

Basic mathematical concepts

Names:

1. Let X be a finite set. Give a recursive definition of the set of subsets of X (the Power set of X). Use union as the operator on the definition
2. Prove by induction on n that
$$\sum_{i=0}^n n = \frac{n(n+1)}{2}$$
3. Using the tree below, give the values of each of the items:
 - a. the depth of the tree
 - b. the ancestors of x_{18}
 - c. the internal nodes of the tree
 - d. the length of the path from x_3 to x_{14}
 - e. the vertex that is the parent of x_{16}
 - f. the vertices children of x_7

