

# AI1110 Assignment

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**12.13.5.4:** Five cards are drawn successively with replacement from a well-shuffled deck of 52 cards.

What is the probability that

- (i) all the five cards are spades?
- (ii) only 3 cards are spades?
- (iii) none is a spade?

**Answer:**

A deck has 52 cards among which 13 are spades. Since we are replacing drawn cards, the probability of getting spade on any draw,  $p = \frac{13}{52} = \frac{1}{4}$ . This is a binomial distribution where getting a card of spades is considered success.

The probability of getting  $r$  successes in a binomial distribution having  $n$  independent Bernoulli trials and probability of success in each Bernoulli trial being  $p$  is

$$P(r) = \binom{n}{r} p^r (1-p)^{n-r}$$

Here,  $p = \frac{1}{4}$  and  $n = 5$ .

(i) Probability that all 5 cards are spades is  $P(5)$ .

$$P(5) = \binom{5}{5} \left(\frac{1}{4}\right)^5 \left(\frac{3}{4}\right)^0 = \frac{1}{1024} \approx 0.00098$$

(ii) Probability that only 3 cards are spades is  $P(3)$ .

$$P(3) = \binom{5}{3} \left(\frac{1}{4}\right)^3 \left(\frac{3}{4}\right)^2 = \frac{45}{512} \approx 0.08789$$

(iii) Probability that no card is spade is  $P(0)$ .

$$P(0) = \binom{5}{0} \left(\frac{1}{4}\right)^0 \left(\frac{3}{4}\right)^5 = \frac{243}{1024} \approx 0.23730$$