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# 1 Abstract

The purpose of this study is to identify the factors that prominently affect the US COVID-19 mortality rate. We used a dataset comprising various information of 1739 different US counties, which contains the variable of interest- the mortality rate of each county, as well as over 300 potential explanatory variables, including but not limited to information on demographic and healthcare. The question of interest is to identify the most appropriate explanatory variables and to find the most suitable and statistically significant linear model to reflect their effects on the mortality rate. We started by identifying the best 9 explanatory variables that were the most reasonable and statistically significant in their respective single models. Then, using the automatic model selection method, we identified the best 2 models for each model size. Next, by comparing their  $R_{adj}^2$ , AIC values, BIC values,  $C_p$  values, and taking multicollinearity into consideration, we selected the final model consisting 4 explanatory variables, including the percentage of the population above 65 years old in the county, the total number of specialist in the county, the incoming number of International immigrants in the county for the past year, and the large-scale region to which the county belongs, which is a categorical variable of 4 large region bounds. Based on our dataset, the linear model consisting of these 4 variables best represent the trend and variation of the mortality rate. Further studies on the US COVID-19 mortality rate is recommended where more suitable explanatory variables are included in order to increase the explanatory power of the model.

## 2 Introduction

For the past 5 months, the coronavirus (COVID-19) pandemic has been raging all over the world. According to the World Health Organization, there are more than 9.44 million confirmed cases worldwide, and the total number of death cases is as high as 483,000 (World Health Organization (2020)). Therefore, we are interested in finding the factors that can potentially explain the COVID-19 mortality rate, as well as the degree to which those factors impact the mortality rate. Since the US has a large number of confirmed cases (USAFacts (2020)), we would use the COVID-19 cases from US and its corresponding counties' data (Killeen et al. (2020)) to analyze the causes of mortality rate of this pandemic.

From our previous report, we have found that there are some factors that presented statistically significant to the mortality rate of COVID-19, which are the factors of region, percentage of elder population, specialists and physicians. Thus, in this report, we would first extend our investigation, specially discovering in reasonable factors that are statistically significant to COVID-19 mortality rate. Based on all these results, we preform statistical analysis in comparing and fitting different models. Ultimately, we wish to gain some important insights from the mortality rate of COVID-19 by finding the best statistical significant model.

## 3 Dataset Description

The first dataset we found was the US COVID-19 data, which recorded the mortality rate under each county (USAFacts (2020)). Another machine-readable dataset (Killeen et al. (2020)) we have used contains socioeconomic, demographic, health care, education and transit data for each county in the 50 states in US. In total, there are 347 different factors in this dataset, such as the population estimate, migration rate, number of females, number of hospitals. Furthermore, both datasets include a key called Federal Information Processing Standard Publication (FIPS) code, which is a five-digit code uniquely identifying each area. Thus, by joining these two data sets together in Excel, we obtained our master data.

Furthermore, we are interested in the mortality rate and has chosen it to be our response variable. To satisfy the normality assumption, we created a column called Mortality, which from taking the natural log of mortality rate of each county. As such, we could use Mortality to be our response variable when computing the statistic models.

## 4 Investigation

In the previous report, we have identified 6 individually significant explanatory variables, including Specialist, Physician\_rate, ElderlyRate, Region, Population, Unemployment\_rate\_2018. Due to the low  $R^2_{adj}$  value in those models, we searched in our dataset for additional explanatory variables that reasonably affects the COVID-19 mortality rate. Among the variables that are reasonable to be included, we selected 3 of them whose single models were tested significant at  $\alpha = 0.05$  level of significance. These additional variables are Poverty, Migration, and Nurse, making a total of 9 variables selected.

The p-value of the global F-tests for the corresponding 9 single-model fittings are listed below. Full single-model summaries are included in the appendix.

Table 1: P-values for Selected Explanatory Variables

| Variable               | p_value   |
|------------------------|-----------|
| ElderlyRate            | 0.0000007 |
| Region                 | 0.0247100 |
| Specialist             | 0.0274500 |
| population             | 0.0144000 |
| Physician_rate         | 0.0460600 |
| Unemployment_rate_2018 | 0.0484100 |
| Poverty                | 0.0250100 |
| Migration              | 0.0027500 |
| Nurse                  | 0.0140400 |

As shown above, all 9 of those explanatory variables are statistically significant; we then select the best model based on those 9 variables. Firstly, we will observe the correlation matrix and VIF of those variables to spot red flags for multicollinearity.

Table 2: Correlation Matrix

|                        | Elderly | Specilist | Physician | Unemployment | Poverty | Migration | Nurse  |
|------------------------|---------|-----------|-----------|--------------|---------|-----------|--------|
| ElderlyRate            | 1.000   | -0.389    | 0.026     | 0.130        | -0.371  | -0.266    | -0.391 |
| Specialist             | -0.389  | 1.000     | 0.127     | -0.049       | 0.958   | 0.855     | 0.983  |
| Physician_rate         | 0.026   | 0.127     | 1.000     | 0.028        | 0.041   | 0.080     | 0.106  |
| Unemployment_rate_2018 | 0.130   | -0.049    | 0.028     | 1.000        | -0.026  | -0.045    | -0.055 |
| Poverty                | -0.371  | 0.958     | 0.041     | -0.026       | 1.000   | 0.835     | 0.939  |
| Migration              | -0.266  | 0.855     | 0.080     | -0.045       | 0.835   | 1.000     | 0.883  |
| Nurse                  | -0.391  | 0.983     | 0.106     | -0.055       | 0.939   | 0.883     | 1.000  |

Table 3: VIF Values

|                        | GVIF      | Df | $\text{GVIF}^{1/(2 \cdot \text{Df})}$ |
|------------------------|-----------|----|---------------------------------------|
| ElderlyRate            | 1.357739  | 1  | 1.165221                              |
| factor(Region)         | 1.924274  | 3  | 1.115264                              |
| Specialist             | 50.404208 | 1  | 7.099592                              |
| factor(population)     | 1.311527  | 1  | 1.145219                              |
| Physician_rate         | 1.986869  | 1  | 1.409563                              |
| Unemployment_rate_2018 | 1.091201  | 1  | 1.044606                              |
| Poverty                | 13.701774 | 1  | 3.701591                              |
| Migration              | 5.028916  | 1  | 2.242524                              |
| Nurse                  | 41.407467 | 1  | 6.434863                              |

Observe the correlation matrix. Using 0.8 as a cutoff, we see signs of multicollinearity issues in the following pairs of variables: Specialist & Poverty, Specialist & Migration, Specialist & Nurse, Poverty & Migration, Poverty & Nurse, Migration & Nurse.

Observe the GVIF values. Using the value 5 as a cutoff, we see signs of multicollinearity issues in Specialist, Poverty, Migration, and Nurse.

## 5 Model Selection

### 5.1 Automatic model selection method

To start our model selection process, we used the stepwise selection method first given the full model as the initial model to find the best model based on algorithm.

```
##
## Call:
## lm(formula = Mortality ~ ElderlyRate + factor(Region) + Specialist +
##     Physician_rate + Unemployment_rate_2018 + Migration)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8599 -0.5010  0.1324  0.6692  3.5356
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -4.051e+00  2.057e-01 -19.690 < 2e-16 ***
## ElderlyRate      2.519e+00  5.377e-01   4.684 3.04e-06 ***
## factor(Region)Northeast -1.827e-01  1.056e-01  -1.730  0.08386 .
## factor(Region)South    -1.338e-01  6.226e-02  -2.149  0.03176 *
## factor(Region)West     -2.880e-01  9.211e-02  -3.127  0.00180 **
## Specialist          3.348e-05  1.599e-05   2.095  0.03636 *
## Physician_rate      9.720e-04  6.566e-04   1.480  0.13894
## Unemployment_rate_2018  3.337e-02  1.993e-02   1.674  0.09422 .
## Migration         -2.206e-05  8.203e-06  -2.690  0.00722 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.034 on 1722 degrees of freedom
```

```
## (8 observations deleted due to missingness)
## Multiple R-squared:  0.0282, Adjusted R-squared:  0.02369
## F-statistic: 6.247 on 8 and 1722 DF,  p-value: 5.454e-08

## Stepwise Model Path
## Analysis of Deviance Table
##
## Initial Model:
## Mortality ~ ElderlyRate + factor(Region) + Specialist + factor(population) +
##     Physician_rate + Unemployment_rate_2018 + Poverty + Migration +
##     Nurse
##
## Final Model:
## Mortality ~ ElderlyRate + factor(Region) + Specialist + Physician_rate +
##     Unemployment_rate_2018 + Migration
##
##
##
##
```

|      | Step                 | Df | Deviance   | Resid. Df | Resid. Dev | AIC      |
|------|----------------------|----|------------|-----------|------------|----------|
| ## 1 |                      |    |            | 1719      | 1839.327   | 129.0726 |
| ## 2 | - Poverty            | 1  | 0.03228038 | 1720      | 1839.359   | 127.1030 |
| ## 3 | - Nurse              | 1  | 0.06151220 | 1721      | 1839.421   | 125.1609 |
| ## 4 | - factor(population) | 1  | 1.03274628 | 1722      | 1840.454   | 124.1325 |

The stepwise method gives the model: Mortality ~ ElderlyRate + factor(Region) + Specialist + Physician\_rate + Unemployment\_rate\_2018 + Migration) as the final model. However, we noticed the p-value for Physician\_rate = 0.13894 >  $\alpha = 0.05$  and the p-value for Unemployment\_rate\_2018 = 0.09422 >  $\alpha = 0.05$ , which do not indicate statistical significance. Thus, the model is not the most suitable model for our dataset.

## 5.2 Model selection process

In order to find the best fitting model, we performed another model selection process by fitting all possible combinations.

Table 4: Variable Reference

| Num | Variable        | Num.1 | Variable.1      | Num.2 | Variable.2             |
|-----|-----------------|-------|-----------------|-------|------------------------|
| 0   | Intercept       | 4     | RegionWest      | 8     | Unemployment_Rate_2018 |
| 1   | ElderlyRate     | 5     | Specialist      | 9     | Poverty                |
| 2   | RegionNorthEast | 6     | populationSmall | 10    | Migration              |
| 3   | RegionSouth     | 7     | PhysicianRate   | 11    | Nurse                  |

Table 5: Model Selection with CP values

|    | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | cp        | adjr2     |
|----|---|---|---|---|---|---|---|---|---|---|----|----|-----------|-----------|
| 1  | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0  | 0  | 16.752134 | 0.0142424 |
| 1  | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1  | 0  | 33.849500 | 0.0045771 |
| 2  | 1 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0  | 0  | 14.784746 | 0.0159160 |
| 2  | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0  | 0  | 15.187326 | 0.0156883 |
| 3  | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0  | 0  | 11.194281 | 0.0185102 |
| 3  | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1  | 0  | 12.616925 | 0.0177050 |
| 4  | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0  | 0  | 10.038394 | 0.0197287 |
| 4  | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1  | 0  | 10.152792 | 0.0196639 |
| 5  | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 1  | 0  | 7.373784  | 0.0218035 |
| 5  | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1  | 1  | 8.298368  | 0.0212796 |
| 6  | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1  | 0  | 6.506799  | 0.0228615 |
| 6  | 1 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 1  | 1  | 7.351198  | 0.0223828 |
| 7  | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 0 | 1  | 0  | 7.242004  | 0.0230119 |
| 7  | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1  | 0  | 7.661512  | 0.0227739 |
| 8  | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 0 | 1  | 0  | 7.052842  | 0.0236871 |
| 8  | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 1  | 1  | 7.399981  | 0.0234901 |
| 9  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1  | 0  | 8.087657  | 0.0236680 |
| 9  | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 0 | 1  | 1  | 8.363984  | 0.0235110 |
| 10 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1  | 1  | 10.030169 | 0.0231330 |
| 10 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1  | 0  | 10.069118 | 0.0231109 |
| 11 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1  | 1  | 12.000000 | 0.0225819 |

From the result, we noticed that models containing at least five variables have a fair Cp value and as the number of variables increases the  $R_{adj}^2$  increases. Then, we consider the following models:

Table 6: Automatic Selection Model Summary

| Model | Regression Equation  |
|-------|--|
| 1     | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Region  |
| 2     | Log of Mortality Rate vs. ElderlyRate + Nurse + Migration + Region   |
| 3     | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Unemployment_rate_2018 + Region   |
| 4     | Log of Mortality Rate vs. ElderlyRate + Nurse + Migration + Unemployment_rate_2018 + Region  |
| 5     | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Unemployment_rate_2018 + Region + population                                    |
| 6     | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Unemployment_rate_2018 + Physician_rate + Region                                |
| 7     | Log of Mortality Rate vs. ElderlyRate + Nurse + Migration + Unemployment_rate_2018 + Physician_rate + Region                                     |
| 8     | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Unemployment_rate_2018 + Physician_rate + Region + population                   |
| 9     | Log of Mortality Rate vs. ElderlyRate + Nurse + Migration + Unemployment_rate_2018 + Physician_rate + Region + population                        |
| 10    | Log of Mortality Rate vs. ElderlyRate + Specialist + Nurse + Migration + Unemployment_rate_2018 + Physician_rate + Region + population           |
| 11    | Log of Mortality Rate vs. ElderlyRate + Specialist + Migration + Unemployment_rate_2018 + Physician_rate + Poverty + Region + population         |
| 12    | Log of Mortality Rate vs. ElderlyRate + Specialist + Nurse + Migration + Unemployment_rate_2018 + Physician_rate + Poverty + Region + population |

Table 7: AIC and BIC values

|         | df | AIC      | BIC      |
|---------|----|----------|----------|
| model1  | 8  | 5039.856 | 5083.508 |
| model2  | 8  | 5040.714 | 5084.366 |
| model3  | 9  | 5038.699 | 5087.807 |
| model4  | 9  | 5039.464 | 5088.573 |
| model5  | 10 | 5040.188 | 5094.752 |
| model6  | 10 | 5038.498 | 5093.062 |
| model7  | 10 | 5038.847 | 5093.412 |
| model8  | 11 | 5039.526 | 5099.547 |
| model9  | 11 | 5039.804 | 5099.825 |
| model10 | 12 | 5041.468 | 5106.946 |
| model11 | 12 | 5041.507 | 5106.985 |
| model12 | 13 | 5043.438 | 5114.372 |

By comparing this result, we notice that model1, model2, model3, and model4 have the lowest AIC and BIC values. Since model1 is included in model3, and model2 is included in model4. First, to compare model1 and model3, we use backward elimination procedure.

Step 1: start by fitting Model3: Mortality~ElderlyRate + Specialist + Migration + Unemployment\_rate\_2018 + factor(Region), and consider the partial t tests for each explanatory variable.

##

## Call:

```
## lm(formula = Mortality ~ ElderlyRate + Specialist + Migration +
##     Unemployment_rate_2018 + factor(Region))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8914 -0.4922  0.1263  0.6632  3.5146
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -3.810e+00  1.263e-01 -30.179 < 2e-16 ***
## ElderlyRate      2.566e+00  5.370e-01   4.779 1.92e-06 ***
## Specialist       3.561e-05  1.593e-05   2.236 0.02549 *
## Migration       -2.253e-05  8.200e-06  -2.747 0.00607 **
## Unemployment_rate_2018  3.528e-02  1.990e-02   1.773 0.07634 .
## factor(Region)Northeast -1.016e-01  9.036e-02  -1.125 0.26080
## factor(Region)South    -1.588e-01  5.995e-02  -2.648 0.00816 **
## factor(Region)West     -2.942e-01  9.205e-02  -3.196 0.00142 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.034 on 1723 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared:  0.02697,    Adjusted R-squared:  0.02301
## F-statistic: 6.821 on 7 and 1723 DF,  p-value: 5.179e-08
```

According to the result, the p-value for  $\text{Unemployment\_rate\_2018} = 0.07634 > \alpha = 0.05$  which means  $\text{Unemployment\_rate\_2018}$  is not statistically significant. Then, we omit the variable  $\text{Unemployment\_rate\_2018}$  from the model.

```
##
## Call:
## lm(formula = Mortality ~ ElderlyRate + Specialist + Migration +
##     factor(Region))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8565 -0.5003  0.1307  0.6712  3.5013
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -3.700e+00  1.099e-01 -33.666 < 2e-16 ***
## ElderlyRate      2.699e+00  5.320e-01   5.073 4.33e-07 ***
## Specialist       3.641e-05  1.593e-05   2.285 0.02241 *
## Migration       -2.297e-05  8.201e-06  -2.801 0.00516 **
## factor(Region)Northeast -8.959e-02  9.016e-02  -0.994 0.32053
## factor(Region)South    -1.422e-01  5.926e-02  -2.400 0.01650 *
## factor(Region)West     -2.641e-01  9.054e-02  -2.917 0.00358 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.035 on 1724 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared:  0.02519,    Adjusted R-squared:  0.0218
## F-statistic: 7.425 on 6 and 1724 DF,  p-value: 7.282e-08
```



Step 2: Repeat the procedure in step 1 with a simplified model excluding the `Unemployment_rate_2018`, which is the our model1. The p-value for `ElderlyRate` =  $4.33e-07 < \alpha = 0.05$ , the p-value for `Specialist` =  $0.02241 < \alpha = 0.05$ , p-value for `Migration` =  $0.00516 < \alpha = 0.05$ , and the p-values for most categories under `Region` are under  $\alpha = 0.05$ . This suggests that all variables inside this model are statistically significant. Thus we cannot further simplify this model and this model would be one of our best models to consider.

Next, to compare model2 and model4, we use the extra sum of squares principle since model2 is nested within model4. So, we performed a hypothesis test on the variable `Unemployment_rate_2018`.

```
##
## Call:
## lm(formula = Mortality ~ ElderlyRate + Nurse + Migration + factor(Region))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8555 -0.5041  0.1376  0.6711  3.4571
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -3.698e+00  1.109e-01 -33.352  < 2e-16 ***
## ElderlyRate      2.695e+00  5.371e-01   5.017  5.79e-07 ***
## Nurse           2.056e-04  9.837e-05   2.090  0.03680 *
## Migration       -2.390e-05  9.150e-06  -2.612  0.00907 **
## factor(Region)Northeast -9.286e-02  9.037e-02  -1.028  0.30427
## factor(Region)South    -1.446e-01  5.924e-02  -2.441  0.01475 *
## factor(Region)West     -2.611e-01  9.052e-02  -2.885  0.00396 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.035 on 1724 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared:  0.02471,    Adjusted R-squared:  0.02131
## F-statistic: 7.279 on 6 and 1724 DF,  p-value: 1.076e-07

##
## Call:
## lm(formula = Mortality ~ ElderlyRate + Nurse + Migration + Unemployment_rate_2018 +
##      factor(Region))
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8908 -0.4927  0.1311  0.6602  3.4712
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    -3.811e+00  1.273e-01 -29.942  < 2e-16 ***
## ElderlyRate      2.562e+00  5.418e-01   4.730  2.43e-06 ***
## Nurse           2.023e-04  9.832e-05   2.058  0.03975 *
## Migration       -2.355e-05  9.146e-06  -2.575  0.01012 *
## Unemployment_rate_2018  3.580e-02  1.990e-02   1.799  0.07214 .
## factor(Region)Northeast -1.051e-01  9.056e-02  -1.161  0.24582
## factor(Region)South    -1.613e-01  5.993e-02  -2.692  0.00717 **
## factor(Region)West     -2.917e-01  9.204e-02  -3.169  0.00155 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 1.034 on 1723 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared: 0.02653, Adjusted R-squared: 0.02258
## F-statistic: 6.709 on 7 and 1723 DF, p-value: 7.293e-08
```

Hypothesis test:

(1)  $H_0: \beta_{unemployment} = 0$  vs.  $H_a: \beta_{unemployment} \neq 0$

(2)  $f_0 = \frac{(1.035-1.034)/(1724-1723)}{1.034/1723} = 1.66634$

```
## [1] 0.1969227
```

(3) p-value =  $P(F_{1,1723} > 1.66634) = 0.197$

(4) Since p-value  $> \alpha = 0.05$ , then we do not reject  $H_0$  at a 5% level of significance, which suggests the addition variable `Unemployment_rate_2018` is not useful.

Thus we choose model2 as one of our best models to consider.

Then, we compare model1 and model2 results. We notice model1 and model2 have the same standard error, but model1 has a lower p-value and higher  $R^2_{adj}$  compared to model2. Thus, we choose model1 to further investigate on. Moreover, we want to investigate on the collinearity of these two variables.

```
##
## Call:
## lm(formula = Mortality ~ ElderlyRate + Specialist + Migration +
##     factor(Region) + Specialist * Migration)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8525 -0.5057  0.1349  0.6702  3.4808
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -3.715e+00  1.113e-01 -33.373  < 2e-16 ***
## ElderlyRate     2.768e+00  5.384e-01   5.141 3.04e-07 ***
## Specialist      3.605e-05  1.594e-05   2.262  0.0238 *
## Migration     -1.429e-05  1.322e-05  -1.081  0.2797
## factor(Region)Northeast -9.857e-02  9.081e-02  -1.086  0.2778
## factor(Region)South   -1.428e-01  5.927e-02  -2.410  0.0160 *
## factor(Region)West    -2.676e-01  9.064e-02  -2.952  0.0032 **
## Specialist:Migration  -1.801e-10  2.151e-10  -0.837  0.4025
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.035 on 1723 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared: 0.02559, Adjusted R-squared: 0.02163
## F-statistic: 6.463 on 7 and 1723 DF, p-value: 1.548e-07

## Analysis of Variance Table
##
## Response: Mortality
##
##              Df Sum Sq Mean Sq F value    Pr(>F)
## ElderlyRate    1  28.05  28.0523  26.1915 3.437e-07 ***
## Specialist      1   0.06   0.0583   0.0545 0.815509
## Migration      1   8.65   8.6463   8.0728 0.004546 **
```

```
## factor(Region)          3   10.95   3.6492   3.4071   0.016987 *
## Specialist:Migration    1    0.75   0.7511   0.7013   0.402473
## Residuals              1723 1845.41   1.0710
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The overall p-value =  $1.548e-07 < \alpha = 0.05$ , which is higher than the model1. The adjusted  $R^2 = 0.02163$  which is lower than 0.0218 from model1, which means the model that includes the interaction term explains less variability. Besides, the p-values for Migration increases to  $0.2797 > \alpha = 0.05$  which do not indicate statistically significant. Besides, the global F-statistic = 6.463 which is lower than 7.425 from model1. Thus, adding the interaction term does not contribute to our study, and we decide to stay with model1.

We notice from previous analysis that Specialist and Migration have a correlation of 0.855, which shows they are highly correlated. Also, Specialist has a VIF value more than 50, and Migration has a VIF value of 5 indicating multicollinearity issue between these two variables. However, for the current dataset, we choose to stay with model1 as our best model, and will need to investigate on this using a larger dataset.

Based on the method we used and models we discussed, we select model1: Mortality  $\sim$  ElderlyRate + Specialist + Migration + factor(Region) as the most suitable model for the given COVID-19 dataset.

## 6 Assumption Checking

### 6.1 Mean of 0:

Looking at the plot of Residuals vs. Fitted values the residuals do appear randomly scatter around the value 0, whereas there are some points are far away (such as observation 99, 898 & 1114) from the majority which results the mean scatter around 0. However, overall it appears to fairly satisfy the assumption of mean of 0.

### 6.2 Independence:

Again the plot of Residuals vs. Fitted values shows the residuals randomly scattered with no apparent trend and thus satisfied.

### 6.3 Constant Variance:

The scale location plot suggests that the majority of residuals are randomly scattered within an upper and lower band around the value 0, which suggests a constant variance. However, since there is a few larger residuals at the bottom and on the left hand side, the red line bulges up and down in the middle of the plot, causing a slightly increase and decrease in variability. However, in general, it is still considered fairly satisfied.

### 6.4 Normality:

The Q-Q plot overall appears good, since most of the residuals are lying on a straight line. However, the normality assumption can only be considered as fairly satisfied, since there are some points at the tails are off the line (such as observation 99, 898 & 1549), suggesting some potential outliers.

### 6.5 Outliers:

It could be seen that there are some potential outliers, as we could find that there are some points off the straight at the tails in Q-Q plot, which appears to be outliers.

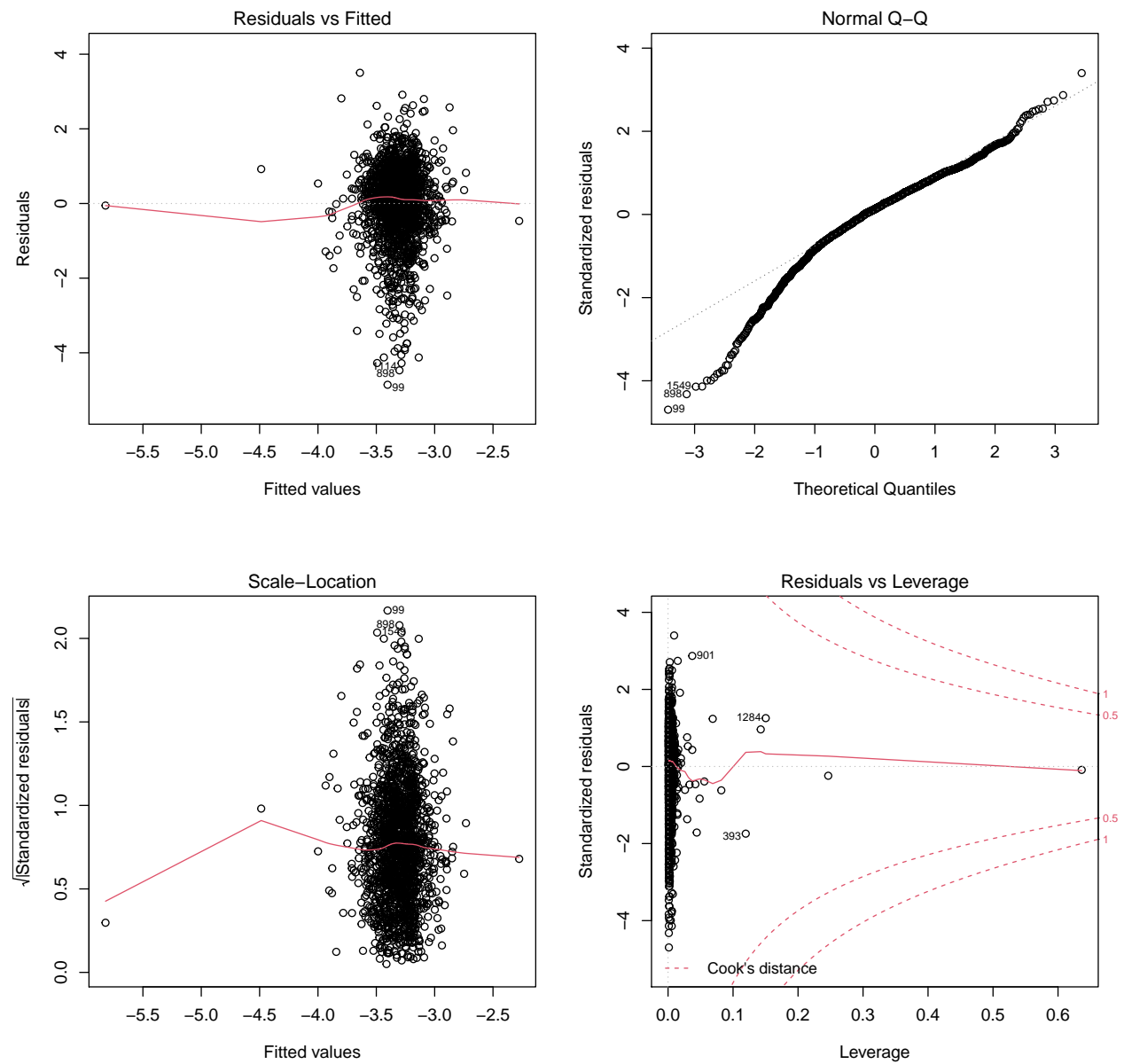


Figure 1: Plot for Model Checking

In terms of the leverage and Standard Residual plot, it could be seen that there is a point on the very right side and a few other points are far away compared to the rest of majority of observations (observations that are greater than the leverage 0.1). As such, those points are considered to have a high leverage, whereas they are all within the Cook's Distance. Thus, these points are considered not to be influential.

## 7 Results

We found that Elderly rate, number of Specialists, number of international migrations, and region are four variables that have major impacts to COVID-19 mortality rate given the dataset. This result matches with our initial speculation. Based on above discussion, the final model is selected to be  $Mortality \sim ElderlyRate + Specialist + Migration + factor(Region)$  as it has high  $R_{adj}^2$  compared to other models and is overall statistically significant. Besides, the hypothesis tests for individual variables indicate statistical significance. Further, the best linear model fitting for these variables is  $Mortality = -3.700e+00 + (2.699e+00)x_{ElderlyRate} + (3.641e-05)x_{Specialist} - (2.297e-05)x_{Migration} - (8.959e-02)x_{Northeast} - (1.422e-01)x_{South} - (2.641e-01)x_{West}$ . However, there can be several limitations of this study and will be discussed below.

## 8 Limitation of Study

Even though we have considered model 1:  $Mortality \sim ElderlyRate + Specialist + Migration + factor(Region)$  as our best model, there are still a great degree of limitation from using this model to analyze the mortality rate of COVID-19. First, model 1 has a low explanatory power. Specially,  $R_{adj}^2 = 0.0218$ , which means model 1 could only explain 2.18% percentage of variability of the mortality rate of COVID-19. This indicates that there is a large room for model improvement. Thus, a further investigation on factors are desired.

Secondly, multicollinearity issue is presented, which not only undermines the statistical significance of an independent variable, but also violates our model independence assumption. For instance, the correlation between Specialist & Migration is as high as 0.855, highlighting a strong positive linear association in this pair variable. In addition, a very high VIF value (50.404208) of Specialist, suggesting that the association will affect the standard errors. Since the multicollinearity issue is considered very severe in this case, we would need to do further investigation and study about the cause of this issue. The solution for this problem could be varied by situation. If it is structural multicollinearity, centering the variables could be helpful. (Frost (2017)). Another potential solution could be linearly combining the independent variables together, such as adding them together. The solution could also depend on our interest. Therefore, this will all require further discussion, since it could also be a situation that is very difficult to resolve.

## 9 Conclusion

## Appendix

```
##
## Call:
## lm(formula = Mortality ~ ElderlyRate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8993 -0.4917  0.1336  0.6605  3.6109
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.74966    0.09149 -40.982 < 2e-16 ***
## ElderlyRate  2.40160    0.48247   4.978 7.07e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.039 on 1737 degrees of freedom
## Multiple R-squared:  0.01406,    Adjusted R-squared:  0.0135
## F-statistic: 24.78 on 1 and 1737 DF,  p-value: 7.072e-07
##
## Call:
## lm(formula = Mortality ~ Region)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9109 -0.4914  0.1316  0.6785  3.0620
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -3.20073    0.04848 -66.017 < 2e-16 ***
## RegionNortheast -0.07649    0.09046  -0.846  0.39790
## RegionSouth    -0.14826    0.05972  -2.482  0.01314 *
## RegionWest     -0.24041    0.09116  -2.637  0.00843 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.044 on 1727 degrees of freedom
## (8 observations deleted due to missingness)
## Multiple R-squared:  0.005412,    Adjusted R-squared:  0.003684
## F-statistic: 3.132 on 3 and 1727 DF,  p-value: 0.02471
##
## Call:
## lm(formula = Mortality ~ Specialist)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9596 -0.4855  0.1351  0.6562  3.2403
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.299e+00  2.565e-02 -128.642 <2e-16 ***
## Specialist  -1.728e-05  7.828e-06   -2.207  0.0274 *
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.045 on 1737 degrees of freedom
## Multiple R-squared:  0.002796,    Adjusted R-squared:  0.002222
## F-statistic: 4.871 on 1 and 1737 DF,  p-value: 0.02745
##
## Call:
## lm(formula = Mortality ~ population)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9877 -0.4918  0.1333  0.6649  3.2686
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -3.40734    0.04648  -73.31  <2e-16 ***
## populationSmall  0.13515    0.05518   2.45   0.0144 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.044 on 1737 degrees of freedom
## Multiple R-squared:  0.003442,    Adjusted R-squared:  0.002869
## F-statistic:      6 on 1 and 1737 DF,  p-value: 0.0144
##
## Call:
## lm(formula = Mortality ~ Physician_rate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.8957 -0.4926  0.1193  0.6658  3.1942
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  -3.5697674  0.1318121 -27.082  <2e-16 ***
## Physician_rate  0.0009903  0.0004961   1.996   0.0461 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.045 on 1737 degrees of freedom
## Multiple R-squared:  0.002289,    Adjusted R-squared:  0.001715
## F-statistic: 3.985 on 1 and 1737 DF,  p-value: 0.04606
##
## Call:
## lm(formula = Mortality ~ Unemployment_rate_2018)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9849 -0.4643  0.1295  0.6592  3.2247
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
```

```

## (Intercept)          -3.46670    0.08251 -42.016   <2e-16 ***
## Unemployment_rate_2018 0.03688    0.01867   1.975    0.0484 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.045 on 1737 degrees of freedom
## Multiple R-squared:  0.002241,   Adjusted R-squared:  0.001666
## F-statistic: 3.901 on 1 and 1737 DF,  p-value: 0.04841

##
## Call:
## lm(formula = Mortality ~ Poverty)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9570 -0.4868  0.1355  0.6550  3.2323
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.300e+00  2.555e-02 -129.168   <2e-16 ***
## Poverty      -3.448e-07  1.537e-07   -2.243    0.025 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.045 on 1737 degrees of freedom
## Multiple R-squared:  0.002888,   Adjusted R-squared:  0.002314
## F-statistic: 5.032 on 1 and 1737 DF,  p-value: 0.02501

##
## Call:
## lm(formula = Mortality ~ Migration)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9585 -0.4795  0.1358  0.6560  3.2221
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.301e+00  2.526e-02 -130.691   < 2e-16 ***
## Migration    -1.269e-05  4.232e-06   -2.999    0.00275 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.044 on 1737 degrees of freedom
## Multiple R-squared:  0.00515,   Adjusted R-squared:  0.004577
## F-statistic: 8.992 on 1 and 1737 DF,  p-value: 0.00275

##
## Call:
## lm(formula = Mortality ~ Nurse)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -4.9610 -0.4833  0.1338  0.6569  3.2986
##

```



```
## Coefficients:
##           Estimate Std. Error  t value Pr(>|t|)
## (Intercept) -3.298e+00  2.566e-02 -128.519  <2e-16 ***
## Nurse       -1.063e-04  4.324e-05   -2.459    0.014 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.044 on 1737 degrees of freedom
## Multiple R-squared:  0.003468,    Adjusted R-squared:  0.002895
## F-statistic: 6.046 on 1 and 1737 DF,  p-value: 0.01404
```

## R Code

## Reference

Frost, Jim. 2017. "Multicollinearity in Regression Analysis: Problems, Detection, and Solutions," September. <https://statisticsbyjim.com/regression/multicollinearity-in-regression-analysis/>.

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USAFacts. 2020. "Coronavirus Locations: COVID-19 Map by County and State," March. <https://usafacts.org/visualizations/coronavirus-covid-19-spread-map/>.

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