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```
\ensuremath{\mathtt{g}} This small matlab demo tests the Binary Iterative Hard Thresholding algorithm
% developed in:
  "Robust 1-bit CS via binary stable embeddings"
L. Jacques, J. Laska, P. Boufounos, and R. Baraniuk
^{\circ} More precisely, using paper notations, two versions of BIHT are tested \$ here on sparse signal reconstruction:
  * the standard BIHT associated to the (LASSO like) minimization of
             min || [ y o A(u) ]_- ||_1 s.t. ||u||_0 \leq K
  * the (less efficient) BIHT-L2 related to
             \label{eq:min} \mbox{min } |\ | \ [ \ y \ o \ A(u) \ ]_- \ |\ |^2_2 \ s.t. \ |\ |u|\ |_0 \ \ \ (2)
 where y = A(x) := sign(Phi*x) are the 1-bit CS measurements of a initial K-sparse signal x in R^N; Phi is a MxN Gaussian Random matrix of entries iid drawn as N(0,1); [s]_-, equals to s if s < 0 and 0 otherwise, is applied component wise on vectors; "o" is the Hadamard product such that (u o v)_i = u_i*v_i for two vectors u and v.
 Considering the (sub) gradient of the minimized energy in (1) and (2), BIHT is solved through the iteration:
        x^{(n+1)} = H_K(x^{(n)} - (1/M)*Phi'*(A(x^{(n)}) - y))
% while BIHT-L2 is solved through:
        x^{(n+1)} = H_K(x^{(n)} - (Y*Phi)' * [(Y*Phi*x^{(n)})]_{-})
^8 with Y = diag(y), \rm H\_K(u) the K-term thresholding keeping the K % highest amplitude of u and zeroing the others.
% Authors: J. Laska, L. Jacques, P. Boufounos, R. Baraniuk
             April, 2011
```

Important parameters and functions

```
N = 2000; % Signal dimension
M = 500; % Number of measurements
K = 15; % Sparsity
% Negative function [.] -
neg = @(in) in.*(in <0);</pre>
```

Generating a unit K-sparse signal in R^N (canonical basis)

```
x0 = zeros(N,1);
rp = randperm(N);
x0(rp(1:K)) = randn(K,1);
x0 = x0/norm(x0);
```

Gaussian sensing matrix and associated 1-bit sensing

```
Phi = randn(M,N);
A = @(in) sign(Phi*in);
y = A(x0);
```

Testing BIHT

```
hd = nnz(y - A(x));
    ii = ii+1;
end

% Now project to sphere
x = x/norm(x);
BIHT_nbiter = ii;
BIHT_12 err = norm(x0 - x)/norm(x0);
BIHT_Hamming_err = nnz(y - A(x));
```

Testing BIHT-12

Plotting results

```
figure;
subplot(3,1,1);
plot(x0, 'linewidth', 2);
title('Original signal')

subplot(3,1,2);
plot(x, 'linewidth', 2);
title(sprintf('BIHT reconstruction, L2 error: %e, Consistency score (Hamming error): %i, BIHT iterations: %i', ...
    BIHT_l2_err, BIHT_Hamming_err, BIHT_nbiter));

subplot(3,1,3);
plot(x_12, 'linewidth', 2);
title(sprintf('BIHT-L2 reconstruction, L2 error: %e, Consistency score (Hamming error): %i, BIHT iterations: %i', ...
    BIHTl2_l2_err, BIHTl2_Hamming_err, BIHTl2_nbiter));
```

