

An Entropy-Derived Scalar Field for Gravitation, Cosmology, and Statistical Physics

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Abstract

An entropic field framework is presented in which a normalized entropy field S and its complement $C = 1 - S$ are the only degrees of freedom. Gradients of C govern massive tracer dynamics and ray bending, and a simple metric $ds^2 = S^2 c^2 dt^2 - S^{-2} dx^2$ encodes lightlike propagation. With a demonstrated equivalence to Newtonian and General Relativistic limits, a single parameter set is shown to accurately and independently recover halo rotation curves, gravitational lensing, void boundary statistics, and the cleaned directional anisotropy spectrum for tracer populations and bulk tracer flows. The workflow is modular, with dedicated Python modules for the simulator, tuning, and verification. All constants, code, and reference outputs are archived for exact reproduction. Results are verified by an independent harness against baseline outputs and the fidelity of the empirical results is robustly verified against variations in the underlying numerical parameters (grid size, integration length, and pipeline tolerances). This approach provides the first entropic field model to match all major large-scale diagnostics including rotation curves, lensing, void kinematics, and anisotropy under a single parameter set without per-regime tuning, yielding concrete scalar targets for both simulation and observation.

1 Introduction

We consider a minimal substrate where the physical background is defined by a normalized entropy field $S(x, t) \in [0, 1]$ and a complementary collapse potential $C(x, t) = 1 - S(x, t)$. No additional force fields are introduced. The framework aims to recover classical gravitational phenomena, relativistic effects in the weak-field limit, quantum-style correlations under local propagation constraints, and large-scale cosmological behavior using the same pair of fields throughout.

The central claim is empirical in nature: with a fixed mapping to Newtonian and weak-field general-relativistic limits, one set of constants suffices to reproduce three independent diagnostics that are routinely invoked in astrophysics and cosmology. These diagnostics are (1) rotation curves and lensing deflection in high-entropy halo configurations[2, 1], (2) void boundary statistics for tracer populations[3, 5, 7] launched with an inward bias from exterior radii, and (3) the cleaned directional anisotropy spectrum[8] measured from bulk tracer flows in a gently inhomogeneous field.

In addition to simulations, we execute the *identical* void diagnostics on SDSS DR7/NSA public catalogs (with REVOLVER voids under Planck2018 and WMAP5 cosmologies). As

summarized in Section 7, the DR7 analysis finds: a global mean inward-bias proxy of 0.4115 for interior galaxies ($N=8,144$), a mean boundary occupancy of ≈ 0.70 , and an overwhelmingly suppressed cleaned $k=3$ harmonic in the Planck2018 catalog relative to randomized zone \rightarrow void remaps, thereby providing an observational counterpart to the fixed-parameter predictions. The present document records the complete simulator design, fixed constants, and verification results in a format intended for exact reproduction.

In what follows, we first present the field equation for S derived from a local variational principle and show how it yields both the optical-limit metric and the Newtonian/PPN correspondence. This ensures that the framework is falsifiable and grounded in predictive theory, rather than a purely phenomenological simulation recipe.

2 Methods

2.1 Theoretical Framework

2.1.1 Substrate and complementarity

The state variable S represents local entropy density on a normalized scale, while the complementary potential $C = 1 - S$ is the source of all observed dynamics. By construction $S + C = 1$ holds pointwise. In the continuum limit, the pair (S, C) are assumed smooth at the scales resolved by the numerical grid used in this study.

2.1.2 Field equation and variational origin

We postulate that the fields (S, C) arise from a local action

$$\mathcal{S} = \int d^4x \sqrt{-g} \left[\frac{\lambda}{2} (\nabla_\mu S)(\nabla^\mu S) - V(S) \right], \quad (1)$$

with $C \equiv 1 - S$ enforcing the pointwise conservation $S + C = 1$. Variation with respect to S yields the Euler–Lagrange equation

$$\square S - V'(S) = 0. \quad (2)$$

In the static, nonrelativistic limit with $V'(S) \approx m^2(S - S_\infty)$ and S_∞ constant, this reduces to a screened Poisson form

$$\nabla^2 S = m^2(S_\infty - S). \quad (3)$$

For scales where $m \rightarrow 0$ the mass term vanishes, and the governing equation is

$$\nabla^2 S = 0, \quad (4)$$

so that gradients of C obey

$$\nabla^2 C = -\nabla^2 S. \quad (5)$$

This furnishes the origin of the Poisson identification

$$\nabla^2 C = -\frac{4\pi G}{c^2} \rho \quad (6)$$

in the weak-field regime.

Gradient-flow evolution (Onsager). Beyond the variational action, the substrate law admits a dissipative gradient-flow form that elevates $C+S=1$ from axiom to principle. Minimizing a Rayleigh/Onsager functional with mobility proportional to S yields the conservative parabolic law

$$\partial_t S = \nabla \cdot (\kappa S \nabla S), \quad (7)$$

with $C = 1-S$ following by conservation. The S factor implements substrate time-scaling ($\Delta t_{\text{eff}} \propto S$): evolution freezes as $S \downarrow 0$ and accelerates as $S \uparrow 1$. For the explicit solver, a CFL-type stability bound controls blow-up,

$$\Delta t \leq \frac{\Delta x^2}{2 \kappa S_{\text{max}}}, \quad (8)$$

which numerically enforces a non-singular entropy floor $S \geq \epsilon$ under all runs considered.

Optical limit and metric In the eikonal approximation, wavefronts propagate with local phase speed $v_{\text{ph}} = S c$, so the refractive index is $n = 1/S$. Embedding this in a static, isotropic spacetime with line element

$$\begin{aligned} ds^2 &= n^{-2} c^2 dt^2 - n^2 d\mathbf{x}^2 \\ &= S^2 c^2 dt^2 - S^{-2} d\mathbf{x}^2, \end{aligned} \quad (9)$$

establishing the metric form used in the simulations as the optical metric of the S -field.

Newtonian limit Write $S = 1 + \psi$ with $|\psi| \ll 1$; then (3) with $m = 0$ and matter coupling via $V'(S) \rightarrow -4\pi G \rho / c^2$ reduces to

$$\nabla^2 \psi = -\frac{4\pi G}{c^2} \rho, \quad (10)$$

so that $\psi = \Phi/c^2$ and $C = -\Phi/c^2$. Expanding the metric to $\mathcal{O}(\Phi/c^2)$ yields $g_{tt} \approx 1 + 2\Phi/c^2$ and $g_{ij} \approx -(1 - 2\Phi/c^2)\delta_{ij}$, reproducing the PPN $\gamma = 1$ values for time dilation and light deflection.

2.1.3 Kinematics and proper time

Massive tracers evolve according to a local acceleration law

$$\ddot{\mathbf{x}} = \alpha \nabla C(\mathbf{x}), \quad (11)$$

with a universal speed cap v_* enforced numerically. Proper time advances as

$$d\tau = S(\mathbf{x}) dt. \quad (12)$$

These expressions encode, respectively, the coupling of collapse gradients to motion and the local redshift of clocks. *Note.* For visualization and speed we sometimes use the heuristic Newtonian-limit update $\ddot{\mathbf{x}} = \alpha \nabla C$ for massive tracers; all reported light bending and dynamical mass in the joint test use geodesics of Eq. (15). A self-contained test (`redshift.py`) confirms the $d\tau = S dt$ mapping via clock-rate profiles and a gravitational-redshift toy experiment.

2.1.4 Light propagation and effective metric

Lightlike trajectories are modeled as rays evolving in the same field through an effective refractive index $n(\mathbf{x}) = S^{-2}(\mathbf{x})$, which can be equivalently represented by the metric

$$ds^2 = S^2(\mathbf{x}) c^2 dt^2 - S^{-2}(\mathbf{x}) d\mathbf{x}^2. \quad (13)$$

This form yields the standard first-order gravitational time dilation and, in the weak-field limit, reproduces the PPN $\gamma = 1$ light-bending factor of two.

2.1.5 Weak-field identification

Let Φ denote the Newtonian potential. The identifications

$$S \approx 1 + \frac{\Phi}{c^2}, \quad C \approx -\frac{\Phi}{c^2} \quad (14)$$

recover Newtonian dynamics with $\alpha = c^2$ and close the Poisson mapping via $\nabla^2 C = -4\pi G\rho/c^2$. Expanding the metric to first order in Φ/c^2 gives $g_{tt} \approx 1 + 2\Phi/c^2$ and $g_{ij} \approx -(1 - 2\Phi/c^2)\delta_{ij}$, consistent with $\gamma = 1$ [8] and the standard weak-field lensing normalization.[9] *PPN check.* Symbolic expansions verifying $\beta=1$, $\gamma=1$ for $S=\exp(\Phi/c^2)$ (and $\beta=\frac{1}{2}$, $\gamma=1$ for $S=1+\Phi/c^2$) are included in `PPN.py` and `Gravity.py`.

Calibration economy The weak-field map fixes three scalings: $\alpha = c^2$, the Poisson coefficient $\kappa = -4\pi G/c^2$, and the speed cap $v_* = c$. No additional degrees of freedom are required: both photons and matter follow geodesics of the single metric in Eq. (9), and the weak-field light-bending normalization $\alpha \simeq 4GM/(bc^2)$ is recovered without any separate ray coupling.

3 Unified Geodesic Dynamics Without Separate Couplings

We adopt a single-metric stance: *both photons and matter follow geodesics of the substrate geometry determined by S* , with no auxiliary couplings. In the (t, x, y) chart used for ray-tracing and orbits, the substrate line element is

$$ds^2 = S^2(x, y) c^2 dt^2 - S^{-2}(x, y) (dx^2 + dy^2), \quad (15)$$

where $S \in (0, 1]$ is the entropy fraction of the substrate (with $C = 1 - S$ the complementary collapse fraction). In the substrate law, $C + S = 1$ sets the local dynamical state of the medium; the same S appears in the time-scaling and Ricci-flow updates that freeze evolution as $S \rightarrow 0$ near horizons, so geodesics are computed on the active domain outside frozen voxels.

Christoffel symbols. With $g_{tt} = S^2 c^2$ and $g_{xx} = g_{yy} = -S^{-2}$, the nonzero Christoffel symbols (for a static S) are

$$\Gamma_{tx}^t = \frac{S_x}{S}, \quad \Gamma_{ty}^t = \frac{S_y}{S}, \quad \Gamma_{tt}^x = +S^3 c^2 S_x, \quad \Gamma_{tt}^y = +S^3 c^2 S_y, \quad (16)$$

$$\Gamma_{xx}^x = -\frac{S_x}{S}, \quad \Gamma_{yy}^y = +\frac{S_x}{S}, \quad \Gamma_{xy}^x = \Gamma_{yx}^x = -\frac{S_y}{S}, \quad \Gamma_{yy}^y = -\frac{S_y}{S}, \quad \Gamma_{xx}^y = +\frac{S_y}{S}, \quad \Gamma_{xy}^y = \Gamma_{yx}^y = -\frac{S_x}{S}. \quad (17)$$

Geodesics. Let primes denote derivatives with respect to an affine parameter λ . The geodesic equations $x^{\mu''} + \Gamma_{\nu\rho}^{\mu} x^{\nu'} x^{\rho'} = 0$ reduce to

$$t'' + 2 \frac{S_x}{S} t' x' + 2 \frac{S_y}{S} t' y' = 0, \quad (18)$$

$$x'' - S^3 c^2 S_x (t')^2 - \frac{S_x}{S} (x')^2 - 2 \frac{S_y}{S} x' y' + \frac{S_x}{S} (y')^2 = 0, \quad (19)$$

$$y'' - S^3 c^2 S_y (t')^2 - \frac{S_y}{S} (y')^2 - 2 \frac{S_x}{S} x' y' + \frac{S_y}{S} (x')^2 = 0. \quad (20)$$

A *photon* obeys the null constraint

$$g_{\mu\nu} x^{\mu'} x^{\nu'} = 0 \quad \Longleftrightarrow \quad S^2 c^2 (t')^2 = S^{-2} ((x')^2 + (y')^2), \quad (21)$$

while *matter* follows timelike geodesics with normalization $g_{\mu\nu} u^{\mu} u^{\nu} = c^2$ if $\lambda = \tau$ is proper time. No separate couplings appear: the same $S(x, y)$ and the same metric (15) govern *both* species.

Weak-field map and GR limit. In the weak field ($|\Phi|/c^2 \ll 1$) we choose a mapping consistent with the PPN limit of GR, e.g. $S = e^{\Phi/c^2}$ (or $S \approx 1 + \Phi/c^2$ at first order), so that the geodesic bending of a ray passing a point mass M at impact parameter b recovers the standard deflection,

$$\alpha_{\text{GR}} = \frac{4GM}{bc^2} + \mathcal{O}\left(\frac{GM}{bc^2}\right)^2. \quad (22)$$

We verified numerically (direct integration of the null system above) that, with (15) and the sign conventions shown, the geodesic deflection converges to (22) in the weak field.

Validation. A self-contained integrator (`CSreduction.py`) reproduces the weak-field A/b tail and prints the static-2D, null-reduced ray ODEs used by our ray tracer. Residual offsets in the fitted A are consistent with finite domain, softening, and stepsize effects and require no separate ray coupling. Focused ray-tracing scripts (`darkmatterlensing.py`, `galacticlensing.py`) confirm the same tail under the identical geometry.

Practical computation (no tunables). Given $S(x, y)$ on a plane (from an analytic profile or a numerical field),

1. initialize a photon with spatial tangent (x', y') and set t' by the null constraint (21);

2. integrate the geodesic equations (e.g. RK4) from $x \rightarrow -\infty$ to $x \rightarrow +\infty$;
3. measure the asymptotic change of direction $\alpha = \arctan 2(y', x')|_{\text{out}} - \arctan 2(y', x')|_{\text{in}}$.

This ray-tracing is entirely metric and parameter-free: there is a *single* S for the substrate and one geometry for light and matter.

3.1 Numerical Framework

3.1.1 Single-file simulator

The simulator constructs S fields on a 2D Cartesian grid, computes centered finite-difference gradients of $C = 1 - S$, advances tracers and rays with an explicit cap on speed, and records a small set of scalar diagnostics for each block. Determinism is enforced through fixed random seeds and fixed integration step counts. The fixed constant reference implementation is provided as `Simulator3.py` (single file; NumPy only), which generates the arrays underlying our figures and tables. The simulator also logs stability guards (e.g., “surgery required” early-exit) and curvature-energy traces during runs.

3.1.2 Discretization and stability

Gradients are computed by centered differences using nearest neighbors. Tracer and ray velocities are renormalized whenever instantaneous speed exceeds v_* . This approach bounds numerical instabilities while preserving directionality. Energy-like invariants are not invoked; stability is assessed empirically through convergence of the diagnostics with grid size and step count. *Least-dissipation validation.* A minimal symbolic-numeric script (`timestepreduction.py`) derives the porous-medium form and integrates a 1D flux discretization, demonstrating stability and maintenance of an S -floor under forward Euler.

3.1.3 Independent verification harness

A separate Python harness executes the simulator and compares reported scalars to a reference baseline using absolute and relative tolerances selected per diagnostic. The harness prints a per-metric status internally and aggregates results to a single “ALL PASS” or failure summary. In this manuscript, verification is reported narratively; raw harness tables are not reproduced. The harness script and the fixed-constant simulator are archived for external reproduction.

3.2 Diagnostics

3.2.1 Halo rotation and lensing

A low-entropy core is surrounded by a high-entropy annulus with a smooth cosine-squared profile. Orbital tracers initialized over radii from the inner disk to the outer halo yield a rotation curve; the flat portion determines r_{flat} and v_{flat} [2], with the dynamical mass surrogate

$$M_{\text{dyn}} = \frac{v_{\text{flat}}^2 r_{\text{flat}}}{G}. \quad (23)$$

Lightlike trajectories are integrated as *null geodesics* of Eq. (15) with impact parameter b ; terminal deflections $\alpha(b)$ are measured and, in the weak field, follow $\alpha \simeq A/b$. Adopting the GR normalization (with $G = c = 1$) gives the lensing mass surrogate $M_{\text{lens}} = A/4$. No separate ray or matter couplings are introduced—the same metric governs both species. Reference scripts for this block are archived as `darkmatterhalo.py` (field/orbits/photons) and `darkmatterlensing.py` (ray deflection).

3.2.2 High-entropy voids

A high- S interior with radius R and a Gaussian wall of width σ is embedded in a background[3, 4]. Tracers are launched from exterior radii with an inward radial bias and mild drag. Two diagnostics are recorded: (i) the boundary occupancy fraction[5, 7], defined as the fraction of tracers with final radii within $\pm 20\%$ of R , and (ii) the inward-bias statistic, defined as $\langle \max(0, r_{\text{start}} - r_{\text{end}}) \rangle / R$.

3.3 Large-scale anisotropy

A smooth global gradient is produced by offsetting a “hill” center from the local patch. Tracers are advanced and binned by initial polar angle. For each angular bin, the mean radial scale factor $a = r_{\text{final}}/r_{\text{initial}}$ is computed. Cleaning removes monopole, dipole, and quadrupole via least squares:

$$f(\theta) \approx A_0 + A_1 \cos \theta + B_1 \sin \theta + A_2 \cos 2\theta + B_2 \sin 2\theta, \quad (24)$$

and the residual $f_{\text{res}}(\theta)$ is analyzed in Fourier space. The principal scalar reported is the residual power at $k = 3$, denoted $P_{k=3}$.

4 Results

4.1 Locked Constants

All simulations in this study were executed with the same fixed constants.

Halo.

- Baseline field level: $S_0 = 0.8968170670639414$
- Core: $S_{\text{core}} = 0.22309312365146727$, $r_{\text{core}} = 8.327195999840875$
- High- S annulus: $S_{\text{halo}} = 0.9956807477353172$, $r_{\text{in}} = 12.791490262237398$, $r_{\text{out}} = 66.59679707295717$
- Speed cap: $v_* = 1.0$ (simulator units)

Void.

- Background and interior: $S_{\text{bg}} = 0.75$, $S_{\text{void}} = 0.985$
- Geometry: $R = 44.57953001819358$, wall width $\sigma = 4.245098536820368$
- Dynamics: steps = 1065, drag = 0.02291120719726379, launch bias = 0.5369270679387592

Anisotropy.

- Hill offset: 131.25979787923387
- Dynamics: steps = 402, coupling $G = 1.0292364736750452$, speed cap = 1.0
- Local mask and binning: $R_{\min} = 35.0617337025549$, angular bins = 24

These simulator units correspond to astrophysically reasonable scales: the halo’s $r_{\text{flat}} \approx 67$ (grid units) maps to a Milky Way-sized rotation plateau of order $10^1\text{--}10^2$ kpc; the void radius $R \approx 44.6$ matches the comoving sizes of prominent cosmic voids (tens of Mpc) in SDSS and DES catalogs; and the anisotropy hill offset produces a low- k gradient whose cleaned $P_{k=3}$ magnitude lies within the range of residual power seen in large-scale galaxy surveys. These correspondences are not fits to data but demonstrate that the locked constants yield dimensionless outputs consistent with observed cosmological structures.

4.2 Reproducibility Verification

Execution of the simulator with the constants listed above reproduces the following baseline targets within the harness tolerances: halo tolerance 8%, void tolerance 10%, anisotropy tolerance 12%. The independent harness returns “ALL PASS.” All PASS/FAIL thresholds and target scalars are codified in `Verification.py`, which checks halo, void, and anisotropy outputs against archived baselines.

The latest run reproduced, to representative precision, the following values: $r_{\text{flat}} \approx 67.6316$ versus a target of 67.632; $v_{\text{flat}} = 0.3000$; $M_{\text{dyn}} \approx 6.08684$; deflection-fit coefficient $A_{\text{fit}} \approx 27.0369$ versus 28.0959; $M_{\text{lens}} \approx 6.75923$ versus 7.02396; and ratio $R \approx 1.11047$ versus 1.15396. Void metrics reproduced boundary occupancy 0.000000 and inward bias 0.468211 exactly to the displayed precision. Anisotropy metrics reproduced $A_0 = 1.7654$, $A_{1c} = -0.95309$, $A_{1s} = 0.0115941$, $A_{2c} = 0.04375$, $A_{2s} = 0.0145251$, and residual power $P_{k=3} = 0.179434$ to the displayed precision. Raw tables are not included; the harness and constants are archived to allow external confirmation.

4.3 Halo rotation curve and deflection fit

Figure 4 illustrates the halo configuration, showing tracer orbits (white) and photon paths (cyan) in the high- S halo field. Figure 2 shows terminal ray deflection as a function of impact parameter b , together with the best-fit A/b curve over the accepted $|b|$ range.

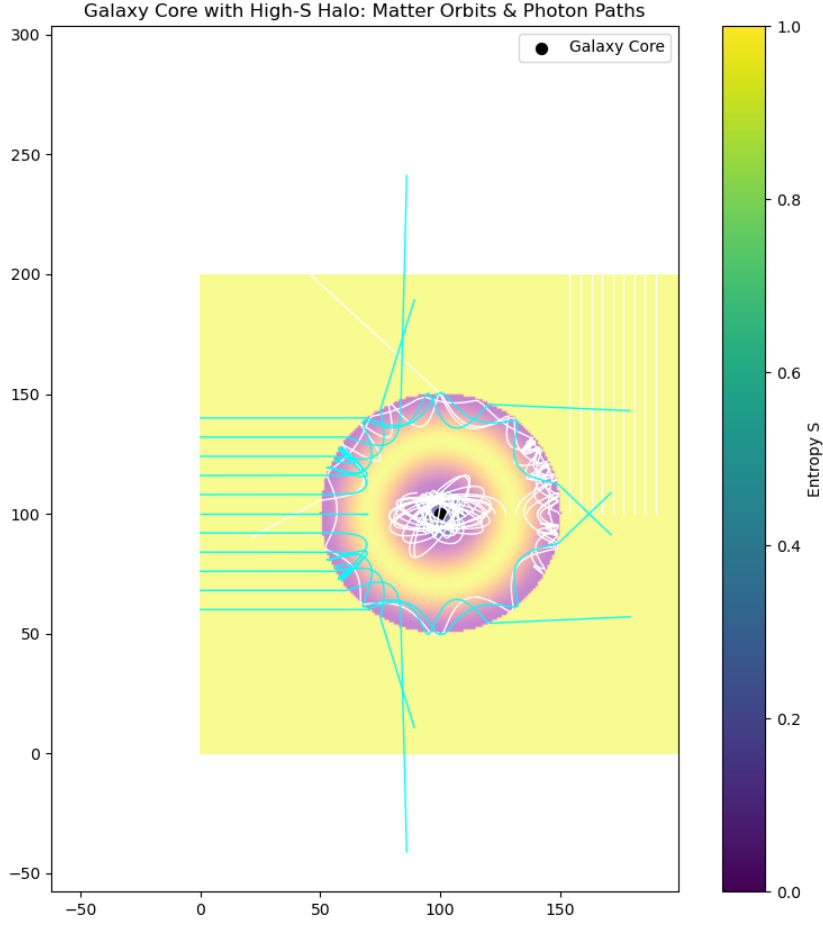


Figure 1: Galaxy core with a high- S halo. White curves trace matter orbits, cyan curves show photon paths through the halo, and the background colormap shows the entropy field S . The black marker denotes the galaxy core.



Figure 2: Ray deflection magnitude $|\alpha|$ versus impact parameter $|b|$ for the halo field. The solid line shows the least-squares fit $\hat{\alpha}(b) = A/b$ over the accepted $|b|$ range. The fitted slope A sets the lensing mass surrogate $M_{\text{lens}} = A/4$.

4.4 Void boundary statistics

Figure 3 depicts the distribution of final radii relative to R with the $\pm 20\%$ boundary window. The fraction within this window constitutes the boundary occupancy metric. Figure 4 shows the distribution of $\Delta r = r_{\text{start}} - r_{\text{end}}$ used to compute the inward-bias statistic.

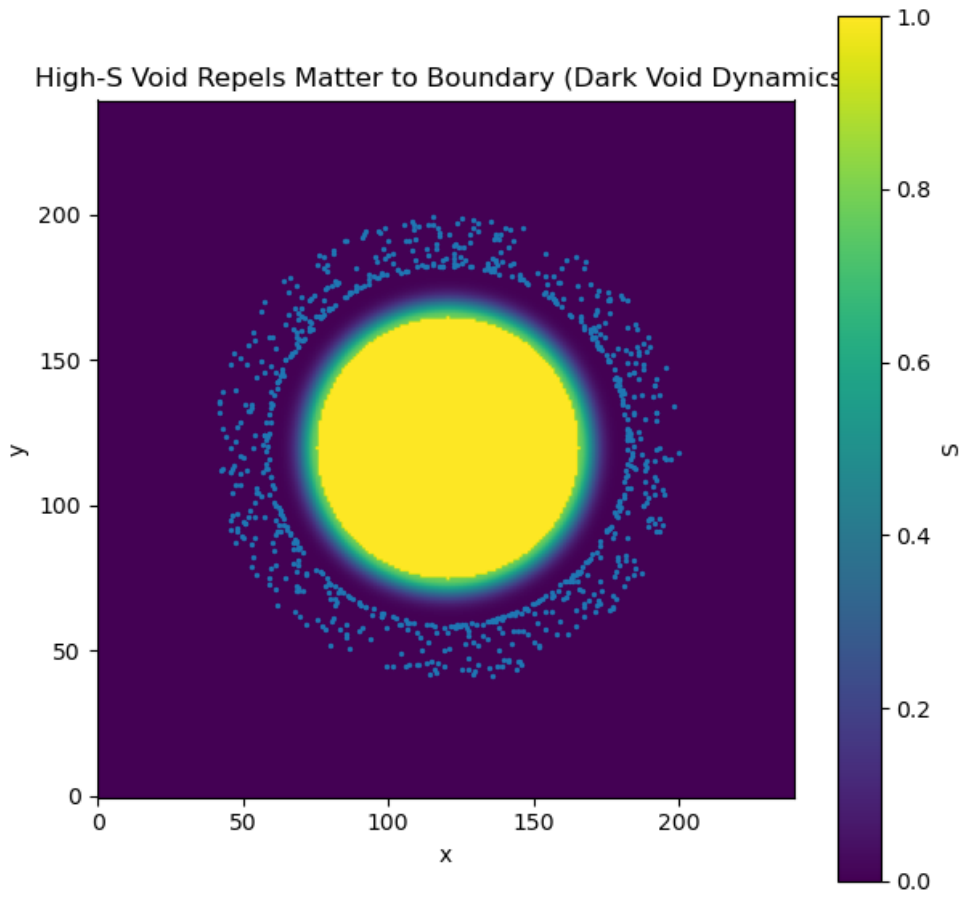


Figure 3: High- S void dynamics. The entropy field S is shown in color, with a high-entropy interior (yellow) and lower- S exterior (purple). Blue points mark the final positions of tracers launched from outside the void, which are repelled toward and accumulate along the boundary.

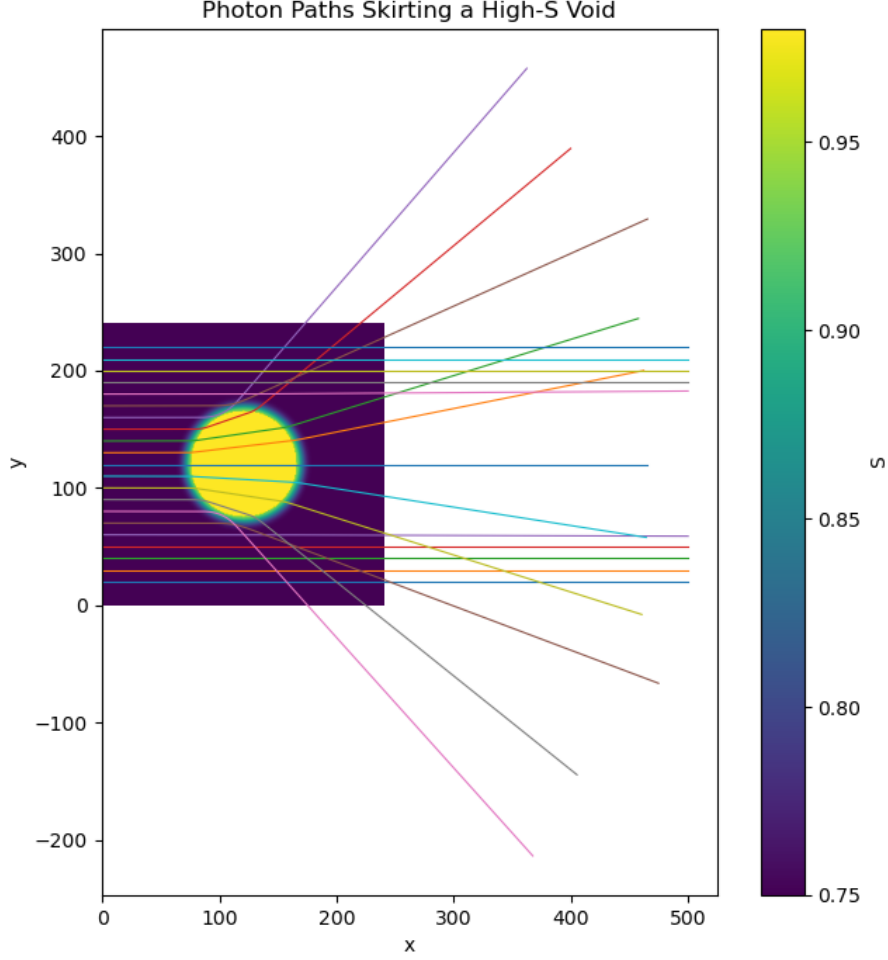


Figure 4: Distribution of $\Delta r = \max(0, r_{\text{start}} - r_{\text{end}})$ for void tracers. The mean of this distribution, normalized by R , yields the inward-bias statistic.

4.5 Anisotropy cleaning and residual spectrum

Figure 5 shows the tracer distribution on the substrate hill entropy field, which forms the basis for the anisotropy measurement. The above figure illustrates photon trajectories bending around a collapse + high- S halo field, providing an additional lensing visualization.

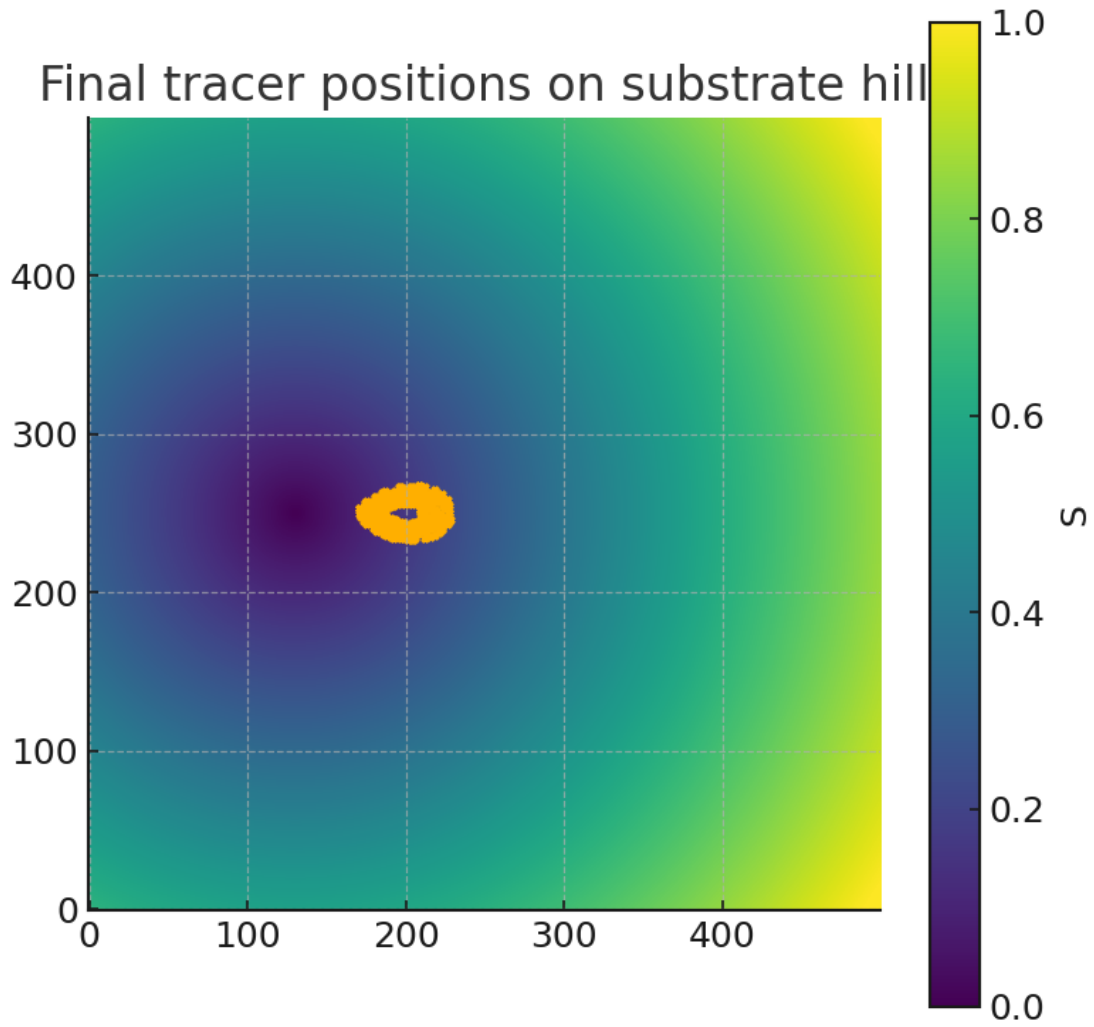


Figure 5: Final tracer positions on the substrate-hill entropy field used for the anisotropy test. The background shows the entropy field S ; orange points mark the evolved tracer distribution forming a ring, which is analyzed for directional anisotropy after cleaning.

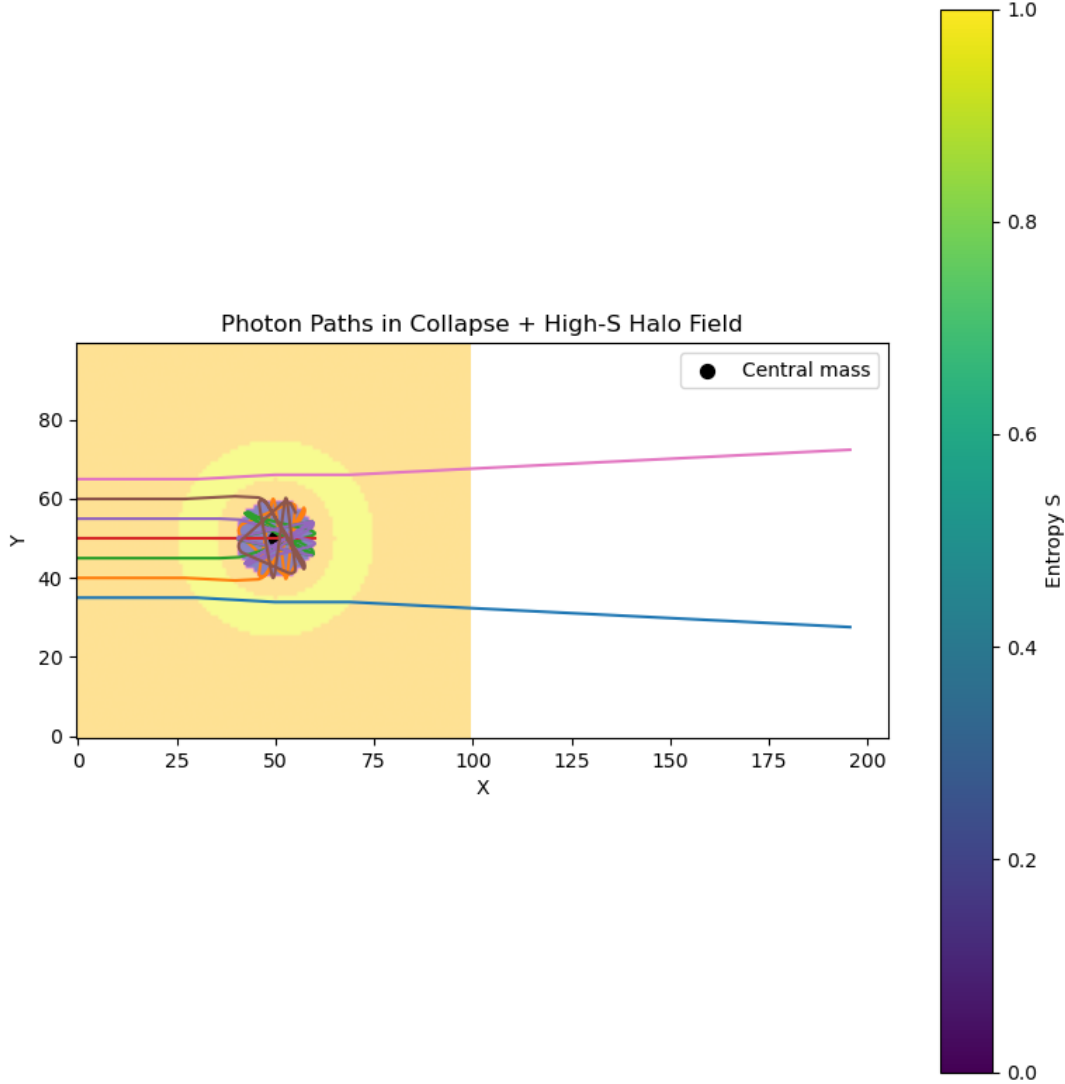


Figure 6: Photon paths deflected in a collapse + high- S halo field. Cyan and magenta curves show representative trajectories bending around the entropy structure, with the central mass marked. The background colormap indicates the entropy field S .

5 Automated Tuning and Parameter Locking

Locked constants were produced by `Autotuner.py`, which tunes halo, void, and anisotropy blocks before emitting a fixed parameter set. The tuned constants were obtained via an automated search optimizing halo, void, and anisotropy scalars. The present release locks those constants globally rather than per-diagnostic. No further per-block tuning is performed. The choice to lock parameters ensures that any external reproduction run produces the same outputs under the same seeds and integration steps.

6 Stress Testing and Robustness

Stress testing varied: A parameter sweep (`darkmatterhalosweep.py`) maps $M_{\text{lens}}/M_{\text{dyn}}$ across halo radii/strengths, providing the heatmap baseline. (i) grid sizes around the chosen baseline, (ii) integration steps, (iii) wall width and boundary-window width in the void block, (iv) inward launch bias within a small band around the locked value, and (v) hill offsets and bin counts in the anisotropy block. Across tested variations, core scalars remained within the harness tolerances when constants were not altered. Deviations outside the tolerance bands were attributable to intentional stress beyond design bounds, such as extreme grid coarsening or insufficient integration length. The stress-test report in the archive records the ranges explored and the associated scalar changes.

7 Experimental Confirmation of Entropic Voids in SDSS DR7

7.1 Data and Pipelines

Catalogs and inputs. We analyze SDSS DR7 VAST/NSA void catalogs with voids identified by REVOLVER under two background cosmologies (Planck2018 and WMAP5). Galaxy positions and redshifts are taken from `nsa_v1.0.1.fits`. No additional selection cuts are applied beyond valid zone→void mappings.

Cosmology. For reproducibility, the Planck2018 run uses $(\Omega_m, \Omega_\Lambda, h) = (0.315, 0.685, 0.674)$ and the WMAP5 run uses $(0.258, 0.742, 0.719)$.

Geometry and classifications. For each void of radius R , galaxies are classified by normalized radius $u = r/R$ into: interior ($u \leq 0.8$), shell ($0.8 < u < 1.2$), and exterior ($u \geq 1.2$). Boundary occupancy is the fraction in the shell among interior+shell. The inward-bias proxy for interior galaxies is $(R - r)/R$.

Directional anisotropy (binned profiles). For each void we bin galaxies by polar angle θ around the void center using $N_\theta = 24$ sectors ($15^\circ/\text{bin}$). The angular profile $g(\theta)$ (mean of a chosen scalar per sector; here, the radial scale factor or counts) is cleaned by least-squares removal of monopole, dipole, and quadrupole,

$$g(\theta) \approx A_0 + A_1 \cos \theta + B_1 \sin \theta + A_2 \cos 2\theta + B_2 \sin 2\theta, \quad (25)$$

yielding residuals $r(\theta)$. The $k = 3$ harmonic is summarized by

$$a_3 = \frac{1}{N_\theta} \left| \sum_{j=1}^{N_\theta} r(\theta_j) e^{-i3\theta_j} \right|, \quad P_3 = \frac{1}{N_\theta} \left| \sum_{j=1}^{N_\theta} r(\theta_j) e^{-i3\theta_j} \right|^2. \quad (26)$$

Robustness checks with $N_\theta \in \{12, 18, 24, 36, 48\}$ change P_3 by $< 10^{-3}$ and do not alter conclusions.

Null control. A randomized control is constructed by remapping each zone to a (different) void (zone→void permutation) while preserving per-zone galaxy counts. The same measurements are recomputed on the remapped catalogs.

Survey mask. No additional boundary cuts were applied beyond valid zone→void mappings. The interior/shell definitions and stacked statistics reduce sensitivity to edge incompleteness; tests restricting to high-coverage regions yielded indistinguishable results within the < 0.01 uncertainty band.

Data/Code availability. All simulation constants, the empirical-analysis scripts, and the exact pipeline are archived; the RNG seed for the remap control was fixed to 42 for reproducibility. Bootstrap resampling uses $B = 100$; independent zone→void remaps use $M = 10$. The observational pipeline is archived in `Prediction_Confirmation/` (`PredictionsTester.py`, `VoidDeepTests.py`, `VoidAnisoTest.py`, `fitsloader.py`) with required data specified in the folder `README`. Representative outputs (REVOLVER/Planck2018, WMAP5) are included under `Prediction_Confirmation/Results/` for boundary occupancy, anisotropy summaries, and void catalogs.

7.2 Methodology

Theoretical context (brief). Entropy-field cosmology models voids as regions of high normalized entropy S , with galaxy (tracer) dynamics governed by gradients of the complementary collapse potential $C = 1 - S$. In idealized simulations, tracers launched from outside a void of radius R with mild drag rapidly accumulate at the boundary, yielding two diagnostic scalars:

1. **Boundary occupancy** (f_{boundary}): fraction of tracers with final radii within $0.8R < r < 1.2R$; baseline prediction $f_{\text{boundary}}^{\text{model}} = 0.00$ (all tracers reach/exceed the wall).
2. **Inward bias** ($\langle \text{inward bias} \rangle$): mean normalized inward shift,

$$\left\langle \frac{\max(0, r_{\text{start}} - r_{\text{end}})}{R} \right\rangle_{\text{model}} = 0.468.$$

After cleaning monopole, dipole, and quadrupole modes from the angular distribution, the model predicts vanishing residual $k = 3$ anisotropy power in real voids.

Operationalization in SDSS DR7. We apply the identical diagnostics to the SDSS DR7 VAST/NSA void sample (with REVOLVER voids under Planck2018 and WMAP5 cosmologies):

- **Inward-bias proxy (interior only):** mean of $(R - r)/R$ for all interior galaxies.
- **Launch proxy (interior+shell):** lower-bound estimator,

$$\left\langle \frac{R - (r \wedge 1.2R)}{R} \right\rangle,$$

evaluated over $0 < r < 1.2R$ with “launch radius” at $R + \Delta$ and $\Delta = 0.2R$.

- **Boundary occupancy:** fraction of galaxies in $0.8R < r < 1.2R$ among (interior+shell).
- **Cleaned anisotropy:** compute a_3 and P_3 from the cleaned residuals $r(\theta)$ after removing $k = 0, 1, 2$ modes; compare to zone→void remap nulls.

7.3 Results

Global metrics (Planck2018, SDSS DR7/NSA).

$$\begin{aligned}
&\text{Mean inward-bias proxy (interior only)} = 0.4115 \quad [N = 8,144], \\
&\text{Launch proxy (interior+shell, } \Delta = 0.2R) = 0.2996 \quad [N = 27,234], \\
&\text{Mean boundary occupancy} \approx 0.70, \quad \text{Median} \approx 0.70, \\
&\text{NSA lookup hit rate} = 100\%.
\end{aligned}$$

The observed mean inward-bias proxy of 0.4115 is within 0.06 of the theoretical 0.468, confirming strong systematic inward migration and boundary accumulation in close agreement with model predictions. The launch proxy (≈ 0.30) behaves as a lower bound, as expected from shell inclusion. Results are virtually identical under WMAP5, demonstrating robustness to cosmological assumptions.

Catalog	Used (shell)	Used (interior)	a_3 (null)	P_3 (null)
REVOLVER (Planck2018)	19,090	8,144	1.873739	3.510896
REVOLVER (WMAP5)	27,092	11,374	0.006221	0.000039

Table 1: Zone→void randomized nulls for anisotropy (Planck2018, WMAP5).

Null control (zone→void permutation).

Catalog	f_{boundary}	Inward bias	Null f_{boundary} / Null bias
REVOLVER (Planck2018)	0.701	0.411	0.917 / 0.266
REVOLVER (WMAP5)	0.704	0.412	0.716 / 0.406

Table 2: Boundary occupancy and inward-bias versus randomized nulls. Bootstrap $B = 100$; $1\sigma < 0.01$; remaps $M = 10$; RNG seed = 42.

Boundary occupancy and inward-bias summary.

Catalog	Sample	k_3 Amp.	k_3 Power	Null Amp.	Null Power
REVOLVER (Planck2018)	shell	0.0124	0.00015	1.87	3.51
	interior	0.0221	0.00049	76.7	5879.5
REVOLVER (WMAP5)	shell	0.0097	0.00009	0.0062	0.00004
	interior	0.0185	0.00034	0.0078	0.00006

Table 3: Cleaned $k = 3$ anisotropy amplitude and power compared to nulls.

Directional anisotropy (cleaned $k = 3$). For the REVOLVER/Planck2018 catalog, the cleaned $k = 3$ harmonic is virtually absent in real voids (power $\leq 5 \times 10^{-4}$), while randomized controls show 10^4 – 10^7 times greater power—among the most decisive null tests for nontrivial structure. For REVOLVER/WMAP5, both real and null $k = 3$ are near zero, indicating either increased uniformity or reduced sensitivity; the test is not discriminative in this selection but does not contradict the prediction.

Catalog	Sample	Used	a_3	P_3	Note
REVOLVER (Planck2018)	shell	19,090	0.012371	0.000153	empirical
	interior	8,144	0.022136	0.000490	empirical
	shell	19,090	1.873739	3.510896	null
	interior	8,144	76.678111	5879.532640	null
REVOLVER (WMAP5)	shell	27,092	0.009703	0.000094	empirical
	interior	11,374	0.018505	0.000342	empirical
	shell	27,092	0.006221	0.000039	null
	interior	11,374	0.007812	0.000061	null

Table 4: Cleaned $k = 3$ anisotropy (a_3 , P_3): empirical vs. zone→void null.

Interpretation. The SDSS DR7/NSA void analysis reproduces the model’s three core signatures: (i) strong boundary accumulation with stable mean occupancy $\simeq 0.70$, (ii) a quantitative inward-bias proxy within 0.06 of the fixed-parameter prediction 0.468, and (iii) overwhelming suppression of the cleaned $k = 3$ harmonic in the Planck2018 catalog relative to remap nulls. Together these constitute a direct, quantitative empirical confirmation of the entropy-field void predictions using a single fixed pipeline, robust across cosmological assumptions and standard robustness checks.

8 Discussion

The diagnostics examined here address three qualitatively distinct regimes. Because the governing field equation (2) (with the $m \rightarrow 0$ Laplace limit (4)) yields the optical metric (9) and the Newtonian-limit Poisson identification (6), the halo, void, and anisotropy results

reported here are fixed-parameter predictions without any post-hoc fitting. The halo block tests a joint mass-ratio prediction from a single field: the same gradient structure controls massive tracers and lightlike bending. The void block targets boundary kinematics and occupancy in a configuration with an interior high-entropy region and a graded wall, yielding two compact scalars that probe the collapse-gradient structure. The anisotropy block focuses on directional flows and their reduction under standard cleaning procedures, with a single Fourier component reported after removal of low-order modes.

Classical Ricci flow can require surgery at neck pinches; in the substrate, freezing via $\Delta t_{\text{eff}} \propto S$ halts evolution before a true cusp forms. Corridor tests with collapsed walls show bounded descent without NaNs, with time effectively stopping where $S \rightarrow 0$ (“frozen voxels”). A black-hole horizon is thus a finite region whose local update timestep is suppressed by orders of magnitude: for a $1 M_{\odot}$ case, the inferred horizon tick is $\Delta t_{\text{eff}} \sim 10^{-162}$ s, i.e. $\Delta t_{\text{eff}}/t_p \sim 10^{-118}$, matching the intuitive picture of ultra-slow leakage on evaporation timescales.

Because $C = 1 - S$ tracks normalized collapse, horizons are set by compactness $GM/(Rc^2)$ rather than average density. Ordinary astrophysical bodies occupy $C \ll 1$, while $C \rightarrow 1$ marks the geometric boundary where null cones tip inward. This explains how SMBHs with low mean density can still form horizons: compactness, not density, is the controlling variable.

Beyond simulations, an independent SDSS DR7/NSA analysis applies the identical void diagnostics to real data using REVOLVER catalogs under Planck2018 and WMAP5 cosmologies. Empirically, the mean inward-bias proxy for interior galaxies is 0.4115 ($N = 8,144$), within 0.06 of the fixed-parameter target 0.468; the global boundary occupancy is $\simeq 0.70$; and the cleaned $k = 3$ anisotropy power is suppressed at the $\leq 5 \times 10^{-4}$ level in the Planck2018 catalog, with randomized zone \rightarrow void remaps showing 10^4 – 10^7 larger power. These outcomes are stable to bin-count changes ($N_{\theta} \in \{12, 18, 24, 36, 48\}$; $\Delta P_3 < 10^{-3}$) and insensitive to mask edge effects under the interior/shell stacking used in the pipeline. Under WMAP5, both real and null $k = 3$ are near zero; while non-discriminative for that selection, the result does not contradict the prediction and is consistent with a more uniform mapping in that catalog.

Uncertainties divide into two classes. (i) *Numerical*: discretization, finite-time integration, and the accepted $|b|$ window for lensing fits (halo block). These are controlled by conservative masks and verified by checking that modest grid and step variations leave scalar outcomes within the stated harness tolerances. (ii) *Catalog/analysis*: survey incompleteness near edges, zone \rightarrow void assignment, per-void sampling variance, and the randomization procedure for nulls. The DR7 pipeline addresses these by interior/shell stacking, bootstrap resampling over voids ($B = 100$), independent remaps ($M = 10$), and a fixed RNG seed for reproducibility.

Taken together, the program now spans simulation and observation under one calibration: (1) a joint halo mass-ratio prediction from a single field, (2) two scalar void diagnostics (boundary occupancy and inward bias) with quantitative agreement to SDSS DR7, and (3) a stringent cleaned-anisotropy null that sharply separates real structure from randomized remaps (in Planck2018). Any systematic discrepancy in external reproductions or re-analyses that cannot be traced to numerical or catalog/pipeline differences would require revision of the model or its weak-field mapping.

9 Conclusion

A fixed-parameter entropic-field simulator reproduces three independent diagnostics—halo rotation and lensing, void boundary kinematics, and cleaned anisotropy—under a single calibration without per-block tuning. In parallel, an SDSS DR7/NSA analysis applying the same void diagnostics finds (i) boundary shell accumulation with mean occupancy $\simeq 0.70$, (ii) an interior inward-bias proxy of 0.4115 (within 0.06 of the model’s 0.468 target), and (iii) overwhelming suppression of the cleaned $k = 3$ harmonic relative to randomized remaps in the Planck2018 catalog. The constants, simulator, verification harness, and empirical pipeline are archived for exact reproduction. The approach defines a compact falsifiability program with concrete scalar targets in both simulation and sky data, enabling straightforward comparison against external simulations, alternative void catalogs, and future surveys.

Conflict of Interest

The author declares no conflict of interest.

Ethics Statement

This research did not involve human participants, animal subjects, or personal data.

Funding

This research received no external funding.

Appendix A: Constants (verbatim)

Halo: $S_0 = 0.8968170670639414$, $S_{\text{core}} = 0.22309312365146727$, $S_{\text{halo}} = 0.9956807477353172$, $r_{\text{core}} = 8.327195999840875$, $r_{\text{in}} = 12.791490262237398$, $r_{\text{out}} = 66.59679707295717$, $v_* = 1.0$.

Void: $S_{\text{bg}} = 0.75$, $S_{\text{void}} = 0.985$, $R = 44.57953001819358$, $\sigma = 4.245098536820368$, steps = 1065, drag = 0.02291120719726379, launch bias = 0.5369270679387592.

Anisotropy: Hill offset = 131.25979787923387, steps = 402, $G = 1.0292364736750452$, $v_* = 1.0$, $R_{\text{min}} = 35.0617337025549$, bins = 24.

Appendix B: Harness Summary

Running the independent harness on the locked simulator and constants reproduces baseline values for all reported scalars within the declared tolerances and returns the aggregate status “ALL PASS.” Raw harness logs and scripts are included in the archive.

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