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Assignment 1

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Download all python codes from

https://github.com/Digjoy12/Signal-Processing/blob/main/Assignment%201/Code/untitled1.py

and latex codes from

https://github.com/Digjoy12/Signal-Processing/blob/main/Assignment%201/main.tex

PROBLEM

(Vectors - Q2.8) By using the concept of equation of a line, prove that the three points $\begin{pmatrix} 3 \\ 0 \end{pmatrix}$, $\begin{pmatrix} -2 \\ -2 \end{pmatrix}$ and $\begin{pmatrix} 8 \\ 2 \end{pmatrix}$ are collinear.

Let,
$$A = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$$
, $B = \begin{pmatrix} -2 \\ -2 \end{pmatrix}$ and $C = \begin{pmatrix} 8 \\ 2 \end{pmatrix}$

Now,

$$B - A = \begin{pmatrix} -2 - 3 \\ -2 - 0 \end{pmatrix} = \begin{pmatrix} -5 \\ -2 \end{pmatrix} \tag{0.0.1}$$

$$C - A = \begin{pmatrix} 8 - 3 \\ 2 - 0 \end{pmatrix} = \begin{pmatrix} 5 \\ 2 \end{pmatrix}$$
 (0.0.2)

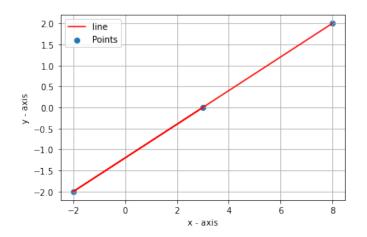
Using matrix transformation,

$$M = \begin{pmatrix} -5 & -2 \\ 5 & 2 \end{pmatrix} \xrightarrow{R_1 \to -R_1} \begin{pmatrix} 5 & 2 \\ 5 & 2 \end{pmatrix} \tag{0.0.6}$$

$$\stackrel{R_2 \to R_2 - R_1}{\longleftrightarrow} \begin{pmatrix} 5 & 2 \\ 0 & 0 \end{pmatrix} \tag{0.0.7}$$

(0.0.8)

 $\implies rank(M) = 1$



Thus, the points are collinear.

Forming the matrix M,

$$M = \begin{pmatrix} B - A & C - A \end{pmatrix}^{\mathsf{T}} \tag{0.0.3}$$

$$= \begin{pmatrix} -5 & 5 \\ -2 & 2 \end{pmatrix}^{\mathsf{T}} \tag{0.0.4}$$

$$= \begin{pmatrix} -5 & -2 \\ 5 & 2 \end{pmatrix} \tag{0.0.5}$$