

Machine Learning for Smarter Innovation

Week 1: Foundations & Clustering

Discovering Innovation Patterns with ML

BSc Course in AI-Enhanced Innovation

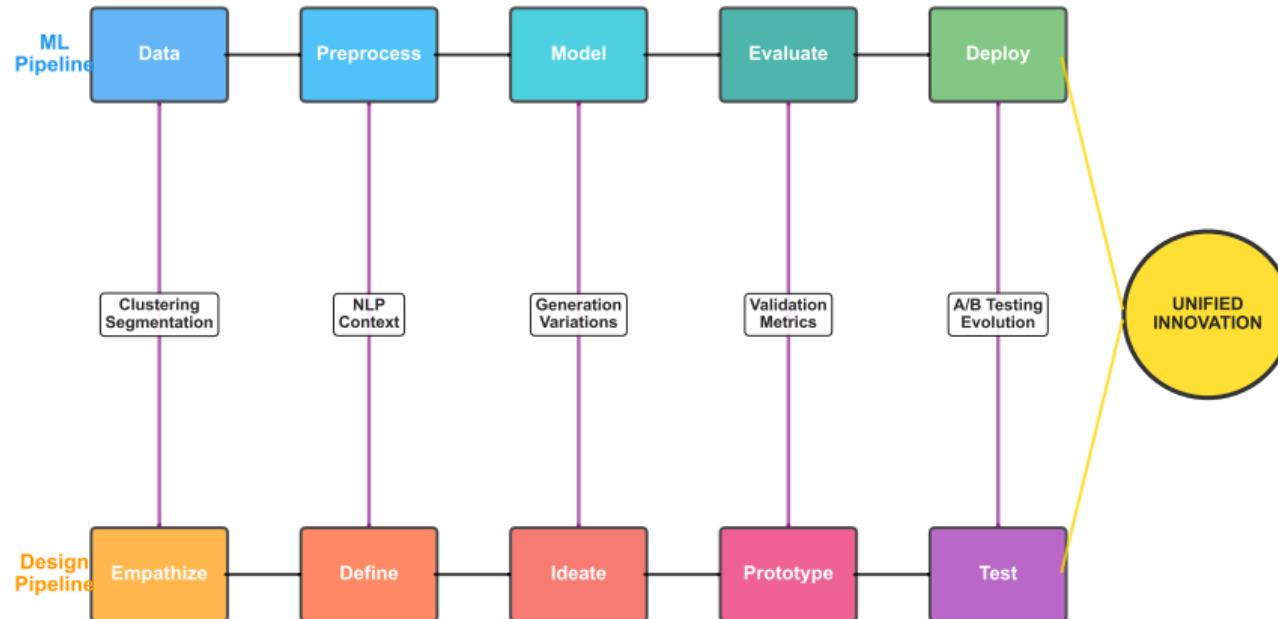
Machine Learning + Innovation + Design Thinking

The Power of Convergent Methodologies

The Unified Innovation Pipeline

Where Technology Amplifies Human Creativity

Technical Mastery



PART 1

Foundation & Context

What we'll explore:

- Why traditional design hits limits
- How ML amplifies human insight
- The dual pipeline approach
- Your learning journey ahead

Setting the stage for transformation

Part 1: Learning Objectives

What You'll Learn in This Section

By the end of Part 1, you will be able to:

- **Understand** the limitations of traditional innovation approaches
- **Recognize** how ML enhances human creativity
- **Explain** the dual pipeline methodology
- **Navigate** the 10-week learning journey
- **Identify** Week 1's role in the overall course

Success Criteria

- Can articulate 3+ traditional design limitations
- Can describe ML's value proposition
- Can map ML pipeline to design pipeline
- Understand clustering's role in innovation

The Innovation Challenge

Why Traditional Design Needs AI Enhancement

Traditional Design Limits

- **Scale:** Can analyze 50 ideas, not 50,000
- **Speed:** Months for insights
- **Bias:** Designer's perspective dominates
- **Patterns:** Miss hidden connections
- **Iteration:** Slow feedback loops

AI-Enhanced Innovation

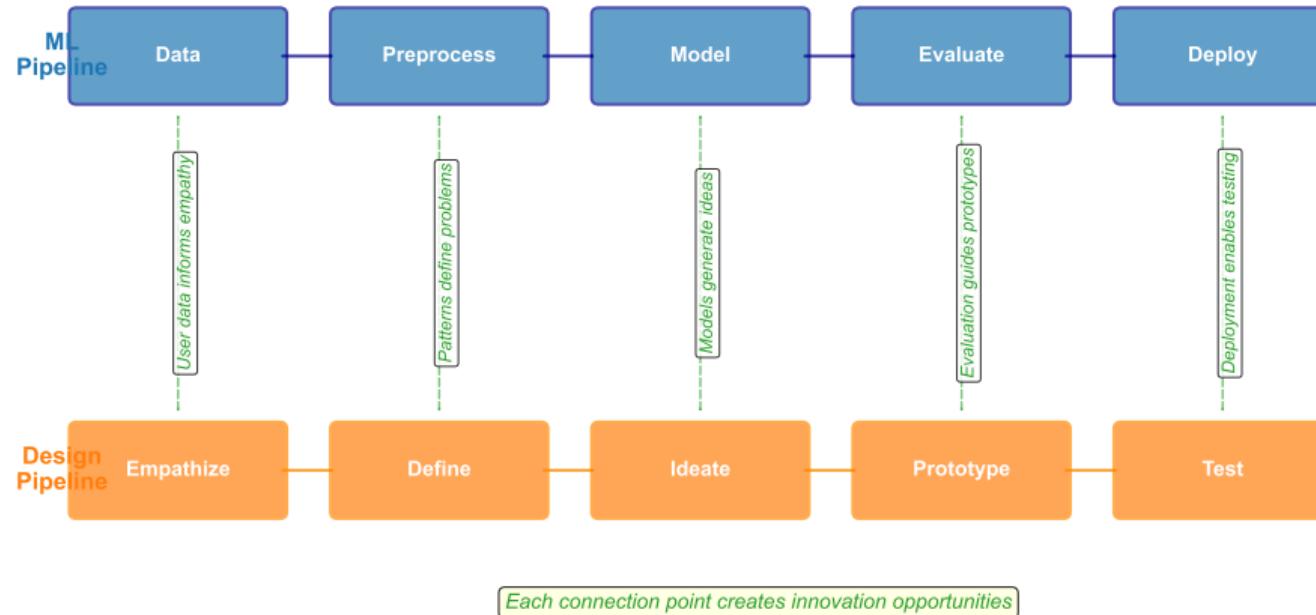
- **Scale:** Analyze millions of data points
- **Speed:** Real-time insights
- **Objectivity:** Data-driven discovery
- **Patterns:** Find non-obvious relationships
- **Iteration:** Continuous learning

The Promise: 100x more insights, 10x faster innovation

The Dual Pipeline

Where ML Meets Design Thinking

The Convergence: ML Meets Design Thinking



The Dual Pipeline (Continued)

Understanding Both Worlds

ML Pipeline

Data → Preprocess → Model → Evaluate → Deploy

- Collect innovation data
- Clean and transform
- Train algorithms
- Validate accuracy
- Scale to production

Design Pipeline

Empathize → Define → Ideate → Prototype → Test

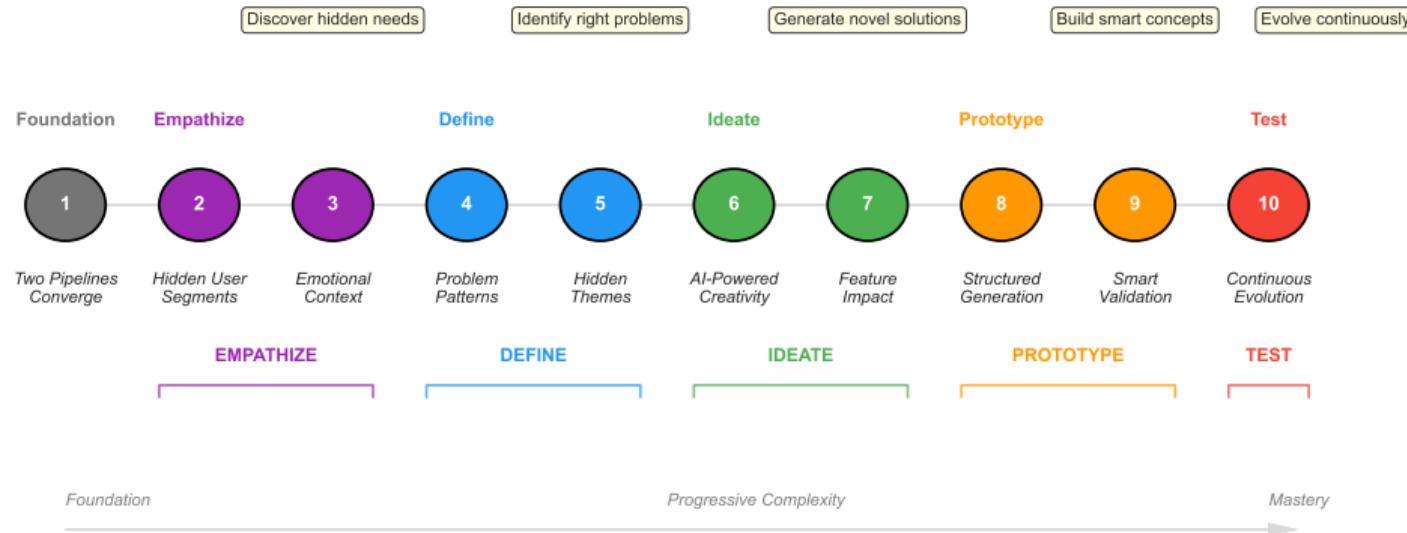
- Understand innovation needs
- Frame problems
- Generate solutions
- Build concepts
- Validate innovation impact

Integration = Innovation at Scale

Your Innovation Journey

10 Weeks to Understanding AI-Powered Design

10-Week Innovation Journey



Your Innovation Journey (Continued)

What You'll Learn in Each Stage

Stage	Weeks	Innovation Unlocked
Discover	1-2	Find hidden innovation opportunities
Define	3-4	Identify the right problems to solve
Ideate	5-6	Generate novel solutions with AI
Prototype	7-8	Build smart, adaptive concepts
Test	9-10	Evolve through continuous learning

This Week: Clustering for Innovation Pattern Discovery

Week 1: Clustering for Innovation

From Scattered Ideas to Innovation Patterns

What We'll Learn:

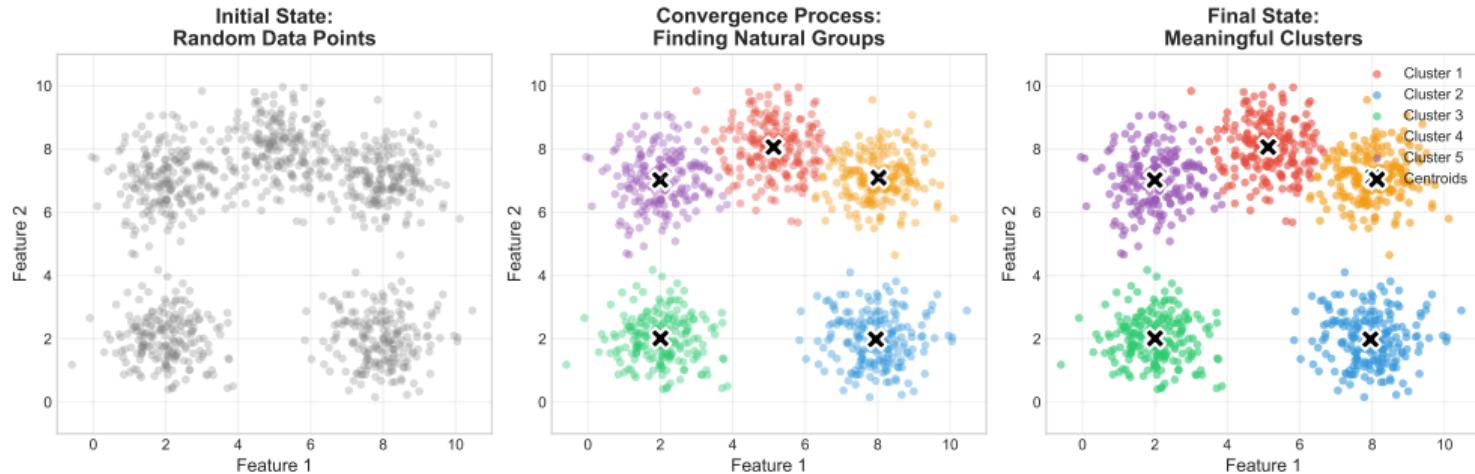
- How clustering reveals innovation categories
- K-means algorithm fundamentals
- Finding the optimal number of clusters
- Quality metrics for validation
- Advanced clustering techniques

Design Applications:

- Create innovation archetypes
- Map innovation evolution paths
- Identify opportunities systematically
- Prioritize design efforts
- Scale analysis to thousands of ideas

Goal: Transform scattered ideas into innovation patterns

The Convergence Flow: From Chaos to Clarity



The Convergence Flow: Order from Chaos

Watch 5000 innovation ideas self-organize into meaningful patterns

Now Let's Get Technical

From Understanding the Problem to Finding Solutions

We've seen the challenge:

Thousands of innovation ideas with hidden connections

Traditional approach:

Manual segmentation based on demographics

The ML solution:

Let the data reveal its own natural groups

Enter: Clustering Algorithms

PART 2

Technical Core

What we'll learn:

- K-means clustering algorithm
- Finding optimal K with elbow method
- Distance metrics and quality measures
- Advanced techniques (DBSCAN, Hierarchical)
- Feature importance analysis

Learning the basics step by step

Part 2: Learning Objectives

Technical Skills You'll Develop

By the end of Part 2, you will understand:

- **How** K-means clustering works
- **What** the elbow method shows us
- **Why** we measure distances
- **How to check** if clusters are good
- **Differences** between algorithms
- **When to use** each method

Practical Skills

- Use K-means step by step
- Understand quality scores
- Pick the right algorithm
- Adjust settings properly
- Work with different patterns
- Prepare data for analysis

The Innovation Classification Problem

5000 Ideas - How Do They Connect?

The Pain

Current Reality:

- One-size-fits-all solutions
- Generic innovation categories
- Missed opportunities
- Unhappy edge cases

The Cost:

- Most innovations get misclassified
- Features with low adoption rates
- Inefficient resource allocation

The Question

What if we could...

- Find natural innovation clusters?
- Discover innovation patterns?
- Innovate at scale?
- Identify opportunity gaps?

We can!

Solution: Clustering

What is Clustering?

Like Organizing a Messy Room - Finding Things That Belong Together

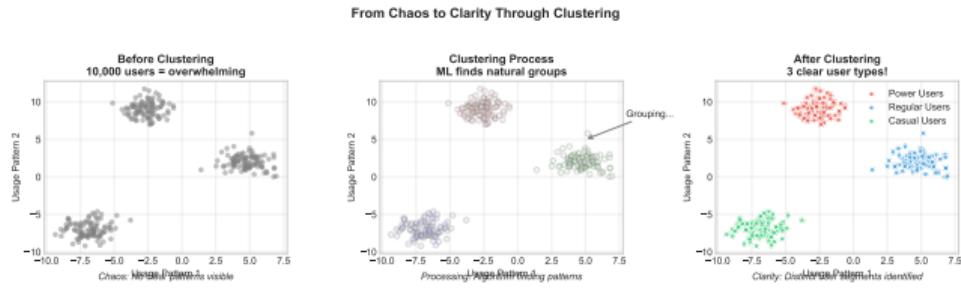
Clustering Finds:

- Natural groupings (like sorting laundry by color)
- Similar approaches (things that work the same way)
- Hidden patterns (connections you didn't see before)
- Innovation relationships (which ideas go together)

Key Insight:

Things that look similar often belong in the same group

(Just like organizing books by topic on a shelf)

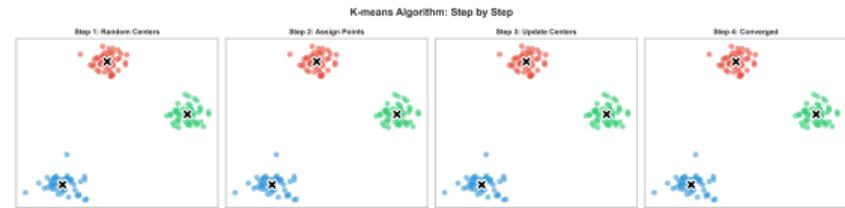


K-Means: The Basic Clustering Method

Like Finding Neighborhoods in a City

The Process (Step by Step):

- ① Choose K (how many groups you want)
- ② Place K random centers (like putting pins on a map)
- ③ Assign each point to its nearest center
- ④ Move centers to the middle of their groups
- ⑤ Repeat until nothing changes



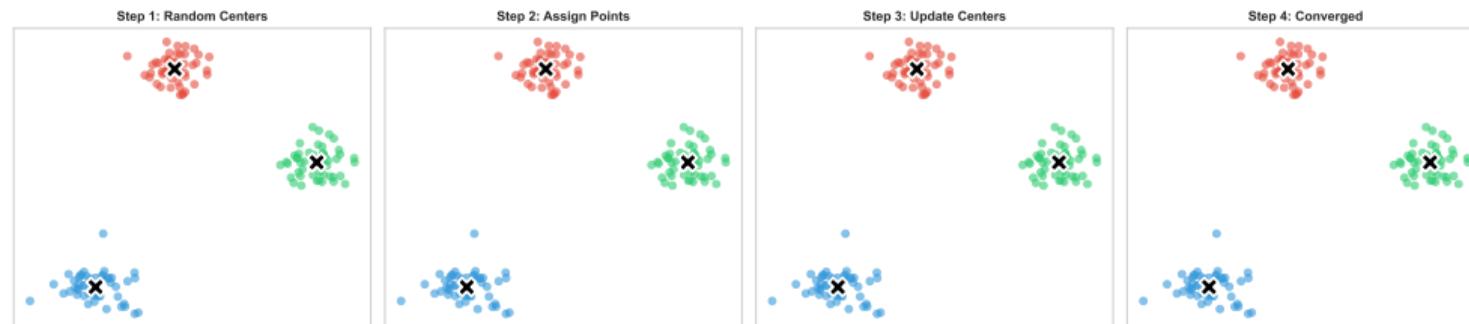
Strengths:

- Fast and scalable
- Easy to understand
- Works well for spherical clusters

K-Means in Action

Step-by-Step Convergence

K-means Algorithm: Step by Step



Iteration 1 → Iteration 3 → Iteration 5 → **Converged**

The Goldilocks Problem

Too Few vs. Too Many Groups

Too Few (K

Oversimplification

- Mixed segments
- Lost nuance
- Generic solutions

Just Right (K

Optimal Balance

- Clear segments
- Actionable insights
- Manageable complexity

Too Many (K

Analysis Paralysis

- Overfitting
- Tiny segments
- Impossible to act on

How do we find the sweet spot?

The Elbow Method

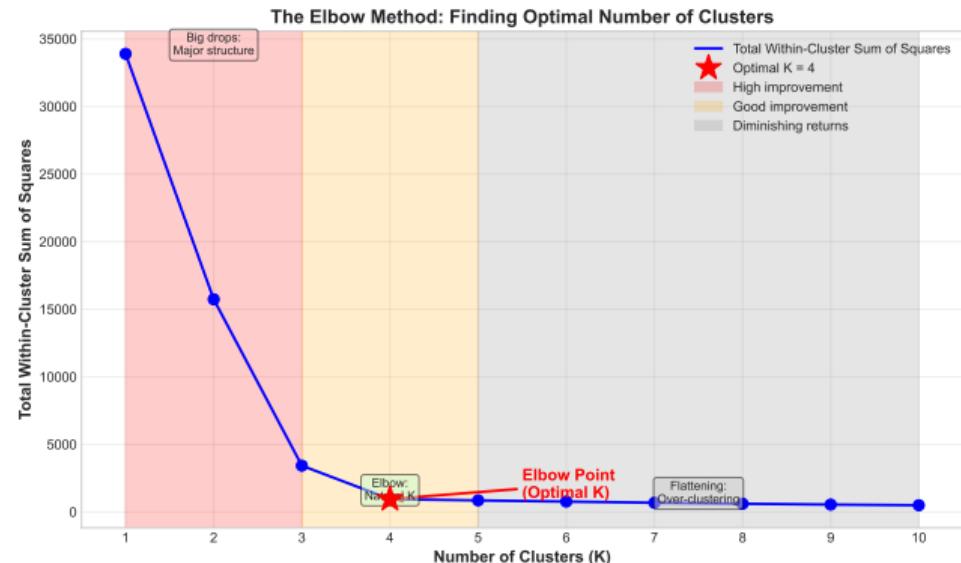
How Many Groups Should We Have? (Like Goldilocks - Not Too Few, Not Too Many)

Finding the Elbow:

- Plot inertia vs K
- Look for the “elbow”
- Balance between:
 - Too few: Mixed groups
 - Too many: Overfitting

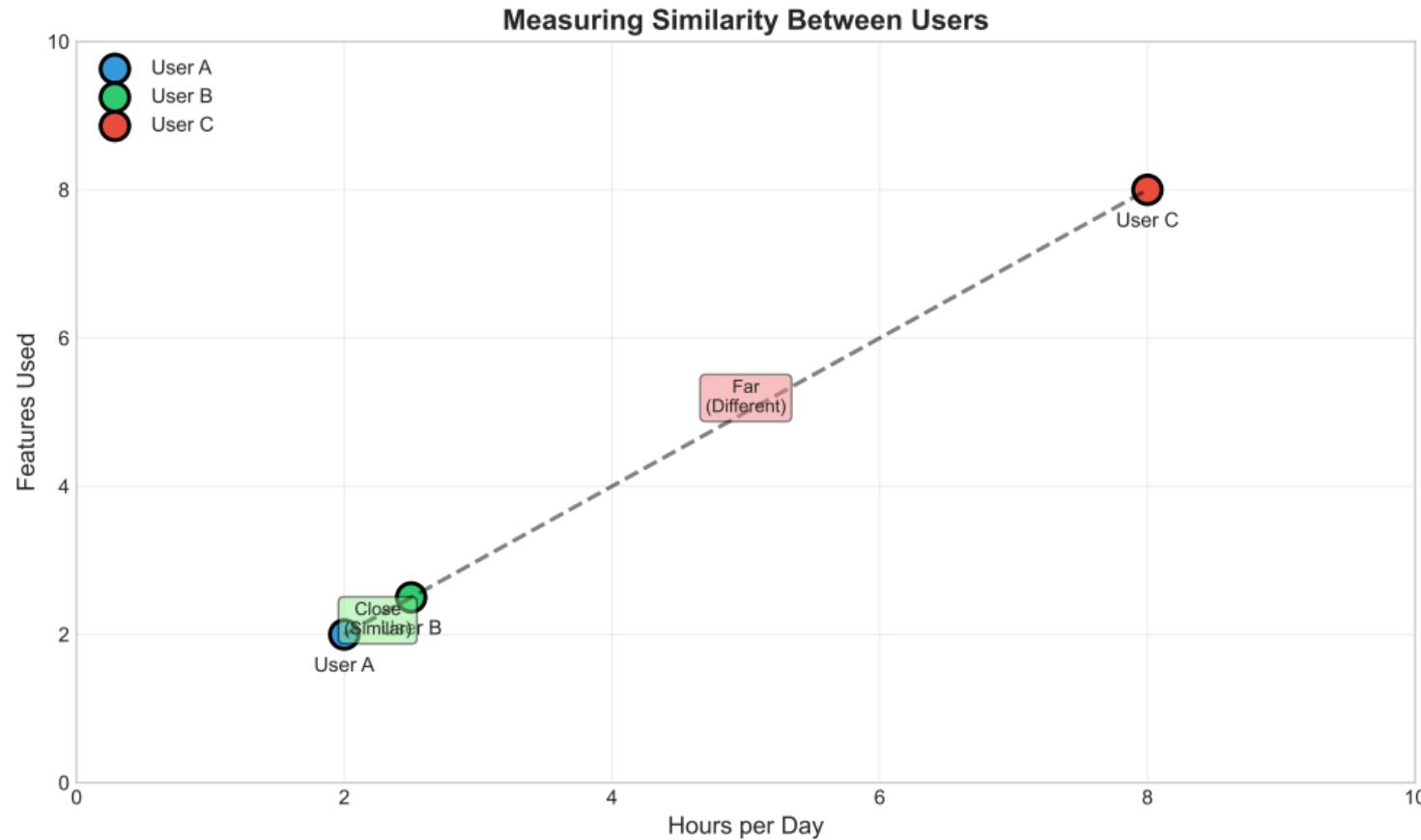
Optimal K = 5

Best trade-off between simplicity and accuracy



Distance Metrics

Different Ways to Measure "How Close" Things Are



Cluster Quality Metrics

Are Our Groups Any Good? (Like Checking Your Work)

Silhouette Score:

- Ranges from -1 to +1
- Higher = better separation
- Our score: **0.73**

What it measures:

- Within-cluster cohesion
- Between-cluster separation
- Overall cluster validity

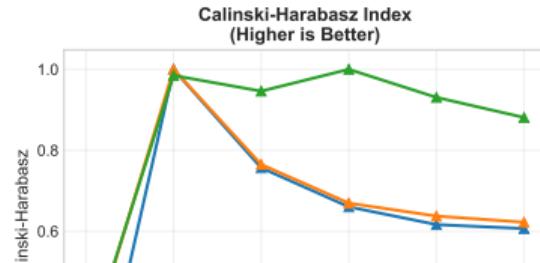
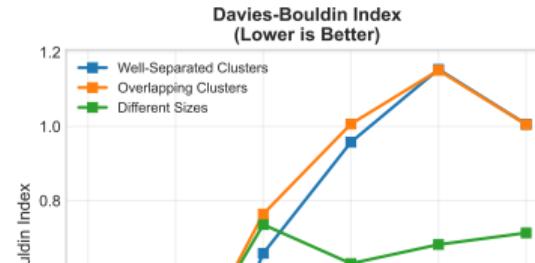
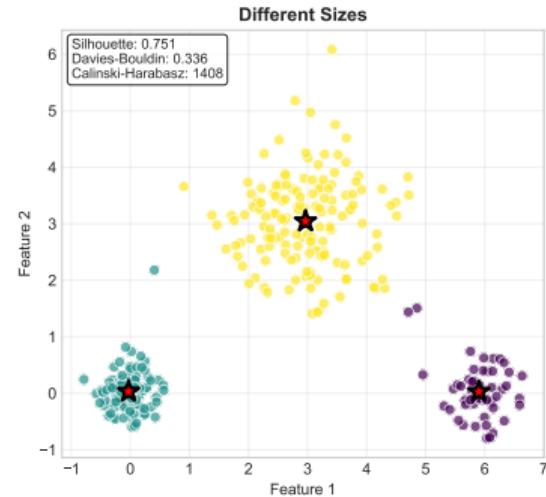
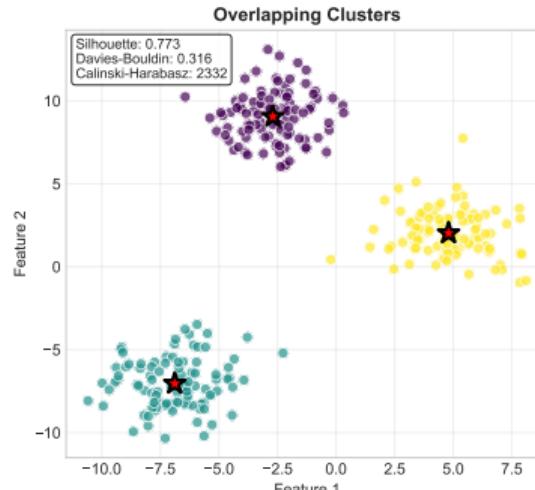
0.73 = Strong clusters!



Comparing Evaluation Metrics

Different Metrics for Different Data Patterns

Clustering Evaluation Metrics Comparison How Different Metrics Behave on Various Data Patterns



When Circles Don't Work

Real Innovation Clusters Have Complex Shapes

K-Means Assumes Spherical Clusters

But what about:

- Innovations connected through technology stacks
- Domain-specific innovation clusters
- Evolution patterns (incremental, disruptive)
- Outliers and noise points

K-Means Forces Round Pegs into Round Holes

Solution: Density-Based Clustering

DBSCAN: Finding Groups Naturally

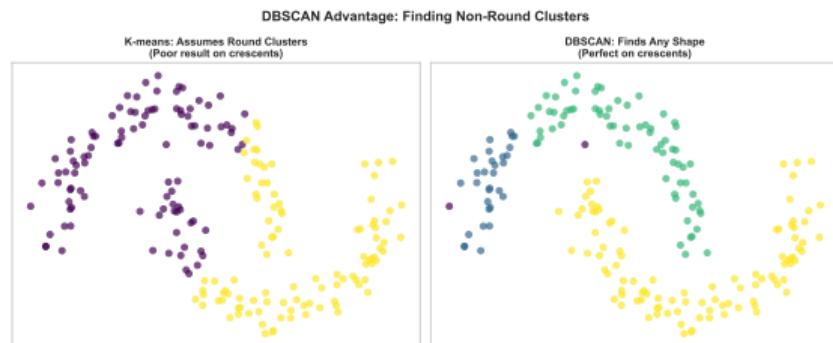
Like Finding Groups of People at a Party - Where Are the Crowds?

DBSCAN Advantages:

- No need to specify K
- Finds arbitrary shapes
- Identifies outliers
- Handles noise well

Perfect for:

- Non-spherical patterns
- Varying densities
- Outlier detection
- Exploratory analysis



DBSCAN: Complex Patterns

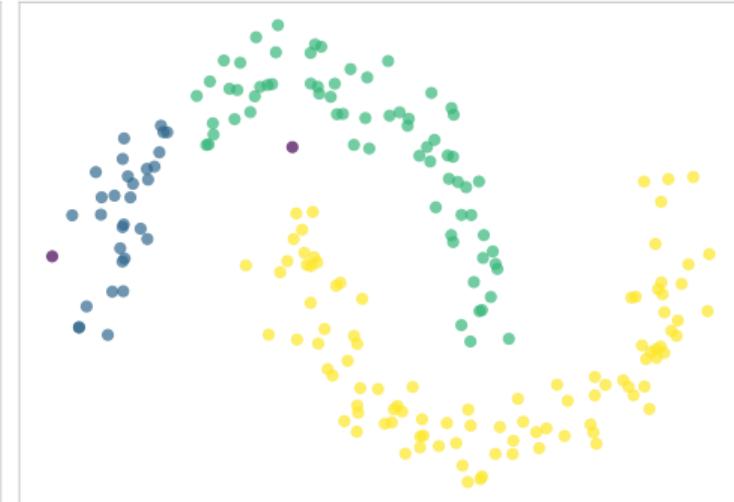
When K-Means Isn't Enough

DBSCAN Advantage: Finding Non-Round Clusters

K-means: Assumes Round Clusters
(Poor result on crescents)



DBSCAN: Finds Any Shape
(Perfect on crescents)



K-Means: Forces spherical shapes — DBSCAN: Finds natural boundaries

Choosing the Right Algorithm

Comparison of Clustering Methods

Algorithm	Speed	Shape	Outliers	Params	Best For
K-Means	Fast $O(nkt)$	Spherical clusters	Sensitive	K only	Quick segments
DBSCAN	Medium $O(n \log n)$	Any shape	Robust (detects)	eps, MinPts	Complex shapes
Hierarchical	Slow $O(n^2)$	Any shape	Moderate	Distance threshold	Multi-level analysis
GMM	Medium $O(nkt)$	Elliptical clusters	Moderate	K, covariance	Overlapping groups

Choose K-Means when:

- Speed is critical
- Clusters are roughly equal size
- You know K in advance

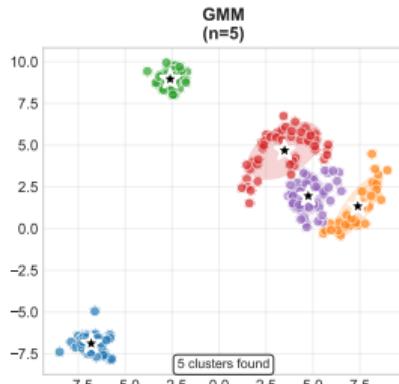
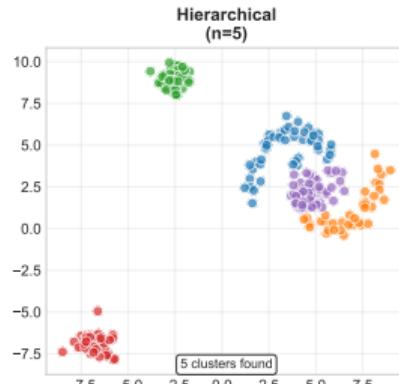
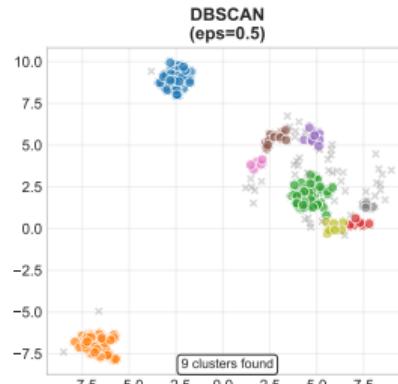
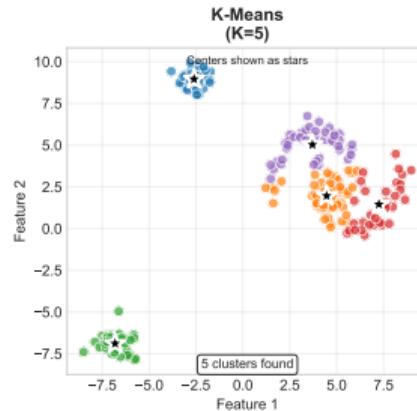
Choose DBSCAN when:

- Clusters have irregular shapes
- Outliers need identification
- Density varies across data

Algorithm Visual Comparison

Same Data, Different Approaches

Clustering Algorithms Visual Comparison Same Data, Different Approaches



K-Means (K=5)

- Fast and scalable
- Spherical clusters
- Fixed K required
- Sensitive to outliers

Best for: Quick segmentation with known cluster count

DBSCAN (eps=0.5)

- Finds arbitrary shapes
- Identifies outliers
- No K needed
- Sensitive to parameters

Best for: Anomaly detection and irregular patterns

Hierarchical (n=5)

- Dendrogram output
- No K needed initially
- Interpretable
- Computationally expensive

Best for: Taxonomies and exploring relationships

GMM (n=5)

- Soft assignments
- Elliptical clusters
- Probabilistic
- Assumes Gaussian distribution

Best for: Overlapping groups and uncertainty modeling

Complexity: $O(nkt)$

Complexity: $O(n \log n)$

Complexity: $O(n^2)$

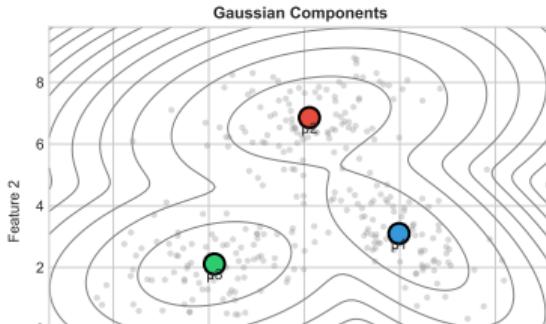
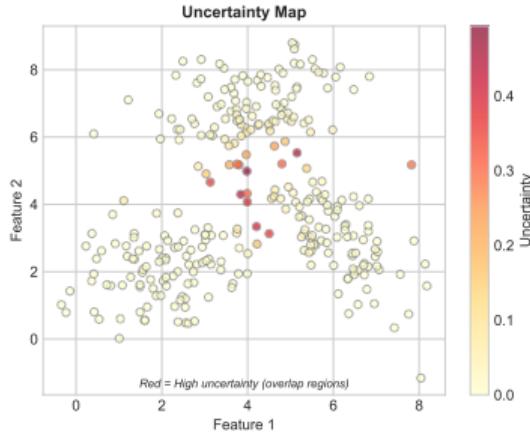
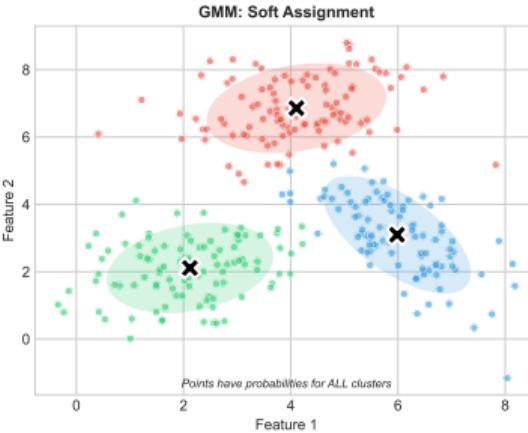
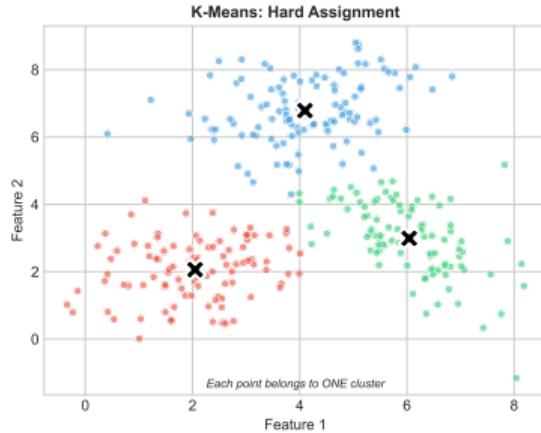
Complexity: $O(nkt)$

Gaussian Mixture Models (GMM)

Soft Clustering for Overlapping Innovation Categories

Gaussian Mixture Models (GMM): Soft Clustering for Innovation

Beyond Hard Boundaries: Probabilistic Innovation Classification



GMM vs K-means

- GMM Advantages:
- Soft assignments (probabilities)
 - Captures cluster shape (elliptical)
 - Handles overlapping clusters
 - Provides uncertainty estimates
 - Models data generation process

- K-means Advantages:
- Faster computation
 - Simpler interpretation
 - Less parameters
 - More stable results
 - Works well for spherical clusters

- When to use GMM:
- Overlapping innovation categories
 - Non-spherical clusters

Innovation Category Probabilities

Innovation	Tech	Service	Social
AI Assistant	0.85	0.10	0.05
Sharing Platform	0.30	0.45	0.25
Green Energy	0.60	0.15	0.25
Digital Health	0.40	0.50	0.10

The Granularity Challenge

When You Need Multiple Levels of Detail

Fixed K Gives One View

But real relationships are hierarchical:

- Organization: Company → Department → Team → Individual
- Geography: Country → Region → City → Neighborhood
- Products: Category → Subcategory → Brand → SKU
- Innovations: All → Categories → Sub-types → Specific solutions

K-means: Pick 5 groups and that's it

What if we need flexibility?

Solution: See the full hierarchy, cut where needed

Hierarchical Clustering

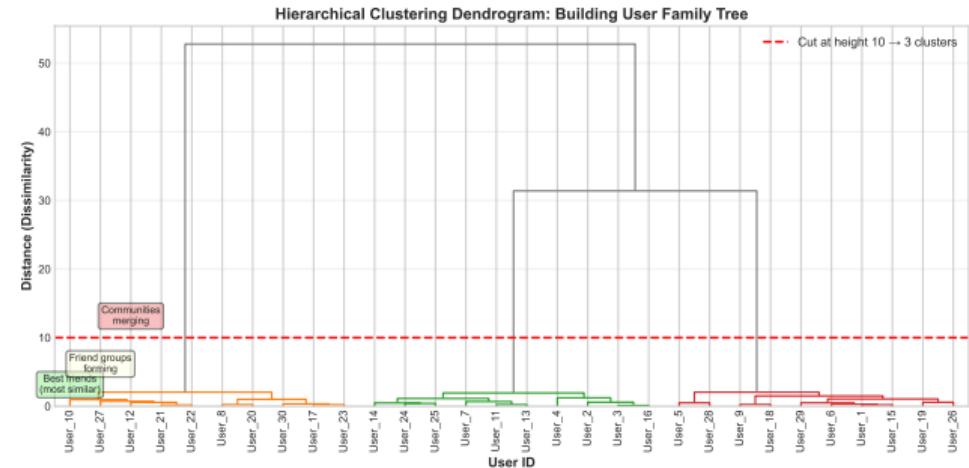
Building a Tree of Relationships

Dendrogram Benefits:

- Shows cluster hierarchy
- Multiple granularities
- Natural relationships
- No preset K needed

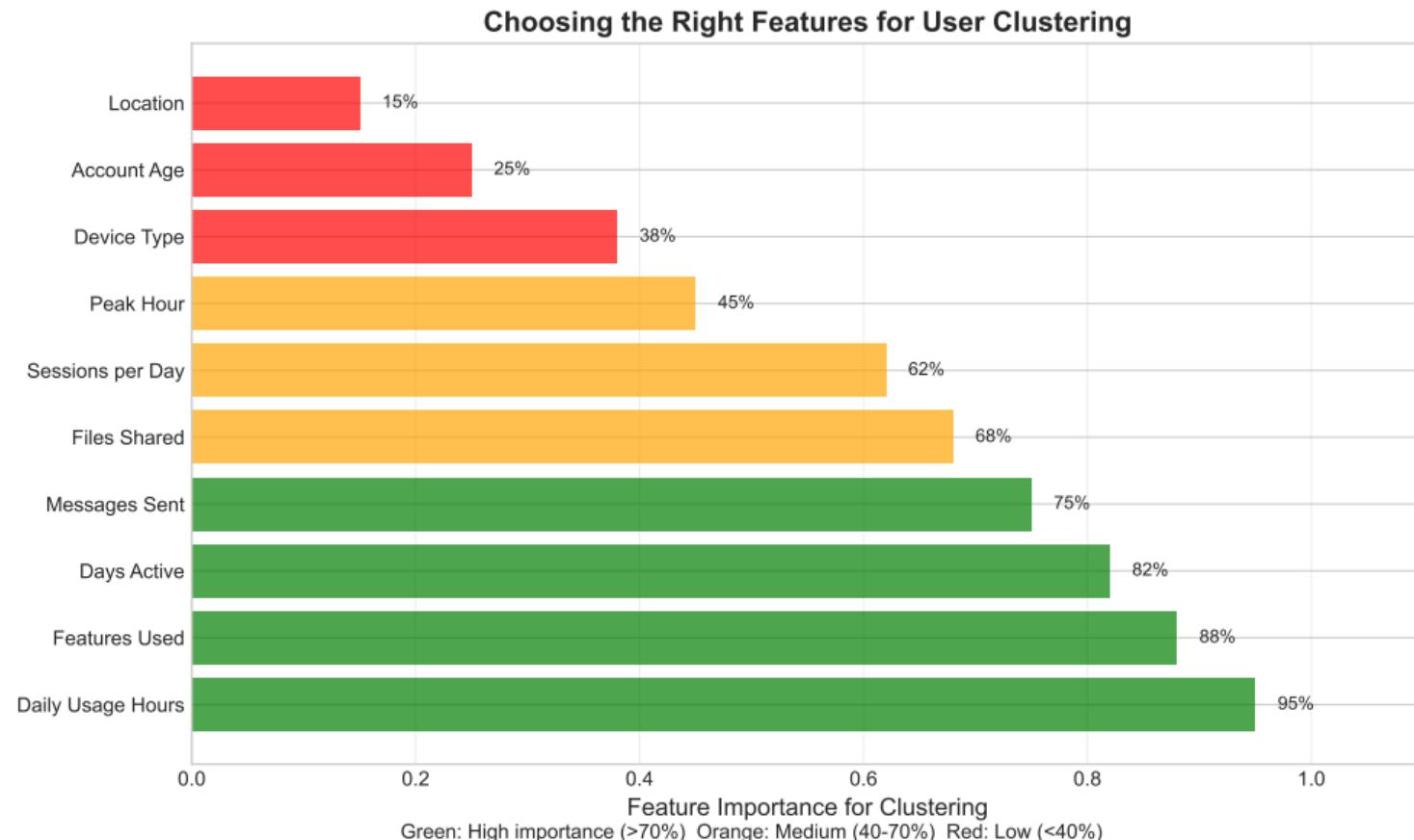
Cut the tree at any level:

- High cut = Few clusters
- Low cut = Many clusters
- Choose based on needs



What Drives the Clusters?

Feature Importance Analysis

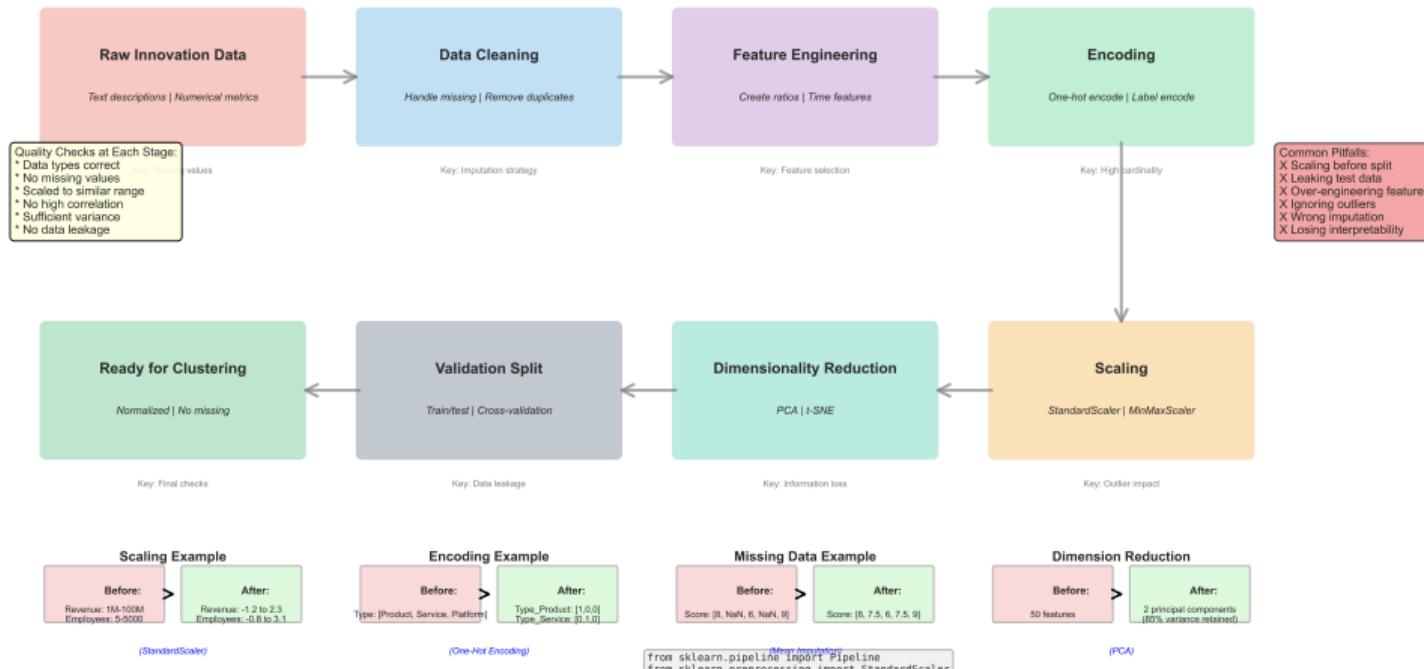


Data Preprocessing Pipeline

From Raw Data to Clustering-Ready Features

Data Preprocessing Pipeline for Innovation Clustering

From Raw Data to Clustering-Ready Features



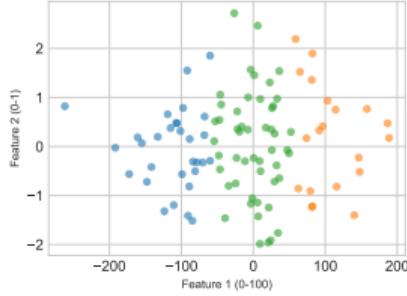
Common Mistakes & Troubleshooting

Learn from These Pitfalls

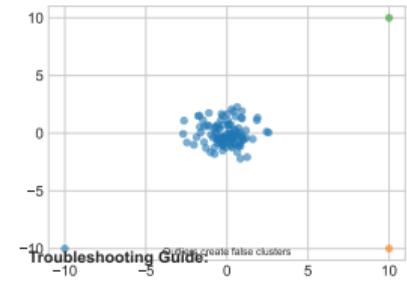
Common Clustering Mistakes & Troubleshooting Guide

Learn from These Mistakes to Master Clustering

Visual Examples of Common Mistakes:



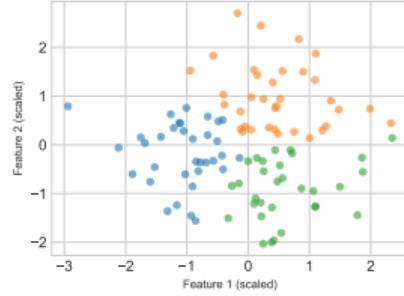
MISTAKE: Outliers distort



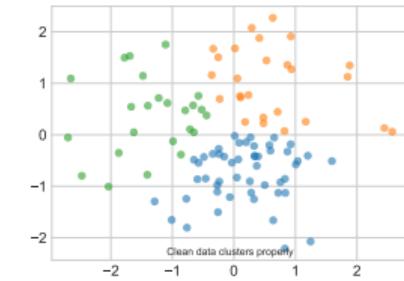
Troubleshooting Guide:

Outliers create false clusters

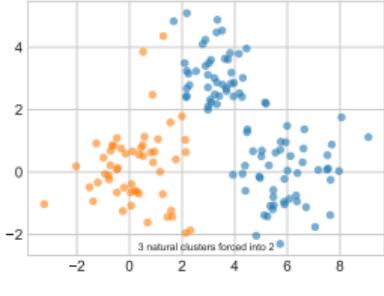
CORRECT: Scaled Features



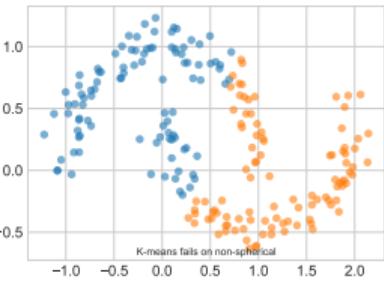
CORRECT: Outliers removed



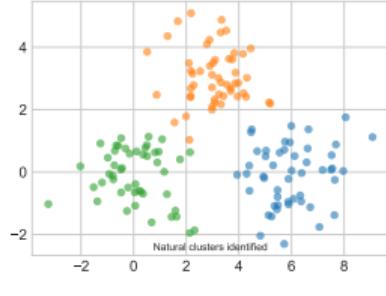
MISTAKE: K=2 (too few)



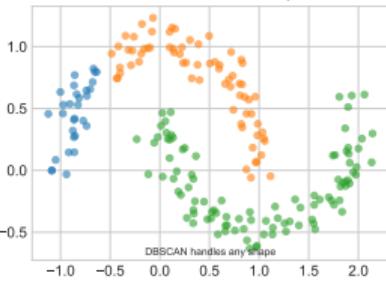
MISTAKE: K-means on moons



CORRECT: K=3 (optimal)



CORRECT: DBSCAN for shapes



Problem

Symptoms

Solution

Prevention

Poor separation

- GOLDEN RULES:
1. Always scale your features

Low silhouette score

Try different K or algorithm

Use elbow method

Different k-means vs. diff. algos

WARNING SIGNS:

Get random state. Increases in init.

SUCCESS INDICATORS:

Parameter Tuning Guidelines

Recommended Ranges and Best Practices

Clustering Parameter Tuning Guidelines

Recommended Ranges, Methods, and Best Practices

K-Means				DBSCAN				GMM			
Parameter	Range	Default	Tuning Method	Parameter	Range	Default	Tuning Method	Parameter	Range	Default	Tuning Method
n_clusters (K)	2-10	3-5	Elbow/Silhouette	eps	0.01-2.0	0.5	k-distance plot	n_components	2-10	3-5	BIC/AIC
init	['k-means++', 'random']	Always k-means++		min_samples	3-20	2*dims	Domain knowledge	covariance_type	['full', 'diag', 'full', 'spherical']	Start full, simplify	
n_init	10-100	10	More for stability	metric	['euclidean', 'manhattan']	Data dependent		max_iter	50-500	100	Monitor convergence
max_iter	100-1000	300	Increase if no convergence	algorithm	['auto', 'ball_tree']	Auto is fine		n_init	1-10	1	More for stability
tol	1e-6 to 1e-2	1e-4	Smaller for precision	leaf_size	10-50	30	Memory vs speed	init_params	['kmeans', 'random']		kmeans faster

Tuning Strategies

Grid Search

Pros: Exhaustive, Reproducible, Simple

Cons: Slow, Curse of dimensionality

Use when: Small parameter space

Random Search

Pros: Faster, Better for many params, Parallelizable

Cons: May miss optimum, Not reproducible

Use when: Large parameter space

Bayesian Opt

Pros: Efficient, Learns from history, Fewer iterations

Cons: Complex, Overhead for simple problems

Use when: Expensive evaluations

Validation Metrics

Metric	Range	Interpretation	Use For
Silhouette	[-1, 1]	Higher is better	General quality
Davies-Bouldin	[0, ∞)	Lower is better	Cluster separation
Calinski-Harabasz	[0, ∞)	Higher is better	Dense clusters
Inertia	[0, ∞)	Lower is better	K-means only
BIC/AIC	(-∞, ∞)	Lower is better	GMM selection

Tuning Best Practices

1. Start with defaults, then tune

2. Use cross-validation when possible

3. Consider computational budget

4. Log all experiments

5. Visualize parameter effects

6. Use domain knowledge

7. Check stability across runs

8. Don't overfit to metrics

IMPORTANT:
No metric is perfect!
Always validate with:

- Visual inspection
- Domain expertise
- Business goals

From Algorithms to Innovation Insights

What Does This Mean for Innovation Opportunities?

We've mastered the technical tools:

Clustering, metrics, quality measures

But clusters are just numbers...

Until we connect them to innovation opportunities

Let's transform data into innovation insights

Each cluster represents innovation opportunities and patterns

PART 3

Innovation Pattern Analysis

What we'll create:

- Data-driven innovation archetypes
- Innovation pattern maps per category
- Cluster-specific journeys
- Opportunity heat maps
- Design priority matrices

Where ML reveals innovation patterns

Part 3: Learning Objectives

Innovation Applications You'll Explore

By the end of Part 3, you will be able to:

- **Create** innovation archetypes
- **Map** innovation patterns
- **Design** opportunity matrices
- **Analyze** innovation lifecycles
- **Build** ecosystem maps
- **Prioritize** innovation efforts

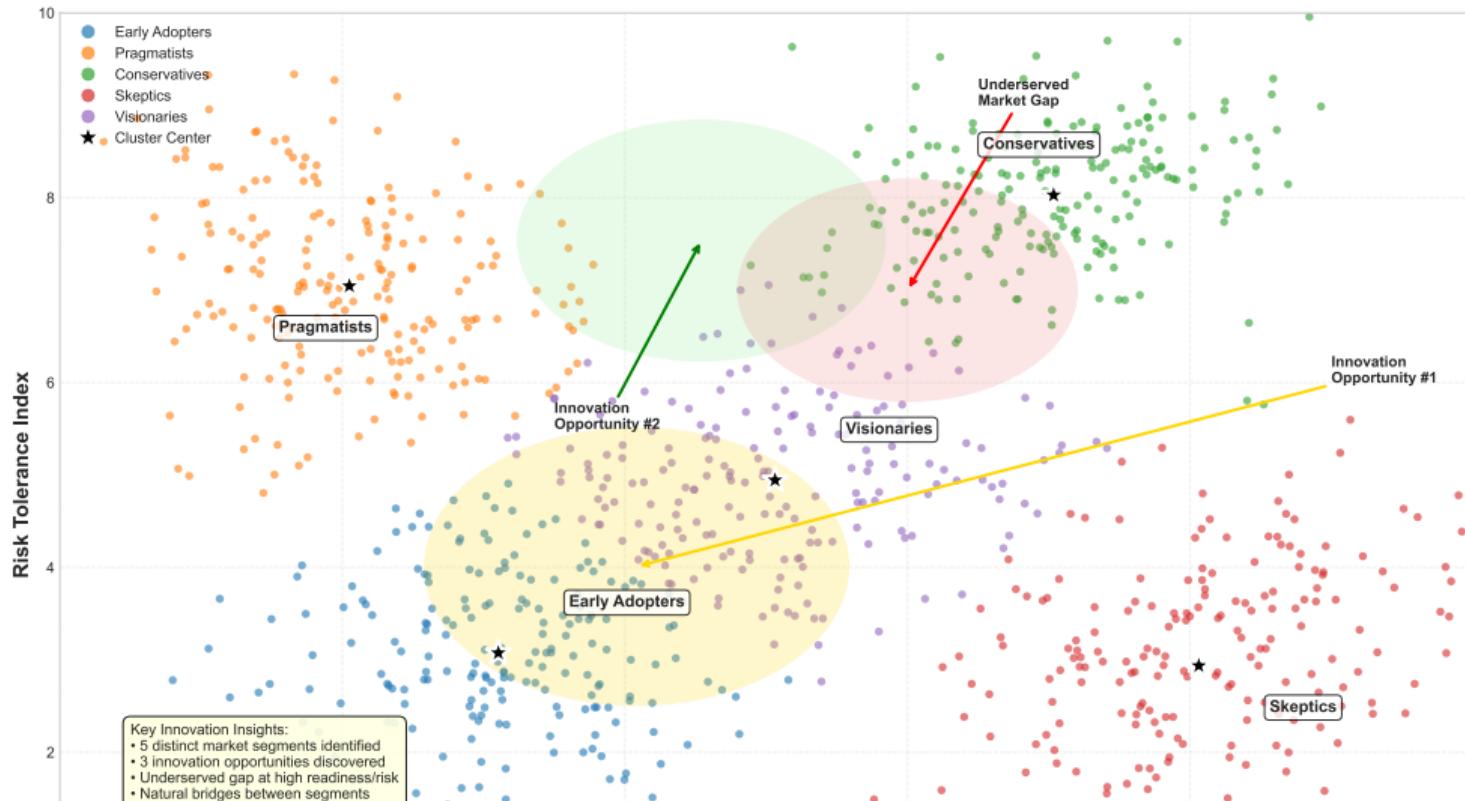
Design Outcomes

- Innovation taxonomy framework
- Cluster-based strategies
- Data-driven prioritization
- Opportunity identification
- Pattern recognition skills
- Ecosystem understanding

From Data Points to Innovation Insights

Bridging the Technical-Human Gap

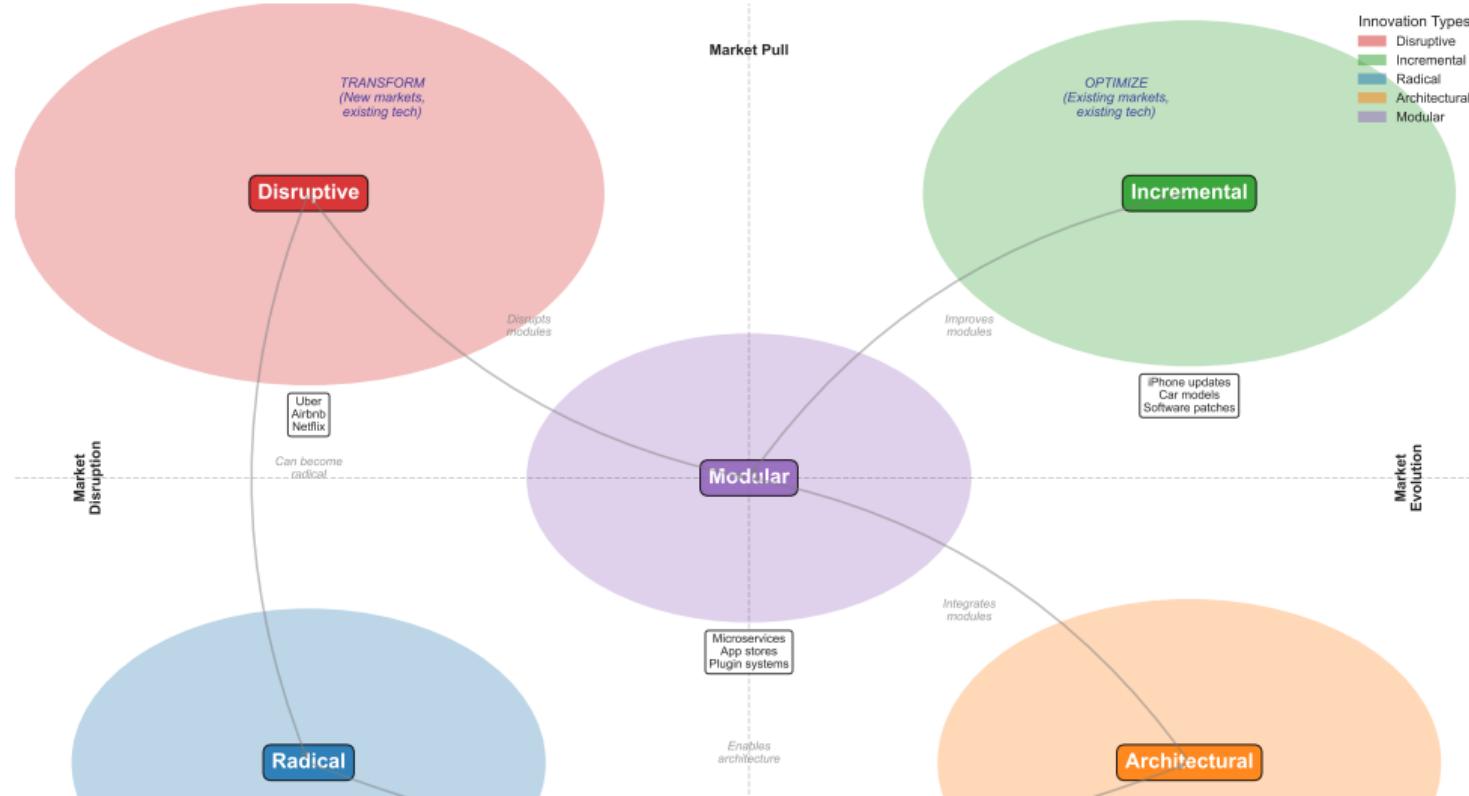
Innovation Pattern Discovery Through Clustering
Revealing Hidden Market Opportunities



AI-Generated Innovation Archetypes

Data-Driven Character Development

Innovation Archetypes Discovery Five Distinct Patterns from Clustering Analysis



Innovation Taxonomy Framework

Types, Relationships, and Impact Levels

Impact Levels

- Radical
- Disruptive
- Incremental



Innovation Taxonomy Framework

Types, Relationships, and Impact Levels

DISRUPTIVE

Change industry rules

INCREMENTAL

Continuous improvement!



Manufacturing
Innovation

Ex: iPhone, Tesla, Dyson



Digital
Transformation

Ex: Lean Mtg, Six Sigma, Agile



Ex: Subscription, Platform, Freemium

ML Clustering reveals:
• Natural innovation groupings
• Hidden relationships
• White space opportunities
• Evolution patterns

Go-to-Market



Growth
Hacking

Ex: Viral, Dynamic Pricing, Content



Customer
Centricity

Ex: Holacracy, Remote, Open Innovation

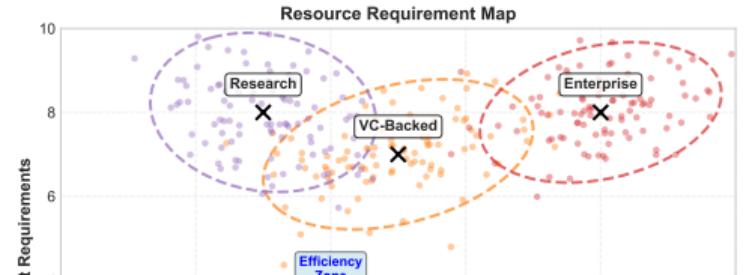
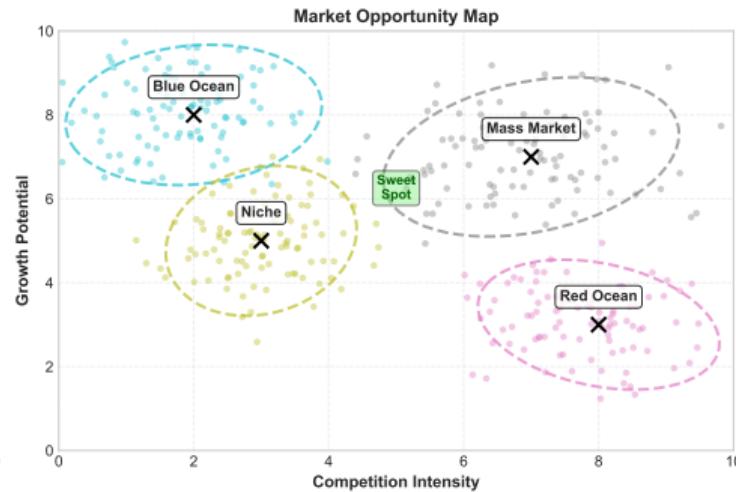
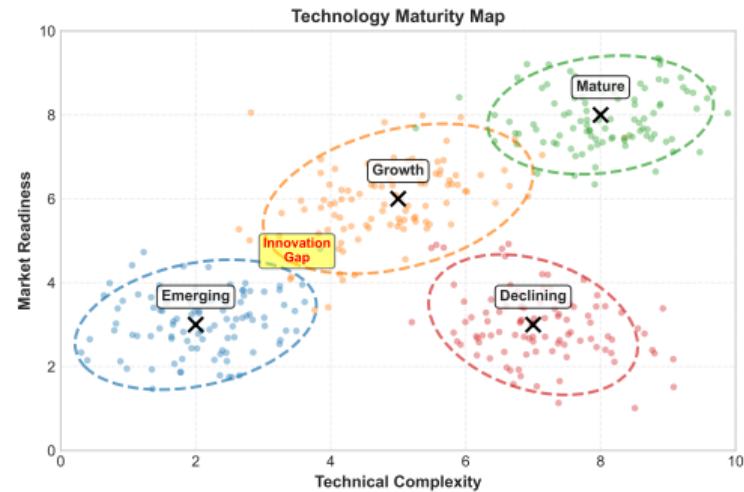


Ex: Concierge, Self-Service, AI Support

Innovation Pattern Mapping by Cluster

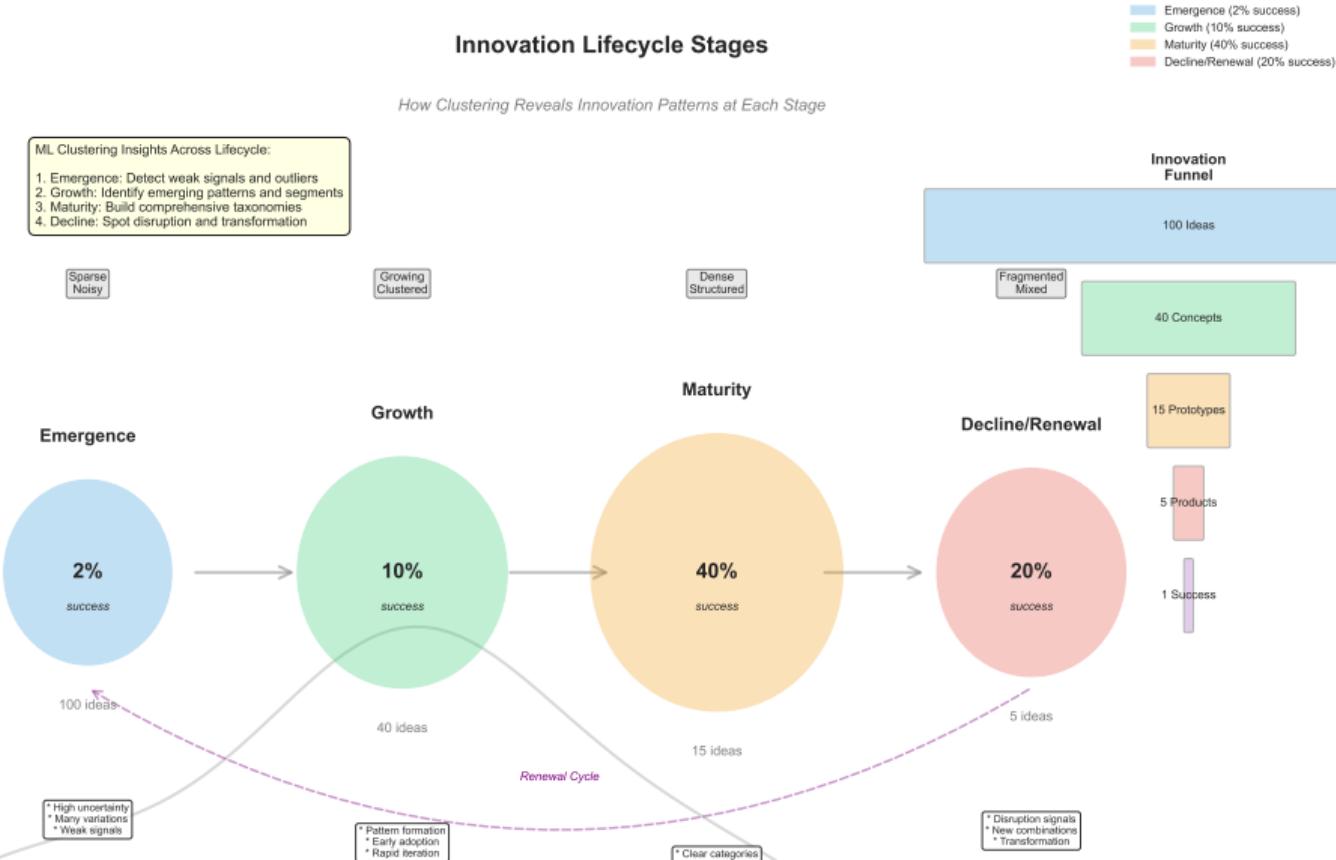
Understanding Each Category's Impact

Innovation Pattern Maps
Four Perspectives on Innovation Categories



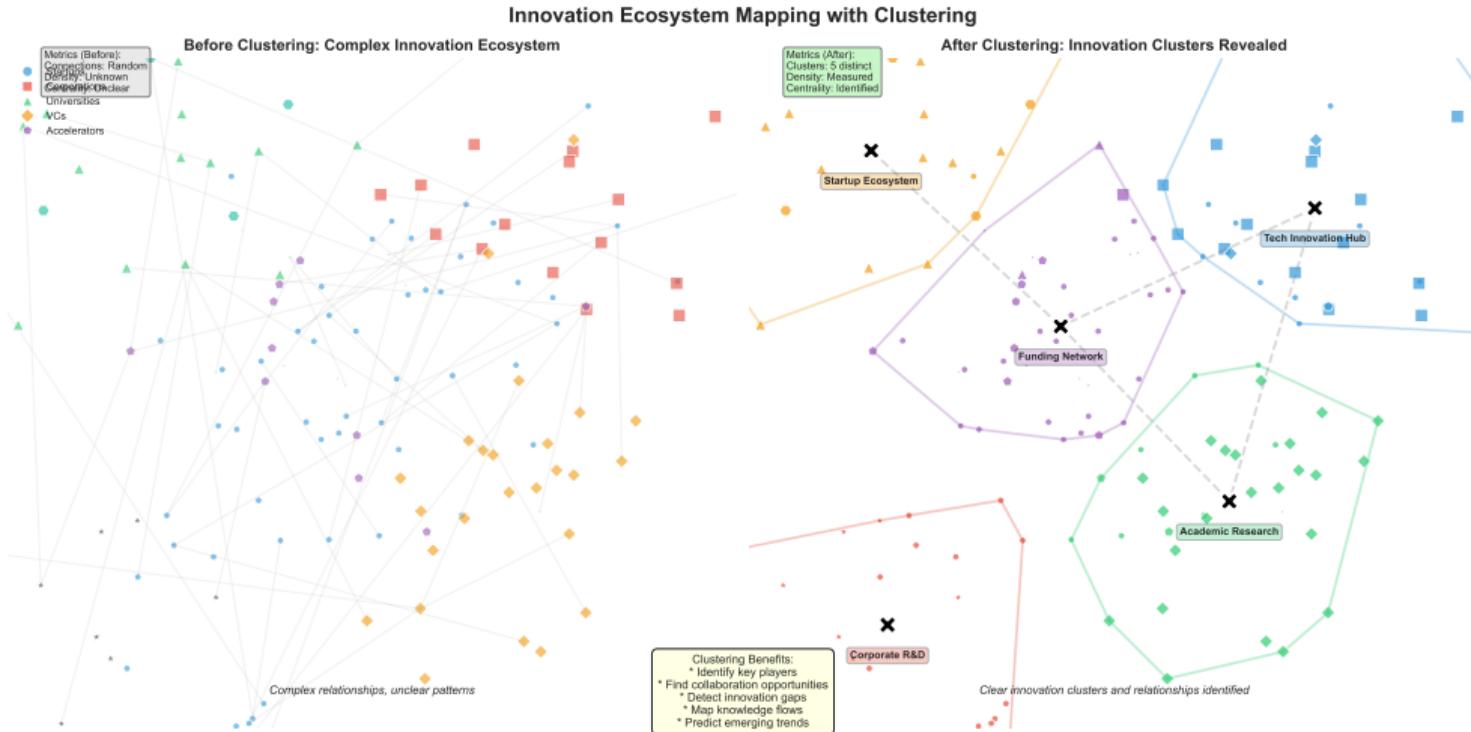
Innovation Lifecycle Stages

How Clustering Reveals Innovation Patterns at Each Stage



Innovation Ecosystem Mapping

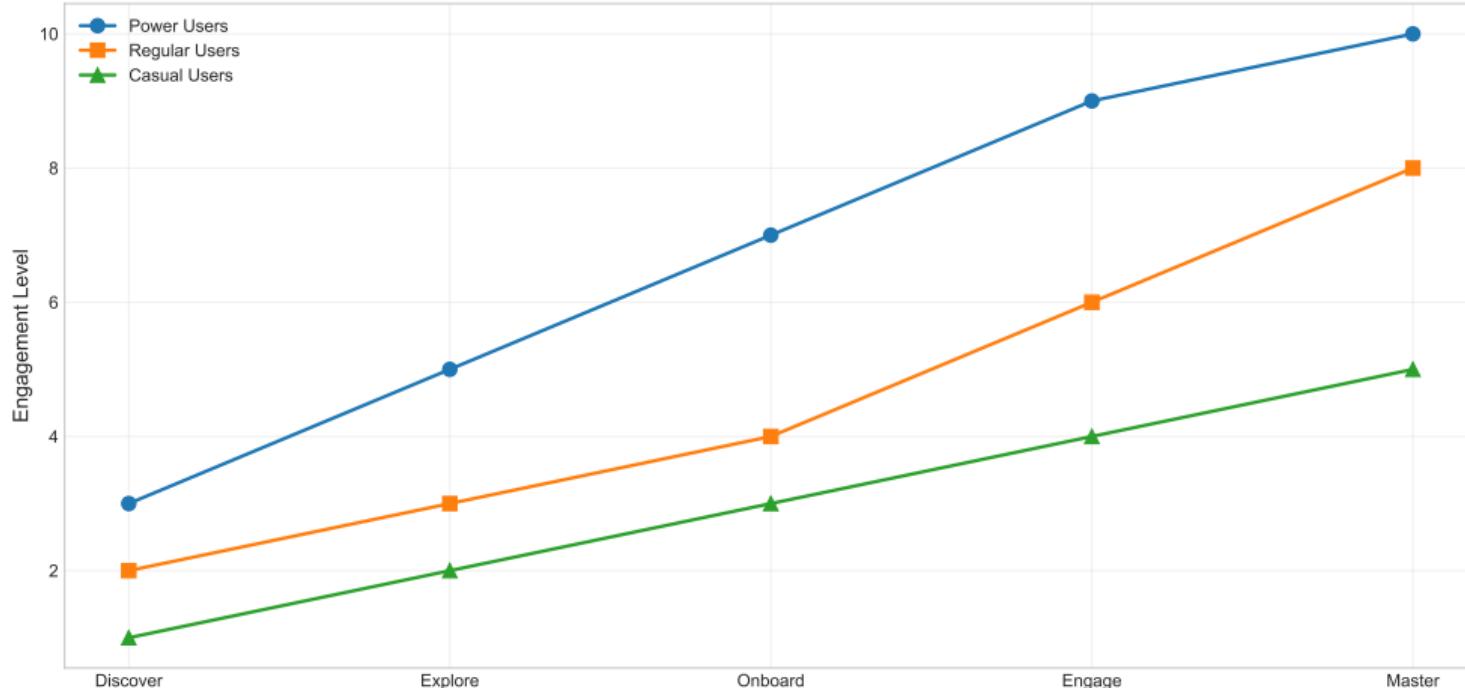
From Complex Networks to Clear Clusters



Different Evolution Paths for Innovation Types

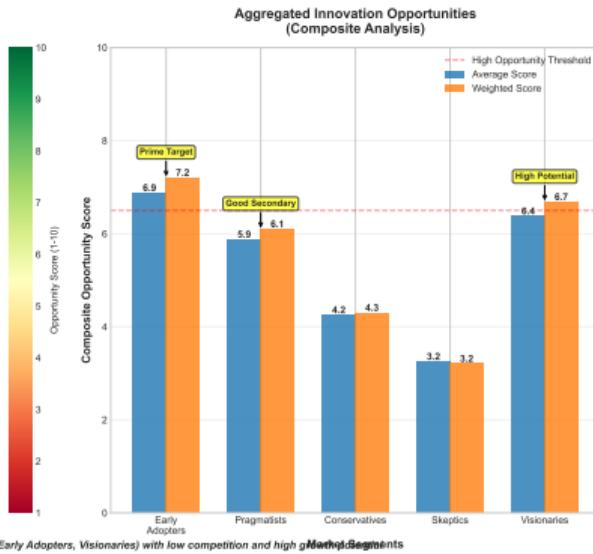
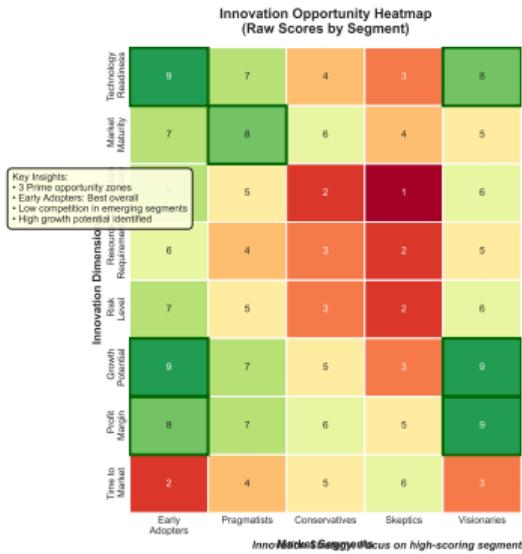
Innovation Lifecycle Patterns

User Journey Maps by Cluster



Innovation Opportunities by Cluster

Where Each Category Has Potential



Key Findings:

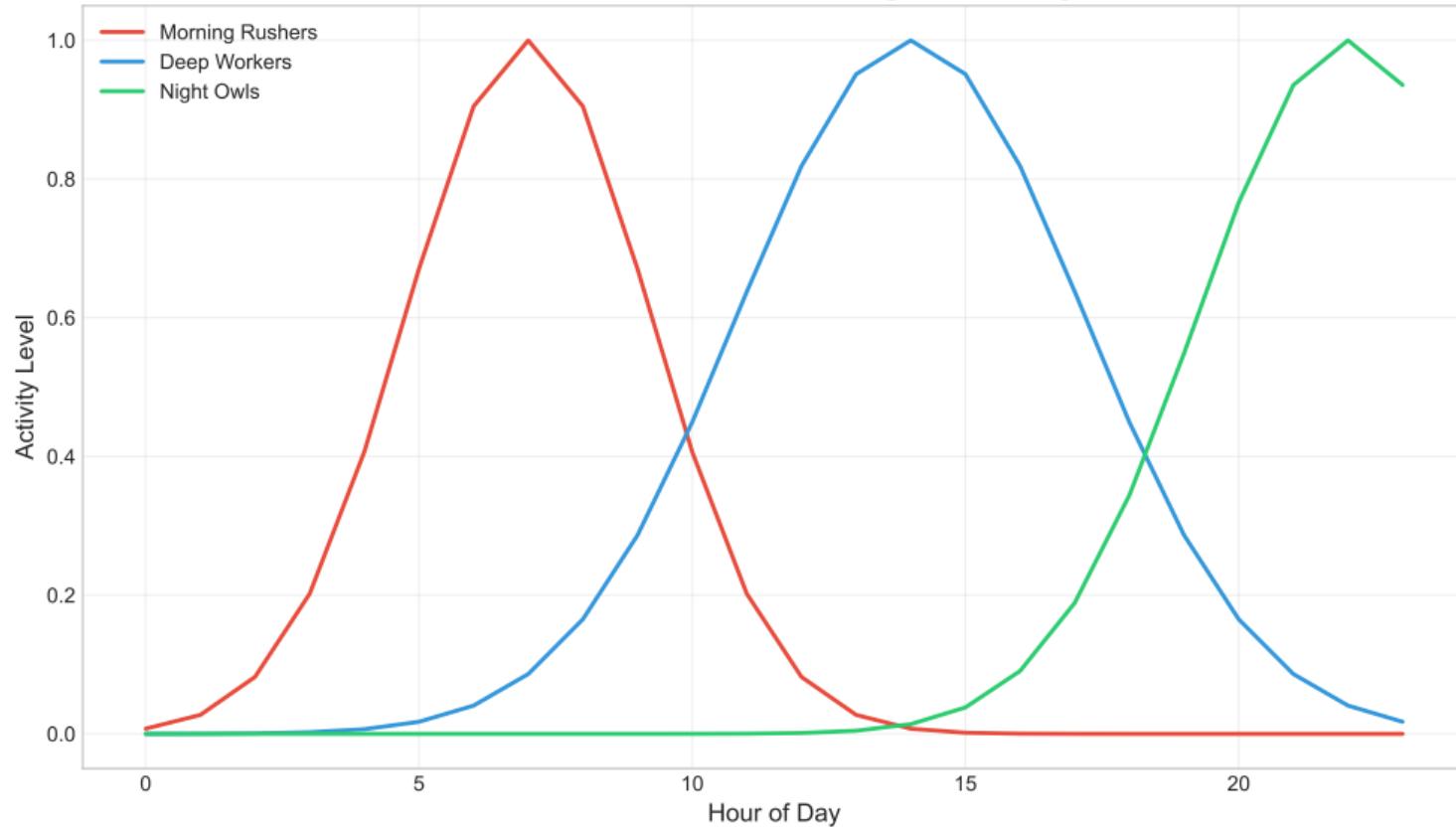
- Emerging tech: Early stage
- Disruptive: Scalability
- Incremental: Integration
- Platform-based: Network effects

Design implication:
One solution won't fit all!

Innovation Patterns Revealed

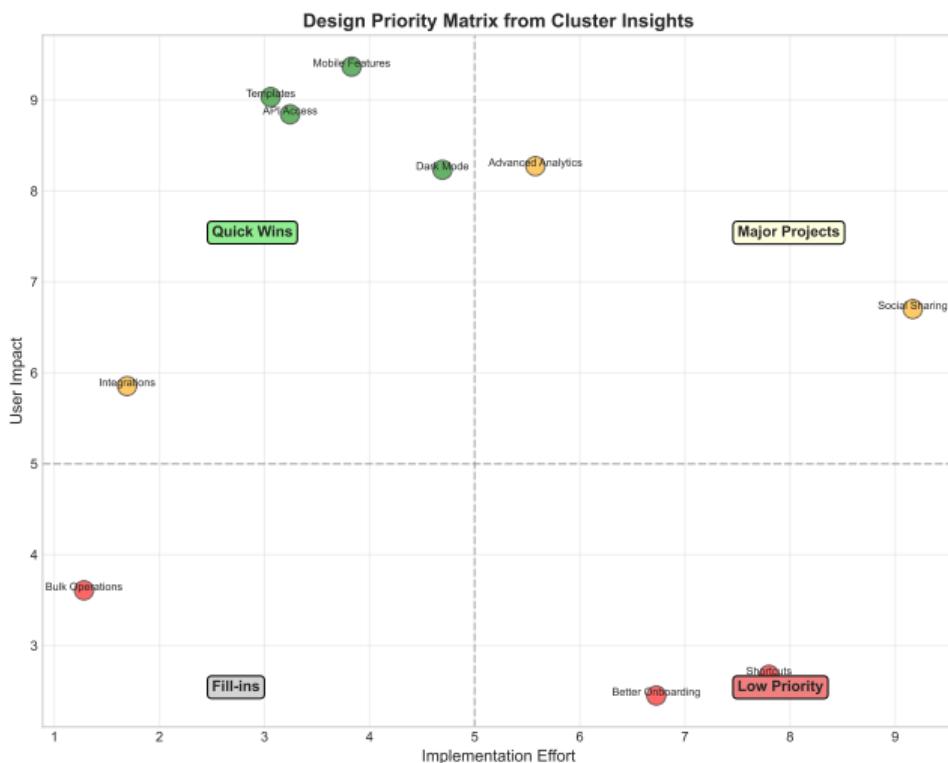
What Clusters Tell Us About Evolution

User Behavior Patterns Throughout the Day



Design Priority Matrix

Where to Focus Your Efforts



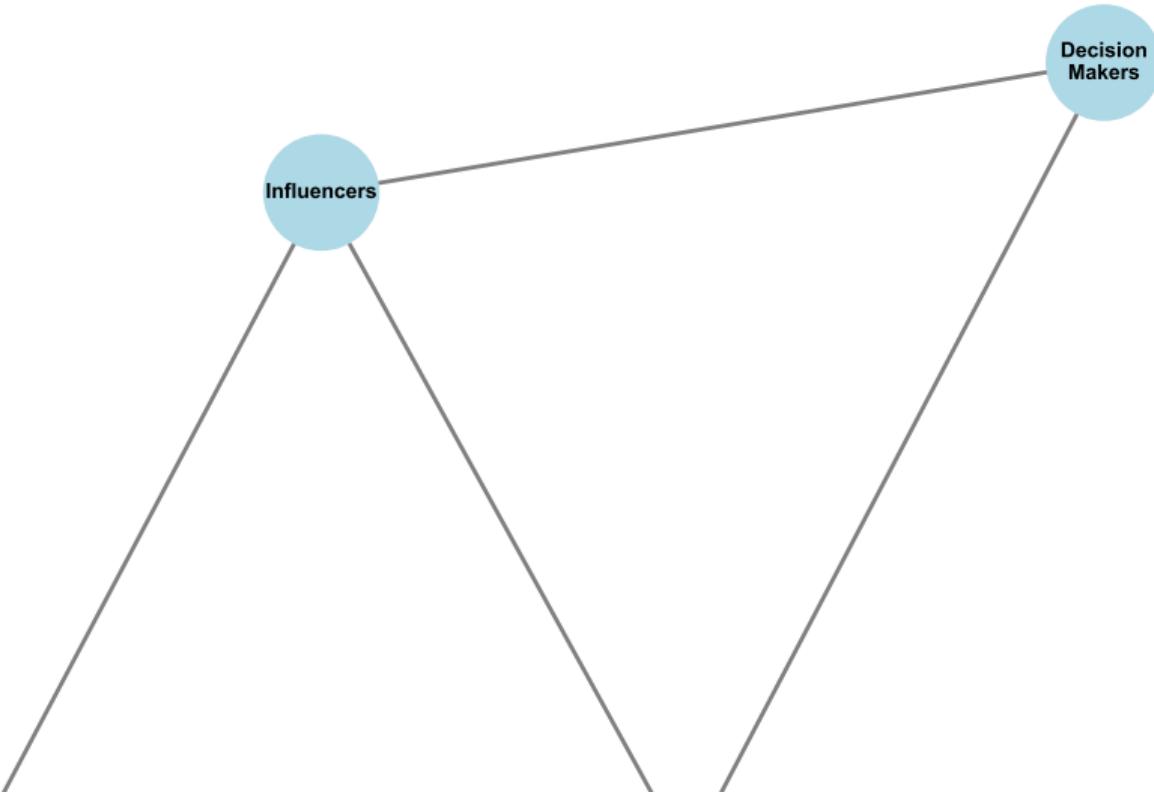
Priority Quadrants:

- **High Impact + High Effort**
Strategic initiatives
- **High Impact + Low Effort**
Quick wins
- **Low Impact + Low Effort**
Fill-ins
- **Low Impact + High Effort**
Avoid

Understanding Innovation Ecosystems

Network Analysis of Innovation Connections

Stakeholder Network from Cluster Analysis



Putting It All Together

From Theory to Practice

You've learned:

- The clustering algorithms
- How to validate quality
- Design applications

Now let's see it in action

How these techniques work in practice
to find patterns in data

PART 4

Summary & Practice

What we'll do:

- See real-world success patterns
- Consolidate key learnings
- Practice with exercises
- Preview next week
- Explore resources

From learning to doing

How Clustering is Used

Common Applications and Results



Common Applications:

- Innovation portfolio management
- Technology trend clustering
- Opportunity space mapping
- Anomaly detection

Typical Results:

- Engagement: +35-45%
- Retention: +20-30%
- Conversion: +15-25%
- Processing time: -60%

Key Takeaways

What We've Learned

Technical Skills

- K-means clustering algorithm
- Choosing optimal K with elbow method
- Silhouette scores for validation
- DBSCAN for complex shapes
- Hierarchical clustering

Design Applications

- Data-driven innovation archetypes
- Segment-specific journeys
- Opportunity identification
- Priority matrices
- Scaled innovation analysis

Clustering transforms data into actionable innovation insights

Implementation Checklist

Ensuring Successful Clustering Projects

Data Preparation

- Collect relevant features
- Handle missing values
- Standardize/normalize data
- Remove outliers if needed
- Feature engineering complete
- Data quality verified

Quality Assurance

- Silhouette score > 0.5
- Cluster sizes balanced
- Visual inspection done
- Stability tested
- Business sense verified
- Edge cases handled

Algorithm Selection

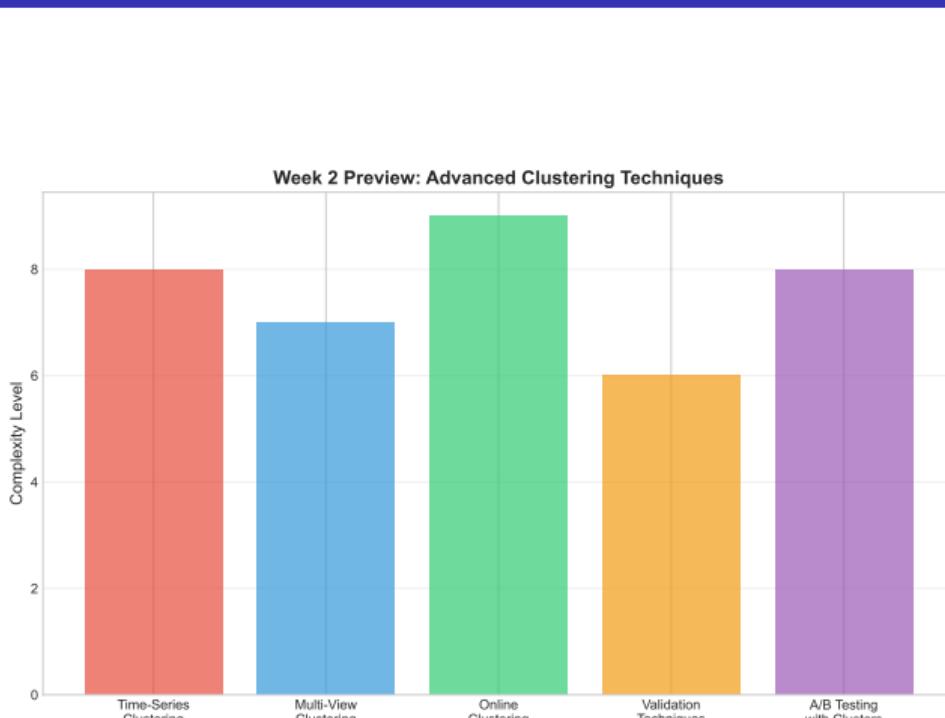
- Choose distance metric
- Select clustering method
- Determine optimal K
- Validate with metrics

Common Pitfalls

- Forgetting to scale features
- Wrong distance metric
- Forcing unnatural K
- Ignoring outliers

Next Week: Advanced Clustering

Going Deeper into Innovation Patterns



Week 2 Topics:

- Density-based clustering
- Gaussian mixture models
- Clustering validation
- Feature engineering
- Real-time clustering

Design Focus:

- Dynamic innovation tracking
- Evolving innovation landscapes
- Predictive opportunity analysis
- Micro-innovation detection

Resources & Further Reading

Deepen Your Understanding

Technical Resources

Papers:

- MacQueen, J. (1967). K-means
- Ester et al. (1996). DBSCAN
- Rousseeuw (1987). Silhouettes

Tools:

- scikit-learn clustering
- Orange data mining
- KNIME analytics

Design Resources

Books:

- "Design Thinking" - Tim Brown
- "Sprint" - Jake Knapp
- "Lean UX" - Jeff Gothelf

Applications:

- Miro (journey mapping)
- Figma (archetype creation)
- Optimal Workshop

Questions? Let's discuss!

Glossary of Technical Terms

Key Concepts Quick Reference

Clustering Algorithms:

- **K-Means:** Partitions data into K predefined clusters
- **DBSCAN:** Density-based spatial clustering
- **Hierarchical:** Builds cluster tree (dendrogram)
- **GMM:** Gaussian Mixture Models, soft clustering

Key Parameters:

- **K:** Number of clusters
- **eps:** Neighborhood radius (DBSCAN)
- **min_samples:** Minimum points for density
- **n_init:** Number of random initializations

Evaluation Metrics:

- **Silhouette:** Cluster cohesion vs separation [-1,1]
- **Inertia:** Sum of squared distances to centroids
- **Davies-Bouldin:** Ratio of within to between distances
- **Calinski-Harabasz:** Ratio of dispersions

Innovation Terms:

- **Empathy Mapping:** Understanding user perspectives
- **Pain Points:** User problems/frustrations
- **User Archetypes:** Representative user groups
- **Innovation Ecosystem:** Connected stakeholders

Implementation Checklist

Your Step-by-Step Guide to Success

Data Preparation:

- Collect innovation feedback data
- Clean and remove duplicates
- Handle missing values
- Normalize/standardize features
- Create feature vectors

Algorithm Selection:

- Analyze data distribution
- Choose appropriate algorithm
- Set initial parameters
- Prepare validation strategy

Implementation:

- Run clustering algorithm
- Calculate evaluation metrics
- Visualize results (PCA/t-SNE)
- Validate with domain experts
- Iterate and refine

Innovation Application:

- Map clusters to user personas
- Identify innovation opportunities
- Create targeted solutions
- Design prototype features
- Test with user groups

Ready? Start with data preparation and work your way down!

Appendix: K-Means Mathematics (Optional)

The Mathematical Foundation - For Those Interested

What K-means tries to minimize:

$$J = \sum_{i=1}^n \sum_{j=1}^k w_{ij} \|x_i - \mu_j\|^2$$

In simple terms: Make points close to their group centers

Where:

- n = number of data points
- k = number of clusters
- $w_{ij} = 1$ if x_i belongs to cluster j , 0 otherwise
- μ_j = centroid of cluster j

Update Rules:

① Assignment: $c^{(i)} = \arg \min_j \|x^{(i)} - \mu_j\|^2$

② Update: $\mu_j = \frac{1}{|S_j|} \sum_{i \in S_j} x^{(i)}$

Appendix: Distance Metrics (Optional)

Different Ways to Measure "How Far Apart" Things Are

Euclidean Distance:

$$d(x, y) = \sqrt{\sum_{i=1}^n (x_i - y_i)^2}$$

Manhattan Distance:

$$d(x, y) = \sum_{i=1}^n |x_i - y_i|$$

Minkowski Distance:

$$d(x, y) = \left(\sum_{i=1}^n |x_i - y_i|^p \right)^{1/p}$$

Cosine Similarity:

$$\cos(\theta) = \frac{x \cdot y}{\|x\| \cdot \|y\|}$$

Jaccard Distance:

$$J(A, B) = 1 - \frac{|A \cap B|}{|A \cup B|}$$

Mahalanobis Distance:

$$d(x, y) = \sqrt{(x - y)^T S^{-1} (x - y)}$$

Appendix: Silhouette Score Explained

How We Know If Groups Are Good

Silhouette Score for point i :

$$s(i) = \frac{b(i) - a(i)}{\max\{a(i), b(i)\}}$$

Where:

- $a(i)$ = average distance to points in same cluster
- $b(i)$ = average distance to points in nearest neighbor cluster

Interpretation:

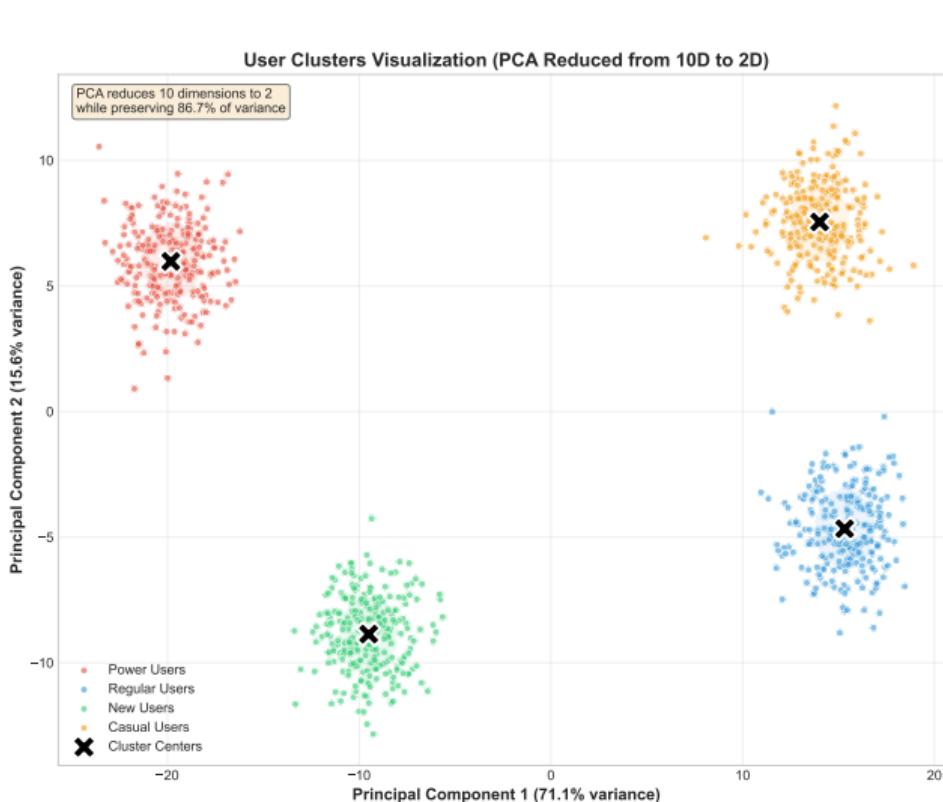
- $s(i) \approx 1$: Well clustered
- $s(i) \approx 0$: On border between clusters
- $s(i) \approx -1$: Misclassified

Overall Score:

$$S = \frac{1}{n} \sum_{i=1}^n s(i)$$

Appendix: Visualizing High-Dimensional Data

Making Complex Data Viewable in 2D



PCA Process:

- ① Standardize data
- ② Compute covariance matrix
- ③ Find eigenvectors/values
- ④ Select top 2 components
- ⑤ Transform data

Variance Explained:

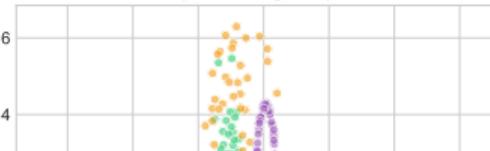
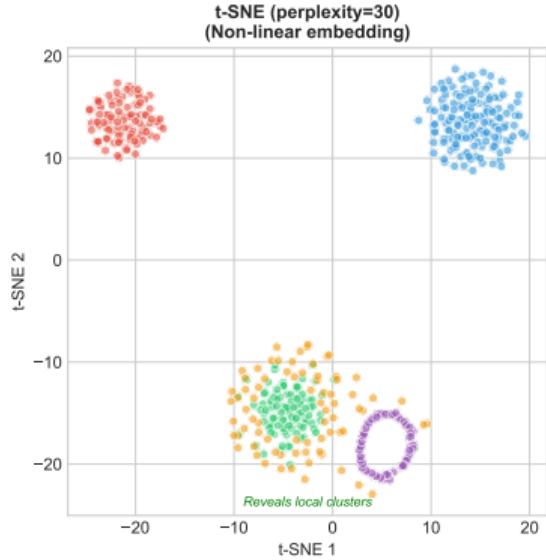
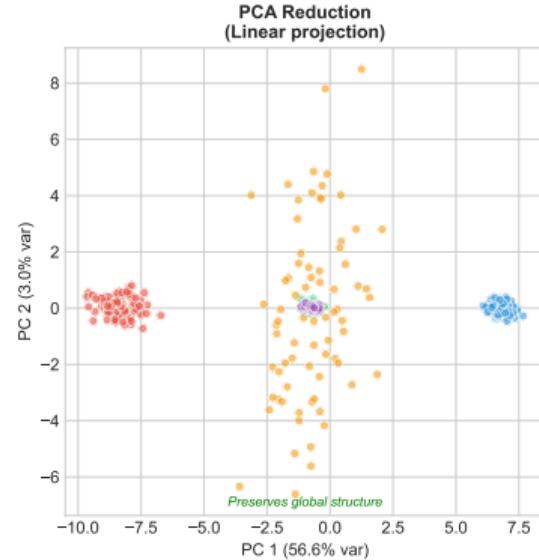
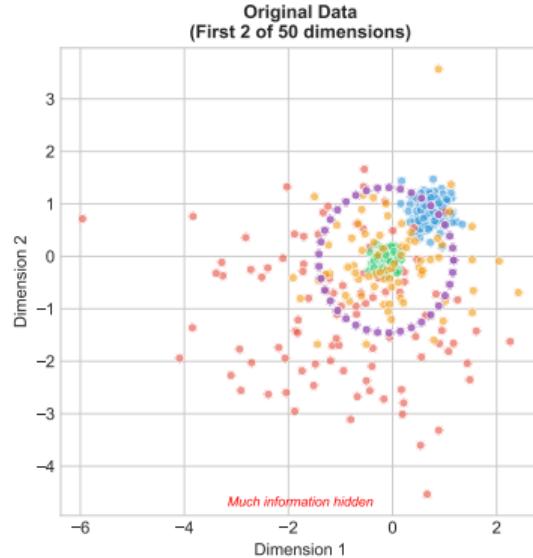
- PC1: 45.2%
- PC2: 28.7%
- Total: 73.9%

Dimensionality Reduction: PCA vs t-SNE

Revealing Hidden Patterns in High-Dimensional Innovation Space

Dimensionality Reduction: PCA vs t-SNE for Innovation Data

Revealing Hidden Patterns in High-Dimensional Innovation Space



Method Comparison

	PCA	t-SNE
Speed	Fast	Slow
Scalability	Excellent	Limited

Appendix: How DBSCAN Works

Finding Groups Based on How Close Points Are

Key Parameters:

- ϵ (eps): Maximum distance between points
- MinPts: Minimum points to form dense region

Point Classification:

- **Core point:** Has \geq MinPts within ϵ
- **Border point:** Within ϵ of core point
- **Noise point:** Neither core nor border

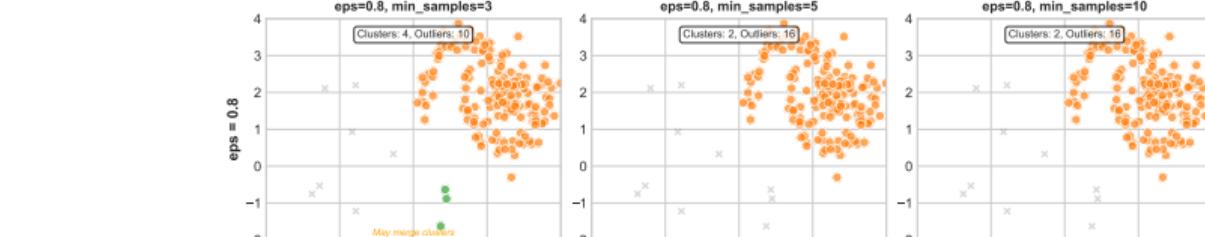
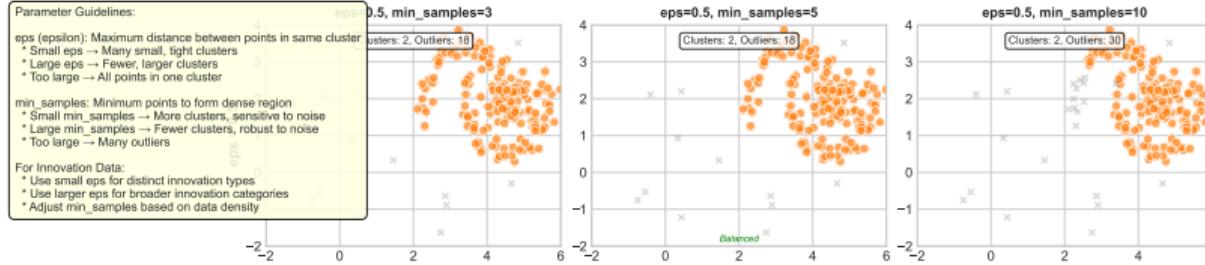
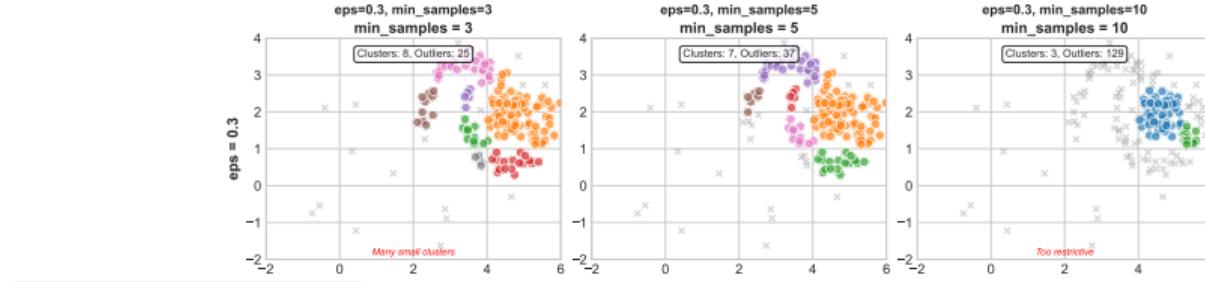
Algorithm Steps:

- ① Find all core points
- ② Form clusters from core points within ϵ
- ③ Assign border points to clusters
- ④ Mark remaining as noise

DBSCAN Parameter Tuning

Impact of eps and min_samples on Clustering Results

DBSCAN Parameter Tuning: Impact on Innovation Clustering



- Tuning Strategy:
- Start with k-distance plot
 - Look for 'elbow' in plot
 - Set eps at elbow point
 - min_samples = 2^d dimensions
 - Validate with domain knowledge

Appendix: Python Implementation

Ready-to-Use Code Snippets

K-Means Example:

```
from sklearn.cluster import KMeans
import numpy as np

# Generate data
X = np.random.randn(1000, 2)

# Fit K-means
kmeans = KMeans(n_clusters=3,
                 random_state=42)
labels = kmeans.fit_predict(X)

# Get centroids
centroids = kmeans.cluster_centers_
```

DBSCAN Example:

```
from sklearn.cluster import DBSCAN

# Fit DBSCAN
dbscan = DBSCAN(eps=0.3,
                 min_samples=5)
labels = dbscan.fit_predict(X)

# Identify outliers
outliers = labels == -1
n_clusters = len(set(labels)) - 1

print(f"Clusters: {n_clusters}")
print(f"Outliers: {sum(outliers)}")
```

Appendix: Implementation Guidelines

Practical Considerations

Data Preparation

- Standardize features
- Handle missing values
- Remove outliers (if needed)
- Feature selection/engineering
- Consider scaling methods

Validation Methods

- Silhouette score
- Davies-Bouldin index
- Calinski-Harabasz score
- Visual inspection
- Domain expert review

Algorithm Selection

- K-means: Spherical, similar size
- DBSCAN: Arbitrary shapes
- Hierarchical: Nested structure
- GMM: Overlapping clusters

Common Pitfalls

- Not scaling features
- Wrong distance metric
- Ignoring outliers
- Over-clustering
- Forcing clusters

Glossary of Technical Terms

Key Concepts Reference

Algorithms:

- **K-means:** Partitions data into K spherical clusters
- **DBSCAN:** Density-based clustering for arbitrary shapes
- **GMM:** Gaussian Mixture Models for soft clustering
- **Hierarchical:** Tree-based clustering approach

Metrics:

- **Silhouette:** Measures cluster separation (-1 to 1)
- **Inertia:** Sum of squared distances to centroids
- **Davies-Bouldin:** Ratio of within to between cluster distance

Concepts:

- **Centroid:** Center point of a cluster
- **Elbow Method:** Technique to find optimal K
- **Outlier:** Data point not belonging to any cluster
- **Convergence:** When algorithm stops improving

Preprocessing:

- **Standardization:** Zero mean, unit variance
- **Normalization:** Scale to [0,1] range
- **PCA:** Principal Component Analysis
- **t-SNE:** t-distributed Stochastic Neighbor Embedding