#### **DIGITAL LOGIC**

Chapter 5 part1: Latches and Flip-flops

2023 Fall

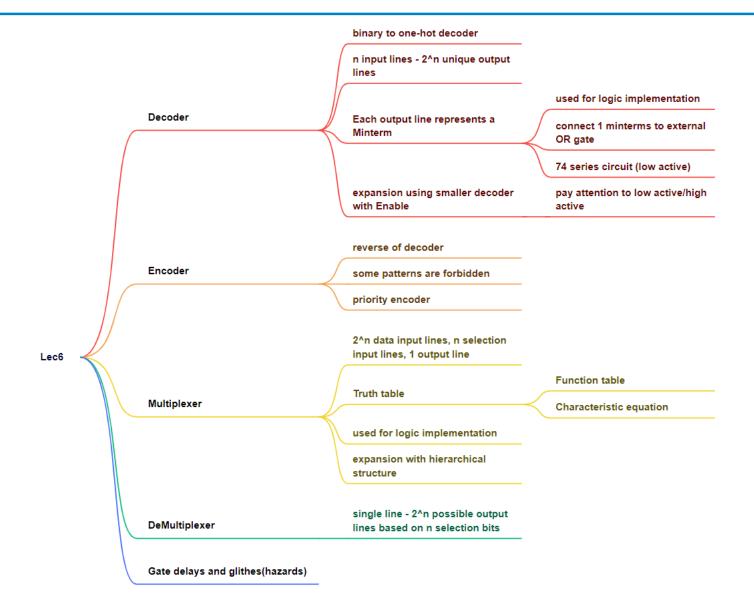


### Today's Agenda

- Recap
- Context
  - Latches
  - Flip-Flops
- Reading: Textbook, Chapter 5.1-5.4



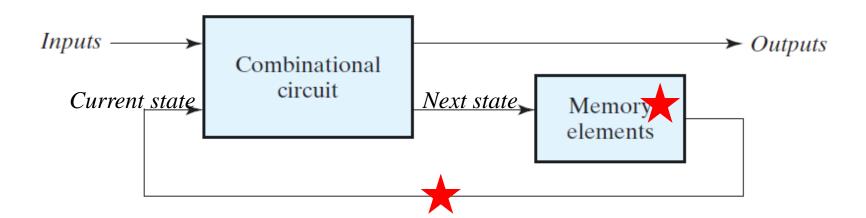
### Recap





### **Sequential Circuits**

- A sequential circuit consists of a combinational circuit to which storage elements are connected to form a feedback path.
  - The binary information stored in the memory elements at any given time defines the state of the sequential circuit.
  - (inputs, current state) => (outputs, next state)— The behavior is specified by a time sequence of inputs and internal states.





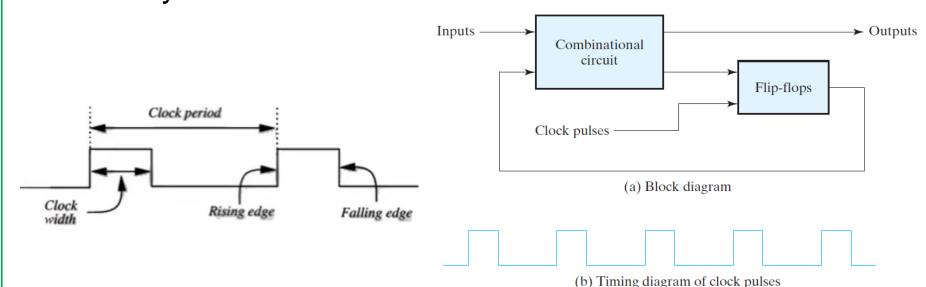
# Synchronous vs. Asynchronous Sequential Circuits

- Sequential circuits are broadly classified into two main categories depending on the timing of their signals.
  - Synchronous sequential circuit (同步时序电路): A system whose behavior can be defined from the knowledge of its signals at discrete instants of time.
  - Asynchronous sequential circuit (异步时序电路): A system whose behavior depends upon input signals at any instant of time and the order in which the inputs change.
- Asynchronous circuit properties
  - Commonly used storage devices are time-delay devices, and the propagation delay of the logic gates (time-delay devices) provides the required storage.
  - Can be viewed as combinational circuit with feedback—May unstable at times



# **Synchronous Sequential Circuits**

- Synchronization usually is achieved by a timing device: clock generator.
  - The outputs are affected only with the application of a clock pulse.
- Clock generator generates a periodic train of clock pulses distributed throughout the system to trigger the memory elements





### **Storage Elements**

- Some definitions:
  - State: all the information about a circuit necessary to explain its future behavior
  - Latches and flip-flops: state elements that store one bit of state
    - SR Latch (SR锁存器)
    - D Latch (D锁存器)
    - D Flip-flop (DFF, D触发器)



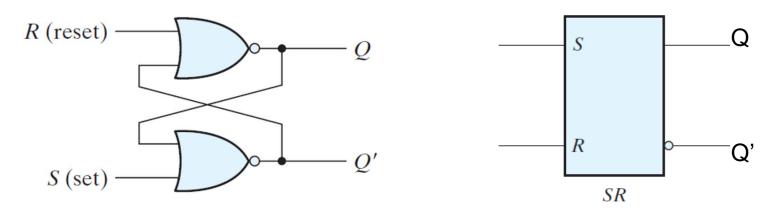
### **Outline**

- Latches
- FlipFlops



# SR (Set/Reset) Latch

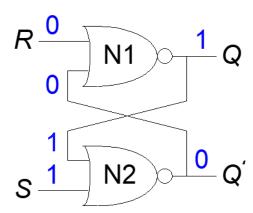
- Latch is an asynchronous sequential circuit (state changes whenever inputs change).
- SR latch is a basic memory element which can store one bit of information
  - Consists of two cross-coupled NOR gates or two cross-coupled NAND gates
  - Two input signals: set (S)/reset(R)
  - Two output signals: Q/Q'
  - Two useful states: set state (Q=1,Q'=0)/reset state(Q=0,Q'=1)

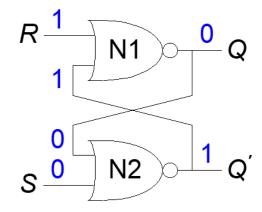




#### **Basic SR Latch with NOR Gate**

- Consider the four possible cases:
  - 1. S = 1, R = 0
  - 2. S = 0, R = 1
  - 3. S = 0, R = 0
  - 4. S = 1, R = 1
- 1. S = 1, R = 0:
  - then Q = 1 and Q' = 0
  - Set the output
- 2. S = 0, R = 1:
  - then Q = 0 and Q' = 1
  - Reset the output

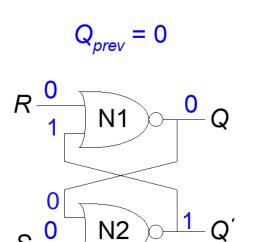


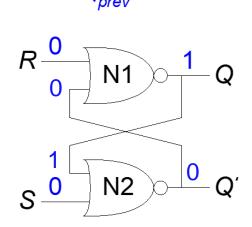


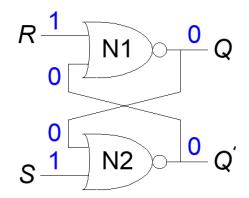


#### **Basic SR Latch with NOR Gate**

- Consider the four possible cases:
  - 1. S = 1, R = 0
  - 2. S = 0, R = 1
  - 3. S = 0, R = 0
  - 4. S = 1, R = 1
- 3. S = 0, R = 0:
  - then  $Q = Q_{prev}$
  - Memory!
- 4. S = 1, R = 1:
  - then Q = 0 and Q' = 0
  - Invalid State!
  - Q' ≠ NOT Q





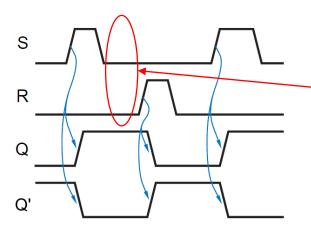




#### **Function Table of SR Latch**

- SR Latch's functionality:
  - S is active → Set
  - R is active → Reset
  - S,R are inactive → Memory
  - S,R are active → Forbidden

S	R	Q	Q'	
0	0	last Q	last Q'	no change
0	1	0	1	reset state
1	0	1	0	set state
1	1	0	0	forbidden



(S,R) must go back to (0,0) before any other change to avoid the occurrence of the undefined state

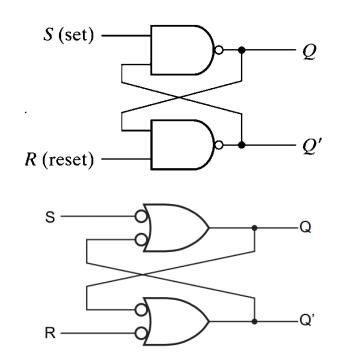


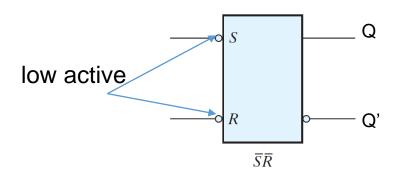
#### S'R' Latch with NAND Gates

#### Low Active Set/Reset inputs

- S is active → Set
- R is active → Reset
- S,R are inactive → Memory
- S,R are active → Forbidden

S	R	Q	Q'	
0	0	1	1	forbidden
0	1	1	0	set state
1	0	0	1	reset state
1	1	last Q	last Q'	no change





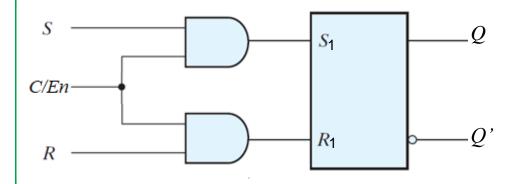
graphic symbol or S'R' Latch

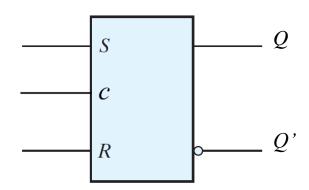


#### **Clocked SR Latch**

- Use Clock (or En) to enable/disable the SR latch
  - C=0, no change (disabled)
  - C=1, operates as normal SR latch (enabled)
- Level sensitive SR Latch
  - However, undefined state when
     C = S= R = 1

С	S	R	Q	Q'	
0	Χ	Χ	last Q	last Q'	no change
1	0	0	last Q	last Q'	no change
1	0	1	0	1	reset state
1	1	0	1	0	set state
1	1	1	0	0	forbidden







#### **D** Latch

- Two inputs: Clk(En), D
  - Clk(En): controls when the output changes
  - D (the data input): controls what the output changes to

	C	D	Q	Q'	
	0	Χ	last Q	last Q'	no change
•	1	0	0	1	Q follows D
	1	1	1	0	Q follows D

- Level sensitive D Latch
  - When CLK = 1,
    - D passes through to Q (transparent)
  - When CLK = 0,
    - Q holds its previous value (opaque)

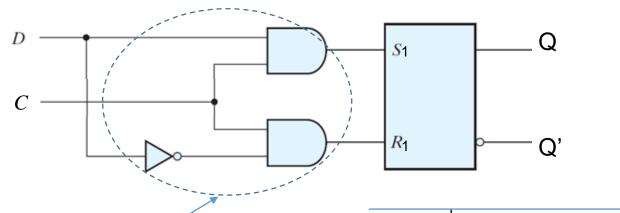
С

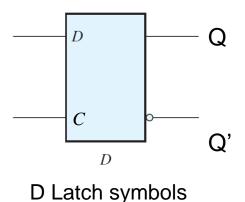
- Can avoid invalid case when
  - Q' ≠ NOT Q



#### D Latch Structure

- D latch is also called Transparent Latch
  - Constructed from a gated SR latch by connecting the D input to S input and D' to R.
  - Avoiding undesirable condition (S=R=1)





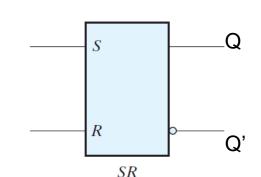
This make sure S and R differs

С	D	Q	Q'	
0	Χ	last Q	last Q'	no change
1	0	0	1	Q follows D
1	1	1	0	Q follows D

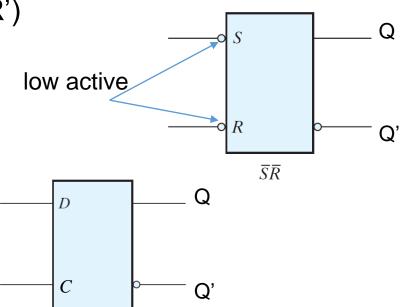


### **Latch Summary**

- SR Latch with NOR gate (SR)
  - Set: Make the output 1
     (S = 1, R = 0, Q = 1)
  - Reset: Make the output 0
     (S = 0, R = 1, Q = 0)
  - Memory: S=R=0



- S'R' Latch with NAND gate (S'R')
  - Set: Make the output 1
     (S = 0, R = 1, Q = 1)
  - Reset: Make the output 0
     (S = 1, R = 0, Q = 0)
  - Memory: S=R=1
- D Latch (D)
  - Make D passes through to Q

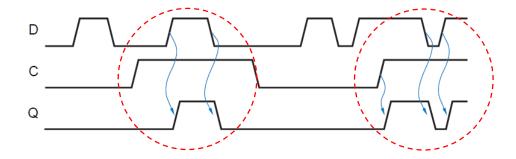


D



#### **Latches Pros and Cons**

- A latch is enabled whenever C=1. (level-sensitive)
  - At any point during C=1, any input changes will propagate to the output (with some small delay)



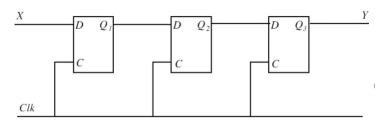
#### Pros

- Useful for level-sensitive applications
- Latches are faster because they have fewer gates and less delay.
- Latches are simpler which means they require less hardware to implement and consume less power.

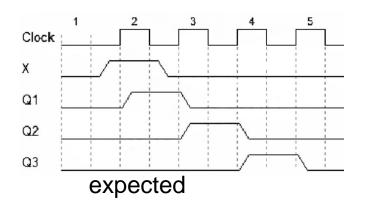


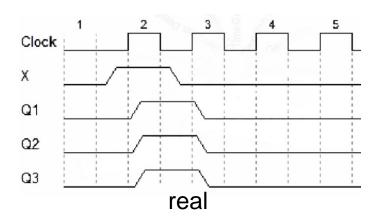
#### **Latches Pros and Cons**

- A latch is enabled whenever C=1. (level-sensitive)
  - At any point during C=1, any input changes will propagate to the output (with some small delay)
- Cons
  - Difficult to retain value
  - Causing erroneous shifting



Unable to shift Q<sub>2</sub> and Q<sub>3</sub> with clock cycles delay







### **Outline**

- Latches
- FlipFlops



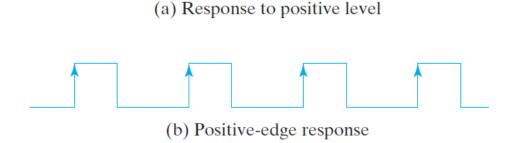
# Flip-Flops (FF)

- Latch or Flip-Flop(FF) state changes by a control input.
  - The event is called trigger.
- A Flip-Flop is a more advanced storage element, typically constructed using two D latches or more complex circuitry.
- Example: D Flip Flop
  - Inputs: CLK, D
  - For a Positive-edge triggered D Flip Flop:
  - Samples D on rising edge of CLK
    - When CLK rises from 0 to 1, D passes through to Q
    - Otherwise, Q holds its previous value
  - Q changes only on rising edge of CLK



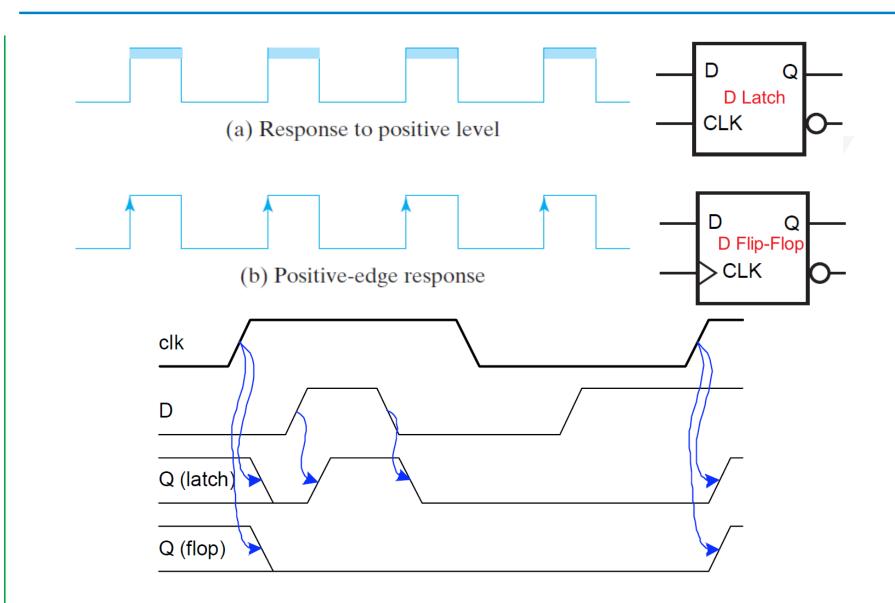
### **Trigger**

- Trigger
  - The state of a latch or flip-flop is switched by a change of the control input
- Level sensitive (level-triggered) (latches)
  - The state transition starts as soon as the clock is during logic 1 (positive level-sensitive) or logic 0 (negative level-sensitive) level
- Edge-triggered (flip-flops)
  - The state transition starts only at positive (positive edgetriggered) or negative edge (negative edge-triggered) of the clock signal





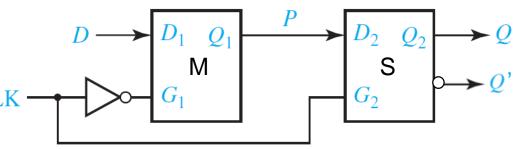
# Level-Sensitive vs. Edge-Triggered





#### **DFF Structure**

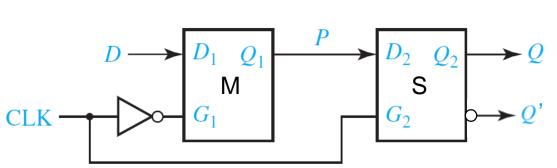
- A D flip-flop is formed by two separate latches
  - A master D latch (negative level sensitive)
  - A slave D latch (positive level sensitive)
- Positive-edge-triggered D flip-flop
  - When CLK = 0
    - master is transparent
    - slave is opaque
    - D passes through to Y
  - When CLK = 1
    - master is opaque
    - slave is transparent
    - Y passes through to Q
  - Thus, on the rising edge of the clock (CLK rises from  $0 \rightarrow 1$ )
    - D passes through to Q



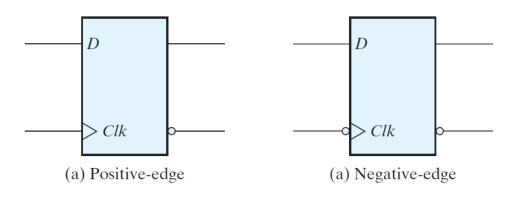


#### **Function Table of DFF**

#### Function table



С	D	Q	Q'	
0	X	last Q	last Q'	no change
1	Χ	last Q	last Q'	no change
	0	0	1	Q follows D
	1	1	0	Q follows D



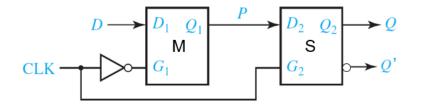
Question: How to design Negative-edge-triggered flip-flop (refer to textbook)

D Flip-Flop Symbols

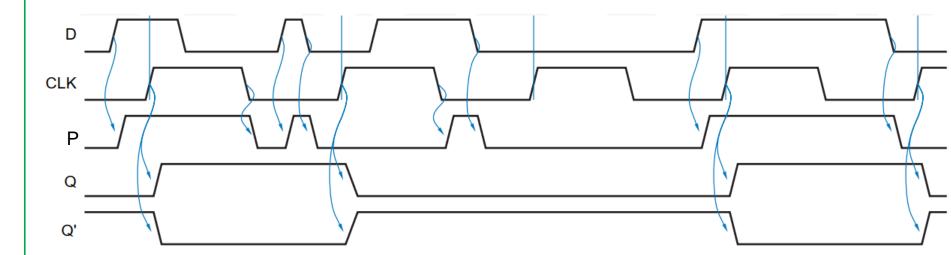


# **Timing Graph of DFF**

- Positive-edge-triggered DFF
  - Q stays stable between two rising edges of the clock signal



С	D	Q	Q'	
0	X	last Q	last Q'	no change
1	Χ	last Q	last Q'	no change
<u>_</u>	0	0	1	Q follows D
	1	1	0	Q follows D

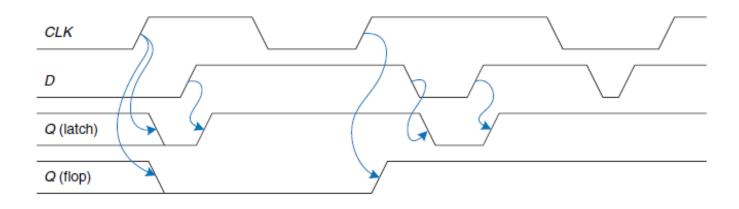




### Flip-flop and Latch Comparison

 Apply the D and CLK inputs to a D latch and a D flipflop, determine the output, Q, of each device.

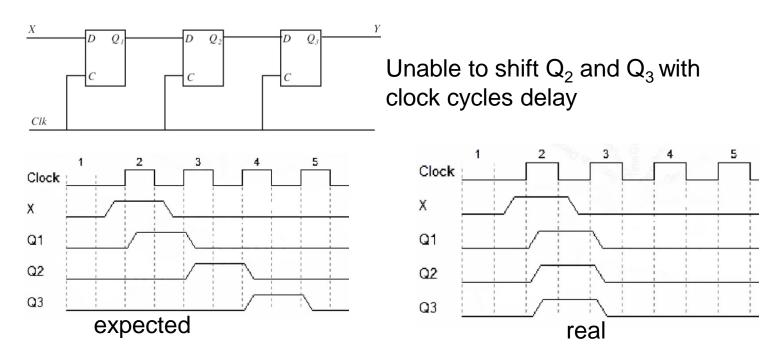




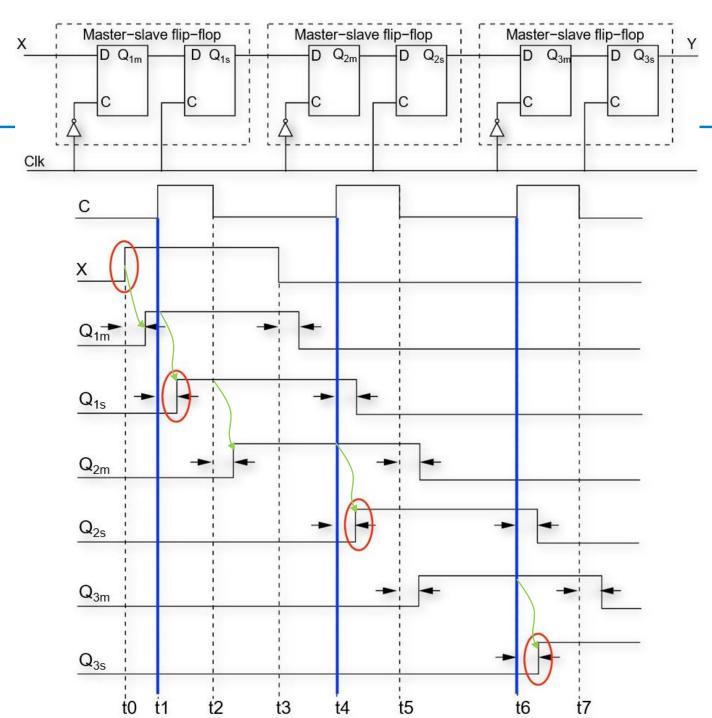


# **Shifting**

 Remember we wanted to shift input with clock cycles delay, but latches didn't work out



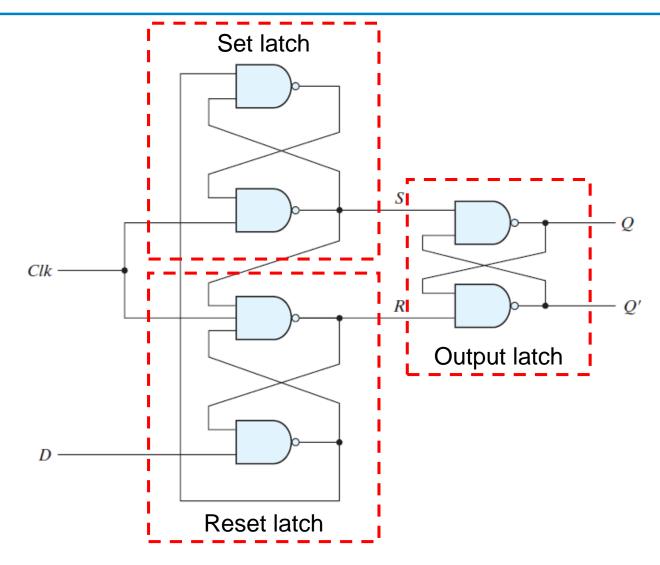
Now we can use FlipFlops







#### **DFF** with three SR Latches

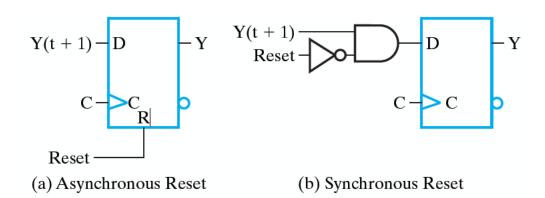


Positive-edge-triggered D flip-flop



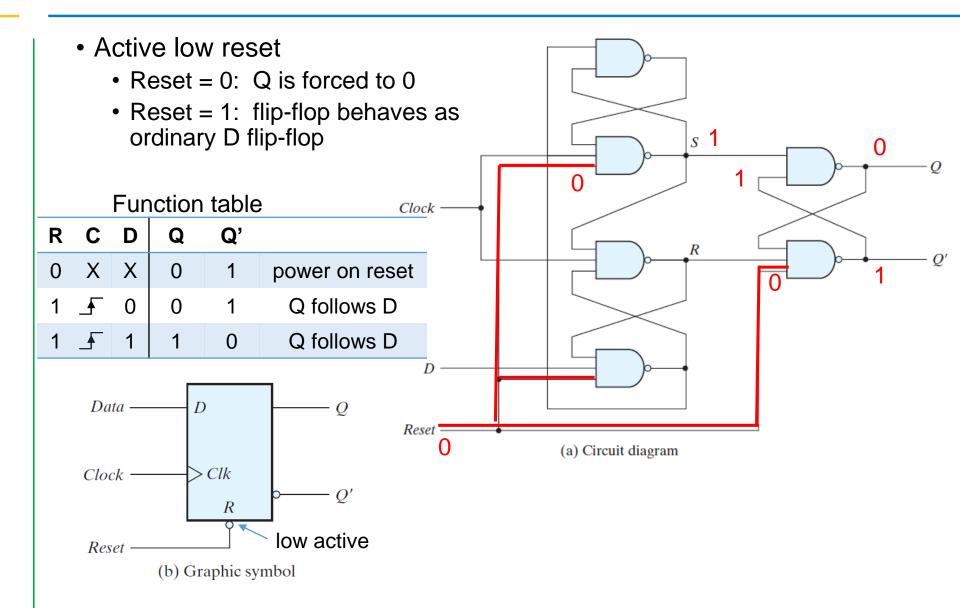
#### **DFF** with Reset

- The state of FFs are unknown when power is on. A direct input can force the FFs to a known state before the system starts.
  - E.g. when Reset = 1, FF's output is forced to 0
- Synchronous vs. asynchronous resettable Flip Flop
  - Asynchronous: resets immediately when Reset = 1
  - Synchronous: resets at the clock edge only





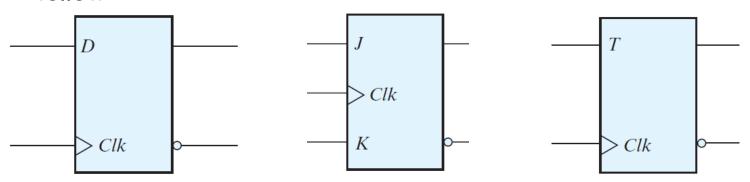
# **DFF with Asynchronous Reset**





### **Types of Flip-Flops**

- Flip-flops are more suitable for synchronous sequential circuits and are often used as the basic memory elements, since they only respond to a transition on a clock input.
- Other types of flip-flops can be constructed by using the DFF and external logic.
- Major FFs
  - D(data), JK, T (toggle) FFs
  - Assume only positive-edge-triggered FFs, block diagram are as follow





#### **Characteristic Table**

 Characteristic table: describe the behavior of a flip-flop based on its input and current state Q(t) just before the rising edge of the clock, and the resulting next state Q(t+1) after the clock transition.

F	Function table							
Clk	D	Q	Q'					
0	X	last Q	last Q'	no change				
1	Χ	last Q	last Q'	no change				
<u>_</u>	0	0	1	Q follows D				
	1	1	0	Q follows D				



D Flip-Flop				
D	Q(t + 1)			
0	0	Reset		
1	1	Set		

Characteristic table

- Characteristic equation: derived from the characteristic table using the map method
  - Characteristic equation of DFF:

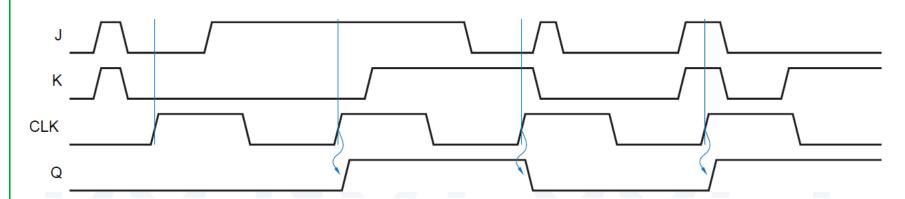
$$Q_{t+1} = D$$



### J-K Flip-Flop

- Positive edge-triggered JKFF
  - At rising edge of clock
    - J = K = 0, Q is unchanged
    - J = K = 1, Q toggles
    - J = 1, K = 0, Q is set to 1
    - J = 0, K = 1, Q is reset to 0
  - At level of clock
    - · Q is unchanged

Function Table					
Clk	J	K	Q	Q'	
0	х	Х	last Q	last Q'	
1	X	Х	last Q	last Q'	
	0	0	last Q	last Q'	
<u>_</u>	0	1	0	1	
	1	0	1	0	
	1	1	last Q'	last Q	





### J-K Flip-Flop

	Chara	acteristic ta	able		J	K	Q(t)	Q(t+1)
JKI	Flip-F	lop		-	0	0	0	0
J	K	Q(t + 1)	)	Derive the Truth table	0	0	1	1
0	0	Q(t)	No change		0	1	0	0
0	1	0	Reset		0	1	1	0
1	0	1	Set		1	0	0	1
1	1	Q'(t)	Complement		1	0	1	1
			Characteri	stic equation of JKFF	1	1	0	1
				JQ(t)' + K'Q(t)	1	1	1	0

#### Algebraically:

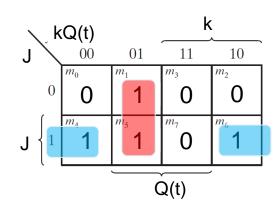
$$Q(t+1) = J'K'Q(t) + J'K \cdot 0 + JK' \cdot 1 + JKQ(t)'$$

$$= J'K'Q(t) + JK' + JKQ(t)'$$

$$= J'K'Q(t) + JK'Q(t) + JK'Q(t)' + JKQ(t)'$$

$$= JQ(t)' + K'Q(t)$$

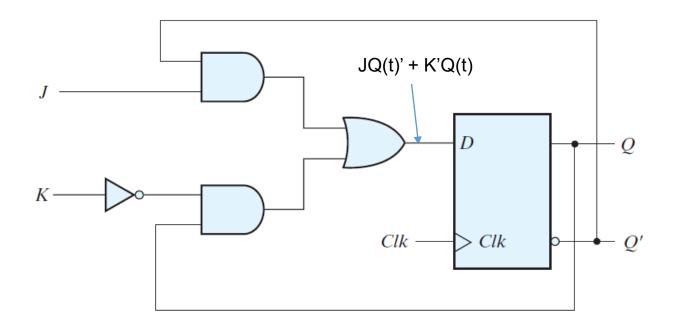
#### K-Map





### J-K Flip-Flop

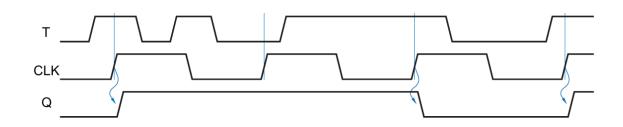
- Implement JKFF using DFF
  - Because in DFF,  $Q_{t+1} = D$
  - Thus, according to JKFF's characteristic equation, Q(t+1) = JQ(t)' + K'Q(t), we can derive D = JQ(t)' + K'Q(t)





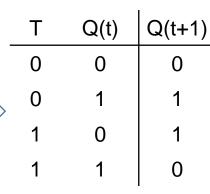
### T Flip-Flop

• T: Toggle



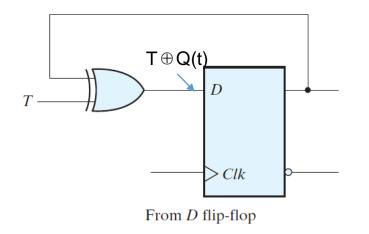
#### **T Flip-Flop**

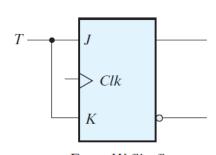
T	Q(t + 1)	
0	Q(t)	No change
1	Q'(t)	Complement



Characteristic equation of TFF

$$Q(t+1) = T'Q(t) + TQ(t)'$$
$$= T \oplus Q(t)$$





From JK flip-flop