

Question Bank

Subject: Numerical Methods

Set-II

Topic: Solution of Algebraic and Transcendental Equations

1. If $f(x)$ is continuous in $[a,b]$ and $f(a)f(b)<0$, then there exist
 - a) At least one real root
 - b) At most one real root
 - c) Exactly one real root
 - d) Exactly one complex root
2. Which of the following does not always guarantee the convergence
 - a) Secant method
 - b) Bisection method
 - c) Regula-falsi method
 - d) Newton-Raphson Method
3. The Newton-Raphson method fails when
 - a) $f'(x)=1$
 - b) $f'(x)=0$
 - c) $f'(x)=-1$
 - d) $f''(x)=0$
4. Condition for convergence of Newton-Raphson method is
 - a) $|f(x)f'(x)| < \{f''(x)\}^2$
 - b) $|f(x)f''(x)| < \{f'(x)\}^2$
 - c) $|f(x)f'(x)| > \{f''(x)\}^2$
 - d) $|f(x)f''(x)| > \{f'(x)\}^2$
5. Regula falsi method used for finding the real roots of a numerical equation is-
 - a) An analytical method
 - b) Graphical method
 - c) Iterative method
 - d) None of these
6. Regula-Falsi method is
 - a) **Conditionally divergent**
 - b) Linearly convergent
 - c) Divergent
 - d) None of these
7. For Newton-Raphson method, the iterative formula is
 - a) $x_{n+1}=x_n +$
 - b) $x_{n+1}=$
 - c) $x_{n+1}=$
 - d) $x_{n+1}=x_n -$
8. One of the roots of the equation $x^2+2x-2=0$ lies in between
 - a) 1 and 2
 - b) 0 and 0.5
 - c) 0.5 and 1.0
 - d) None of these
9. Newton-Raphson method is also known as method of
 - a) Straight line
 - b) Tangent

- c) Normal
d) Cyclic
10. The order of convergence of Newton-Raphson method is
a) 3
b) 2
c) 1
d) 4
11. Under the condition that $f(a)$, $f(b)$ have opposites and $a < b$ the first approximation of the one of the roots of $f(x)=0$ by Regula-Falsi method is given by
a)
b)
c)
d)
12. Newton-Raphson method formula for (Where N is a positive integer) is
a) $x_{n+1} = Nx_n$
b) $x_{n+1} = x_n(2 - Nx_n)$
c) $x_{n+1} = x_n(2 + Nx_n)$
d) $x_{n+1} = Nx_{n-1}$
13. Bisection method is _____ but _____
a) Fast, fails
b) Fast, sometimes fails
c) Fast, never fails
d) Slow, never fails
14. Newton-Raphson method formula for finding the square root of a real number R from the equation $x^2 - R = 0$ is
a) $x_{n+1} =$
b) $x_{n+1} = (x_n +)$
c) $x_{n+1} = (x_n -)$
d) None of these
15. Find the root of the following equation by Newton-Raphson method correct up to 3 decimal places: $x^3 - 3x + 1 = 0$
Ans: 1.532
16. Find the root of the following equation by Regula-Falsi method correct up to 3 decimal places:
 $xe^x - 3 = 0$
Ans: 1.060
17. Find the root of the following equation by Bisection method correct up to 3 decimal places:
 $x^3 - 4x - 9 = 0$
Ans: 2.7065

Topic: Numerical Solution of Ordinary Differential Equations

1. Runge-Kutta formula has a truncation error, which is order of-
a) h^2
b) h^4
c) h^5
d) None of these

2. The truncation error of Euler's method is order of
 - a) h
 - b) h^2**
 - c) h^3
 - d) None of these
3. Milne's predictor-corrector method is a single step method
 - a) False
 - b) True**
4. If $y(0)=2$, the value of k_2 according to Runge-Kutta of 2nd order is ($h=0.2$)
 - a) 0.1**
 - b) 0.01
 - c) 0.4
 - d) 0.04
5. For solving ordinary differential equation, the Euler's formula is
 - a)
 - b)**
 - c)
 - d)
6. Runge-Kutta method of fourth order is used to solve
 - a) A first order ordinary differential equation numerically
 - b) A system of linear equations
 - c) A first-order partial differential equations numerically
 - d) None of these**
7. Modified Euler's method has a truncation error of the order
 - a) h
 - b) h^2
 - c) h^4
 - d) h^3**
8. Milne's predictor formula is-
 - a)
 - b)
 - c)
 - d)**
9. Milne's corrector formula is-
 - a)
 - b)
 - c)
 - d)**
10. Use Taylor series method to solve the differential equation given $y(0)=1$ and find $y(0.03)$
Ans: 0.97001
11. Use Euler's method, find the approximate value of y corresponding to $x=1$ given that $y=1$ when $x=0$
Ans: 3.18
12. Using modified Euler's method, find an approximate value of y at $x=0.3$ given that $y(0)=1$.
Ans: 1.3997
13. Given that $y(0)=0$. Use the fourth order Runge-Kutta method to find $y(0.2)$
Ans: 0.2027
14. Compute $y(2)$ by Milne's predictor-corrector method if given $y(0)=2$, $y(0.5)=2.636$, $y(0.4)=0.4228$ and $y(0.6)=0.6841$.
Ans: 6.8710, 6.8732

Topic: Numerical Solution of a System of Linear Equations

1. When the Gauss elimination method is used to solve $BX=A$, B is transformed into
 - a) A lower triangular matrix
 - b) An upper triangular matrix
 - c) Zero matrix
 - d) None of these
2. Diagonal dominance is must for
 - a) Gauss-Seidel method
 - b) Gauss-Jordan method
 - c) Gauss-elimination method
 - d) None of these
3. Gauss elimination method does not fail even if one of the pivot element is equal to zero
 - a) True
 - b) False**
4. When Gauss-Jordan method is used to solve the system of equations which can be written in the form $AX=B$, A must be a
 - a) Singular matrix
 - b) Non-singular matrix**
 - c) Diagonal matrix
 - d) Orthogonal matrix
5. Solve the system of equations by Gauss-elimination method
$$\begin{aligned}x+4y+3z &= 1 \\ 2x+y+4z &= 4 \\ x-3y-2z &= 5\end{aligned}$$

Ans: $x=3$, $y=-2$, $z=2$
6. Solve the system of equations by Gauss-Seidel method correct up to 3 decimal places
$$\begin{aligned}x+y+54z &= 110 \\ 27x+6y-z &= 85 \\ 6x+15y+2z &= 72\end{aligned}$$