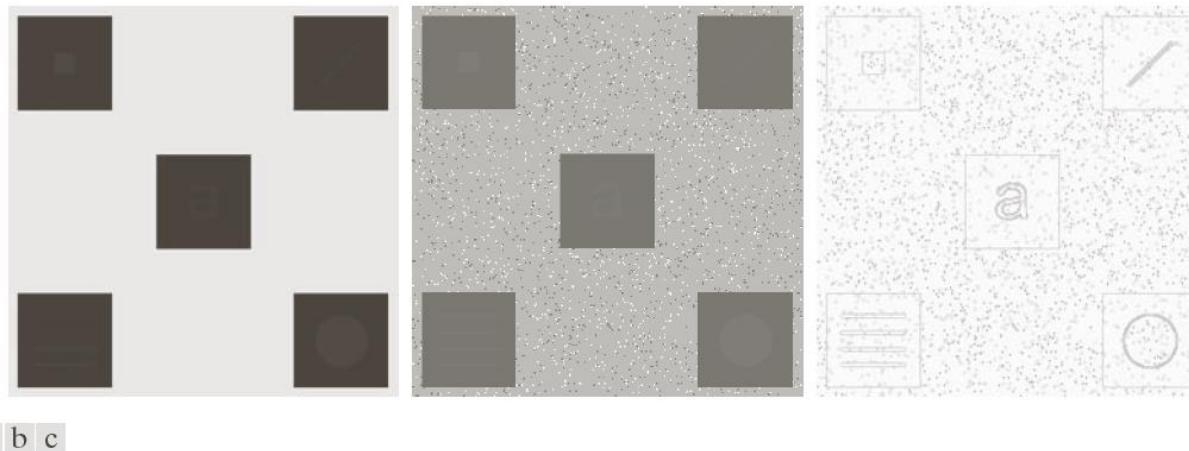
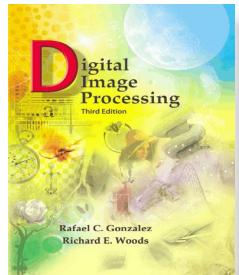


FIGURE 3.26 (a) Original image. (b) Result of global histogram equalization. (c) Result of local histogram equalization applied to (a), using a neighborhood of size 3×3 .

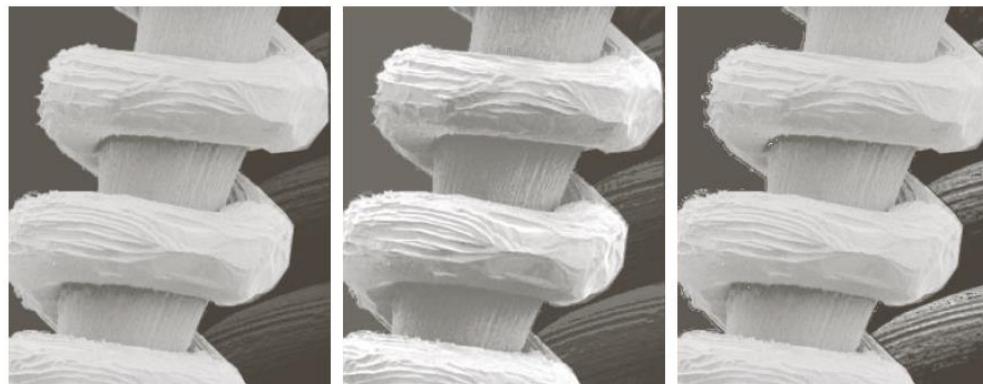


Digital Image Processing, 3rd ed.

Gonzalez & Woods

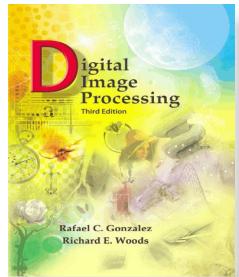
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a b c

FIGURE 3.27 (a) SEM image of a tungsten filament magnified approximately 130×. (b) Result of global histogram equalization. (c) Image enhanced using local histogram statistics. (Original image courtesy of Mr. Michael Shaffer, Department of Geological Sciences, University of Oregon, Eugene.)



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

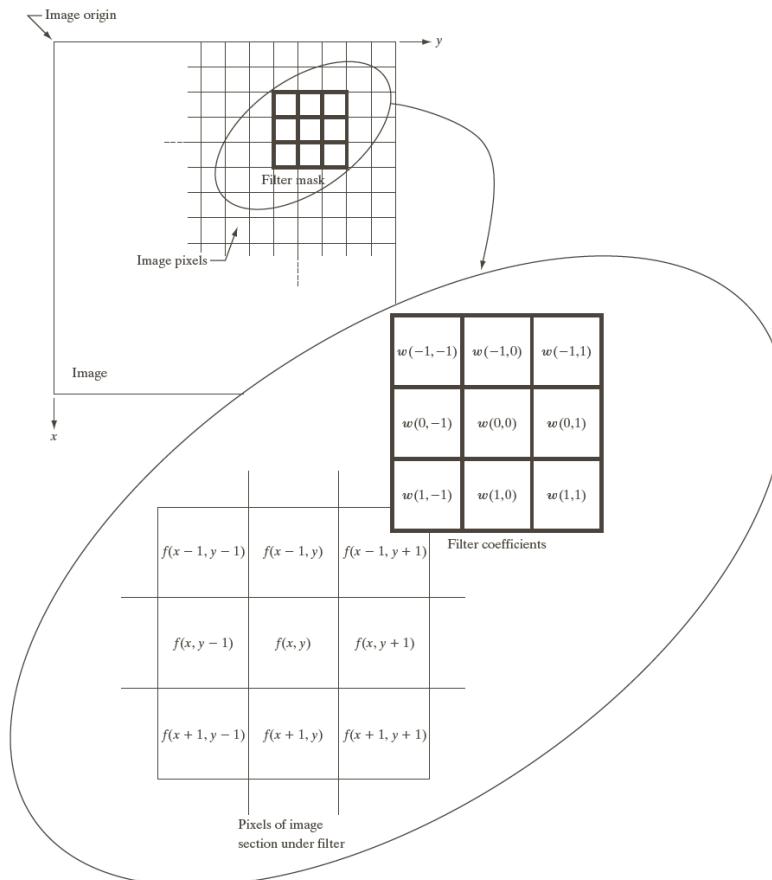
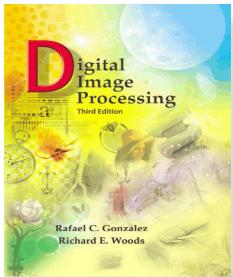


FIGURE 3.28 The mechanics of linear spatial filtering using a 3×3 filter mask. The form chosen to denote the coordinates of the filter mask coefficients simplifies writing expressions for linear filtering.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

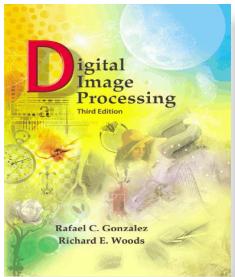
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

Correlation			Convolution		
(a)	$\begin{matrix} \nearrow \text{Origin} & f \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{matrix}$	w	$\begin{matrix} \nearrow \text{Origin} & f \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{matrix}$	w rotated 180°	(i)
(b)	$\begin{matrix} & \downarrow \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 2 & 8 \end{matrix}$		$\begin{matrix} & \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	$\begin{matrix} & \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	(j)
	Starting position alignment				
(c)	$\begin{matrix} & \downarrow & \text{Zero padding} & \downarrow \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 2 & 8 \end{matrix}$		$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	(k)
(d)	$\begin{matrix} & \uparrow \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 2 & 8 \end{matrix}$	Position after one shift	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	(l)
(e)	$\begin{matrix} & \uparrow \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 2 & 8 \end{matrix}$	Position after four shifts	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	(m)
(f)	$\begin{matrix} & \uparrow \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 2 & 3 & 2 & 8 \end{matrix}$	Final position	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	$\begin{matrix} & \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 2 & 3 & 2 & 1 \end{matrix}$	(n)
(g)	Full correlation result		Full convolution result		
	$0 & 0 & 0 & 8 & 2 & 3 & 2 & 1 & 0 & 0 & 0 & 0$		$0 & 0 & 0 & 1 & 2 & 3 & 2 & 8 & 0 & 0 & 0 & 0$		(o)
(h)	$0 & 8 & 2 & 3 & 2 & 1 & 0 & 0$	Cropped correlation result	$0 & 1 & 2 & 3 & 2 & 8 & 0 & 0$	Cropped convolution result	(p)

FIGURE 3.29 Illustration of 1-D correlation and convolution of a filter with a discrete unit impulse. Note that correlation and convolution are functions of *displacement*.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

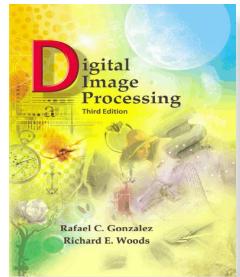
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

		Padded f		
		0 1 0		
\swarrow Origin $f(x, y)$		0 1 0 0 1 2 3 0 0 0 0 0 0 0 0 0 4 5 6 0 0 0 0 0 0 0 0 0 7 8 9 0 0 0 0	(a)	(b)
\swarrow Initial position for w		1 2 3 0 0 0 0 0 0 0 4 5 6 0 0 0 0 0 0 0 7 8 9 0 1 0	Full correlation result	Cropped correlation result
		0 9 8 7 0 0 0 0 0 0 0 0 0 0 6 5 4 0 0 0 0 0 0 0 0 0 0 3 2 1 0	(d)	0 0 0 0 0 0 0 9 8 7 0 0 6 5 4 0 0 3 2 1 0 0 0 0 0 0 0
		(c)	(e)	
\swarrow Rotated w		9 8 7 0 0 0 0 0 0 0 16 5 4 0 0 0 0 0 0 0 3 2 1 0 1 0	Full convolution result	Cropped convolution result
		0 1 2 3 0 0 0 0 0 0 0 0 0 0 4 5 6 0 0 0 0 0 0 0 0 0 0 7 8 9 0	(g)	0 0 0 0 0 0 0 1 2 3 0 0 4 5 6 0 0 7 8 9 0 0 0 0 0 0 0
		(f)	(h)	

FIGURE 3.30
Correlation
(middle row) and
convolution (last
row) of a 2-D
filter with a 2-D
discrete, unit
impulse. The 0s
are shown in gray
to simplify visual
analysis.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

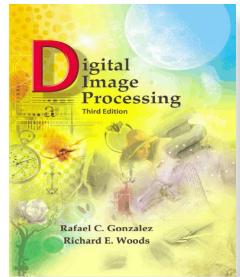
Chapter 3

Intensity Transformations & Spatial Filtering

w_1	w_2	w_3
w_4	w_5	w_6
w_7	w_8	w_9

FIGURE 3.31

Another representation of a general 3×3 filter mask.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

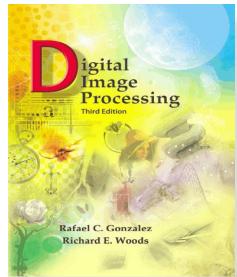
Intensity Transformations & Spatial Filtering

$$\frac{1}{9} \times \begin{array}{|c|c|c|} \hline 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ \hline 1 & 1 & 1 \\ \hline \end{array}$$

$$\frac{1}{16} \times \begin{array}{|c|c|c|} \hline 1 & 2 & 1 \\ \hline 2 & 4 & 2 \\ \hline 1 & 2 & 1 \\ \hline \end{array}$$

a b

FIGURE 3.32 Two 3×3 smoothing (averaging) filter masks. The constant multiplier in front of each mask is equal to 1 divided by the sum of the values of its coefficients, as is required to compute an average.



Digital Image Processing, 3rd ed.

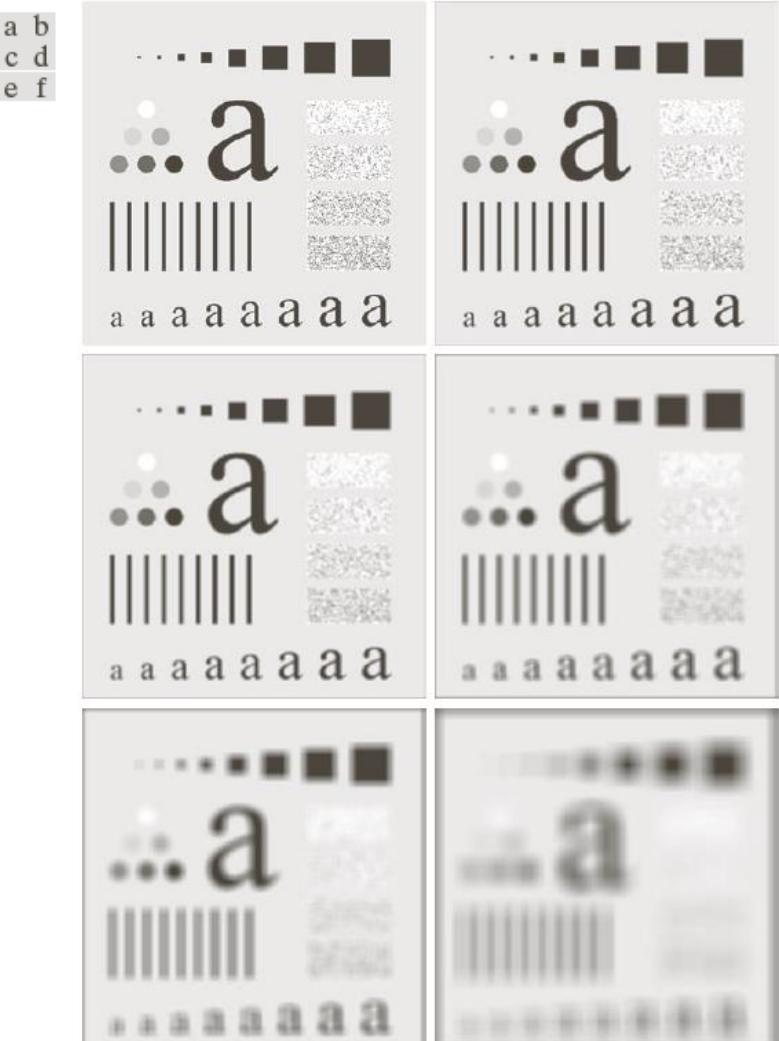
Gonzalez & Woods

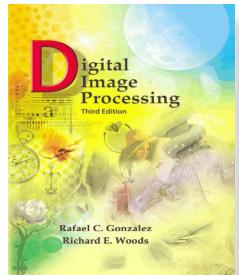
www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

FIGURE 3.33 (a) Original image, of size 500×500 pixels. (b)–(f) Results of smoothing with square averaging filter masks of sizes $m = 3, 5, 9, 15$, and 35 , respectively. The black squares at the top are of sizes $3, 5, 9, 15, 25, 35, 45$, and 55 pixels, respectively; their borders are 25 pixels apart. The letters at the bottom range in size from 10 to 24 points, in increments of 2 points; the large letter at the top is 60 points. The vertical bars are 5 pixels wide and 100 pixels high; their separation is 20 pixels. The diameter of the circles is 25 pixels, and their borders are 15 pixels apart; their intensity levels range from 0% to 100% black in increments of 20%. The background of the image is 10% black. The noisy rectangles are of size 50×120 pixels.





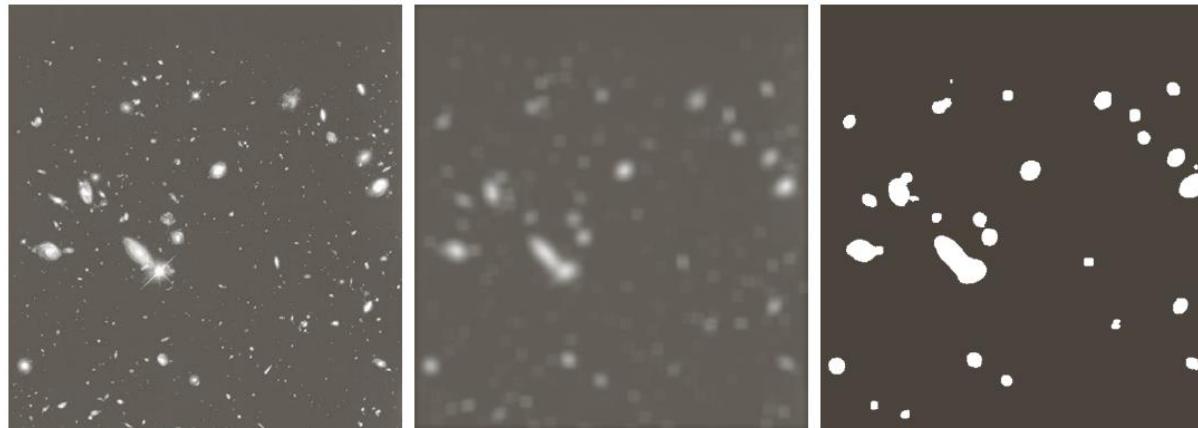
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

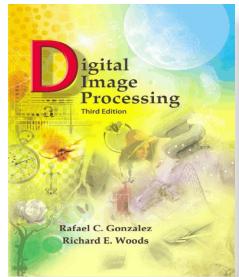
Chapter 3

Intensity Transformations & Spatial Filtering



a b c

FIGURE 3.34 (a) Image of size 528×485 pixels from the Hubble Space Telescope. (b) Image filtered with a 15×15 averaging mask. (c) Result of thresholding (b). (Original image courtesy of NASA.)



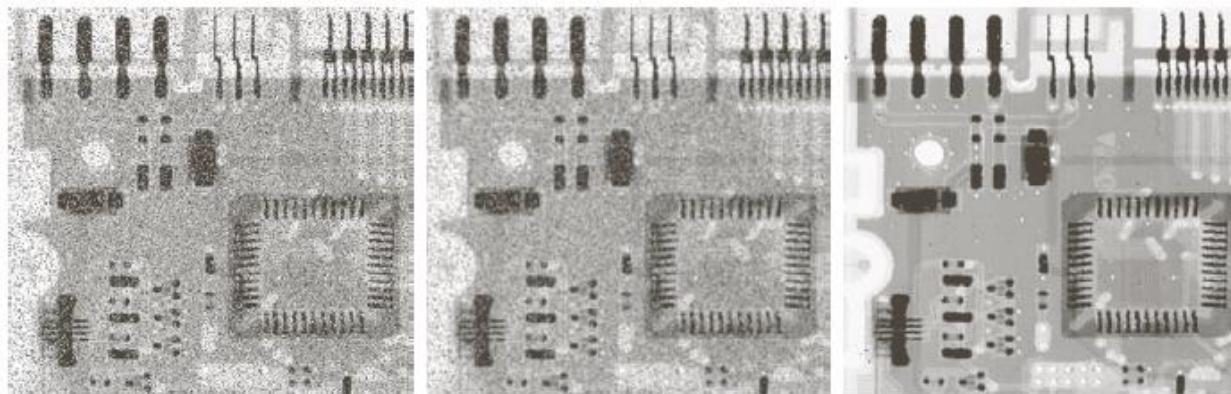
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

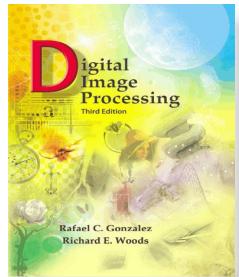
Chapter 3

Intensity Transformations & Spatial Filtering



a b c

FIGURE 3.35 (a) X-ray image of circuit board corrupted by salt-and-pepper noise. (b) Noise reduction with a 3×3 averaging mask. (c) Noise reduction with a 3×3 median filter. (Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)



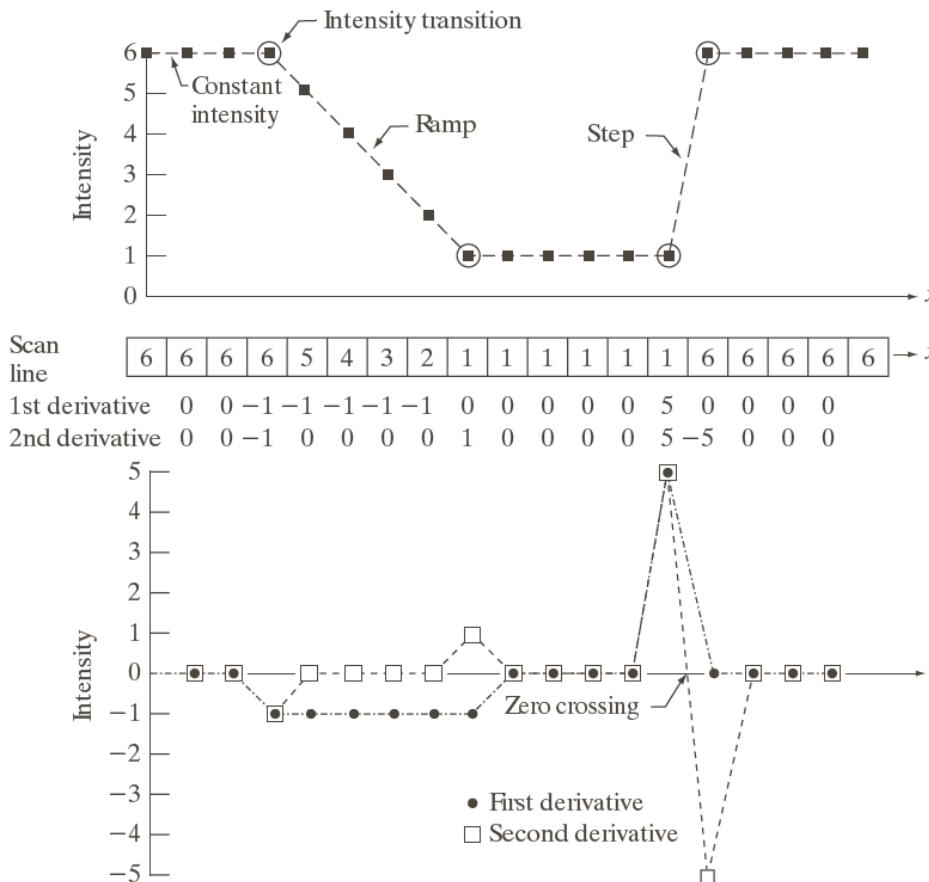
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

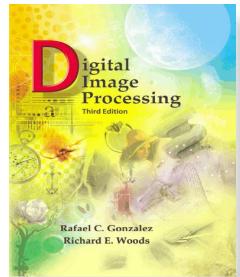
Chapter 3

Intensity Transformations & Spatial Filtering



a
b
c

FIGURE 3.36
Illustration of the first and second derivatives of a 1-D digital function representing a section of a horizontal intensity profile from an image. In (a) and (c) data points are joined by dashed lines as a visualization aid.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

0	1	0
1	-4	1
0	1	0
0	-1	0
-1	4	-1
0	-1	0

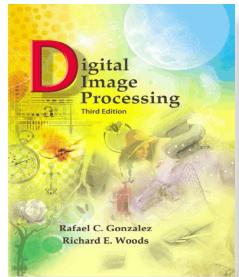
1	1	1
1	-8	1
1	1	1

-1	-1	-1
-1	8	-1
-1	-1	-1

a b
c d

FIGURE 3.37

- (a) Filter mask used to implement Eq. (3.6-6).
(b) Mask used to implement an extension of this equation that includes the diagonal terms.
(c) and (d) Two other implementations of the Laplacian found frequently in practice.

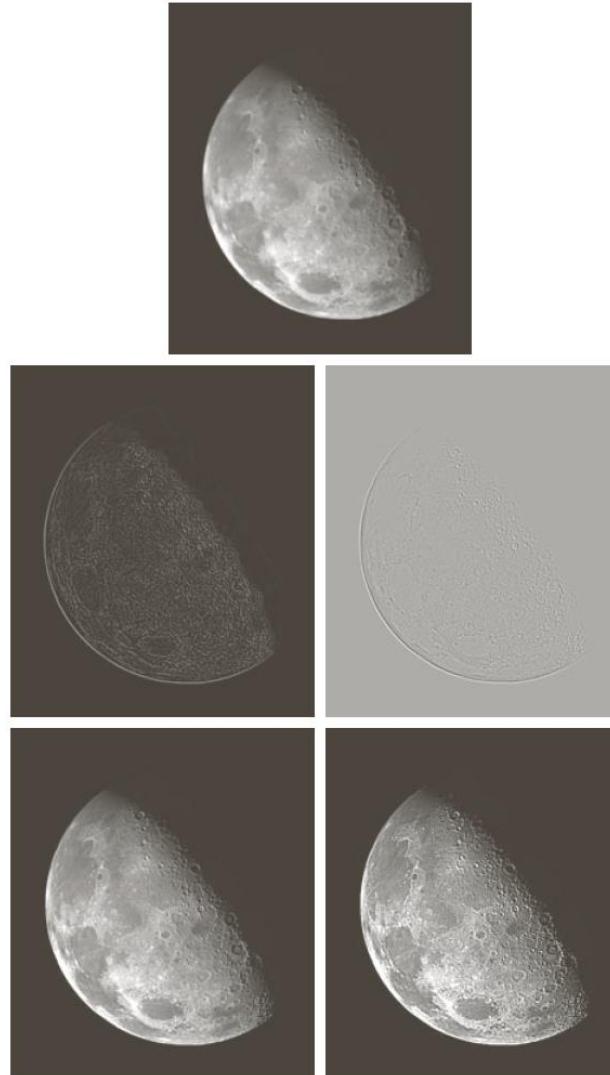


Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

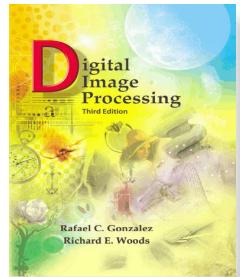
Chapter 3 Intensity Transformations & Spatial Filtering



a
b c
d e

FIGURE 3.38

(a) Blurred image of the North Pole of the moon.
(b) Laplacian without scaling.
(c) Laplacian with scaling.
(d) Image sharpened using the mask in Fig. 3.37(a).
(e) Result of using the mask in Fig. 3.37(b).
(Original image courtesy of NASA.)



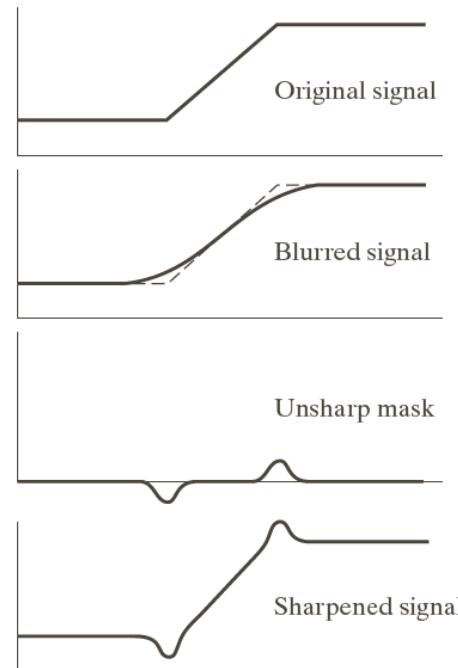
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

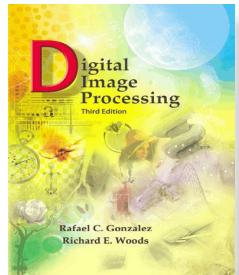
Chapter 3

Intensity Transformations & Spatial Filtering



a
b
c
d

FIGURE 3.39 1-D illustration of the mechanics of unsharp masking. (a) Original signal. (b) Blurred signal with original shown dashed for reference. (c) Unsharp mask. (d) Sharpened signal, obtained by adding (c) to (a).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

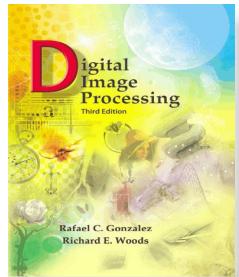
Intensity Transformations & Spatial Filtering



a
b
c
d
e

FIGURE 3.40

- (a) Original image.
- (b) Result of blurring with a Gaussian filter.
- (c) Unsharp mask.
- (d) Result of using unsharp masking.
- (e) Result of using highboost filtering.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

z_1	z_2	z_3
z_4	z_5	z_6
z_7	z_8	z_9

-1	0	0
0	1	-1

-1	-2	-1
0	0	0
1	2	1

-1	0	1
-2	0	2
-1	0	1

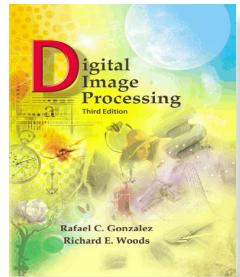
a
b c
d e

FIGURE 3.41

A 3×3 region of an image (the z s are intensity values).

(b)–(c) Roberts cross gradient operators.

(d)–(e) Sobel operators. All the mask coefficients sum to zero, as expected of a derivative operator.

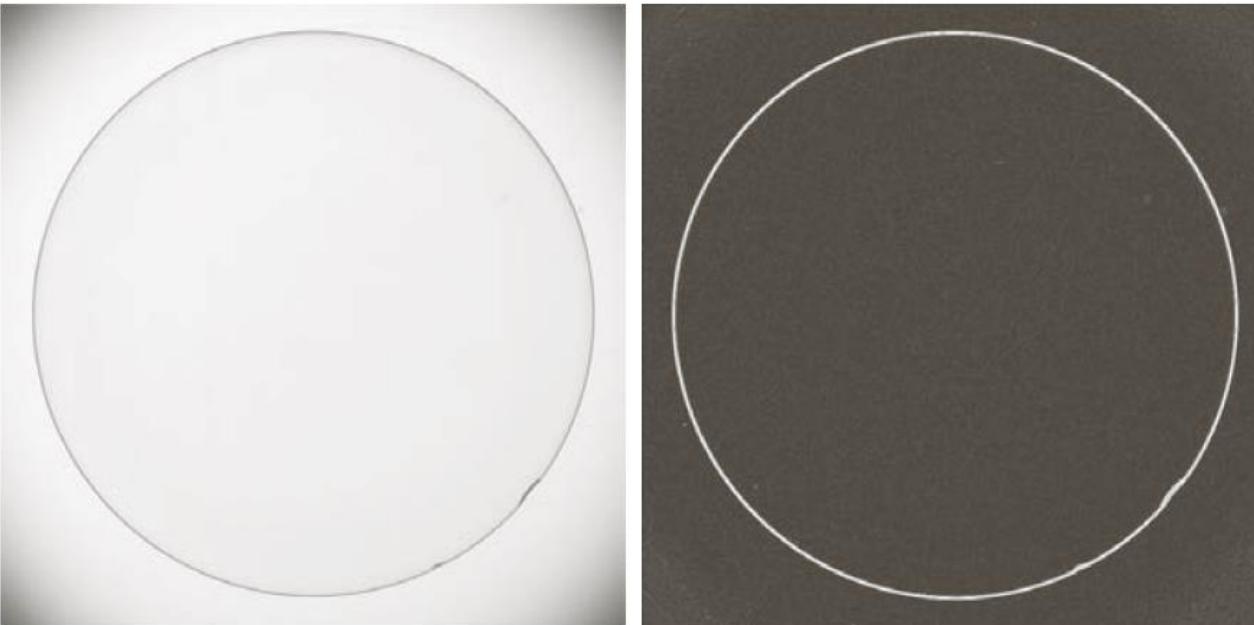


Digital Image Processing, 3rd ed.

Gonzalez & Woods

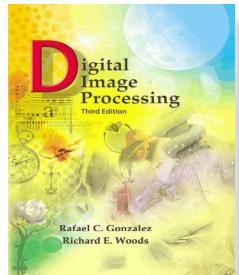
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a b

FIGURE 3.42
(a) Optical image of contact lens (note defects on the boundary at 4 and 5 o'clock).
(b) Sobel gradient.
(Original image courtesy of Pete Sites, Perceptics Corporation.)

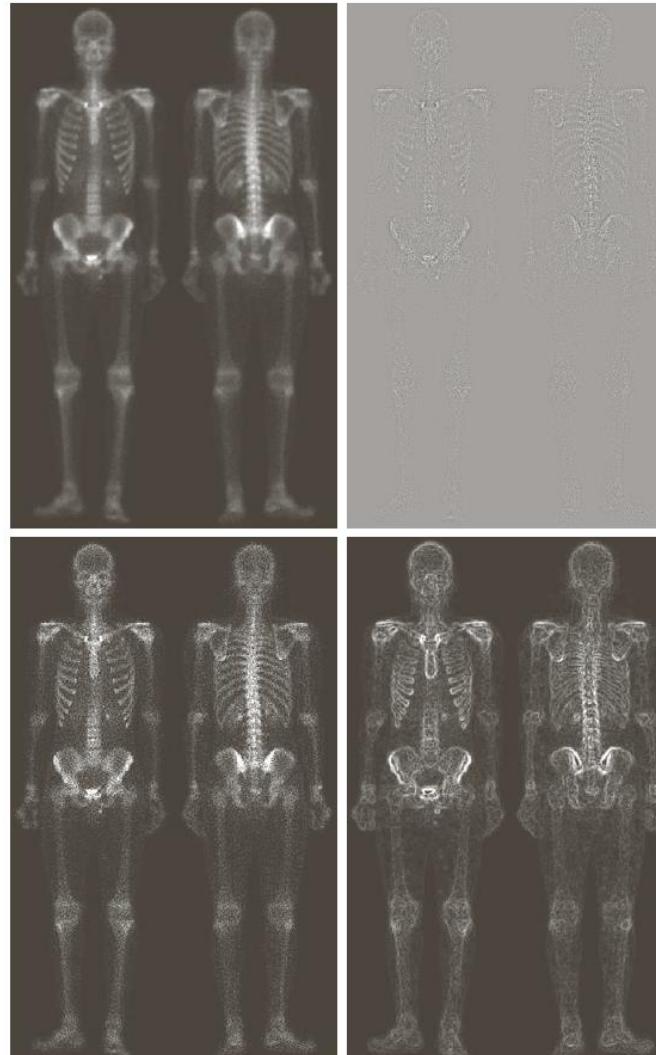


Digital Image Processing, 3rd ed.

Gonzalez & Woods

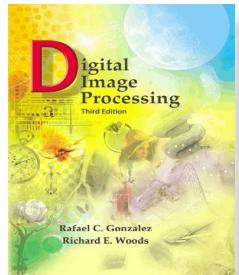
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a | b
c | d

FIGURE 3.43
(a) Image of
whole body bone
scan.
(b) Laplacian of
(a). (c) Sharpened
image obtained by
adding (a) and (b).
(d) Sobel gradient
of (a).



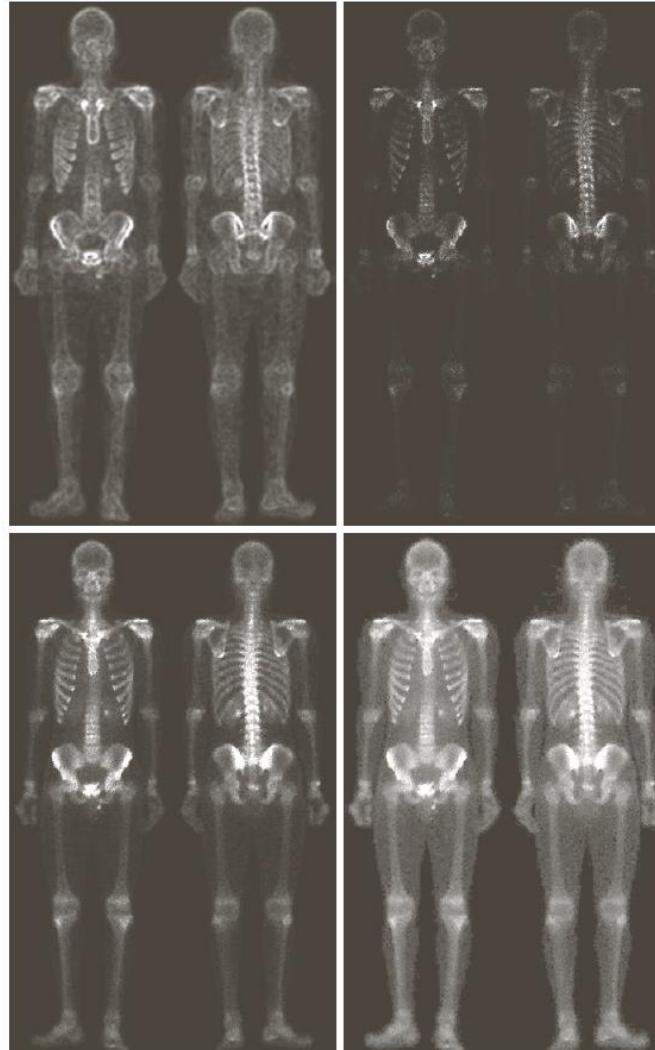
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

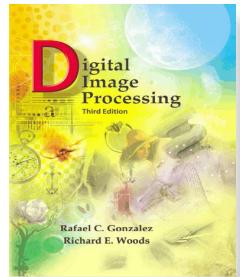
Chapter 3

Intensity Transformations & Spatial Filtering



e | f
g | h

FIGURE 3.43
(Continued)
(e) Sobel image smoothed with a 5×5 averaging filter. (f) Mask image formed by the product of (c) and (e).
(g) Sharpened image obtained by the sum of (a) and (f). (h) Final result obtained by applying a power-law transformation to (g). Compare (g) and (h) with (a). (Original image courtesy of G.E. Medical Systems.)



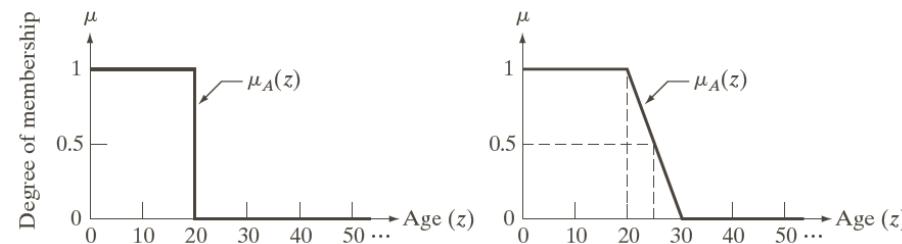
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

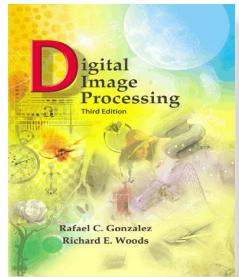
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.44
Membership functions used to generate (a) a crisp set, and (b) a fuzzy set.



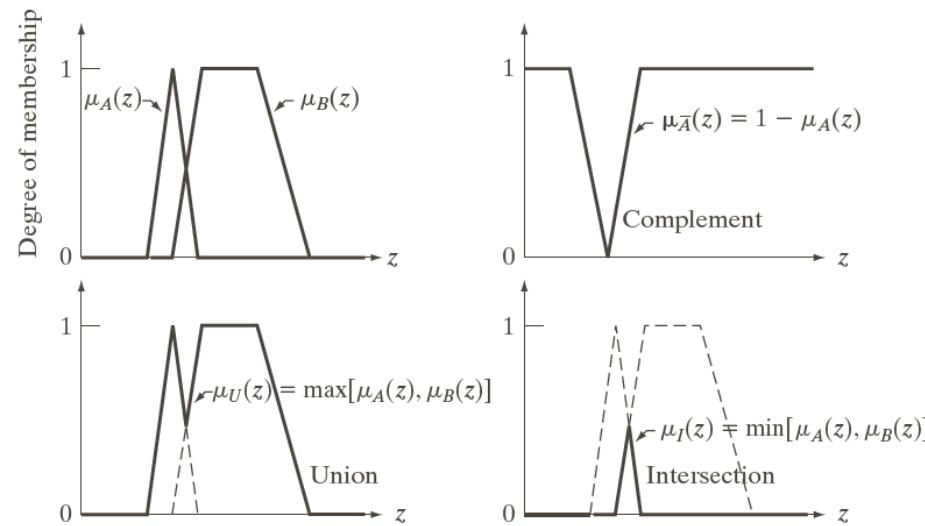
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

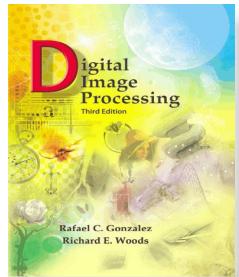
Chapter 3

Intensity Transformations & Spatial Filtering



a b
c d

FIGURE 3.45
(a) Membership functions of two sets, A and B . (b) Membership function of the complement of A .
(c) and (d) Membership functions of the union and intersection of the two sets.



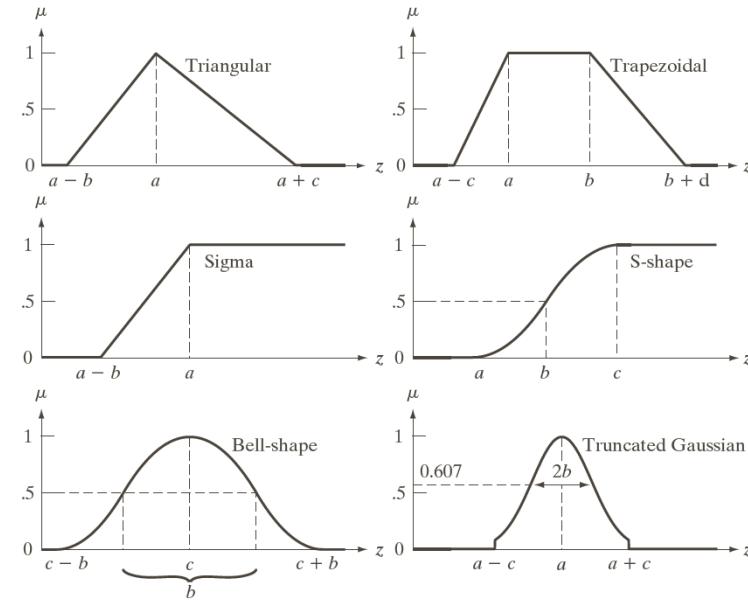
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

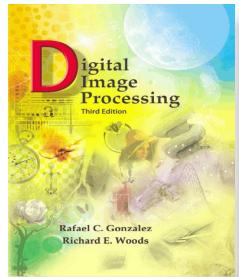
Chapter 3

Intensity Transformations & Spatial Filtering



a	b
c	d
e	f

FIGURE 3.46
Membership
functions
cor-
responding to Eqs.
(3.8-6)–(3.8-11).



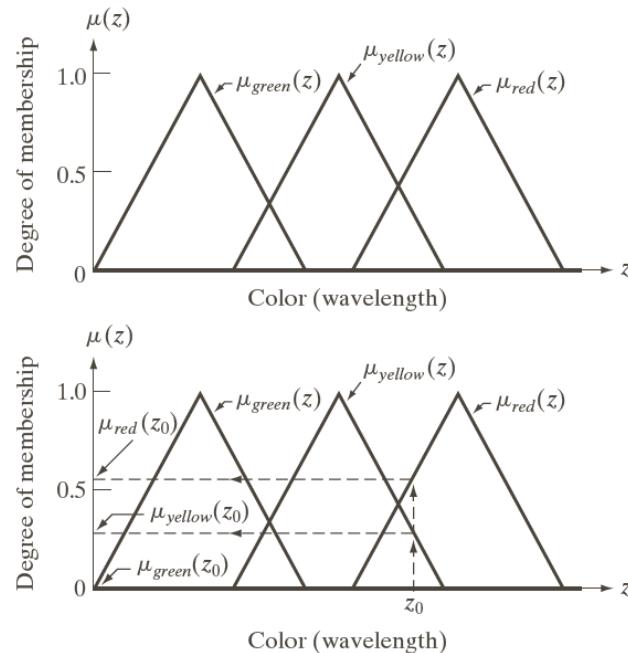
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

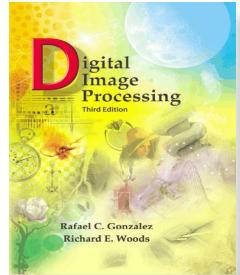
Intensity Transformations & Spatial Filtering



a
b

FIGURE 3.47

(a) Membership functions used to fuzzify color.
(b) Fuzzifying a specific color z_0 . (Curves describing color sensation are bell shaped; see Section 6.1 for an example. However, using triangular shapes as an approximation is common practice when working with fuzzy sets.)



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

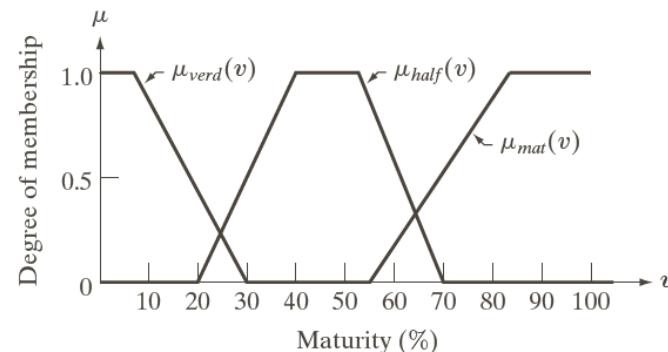
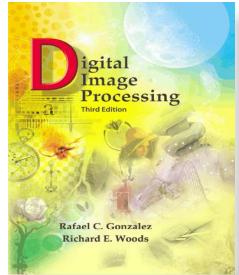


FIGURE 3.48
Membership
functions
characterizing the
outputs *verdant*,
half-mature, and
mature.



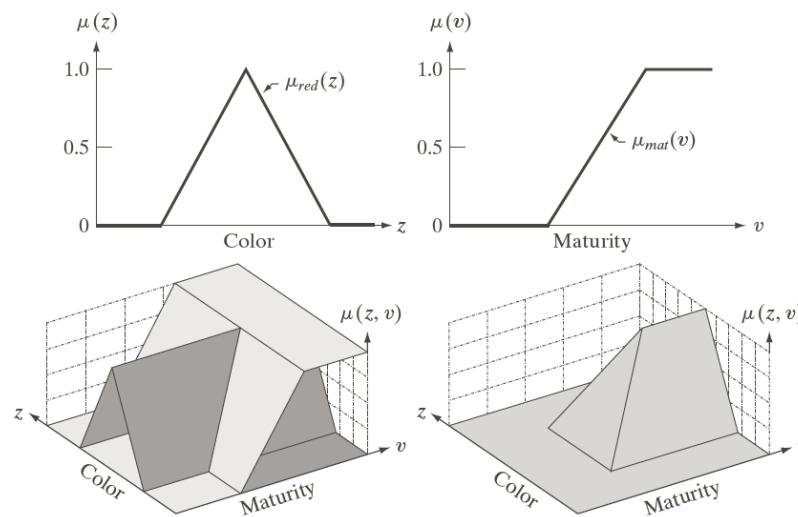
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

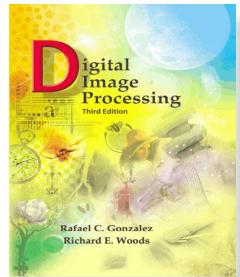
Intensity Transformations & Spatial Filtering



a	b
c	d

FIGURE 3.49

(a) Shape of the membership function associated with the color red, and
(b) corresponding output membership function. These two functions are associated by rule R_3 .
(c) Combined representation of the two functions. The representation is 2-D because the independent variables in (a) and (b) are different.
(d) The AND of (a) and (b), as defined in Eq. (3.8-5).



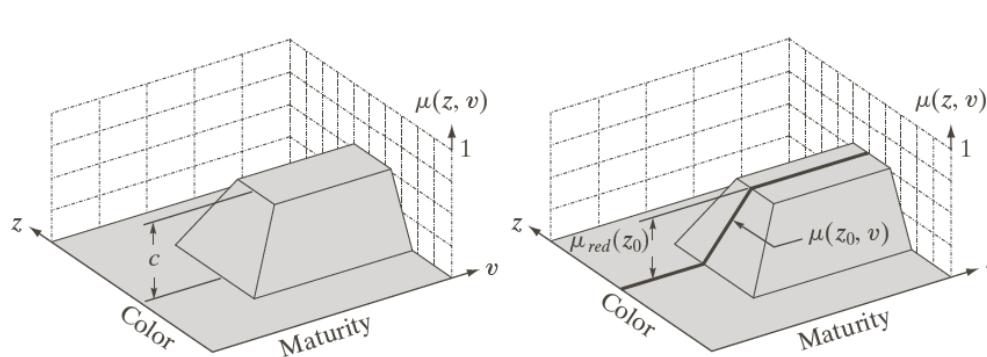
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

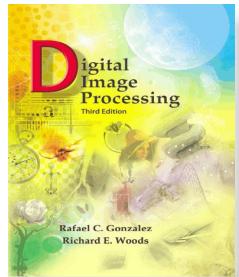
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.50
(a) Result of computing the minimum of an arbitrary constant, c , and function $\mu_2(z, v)$ from Eq. (3.8-12). The minimum is equivalent to an AND operation.
(b) Cross section (dark line) at a specific color, z_0 .



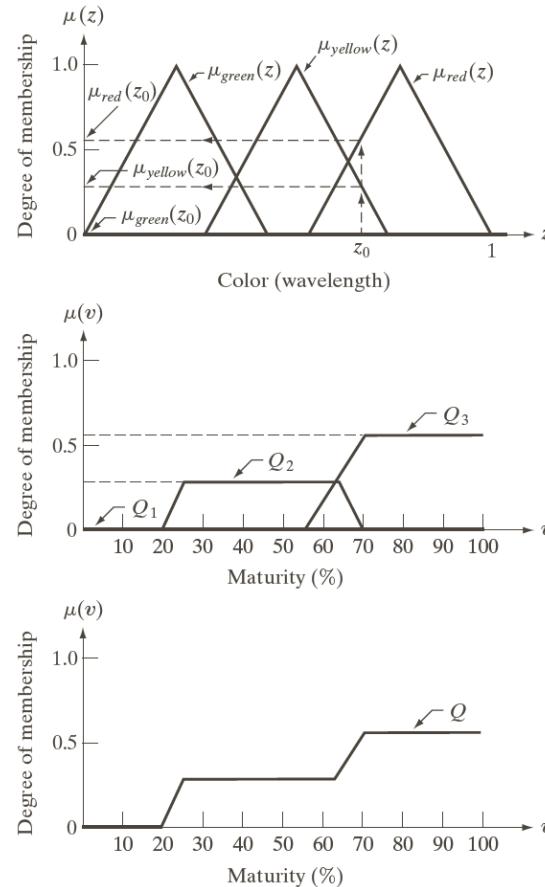
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

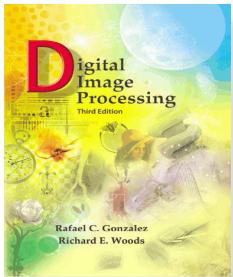
Chapter 3

Intensity Transformations & Spatial Filtering



a
b
c

FIGURE 3.51
(a) Membership functions with a specific color, z_0 , selected.
(b) Individual fuzzy sets obtained from Eqs. (3.8-13)–(3.8-15). (c) Final fuzzy set obtained by using Eq. (3.8-16) or (3.8-17).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

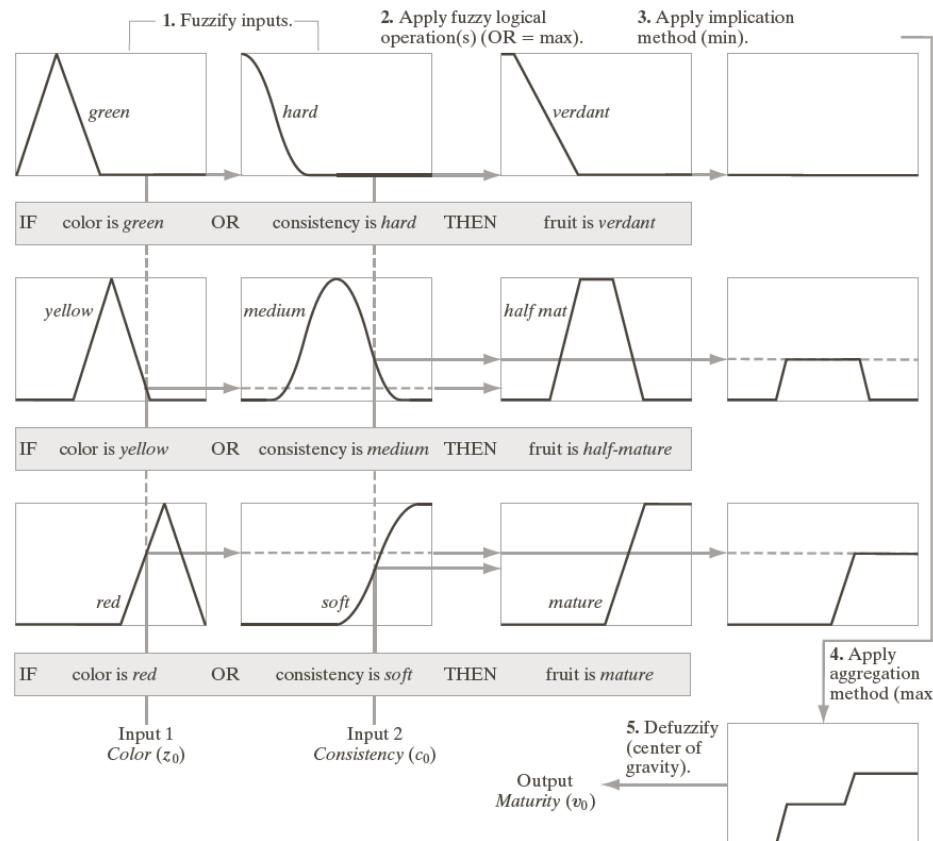
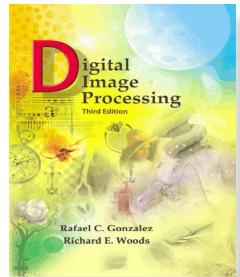


FIGURE 3.52 Example illustrating the five basic steps used typically to implement a fuzzy, rule-based system: (1) fuzzification, (2) logical operations (only OR was used in this example), (3) implication, (4) aggregation, and (5) defuzzification.



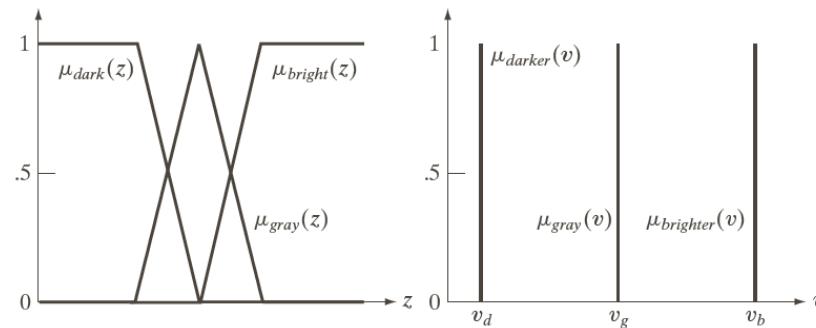
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

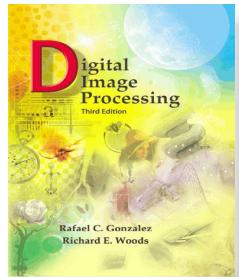
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.53
(a) Input and
(b) output
membership
functions for
fuzzy, rule-based
contrast
enhancement.

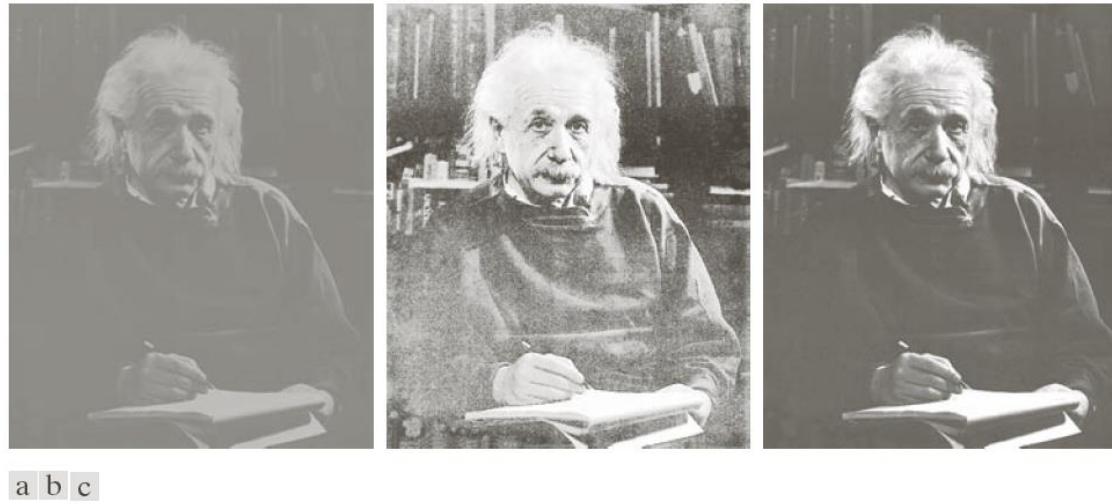


Digital Image Processing, 3rd ed.

Gonzalez & Woods

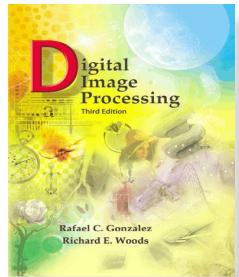
www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering



a b c

FIGURE 3.54 (a) Low-contrast image. (b) Result of histogram equalization. (c) Result of using fuzzy, rule-based contrast enhancement.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

Intensity Transformations & Spatial Filtering

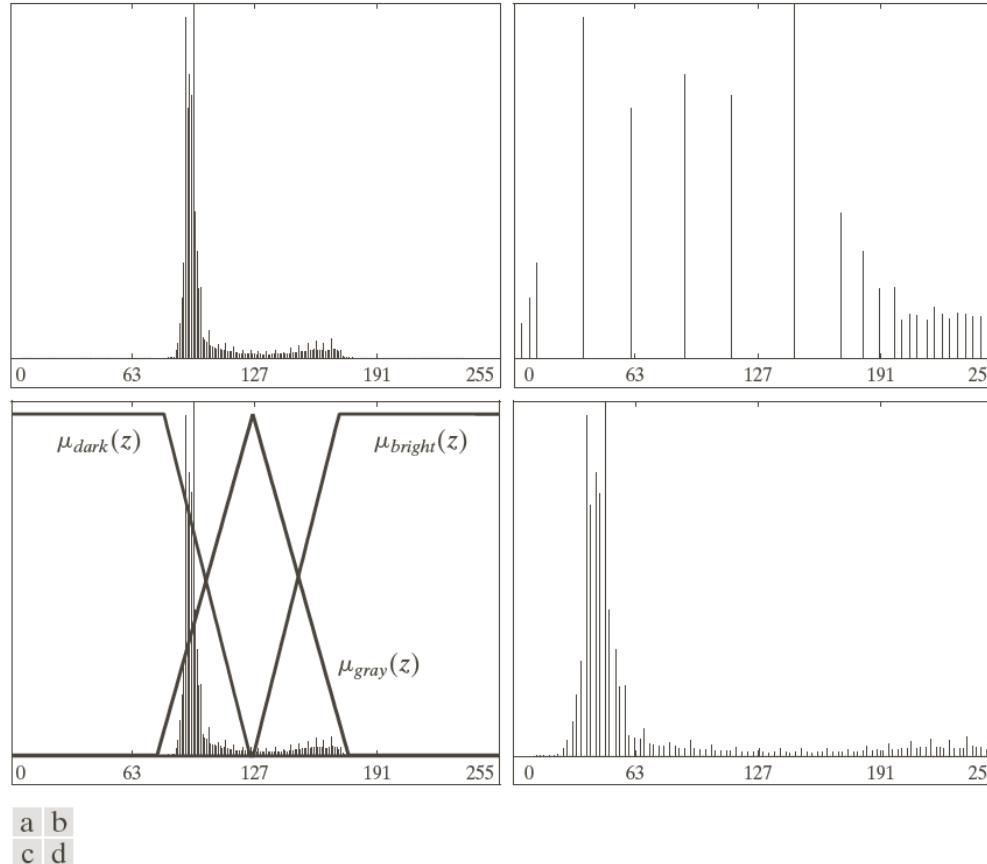
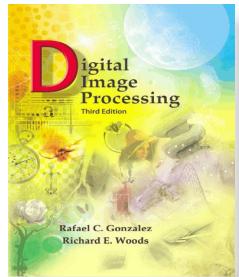


FIGURE 3.55 (a) and (b) Histograms of Figs. 3.54(a) and (b). (c) Input membership functions superimposed on (a). (d) Histogram of Fig. 3.54(c).



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3

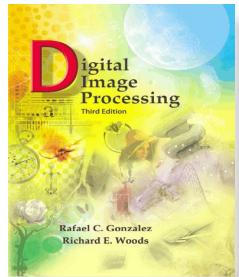
Intensity Transformations & Spatial Filtering

z_1	z_2	z_3	d_1	d_2	d_3
z_4	z_5	z_6	d_4	0	d_6
z_7	z_8	z_9	d_7	d_8	d_9

Pixel neighborhood Intensity differences

a | b

FIGURE 3.56 (a) A 3×3 pixel neighborhood, and (b) corresponding intensity differences between the center pixels and its neighbors. Only d_2 , d_4 , d_6 , and d_8 were used in the present application to simplify the discussion.



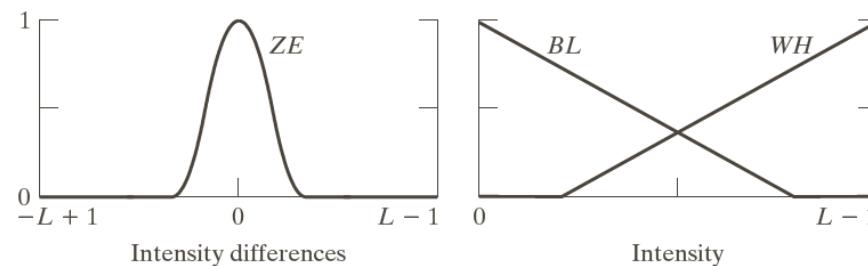
Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

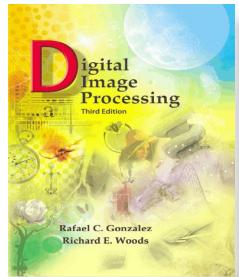
Chapter 3

Intensity Transformations & Spatial Filtering



a b

FIGURE 3.57
(a) Membership function of the fuzzy set *zero*.
(b) Membership functions of the fuzzy sets *black* and *white*.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering

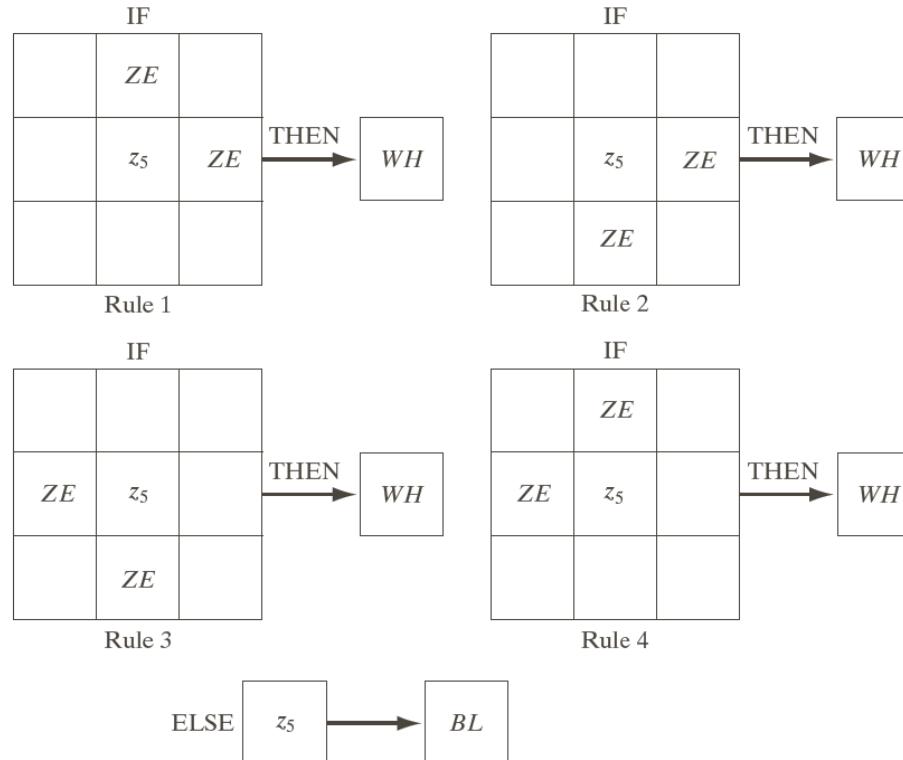
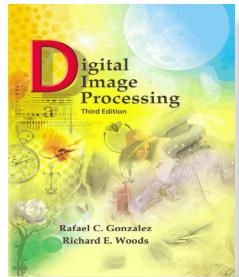


FIGURE 3.58
Fuzzy rules for
boundary
detection.



Digital Image Processing, 3rd ed.

Gonzalez & Woods

www.ImageProcessingPlace.com

Chapter 3 Intensity Transformations & Spatial Filtering

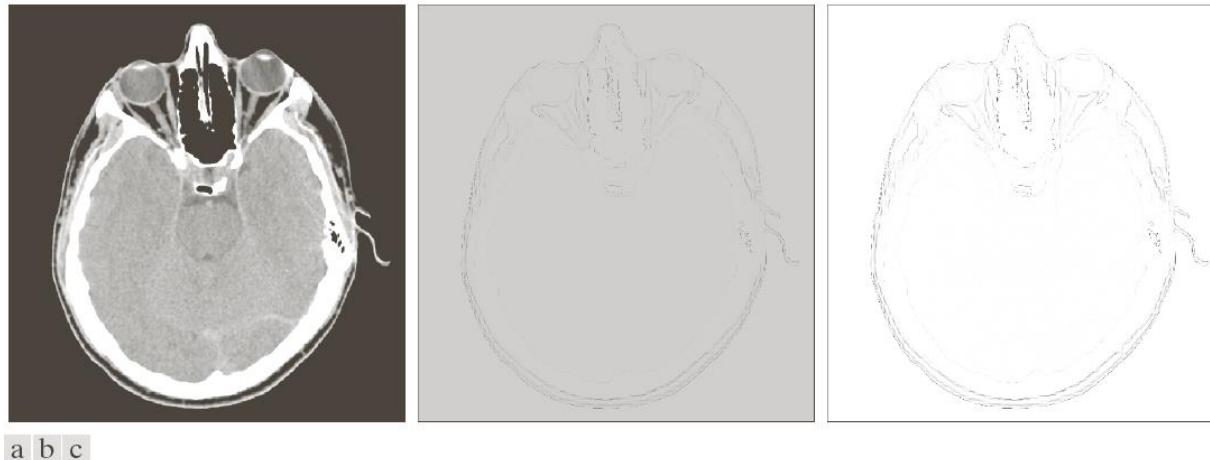


FIGURE 3.59 (a) CT scan of a human head. (b) Result of fuzzy spatial filtering using the membership functions in Fig. 3.57 and the rules in Fig. 3.58. (c) Result after intensity scaling. The thin black picture borders in (b) and (c) were added for clarity; they are not part of the data. (Original image courtesy of Dr. David R. Pickens, Vanderbilt University.)