

# L02: Logistic Regression

## Classification with Probability Estimates

Methods and Algorithms

Spring 2026

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- 6 Summary

**By the end of this lecture, you will be able to:**

1. Explain how logistic regression models binary outcomes
2. Derive the maximum likelihood estimation for logistic regression
3. Interpret classification metrics (precision, recall, AUC)
4. Apply logistic regression for credit scoring decisions

**Finance Application:** Credit scoring and probability of default (PD)

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These objectives span Bloom's levels: Understand, Apply, Analyze

# Why Logistic Regression?

## The Business Problem

- Banks must decide: approve or reject loan applications
- Need probability of default, not just yes/no prediction
- Regulatory requirement: interpretable, auditable models

## Why Not Linear Regression?

- Linear regression can predict values outside  $[0,1]$
- Binary outcomes need probability-based approach
- Logistic regression outputs calibrated probabilities

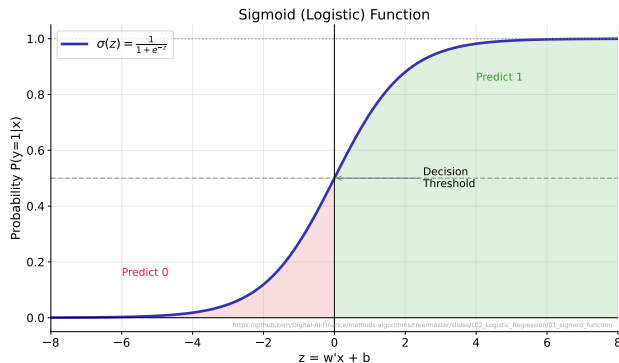
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Logistic regression: the industry standard for credit scoring since 1980s

# The Sigmoid Function

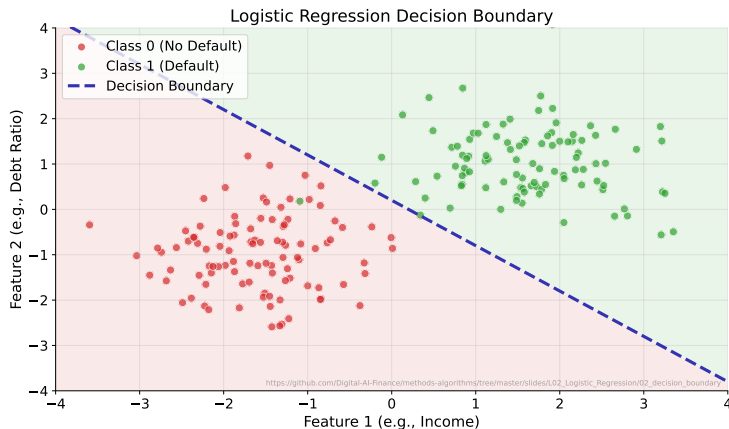
## From Linear to Probability

- Maps any real number to (0, 1) range
- Smooth, differentiable, interpretable



$\sigma(z) = 1/(1 + e^{-z})$  transforms linear combination to probability

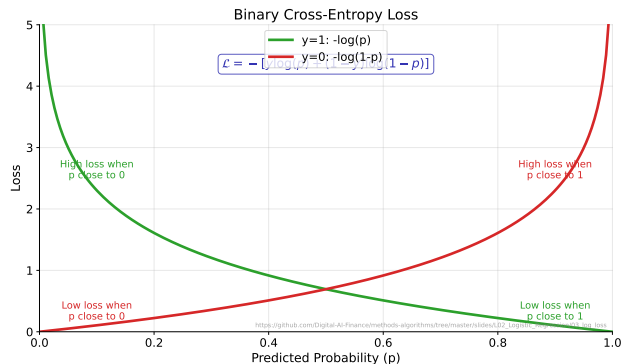
# Decision Boundary



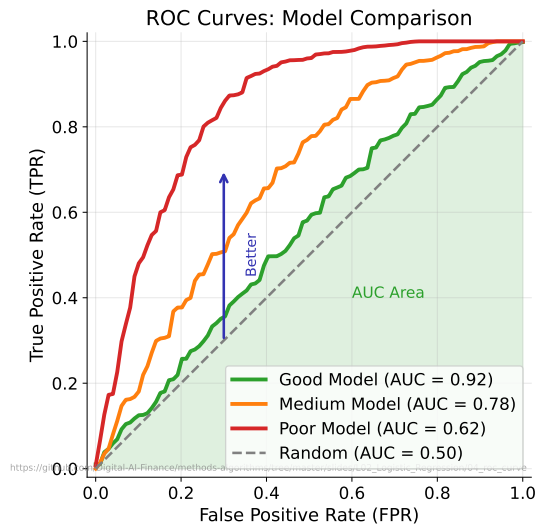
The decision boundary is where  $P(y = 1|x) = 0.5$ , i.e.,  $w'x + b = 0$

## Why Not MSE?

- MSE with sigmoid creates non-convex loss landscape
- Cross-entropy is convex, guarantees global optimum



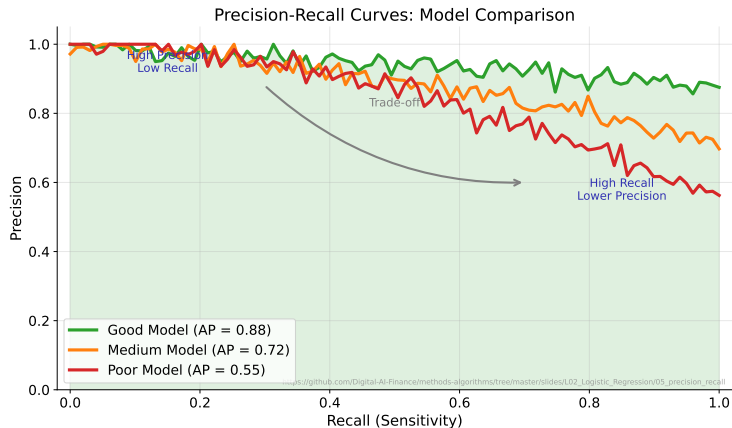
Heavily penalizes confident wrong predictions



AUC = probability random positive ranks higher than random negative



# Precision-Recall Trade-off



Use PR curve when classes are imbalanced (common in fraud detection)

# Confusion Matrix: Reading the Results

Confusion Matrix: Credit Default Prediction

Actual Label	Predicted Label	
	Predicted: No Default	Predicted: Default
Actual: No Default	<b>TN</b> (True Negative) 850	<b>FP</b> (False Positive) 50
Actual: Default	<b>FN</b> (False Negative) 30	<b>TP</b> (True Positive) 70

Accuracy: 92.0%  
Precision: 58.3%  
Recall: 70.0%  
F1 Score: 0.64

[https://github.com/Digital-AI-Finance/methods-algorithms/tree/master/slides/L02\\_Logistic\\_Regression/06\\_confusion\\_matrix](https://github.com/Digital-AI-Finance/methods-algorithms/tree/master/slides/L02_Logistic_Regression/06_confusion_matrix)

**FP = approve bad loans (costly), FN = reject good customers (lost revenue)**

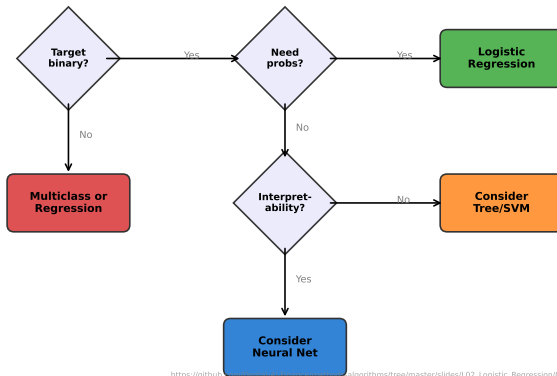
## Open the Colab Notebook

- Exercise 1: Implement logistic regression from scratch
- Exercise 2: Train model on credit scoring data
- Exercise 3: Evaluate with ROC curve and confusion matrix

**Link:** See course materials on GitHub

# When to Use Logistic Regression

## Logistic Regression Decision Guide



[https://github.com/DataCamp/algorithms/tree/master/slides/L02\\_Logistic\\_Regression/07\\_decision\\_flowchart](https://github.com/DataCamp/algorithms/tree/master/slides/L02_Logistic_Regression/07_decision_flowchart)

**Key strengths: interpretable coefficients, probability outputs, fast training**

# References

- James et al. (2021). *Introduction to Statistical Learning*. <https://www.statlearning.com/>
- Hastie et al. (2009). *Elements of Statistical Learning*. <https://hastie.su.domains/ElemStatLearn/>