## 1

## Assignment:- 1

## AI1110: Probability and Random Variables Indian Institute of Technology, Hyderabad

## CS22BTECH11017

Dikshant Khandelwal 30 April, 2023

Exercise 12.13.1.10 A black and a red dice are rolled.

- (a) Find the conditional probability of obtaining a sum greater than 9, given that the black die resulted in a 5.
- (b) Find the conditional probability of obtaining the sum 8, given that the red die resulted in a number less than 4.

**Solution.** Let *X* and *Y* be the random variables denoting the number which comes up on black and red die respectively.

Let us define cumulative frequency distribution of some random variable A,

$$F_A(i) = \Pr\left(A \le i\right) \tag{1}$$

$$F_X(i) = F_Y(i) = \begin{cases} 0 & i < 1 \\ \frac{i}{6} & 0 < i \le 6 \\ 1 & i > 6 \end{cases}$$
 (2)

(b)

$$\Pr(X + Y = 8 | Y < 4) = \frac{\Pr(X + Y = 8, Y < 4)}{\Pr(Y < 4)}$$

$$= \frac{\sum_{i=2}^{i=3} \Pr(X = 8 - i, Y = i)}{F_Y(3)}$$

$$= \frac{\sum_{i=2}^{i=3} \Pr(X = 8 - i) \Pr(Y = i)}{F_Y(3)}$$
(11)

$$=\frac{\left(\frac{2}{36}\right)}{\frac{3}{6}}\tag{12}$$

$$=\frac{1}{9}\approx 0.11\tag{13}$$

$$\therefore \Pr(X + Y = 8 | Y < 5) = \frac{1}{9} \approx 0.11$$
 (14)

(a)

$$\Pr(X + Y > 9 | X = 5) = \frac{\Pr(X + Y > 9, X = 5)}{\Pr(X = 5)}$$

$$= \Pr(Y > 4) \qquad (4)$$

$$= F_Y(6) - F_Y(4) \qquad (5)$$

$$= 1 - \frac{4}{6} \qquad (6)$$

$$= \frac{1}{3} \approx 0.33 \qquad (7)$$

$$\therefore \Pr(X + Y > 9 | X = 5) = \frac{1}{3} \approx 0.33$$
 (8)