

CS 342 - 03
Operating Systems
Homework 3

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1)

	<u>Allocation</u>	<u>Need</u>	Remaining = 15 - A - B
P1	A	10 - A	
P2	B	12 - B	

To be safe $\Rightarrow B \leq 5$ or $A \leq 3$

$$\begin{array}{ccc} \downarrow & & \downarrow \\ 10 - A \leq 15 - A - B & & 12 - B \leq 15 - A - B \\ B \leq 5 & & A \leq 3 \end{array}$$

Total = $13 \cdot 4 + 6 \cdot 6 = 78$ safe state

2) After alloc, remaining resource $\Rightarrow (3, 3, 0)$

Finish P4 \rightarrow new = (4, 3, 1)

Finish P1 \rightarrow new = (5, 3, 1)

P2, P3, P5 requires more than available, so none of them will finish.
This results deadlock.

4)

a) Virtual addr = 36 bits = 2^{36} bytes
 Page size = 16 KB = 2^{14} bytes

$$\left. \begin{array}{l} \text{Virtual addr} = 2^{36} \text{ bytes} \\ \text{Page size} = 2^{14} \text{ bytes} \end{array} \right\} \frac{2^{36}}{2^{14}} = 2^{22} \text{ pages}$$

$$2^{22} \cdot 2^3 = 2^{25} = 32 \text{ MB}$$

b) 2^{11} entries in 2^{nd} level $\rightarrow 2^{11} \cdot 2^{14} = 2^{25} = 32 \text{ MB}$

$$\frac{128}{32} + \frac{64}{32} + \frac{32}{32} + 1 \text{ top level} = 8 \text{ tables}$$

$$8 \cdot 16 \text{ KB} = 128 \text{ KB}$$

c) $\frac{2^{32}}{2^{14}} = 2^{18}$ entries $2^{18} \cdot 2^3 = 2^{21} = 2 \text{ MB}$

5)

a) Block size = 4 KB

Pointer size = 8 byte

$$12 \text{ direct} = 12 \cdot 4 = 48 \text{ KB}$$

$$1 \text{ single indirect} = 512 \cdot 4 = 2048 \text{ KB} = 2 \text{ MB}$$

$$1 \text{ double } " = 512^2 \cdot 4 = 16 \text{ B}$$

$$1 \text{ triple } " = 512^3 \cdot 4 = 512 \text{ GB}$$

$$\text{max size} = 512 \text{ GB} + 4 \text{ GB} + 2 \text{ MB} + 48 \text{ KB}$$

b) $30 \text{ KB} \Rightarrow \frac{30 \cdot 2^{10}}{2^{12}} = 8 < 12$ index is enough

$$256 \text{ KB} \Rightarrow \frac{2^{18}}{2^{12}} = 64 > 12 \text{ not enough} \Rightarrow \frac{52}{512} = 1 \text{ block}$$

$$15 \text{ MB} \Rightarrow \frac{15 \cdot 2^{20}}{2^{12}} = 3048 > 12 \text{ not enough} \Rightarrow \frac{3036}{512} = 6 \text{ blocks}$$

$$512 \text{ MB} \Rightarrow \frac{2^{29}}{2^{12}} = 2^{17} > 12 \text{ not enough} \Rightarrow \frac{2^{17} - 12}{2^9} = 2^8 = 256 \text{ blocks}$$

$$32 \text{ GB} \Rightarrow \frac{2^{35}}{2^{12}} = 2^{23} > 12 \text{ not enough} \Rightarrow \frac{2^{23} - 12}{2^9} = 2^{14} \text{ blocks}$$

c) $16 \text{ KB} = \frac{2^{14}}{12 \cdot 2^{12}} = 0 \Rightarrow \text{mod} = 4 \Rightarrow \text{total of 4 read}$

$$64 \text{ MB} = \frac{2^{26}}{2^{12}} = 2^{14} \Rightarrow \text{pointed by double indirect} \Rightarrow 6 \text{ read is needed}$$

7) 4KB \rightarrow unit size

9 disks \rightarrow 8 blocks 1 parity block

RPM: 1500

Avg: 4ms

max rate: 100 MB/s

$$a) T_{ro} = \underbrace{T_{seek}}_{6.04ms} + \underbrace{T_{rotation}}_{2ms} + \underbrace{T_{transfer}}_{0.04ms}$$

$$R = 0.66 \text{ MB/s}$$

$$\overset{\uparrow}{9} \times \overset{\downarrow}{R} = 5.94 \text{ MB/s} \Rightarrow \text{random read}$$

$$b) T_{transfer} = 1000 \text{ ms}$$

$$T_{rotation} = 2 \text{ ms}$$

$$T_{io} = 1006 \text{ ms} \quad S = 99.4 \text{ MB/s}$$

$$(N-1) \times S = 795.2 \text{ MB/s}$$

$$8) \text{MTTDL} = \frac{\text{MTTF}^2}{N \times (N-1) \times \text{MTTR}} = \frac{50000^2}{9 \times 8 \times 48} = 72380 \text{ hours} \approx 8.25 \text{ years}$$